# Measurement of $D\overline{D}$ Decays from the $\psi(3770)$ Resonance

Andy Julin

University of Minnesota - Twin Cities

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- **6** Exploration of the Non- $D\overline{D}$  Branching Fraction
- Conclusion

# Introduction

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## Really Quick Overview

#### Goal: Describe $\psi(3770) \rightarrow D\overline{D}$ cross section as a function of energy

- ullet Measure parameters of the  $\psi(3770)$  such as mass and decay width
- ullet Investigate branching fraction of non- $D\overline{D}$  decays from  $\psi(3770)$

#### How is that actually done?

- ullet Examine collisions of  $e^+e^-$  tuned to energies near  $\psi(3770)$  mass
- $\bullet$  Identify  $D\overline{D}$  production by subtracting backgrounds from total
- Fit to cross section using formula based on  $M^{\psi(3770)}, \Gamma^{\psi(3770)}, \ldots$
- ullet Use results to determine  $\psi(3770)$  parameters and explore non- $D\overline{D}$

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# Why does this need to be done? ( $D\overline{D}$ Cross Section)

- Previous experiments have provided conflicting results
  - Largely did not include effects from interference

$M^{\psi(3770)}$	(No Interference)	$M^{\psi(3770)}$ [MeV] (With Interference)	)
BES-II	$3772.0 \pm 1.9$	BaBar $3778.8\pm1.9\pm0.9$	
Belle	$3776.0 \pm 5.0 \pm 4.0$	KEDR 3779.2 <sup>+1.8</sup> +0.5 +0.3	
BaBar	$3775.5\pm2.4\pm0.5$		

- Those including interference found it necessary to properly fit results
  - Statistics available were insufficient to fully resolve discrepancy
  - BESIII has much larger data sample available over this region
- Our analysis follows similarly to KEDR collaboration procedure
  - ullet Include interference between  $\psi(3770)$  and nearby  $\psi(2S)$  in fit shape

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# Why does this need to be done? (Non- $D\overline{D}$ )

Previous experiments have provided very conflicting results

$\Gamma(\psi(3770)  o non-D\overline{D}) \; (BESII)$	$\Gamma(\psi(3770)  o non-D\overline{D}) \; (CLEO-C)$	
$(15.1 \pm 5.6 \pm 1.8)\%$	$(-3.3\pm1.4^{+6.6}_{-4.8})\%$	

- Impossible to directly determine  $q\bar{q}$  (uds) contribution at  $\psi(3770)$ 
  - Cannot reliably be separated from  $D\overline{D}$  decays
- ullet Use extrapolation from lower energy points (below  $\psi(2S)$ )
  - ullet Assume  $e^+e^ightarrow qar q$  scales as function of energy (1/s)

# (Another) Really Quick Overview

- Must reconstruct D candidates from decays into other particles
  - (lifetime of D) vs. (available energy)  $\rightarrow$  (very small displacement)
  - Use analysis software to look for proper combinations of particles
- Model particle decays with computer simulations: Monte Carlo (MC)
  - ullet Analyze decays mistakable for  $D\overline{D}$  production (e.g.,  $e^+e^- o au^+ au^-$ )
  - Determine rate of correct identification in DD samples
- Process data/MC identically and subtract backgrounds to get signal
  - ullet Compare rate of data collisions (luminosity:  ${\cal L}$ ) to get cross section  $(\sigma)$
- Acceleration of charged particles incurs radiative effects
  - Initial State Radiation (ISR) reduces total energy before collisions
  - Requires correction to accurately describe production cross section

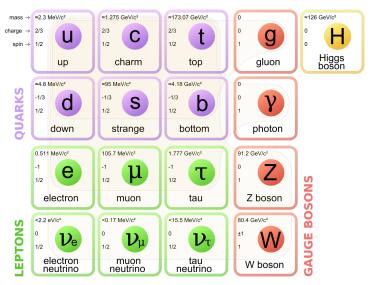
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# Theoretical Background

#### **Fundamental Forces**

- 1) Electromagnetic (QED)
  - Responsible for attracting / repelling electrically charged objects
  - Mediated by the massless photon  $(\gamma)$
  - Very precisely calculable using perturbation theory
- 2) Weak
  - Responsible for radioactive decays and flavor changes
  - ullet Mediated by the very heavy  $W^\pm$  and Z
  - Led to discovery of C and CP violation
- 3) Strong (QCD)
  - Responsible for binding together hadrons
  - Mediated by the massless gluon (g)
  - Complicated calculations not described by perturbation theory
- 4) Gravity Negligible at this mass scale

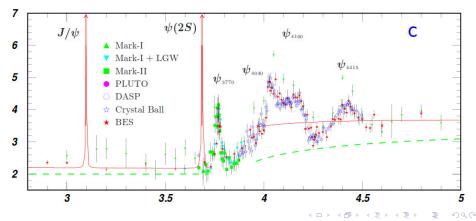
#### Standard Standard Model Slide



#### Charmonium

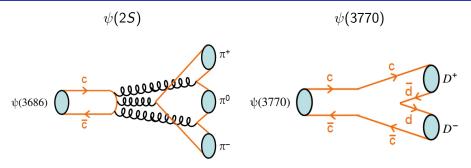
Resonances formed by a  $c\bar{c}$  pair:  $J/\psi$ ,  $\psi(2S)$ ,  $\psi(3770)$ , ...

- ullet  $\psi(2S)$  and  $\psi(3770)$  originally interpreted as excited states of  $J/\psi$
- Evidence of mixed-states suggests more complicated picture



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# Decay Suppression (OZI Rule)



- Requires hard gluons for decay
- Very narrow decay width
  - $\Gamma_{\psi(2S)} = 0.286 \, \text{MeV}$

- Decays via open charm  $(D\overline{D})$
- Much wider decay width
  - $\Gamma_{\psi(3770)} = 27.5 \,\mathrm{MeV}$

Addition of  $D\overline{D}$  decays introduces drastically different behavior!

# Accelerator and Detector

# Institute of High Energy Physics (IHEP)

BESIII is hosted at the IHEP Campus located in Beijing, China



#### Accelerator - Beijing Electron-Positron Collider II (BEPCII)

- Create positrons by firing electrons into stationary material
  - Generates high energy  $\gamma$ s which interact with material to form  $e^+e^-$
- Separate newly created positrons magnetically
- Accelerate positrons in linear accelerator and feed into storage ring
- Accelerate electrons and feed into the oppositely circulating ring
  - Electrons readily available, so extraction from photons unnecessary
- Focus each beam using magnets along storage rings until collision





# Detector - Beijing Spectrometer III (BESIII)

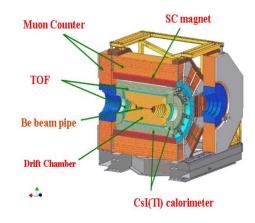
Collision of beams tuned to occur at central point of detector

Beams angled during collision to improve integrated luminosity

#### Four main subdetector systems:

- Multi-Layer Drift Chamber
- Time-of-Flight
- Electromagnetic Calorimeter
- Muon Identifier

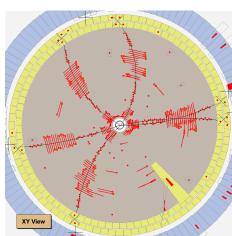




# Multi-Layer Drift Chamber (MDC)

- Reconstruct charged tracks from interactions with sense wires (hits)
  - Wires surrounded by ionizable gas
  - Initial ionization due to particle triggers avalanche of electrons
  - High electric field near wires draws in released electrons to measure energy deposited
- Determine properties of particle from curvature in magnetic field
  - Radius determines momentum
  - Direction determines charge
- Energy deposition rate (dE/dx) helps determine particle candidate

#### **BESIII Event Display**



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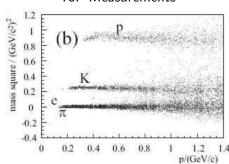
# Time-of-Flight (ToF)

- Measure particle velocity using travel time after initial collision
  - Scintillator bands located at 0.81 m and 0.86 m from interaction point
  - Attached to photomultiplier tubes to measure light output
- Helps distinguish between  $K^{\pm}$  and  $\pi^{\pm}$  candidates at lower momenta
  - Combined with dE/dx measurements in MDC to set particle hypothesis

# MDC Measurements Normalized dEdx pulse height 0.8 0.6

0.4

#### ToF Measurements



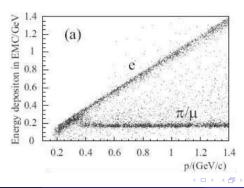
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p/(GeV/c)

# Electromagnetic Calorimeter (EMC)

- Measure energy deposited by electron and photon tracks
  - Other particles are generally relativistic and thereby minimum ionizing
    - These deposit relatively constant energy, independent of momenta
  - Use CsI(TI) crystals attached to photodiodes to measure energy
    - Energy lost primarily in gaps of arrangement or out the back of crystals
- ullet Allows reconstruction of purely neutral decays, such as  $\pi^0 o \gamma\gamma$



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# Muon Identifier (MUC)

- Identify tracks traversing through multiple layers as muons
  - Most particle types will be stopped before reaching the MUC
    - Electrons susceptible to Bremsstrahlung radiation
    - Kaons and pions susceptible to strong interactions
  - Requires muons with  $p > 0.4 \, \text{GeV}$  for appropriate curvature

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#### Triggering System

- Events filtered through two-step process
  - L1: Hardware Extracts information from various subdetectors
    - MDC
      - Examines the number of superlayers each track passes through Superlayer: a collection of wires at same radial distance
      - Applies a cut on minimum transverse momentum for each
    - ToF
- Examines number of hits in barrel and endcap regions
- Checks for hits which are on opposite sides of the detector
- EMC
  - Examines clustering of deposited energy around local maximum
- L3: Software Assembles information to decide if potentially relevant
- Quickly and efficiently removes non-physics background events
  - $\bullet$  e.g., reduces beam-related backgrounds from  ${\sim}13\,\text{MHz}$  to  ${\sim}1\,\text{kHz}$

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# **Analysis Software**

#### Monte Carlo Generation

- Create simulations of detector construction and particle interactions
  - Simulate material composition and detector response using GEANT4
  - Simulate particle decay behavior using physics generators
- ullet Generate  $D\overline{D}$  components to determine accuracy of reconstruction
  - Check how often generated decay matches reconstructed decay
- Generate decays which could be mistaken as  $D\overline{D}$  in reconstruction  $e^+e^- \to \tau^+\tau^-, \quad e^+e^- \to \gamma\psi(2S), \quad e^+e^- \to q\bar{q}(uds), \quad \dots$
- Identify contributions of generated background samples seen in data
  - Subtract background components from data to estimate signal events

#### **Data Processing**

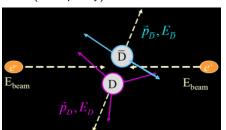
- Process samples using BESIII Offline Software System (BOSS)
  - Use information gathered by subdetectors to reconstruct events
  - Extract relevant physical parameters (E, p, ...) from each track
- Reconstruct D candidates using 'D-Tagging' process
  - Search over combinations of tracks to best match decay products
  - Take best set of tracks based on characteristics of tag

$$\Delta E = E_{ ext{beam}} - E_{ ext{tag}}$$
  $m_{ ext{BC}} = \sqrt{E_{ ext{beam}}^2 - |ec{p_{ ext{tag}}^2}|^2}$ 

Treat both data and Monte Carlo (MC) samples identically

#### D-Tagging

- Reconstruct D candidates from decays  $D \to \{\pi^{\pm}, \ K^{\pm}, \ \pi^{0}, \ K_{c}^{0}\}$
- Modes selected based on reconstruction efficiency
  - High branching fractions
  - Manageable number of tracks (multiplicity)



#### Reconstructed Modes\*

(0) 
$$D^0 \to K^- \pi^+$$

(1) 
$$D^0 \to K^- \pi^+ \pi^0$$

(3) 
$$D^0 \to K^- \pi^+ \pi^+ \pi^-$$

(200) 
$$D^+ \to K^- \pi^+ \pi^+$$

(201) 
$$D^+ \to K^- \pi^+ \pi^+ \pi^0$$

(202) 
$$D^+ \to K_S^0 \pi^+$$

(203) 
$$D^+ \to K_S^0 \pi^+ \pi^0$$

(204) 
$$D^+ \to K_S^0 \pi^+ \pi^+ \pi^-$$

(205) 
$$D^+ \to K^+ K^- \pi^+$$

<sup>\*</sup>Charge conjugation implied

# Measurement of the $D\overline{D}$ Cross Section

#### Overview for $\overline{DD}$ Cross Section

- Construct parametrization used to compare to measured data points
- List data samples with their luminosities / center-of-mass energies
- Describe signal and background component identification
- Show calculation of reconstruction efficiency for  $D\overline{D}$  events
- Combine everything into cross section and discuss fitting procedure
- Assess systematic uncertainties from parameters used in analysis

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# Derivation of $\sigma(\psi(3770) \to D\overline{D})$

Need to convert integral expression into measurable function

$$\sigma_{D\overline{D}}^{RC}(W) = \int z_{D\overline{D}}(W\sqrt{1-x}) \, \sigma_{D\overline{D}}(W\sqrt{1-x}) \, \mathcal{F}(x,W^2) \, dx$$

- $\mathbf{z}_{D\overline{D}}$ : Coulomb interaction  $(D^+D^-)$  and mass constraints
- $\sigma_{D\overline{D}}$ : Born level (lowest order) cross section
- F: Initial State Radiation (ISR) correction [Kuraev and Fadin]
- x: Fraction of energy radiated away
- Strategy: split into small intervals and numerically integrate
  - Treat  $\mathbf{z}_{D^+D^-}$  and  $\sigma_{D\overline{D}}$  as constant in each interval
  - Integrate  $\mathcal{F}(x, W^2) = \beta x^{\beta-1} F(W^2)$  over x

$$\beta = \frac{2\alpha}{\pi}(L-1), \qquad L = \log\left(\frac{W^2}{m_e^2}\right)$$

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ullet Obtain complicated, but calculable function for  $D\overline{D}$  cross section

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#### Form Factors

Need to parameterize the form factor in the Born level cross section

$$\sigma_{D\overline{D}}(W) = \frac{\pi \alpha^2}{3W^2} \beta_D^3 |F_D(W)|^2, \qquad \beta_D = \sqrt{1 - \frac{4m_D^2}{W^2}}$$

• Comprised of resonant (R) and non-resonant (NR) components

$$F_D(W) = F_D^{NR}(W) + \sum_r F_D^{R_r}(W) e^{i\phi_r}$$

Resonant components parametrized by Breit-Wigner shape

$$F_D^R(W) = \frac{6 W \sqrt{(\Gamma_{ee}/\alpha^2)(\Gamma_{D\overline{D}}(W)/\beta_D^3)}}{M^2 - W^2 - iM\Gamma(W)}, \qquad \Gamma_{D\overline{D}}(W) = \Gamma(W) \times \mathcal{B}_{D\overline{D}}$$

- Non-resonant component has no definitive parametrization
  - Investigate two potential models for analysis
    - Exponential: generic form to approximate shape
    - Vector Dominance Model (VDM): physically based parameters

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#### Form Factor Models

#### **Exponential Model**

$$F_D^{NR} = F_{NR} \exp(-q_D^2/a_{NR}^2)$$

- Fit Parameters
  - F<sub>NR</sub>: Amplitude
  - a<sub>NR</sub>: Width
- Used for systematic check

#### **Vector Dominance Model**

$$F_D^{NR}(W) = F_D^{\psi(2S)}(W) + F_0$$

- Fit Parameters
  - $\Gamma^{\psi(2S)}$ : Decay width for  $\psi(2S)^*$
  - $F_0$ : Higher resonances ( $\psi(4040)$ )
- Used for final results
- Use  $M^{\psi(3770)}$  in place of  $M^{\psi(2S)}$ 
  - Avoid mass below  $D\overline{D}$  threshold
  - \*Unclear physical meaning

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## Data Samples

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- Use scan data to determine overall cross section shape
  - Taken over 3.735 GeV  $\leq E_{\rm cm} \leq$  3.870 GeV and split into 34 bins
  - Chosen to be above  $D^0\overline{D^0}$  threshold and below  $D^{*0}\overline{D^0}$  threshold
  - Includes two bins below  $D^+D^-$  threshold which have zero production
  - Luminosity measured using  $e^+e^- o e^+e^-(\gamma)$  events  $(\mathcal{L}=69.80\,\mathrm{pb^{-1}})$
- Use additional high statistics samples for comparison measurements

Name	$E_{\rm cm}$ [GeV]	$\mathcal{L}$
On-Peak $\psi$ (3770) $^{\dagger}$	3.773	$2.93{ m fb}^{-1}$
XYZ-Scan	3.810	$50.54{ m pb}^{-1}$
R-Scan	3.850	$7.95{ m pb}^{-1}$

 $<sup>^\</sup>dagger Analysis$  of  $D\overline{D}$  cross section performed independently

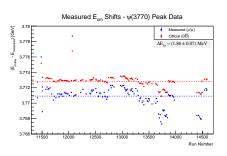
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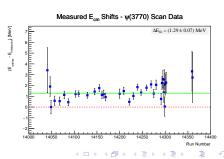
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## Center-of-Mass Energy

#### Accurate $E_{cm}$ required for precise determination of $M^{\psi(3770)}$

- Measure  $E_{\rm cm}$  using  $M_{\rm inv}$  of 'On-Peak  $\psi(3770)$ '  $e^+e^- o \mu^+\mu^-$  events
- ullet Compare results to separate, trustworthy procedure using  $D\overline{D}$  events
  - ullet Difference in average values determines correction to  $\mu^+\mu^-$  procedure
- Measure  $E_{cm}$  for scan data using  $\mu^+\mu^-$  procedure
  - Shift values by correction from  $D\overline{D}$  procedure to get final results





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#### Monte Carlo Generation

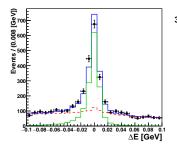
- Generate MC samples to help identify signal and background rates
  - Signal:  $\psi(3770) \rightarrow D^0 \overline{D^0}, \qquad \psi(3770) \rightarrow D^+ D^-$
  - Background:  $q\bar{q}, \quad \tau^+\tau^-, \quad \gamma J/\psi, \quad \gamma \psi(2S)$
  - ullet Events per sample of  ${\sim}10^6\text{-}10^7$  depending on decay type
  - ullet Decays simulated using run-dependent  $E_{\rm cm}$  and accelerator conditions

- ullet Samples of  $\psi(3770) o D\overline{D}$  generated using our cross section results
  - Use Born cross section from final fit results to improve MC generator
  - Requires iteration of MC generation to properly reflect true shape
    - Performed five iterations of input shapes during analysis

## Signal Determination

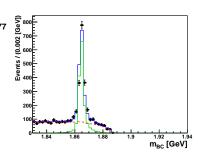
- Measure  $D^0\overline{D^0}$  /  $D^+D^-$  yields separately with 2D fit
  - ullet Extract  $\Delta E$  and  $m_{
    m BC}$  distributions and arrange MC samples into groups
    - (1) Proper *D*-tags

- $(3) q\bar{q}$
- (2) Improper *D*-tags
- (4)  $\tau^+\tau^- + \gamma J/\psi + \gamma \psi(2S)$
- Float normalizations of each group to fit data distributions  $(\chi^2)$





Bin 14 - D<sup>0</sup>



## **Efficiency Correction**

- Correct for *D* reconstruction efficiency to determine total production
  - ullet Average MC candidate amounts ( $N_{\rm prop}$  vs.  $N_{\rm gen}$ ) over decay modes

$$\epsilon_D = \sum_i \epsilon_i_{\mathsf{rec}} \, \mathcal{B}_i = \sum_i \left( \frac{N_i_{\mathsf{prop}}}{N_i_{\mathsf{gen}}} \right) \mathcal{B}_i$$

Decay Mode $(i)$	PDG $\mathcal{B}_i$ [%]	MC Efficiency $\epsilon_{i \text{ rec}}$			
$D^0  o K^-  \pi^+$	$3.89 \pm 0.05$	$0.7002 \pm 0.0011$			
$D^0  o K^-  \pi^+  \pi^0$	$13.93\pm0.50$	$0.3794 \pm 0.0004$			
$D^0  ightarrow K^-  \pi^+  \pi^+  \pi^-$	$8.11 \pm 0.21$	$0.3988 \pm 0.0006$			
$\epsilon_{D^0} = (11.245 \pm 0.020)\%$					
$D^+  ightarrow K^-  \pi^+  \pi^+$	$9.13 \pm 0.19$	$0.5471 \pm 0.0007$			
$D^+  ightarrow K^-  \pi^+  \pi^+  \pi^0$	$5.99 \pm 0.18$	$0.2739 \pm 0.0006$			
$D^+ o K^0_S\pi^+$	$1.47\pm0.07$	$0.3883 \pm 0.0014$			
$D^+ o  extstyle K_S^0\pi^+\pi^0$	$6.99\pm0.27$	$0.2079 \pm 0.0005$			
$D^+  ightarrow \mathit{K}^0_\mathit{S}  \pi^+  \pi^+  \pi^-$	$3.12\pm0.11$	$0.2237 \pm 0.0007$			
$D^+  o K^+  K^-  \pi^+$	$0.95\pm0.03$	$0.4317 \pm 0.0018$			
$\epsilon_{D^+} = (9.770 \pm 0.063)\%$					

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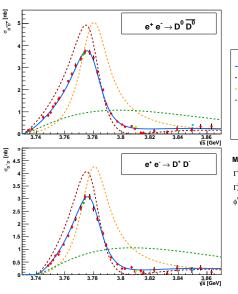
## **Cross Section Fitting**

- Use signal amount, efficiency, and luminosity to find cross sections:
  - Include factor of 2 to correct for double counting  $(D \text{ vs. } D\overline{D})$

$$\sigma_{D\overline{D}}^{RC}(E_i) = \frac{N_D(E_i)}{2 \epsilon_D(E_i) \mathcal{L}(E_i)}$$

- ullet Fit to theoretical parametrization to determine  $\psi(3770)$  parameters
  - $M^{\psi(3770)}$   $\Gamma^{\psi(3770)}$   $\Gamma^{\psi(3770)\to D\overline{D}}_{ee}$   $\phi^{\psi(3770)}$
  - Use  $\Gamma_{ee}^{\psi(3770)\to D\overline{D}}$  in place of known  $\mathcal{B}_{nD\overline{D}}$  or  $\Gamma_{ee}^{\psi(3770)}$
- Two additional fit parameters depending on form factor choice
  - Exponential:  $F_{NR}$   $a_{NR}$  VDM:  $\Gamma^{\psi(2S)}$   $F_0$
- ullet Minimize sum of  $\chi^2$  with simultaneous fit to  $D^0$  and  $D^+$

#### **Exponential Results**



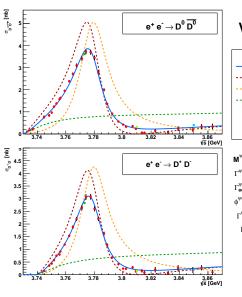
# Exponential Fit Results



```
\begin{split} M_{\bullet}^{V(3770)} &= (3.7821 \pm 0.0003) \\ \Gamma_{\bullet}^{V(3770)} &= (2.6004 \pm 0.0597) \times 10^{-2} \\ \Gamma_{ee}^{V(3770)} &= (2.3313 \pm 0.1016) \times 10^{-7} \\ \phi_{\bullet}^{V(3770)} &= (3.7455 \pm 0.0388) \end{split}
```

=  $(2.0844 \pm 0.0752) \times 10$ =  $(4.2701 \pm 0.1336) \times 10^{-1}$ 

#### Vector Dominance Model Results



#### **VDM Fit Results**



$$\mathbb{V}^{(3770)} = (3.7808 \pm 0.0002)$$
 $\mathbb{V}^{(3770)} = (2.4098 \pm 0.0534) \times 10^{-2}$ 
 $\mathbb{V}^{(3770)} = (2.1583 \pm 0.0867) \times 10^{-7}$ 
 $\mathbb{V}^{(3770)} = (3.6149 \pm 0.0435)$ 

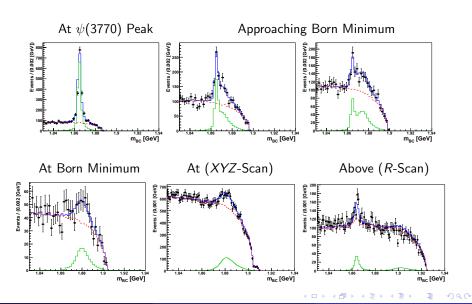
=  $(1.1491 \pm 0.1236) \times 10^{-2}$ =  $(-2.8845 \pm 0.4462)$ 

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#### Results Overview

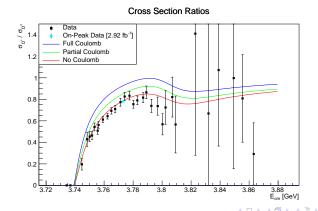
- Both form factor choices show generally good agreement
  - Excess in  $\chi^2$  largely due to two  $D^0$  points just above 3.81 GeV
  - Could indicate need for improved model in higher energy region
- ullet Values for  $\psi(3770)$  parameters primarily dependent on peak region
  - Consistent shape in this region emphasizes quality of results
- Inteference related to behavior of Born level cross section
  - Reappearance of Born level events is strong indication of interference
  - Impossible to reproduce with two non-interfering Breit-Wigner shapes

### Born Level Event Contribution in $m_{BC}$



#### Coulomb Interaction

- Results shown previously use  $z_{D^+D^-} = 1$  for calculations
  - Significantly worse results when including value for  $\mathbf{z}_{D^+D^-}$   $(\chi^2_r \approx 5)$
- Ratio of cross sections  $(\sigma_{D^+}/\sigma_{D^0})$  prefers  $z_{D^+D^-}$  value excluded
  - ullet Unclear explanation for behavior, but consistent with  $\Upsilon(4S) o B\overline{B}$



## Systematic Uncertainties

- Examine uncertainty from parameters involved throughout procedure
  - Individually increase / decrease value by the uncertainty of each
  - Re-fit cross section with altered values and take maximal variation
- Many uncertainties adjust overall scale of cross section normalization
  - Only affects the value of  $\Gamma_{ee}^{\psi(3770)\to D\overline{D}}$

Name	Change	Description
Luminosity	$\mathcal{L}$	1.0 %
$\pi^\pm/{\it K}^\pm$ Tracking	$\epsilon_{i}$ rec	$1.0\%$ per $\pi^\pm$ or $\mathit{K}^\pm$ in the mode
$\pi^0$ Tracking	$\epsilon_{i \;  m rec}$	$2.0\%$ per $\pi^0$ in the mode
$K_S^0$ Tracking	$\epsilon_{i \;  m rec}$	$1.5\%$ per $K_S^0$ in the mode
Single Tag Fits	$N_D$	Adjust by fit difference (small)
PDG Branching Fractions	$\epsilon_{i \;  m rec}$	Adjust by PDG errors

## Systematic Uncertainties

#### Meson Radii

- Adjust values of  $R_{\psi(2S)}$  and  $R_{\psi(3770)}$  by 25 % (from KEDR)
- Take max variation over all four combinations of up / down on each
- Most significant source of systematic uncertainty
- MC Iteration (negligible)
  - Take difference in parameters before / after Born level modification
- MC ISR Generation (negligible)
  - Take difference in fit results with KKMC vs. ConExc generators
- Intermediate Resonances (negligible)
  - $\bullet$  Examine effects of  $\rho^0 \to \pi^+\pi^-$  in the mode  $D^+ \to {\it K}^-\,\pi^+\,\pi^+$
  - ullet Take difference in  $K\pi$  vs.  $\pi\pi$  invariant mass splits using 'On-Peak' data

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## Systematic Uncertainties

• Uncertainties summed in quadrature (assumed independent)

Systematic	$M^{\psi(3770)}$ [%]	$\Gamma^{\psi(3770)}$ [%]	$\Gamma_{ee}^{\psi(3770) o D\overline{D}}$ [%]	$\phi^{\psi(3770)}$ [%]
Luminosity	0.000	0.004	1.005	0.014
$K^\pm/\pi^\pm$ Tracking	0.000	0.008	2.646	0.033
$\pi^{0}$ Tracking	0.000	0.012	0.746	0.028
$K_S^0$ Tracking	0.000	0.004	0.260	0.019
Single Tag Fits	0.000	0.012	0.213	0.008
PDG Errors	0.000	0.017	2.840	0.036
Meson Radii	0.016	2.411	3.512	1.477
Total [%]	0.016	2.411	5.389	1.479

- Total contribution similar to statistical error for most parameters
  - ullet Value for  $M^{\psi(3770)}$  is small, but has very small statistical error

	$M^{\psi(3770)}$	$\Gamma^{\psi(3770)}$	$\Gamma_{ee}^{\psi(3770) o D\overline{D}}$	$\phi^{\psi(3770)}$
$\sigma_{\sf sys}/\sigma_{\sf stat}$	3.000	1.088	1.342	1.229

### Form Factor Uncertainty

- Notable discrepancy between choices of non-resonant form factor
  - Both methods provide reasonably good fit with data
  - Use difference of Exponential and VDM fit values as uncertainty
  - Follow example of KEDR by treating as model-dependent uncertainty

Form Factor	$M^{\psi(3770)}$ [GeV]	$\Gamma^{\psi(3770)}$ [MeV]	$\Gamma^{\psi(3770) o D\overline{D}}_{ee}\left[eV ight]$	$\phi^{\psi$ (3770) [°]
Exponential	3.7821	26.004	233.13	214.60
VDM	3.7808	24.098	215.83	207.12
Difference	0.0013	1.906	17.30	7.48

#### Final Results

Results not limited by statistics, but by model-dependency

$M^{\psi(3770)}$	$3780.8 \pm 0.2 \pm 0.6 \pm 1.3$	[MeV]
$\Gamma^{\psi(3770)}$	$24.1 \pm 0.5 \pm 0.6 \pm 1.9$	[MeV]
$\Gamma_{ee}^{\psi(3770) o D\overline{D}}$	$216~\pm~9~\pm11~\pm17$	[eV]
$\phi^{\psi}$ (3770)	$207~\pm~3~\pm~3~\pm~7$	[°]

Errors are statistical, systematic, and model-dependent, respectively

Results consistent with KEDR and very inconsistent with PDG

Method	$M^{\psi(3770)}$ [MeV]	$\Gamma^{\psi(3770)}$ [MeV]	$\Gamma^{\psi(3770) o D\overline{D}}_{ee}\left[eV ight]$
Exponential	$3782.1 {\pm} 0.3 {\pm} 0.6 {\pm} 1.3$	$26.0 \pm 0.6 \pm 0.7 \pm 1.9$	$233 \pm 10 \pm 13 \pm 17$
VDM	$3780.8 \pm 0.2 \pm 0.6 \pm 1.3$	$24.1 \pm 0.6 \pm 0.6 \pm 1.9$	$216\pm9\pm12\pm17$
KEDR	3779.2 <sup>+1.8+0.5+0.3</sup> -1.7-0.7-0.3	$24.9^{+4.6+0.5+0.2}_{-4.0-0.6-0.9}$	$154_{-58-9}^{+79+17+13}, \\ 414_{-80-26-10}^{+72+24+90}$
PDG	$3773.15 \pm 0.33$	$27.2 \pm 0.9$	$[262\pm18] imes~\mathcal{B}_{D\overline{D}}$
	·	·	

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# Exploration of the Non-DD Branching Fraction

## Overview for Non- $D\overline{D}$ Branching Fraction

- List data samples with their luminosities / center-of-mass energies
- Detail event selection criteria and group cut methods
- Show hadronic signal counting fits and background subtraction
- Describe efficiency extrapolation using lower energy data points
- Examine procedure for  $\psi(3770)$  data with  $D\overline{D}$  component
- ullet Investigate alternative expressions for the  $\psi(2S)$  cross section

#### Data Samples

- Use data from continuum (Old/New) and  $\psi(3770)$  (R1/R2)
  - Begin with continuum data and use to extrapolate to  $\psi(3770)$  data
- E<sub>cm</sub> measured as before
  - 4-6 MeV shift in new continuum samples
  - No shift for old continuum samples

$E_{cm}$ [GeV]	Luminosity $[pb^{-1}]$
3.496	$3.680 \pm 0.009$
3.538	$\textbf{3.481} \pm \textbf{0.009}$
3.596	$\textbf{0.395} \pm \textbf{0.019}$
3.644	$5.420\pm0.009$
3.665	$4.669 \pm 0.009$
3.650	$44.334 \pm 0.009$
3.773	$926.922 \pm 0.092$
3.773	$1978.920 \pm 0.091$
	3.496 3.538 3.596 3.644 3.665 3.650 3.773

- Requires precise  $E_{cm}$  measurement for extrapolation procedure
  - Cross section of  $\psi(2S)$  rapidly changes near its peak

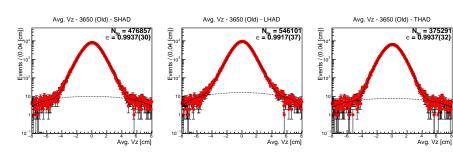
#### **Event Selection Criteria**

- Apply cuts on charged (neutral) tracks in the MDC (EMC)
- Apply cuts on highest energy / momentum
  - Removes  $e^+e^- o \{e^+e^-, \, \gamma\gamma\}$  backgrounds
- Apply groups of cuts to select multihadron events
  - Number of Tracks
  - Visible Energy
  - Visible Momentum (z-direction)
  - Max Shower Energy
  - Total Shower Energy
- Values for group cuts dependent on level of impact
  - Standard (SHAD), Loose (LHAD), Tight (THAD)

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## Signal Counting

- ullet Identify events using average distance of closest approach in z  $(V_z)$ 
  - Signal tracks will originate within few cm of vertex
  - Background tracks can originate away from collision point
- ullet Fit with a double Gaussian (sig) + 2<sup>nd</sup>-order polynomial (bkg) shape



#### **Background Subtraction**

Need to determine background contributions seen in data

$$N_{\mathsf{had}} = \mathcal{L} imes \sigma imes \epsilon_{\mathsf{MC}} = \mathcal{L} imes \sigma imes \left( rac{N_{\mathsf{rec}}}{N_{\mathsf{gen}}} 
ight)$$

#### 3650 (Old) Reconstruction

Sample	$\sigma$ [nb]	$\epsilon_{MC}$ (SHAD) [%]	$\epsilon_{MC}$ (LHAD) [%]	$\epsilon_{MC}$ (THAD) [%]
$e^+e^-$	554.562	$0.0006 \pm 0.0002$	$0.0008 \pm 0.0002$	$0.0001 \pm 0.0001$
$\mu^+\mu^-$	5.560	$0.0033 \pm 0.0004$	$0.0044 \pm 0.0005$	$0.0029 \pm 0.0004$
$ au^+ au^-$	1.844	$12.8351 \pm 0.0255$	$28.7692 \pm 0.0382$	$9.9371 \pm 0.0224$
$\gamma J/\psi$	1.260	$45.9222 \pm 0.0482$	$55.1722 \pm 0.0529$	$34.1250 \pm 0.0416$
$\gamma\gamma$	21.530	$0.0009 \pm 0.0002$	$0.0010\pm0.0002$	$0.0005 \pm 0.0002$
$2\gamma$	1.257	$2.4109 \pm 0.0110$	$4.6297 \pm 0.0153$	$1.6468 \pm 0.0091$
$\psi$ (2 $S$ ) $^{\dagger}$	0.150	$62.9891 \pm 0.0078$	$69.2882 \pm 0.0082$	$51.6942 \pm 0.0071$

 $^\dagger$ Contribution from  $\psi(2S)$  assumes standard Breit-Wigner shape

#### **Background Subtraction**

- Subtract backgrounds from total data events to get signal hadrons
  - Ignore negligible samples for extrapolation  $\{e^+e^-,\ \mu^+\mu^-,\ \gamma\gamma\}$

3650 (Old) Results

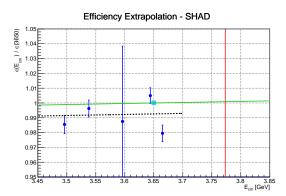
		\ /		
Sample	N <sub>had</sub> (SHAD)	N <sub>had</sub> (LHAD)	N <sub>had</sub> (THA	4D)
Data	$477001 \pm 691$	$546546 \pm 739$	375380 $\pm$	613
$e^+e^-{}^*$	$149 \pm 43$	$187 \pm 48$	12 $\pm$	12
$\mu^+\mu^-{}^*$	8 ± 1	$11\pm1$	$7 \pm$	1
$ au^+ au^-$	$10490\pm30$	$23514 \pm 59$	8122 $\pm$	25
$\gamma  extbf{ extit{J}}/\psi$	$25658 \pm 60$	$30826 \pm 71$	19067 $\pm$	46
$\gamma\gamma^*$	9 ± 2	$10\pm2$	4 $\pm$	1
$2\gamma$	1443 $\pm$ 7	$2771 \pm 11$	986 $\pm$	6
$\psi$ (2 ${\cal S})^{\dagger}$	4175 $\pm$ 9	$4593 \pm 10$	3427 $\pm$	7
Hadrons	$435234 \pm 694$	$484842 \pm 745$	343779 $\pm$	615

 $<sup>^\</sup>dagger$ Contribution from  $\psi(2S)$  assumes standard Breit-Wigner shape

### Efficiency Extrapolation

- Contribution of  $q\bar{q}$  events above  $D\bar{D}$  threshold not well modeled
  - Repeat procedure for new continuum data to extrapolate

$$\frac{\epsilon(E_{cm})}{\epsilon(3650)} = \left[\frac{N_{had}(E_{cm})}{N_{had}(3650)}\right] \left[\frac{\mathcal{L}(3650)}{\mathcal{L}(E_{cm})}\right] \left[\frac{E_{cm}}{3650}\right]^2$$



## Procedure for $\psi(3770)$ Data

- Repeat procedure for  $\psi(3770)$  data samples
  - ullet Use extrapolation to determine  $qar{q}$  background contribution
- Modify included backgrounds to account for  $D\overline{D}$  threshold
  - Use measurement of  $\psi(3770) o D\overline{D}$  cross section for  $D\overline{D}$  component
    - Use measurement from 'On-Peak' sample for initial exploration
  - Switch direct contribution from  $\psi(2S)$  to radiative decays  $(\gamma\psi(2S))$ 
    - Use measurements from CLEO-c and BESIII for cross section value
  - $\bullet$  Neglect  $2\gamma$  events due to minimal contribution in this region
- Need data-driven procedure to correctly determine  $D\overline{D}$  efficiencies
  - MC samples unreliable at modeling track multiplicities
  - Re-weight MC samples based off differences seen in data
    - Scale by track multiplicity ratios for data / MC

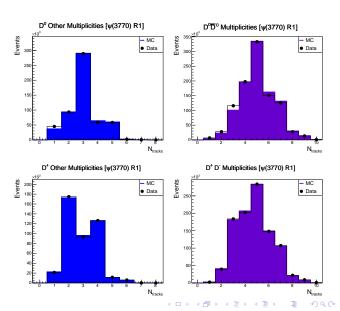
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## $D\overline{D}$ Efficiency Correction

Group	Multiplicity
SHAD	$N_{\rm tracks} > 2$
LHAD	$N_{ m tracks} > 1$
THAD	$N_{\rm tracks} > 3$

$\psi$ (3770) R1 - $D^0$		0) R1 - <i>D</i> <sup>0</sup>
	Group	$(\epsilon_{Data}/\epsilon_{MC})$
	SHAD	0.9751
	LHAD	0.9930
	THAD	0.9662
- 1		

$\psi$ (3770) R1 - $D^+$		
Group	$(\epsilon_{Data}/\epsilon_{MC})$	
SHAD	0.9992	
LHAD	1.0018	
THAD	1.0064	



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## Hadronic Counts - $\psi(3770)$ (R1)

$\psi$ (3770) (R1)	Reconstruction
--------------------	----------------

Sample	$\sigma$ [nb]	$\epsilon_{MC}$ (SHAD) [%]	$\epsilon_{MC}$ (LHAD) [%]	$\epsilon_{MC}$ (THAD) [%]
$\overline{D^0\overline{D^0}}$	3.615	$73.9324 \pm 0.0142$	$79.8496 \pm 0.0147$	$60.3601 \pm 0.0128$
$D^+D^-$	2.830	$61.4048 \pm 0.0146$	$68.8212 \pm 0.0154$	$49.4007 \pm 0.0131$
$ au^+ au^-$	2.652	$12.7566 \pm 0.0253$	$28.0142 \pm 0.0374$	$9.8776 \pm 0.0222$
$\gamma J/\psi$	0.986	$46.6185 \pm 0.0206$	$56.2494 \pm 0.0227$	$34.7544 \pm 0.0178$
$\gamma\psi$ (2 $S$ )	3.009	$63.2551 \pm 0.0137$	$69.9696 \pm 0.0144$	$51.5643 \pm 0.0123$

#### $\psi$ (3770) (R1) Results

Sample	N <sub>had</sub> (SHAD)	N <sub>had</sub> (LHAD)	N <sub>had</sub> (THAD)
Data	$15694505 \pm 3962$	$17722728 \pm 4210$	$12580701 \pm 3547$
$qar{q}^\dagger$	$8522688 \pm 71353$	$9330411 \pm 76320$	$6789405 \pm 61599$
$D^0\overline{D^0}$	$2477345 \pm 534$	$2675620 \pm 560$	$2022561 \pm 473$
$D^+D^-$	$1610764 \pm 414$	$1805311 \pm 442$	$1295875 \pm 366$
$ au^+ au^-$	$313542 \pm 622$	$688559 \pm 922$	$242781 \pm 547$
$\gamma  extcolor{J}/\psi$	$425891 \pm 193$	$513875 \pm 213$	$317504 \pm 166$
$\gamma\psi$ (2 $S$ )	$1764254 \pm 419$	$1951528 \pm 445$	$1438185 \pm 372$
Hadrons	$490569 \pm 71795$	$658730 \pm 76807$	$401064 \pm 61995$

## Initial Exploration of $\psi(3770)$ Data

- Convert hadronic signal to non- $D\overline{D}$  cross section
  - Assume efficiency is similar to that for  $\gamma\psi(2S)$  decays

$$\sigma(\psi(3770) o \mathsf{non-}D\overline{D}) = rac{N_{\mathsf{non-}D\overline{D}}}{\epsilon_{\mathsf{non-}D\overline{D}} imes \mathcal{L}}$$

Sample	$\sigma_{non\text{-}D\overline{D}}$ (SHAD)	$\sigma_{non ext{-}D\overline{D}}$ (LHAD)	$\sigma_{non ext{-}D\overline{D}}$ (THAD)
$\psi$ (3770) (R1)	$0.9892 \pm 0.1219$	$1.1679 \pm 0.1179$	$0.9925 \pm 0.1291$
$\psi$ (3770) (R2)	$1.0877 \pm 0.1224$	$1.2926 \pm 0.1183$	$1.1142 \pm 0.1298$
Lum. Weighted	$1.0563 \pm 0.1223$	$1.2528 \pm 0.1182$	$1.0754 \pm 0.1296$

- ullet Likely overestimated due to assumption of Breit-Wigner for  $\psi(2S)$
- ullet Convert cross section to branching fraction using  $D\overline{D}$  measurements

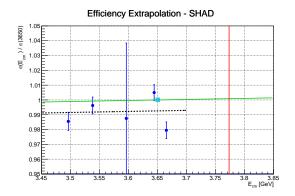
$$\Gamma(\psi(3770) o \mathsf{non-}D\overline{D}) = \frac{\sigma(\psi(3770) o \mathsf{non-}D\overline{D})}{\sigma(\psi(3770) o D\overline{D}) + \sigma(\psi(3770) o \mathsf{non-}D\overline{D})}$$

#### Begin exploratory analysis - NOT OFFICIAL MEASUREMENTS

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## Investigation I: Standard Breit-Wigner for $\psi(2S)$

- $\psi(2S)$  calculated as standard Breit-Wigner
- Significant drop in last point of efficiency ratio
- Upper bound for branching fraction



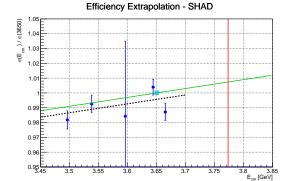
Sample	$BF_{\text{non-}D\overline{D}}$ (SHAD)	$BF_{\text{non-}D\overline{D}}$ (LHAD)	$BF_{\text{non-}D\overline{D}}$ (THAD)
$\psi$ (3770) (R1)	$0.1331 \pm 0.0183$	$0.1534 \pm 0.0185$	$0.1334 \pm 0.0190$
$\psi$ (3770) (R2)	$0.1444 \pm 0.0186$	$0.1671 \pm 0.0189$	$0.1474 \pm 0.0193$
Lum. Weighted	$0.1408 \pm 0.0185$	$0.1627 \pm 0.0187$	$0.1430 \pm 0.0192$

#### Investigation II: Continuum Ratio Estimation

•  $\psi(2S)$  approximated by

$$rac{\sigma_{
m res}}{\sigma_{
m cont}(E_{
m cm})} = rac{\sqrt{2\pi} \ (M_{
m res} - E_{
m cm})^2}{\Gamma_{
m res} imes \delta_{E_{
m cm}}}$$

- Use  $\sigma_{\psi(2S)}$  from BESIII
  - ullet  $\delta_{E_{
    m cm}}pprox 1.5\,{
    m MeV}$
- Estimated value for branching fraction



Sample	$BF_{\text{non-}D\overline{D}}$ (SHAD)	$BF_{\text{non-}D\overline{D}}$ (LHAD)	$BF_{\text{non-}D\overline{D}}$ (THAD)
$\psi$ (3770) (R1)	$0.1149 \pm 0.0180$	$0.1361 \pm 0.0181$	$0.1152 \pm 0.0188$
$\psi$ (3770) (R2)	$0.1267 \pm\ 0.0183$	$0.1504 \pm 0.0185$	$0.1297 \pm 0.0190$
Lum. Weighted	$0.1230 \pm 0.0182$	$0.1458 \pm 0.0183$	$0.1251 \pm 0.0190$

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## Investigation III: No $\psi(2S)$ Contribution

- $\psi(2S)$  ignored
- Inaccurate assumption
- Lower bound for branching fraction



Sample	$BF_{\text{non-}D\overline{D}}$ (SHAD)	$BF_{\text{non-}D\overline{D}}$ (LHAD)	$BF_{\text{non-}D\overline{D}}$ (THAD)
$\psi$ (3770) (R1)	$0.0876 \pm 0.0178$	$0.1102 \pm 0.0176$	$0.0878 \pm 0.0187$
$\psi$ (3770) (R2)	$0.1002 \pm 0.0180$	$0.1254 \pm 0.0179$	$0.1033 \pm 0.0188$
Lum. Weighted	$0.0962 \pm 0.0179$	$0.1205 \pm 0.0178$	$0.0983 \pm 0.0188$

## Conclusion

#### Conclusion

Result: Described  $\psi(3770) \rightarrow D\overline{D}$  cross section shape near  $\psi(3770)$ 

- Measured  $\psi(3770)$  parameters more precisely than ever before
  - Form factor model choice still major source of uncertainty
- Found clear indication for needing interference (Born level shape)
  - Reappearance above minimum impossible for non-interfering shapes
  - Splitting of  $m_{BC}$  peaks further validates behavior seen
- Explored progress on non- $D\overline{D}$  branching fraction (no official results)
  - Determined rough bounds on value through simple assumptions
  - ullet Precise  $\psi(2S)$  cross section allows for quickly updated measurement
  - ullet Data taking near  $\psi(2S)$  planned by BESIII for next year

# Backup Slides

#### Monte Carlo Generators

#### KKMC

- Used to model electroweak interactions:  $e^+e^- \rightarrow f\bar{f} + (n)\gamma$  $f = \{\mu^-, \tau^-, u, d, s, c, b\}$  and  $(n)\gamma = (additional photons)$
- ullet Decays  $far{f}$  pair based on involved fermions (TAUOLA, PYTHIA)
- Takes into account initial- and final-state radiation (ISR / FSR)
  - $\bullet$  For resonances, only handles ISR, then passes off  $\gamma^*$  to BesEvtGen

#### BesEvtGen

- Handles resonance decay as well as radiative effects
  - ullet Reduced  $E_{cm}$  such that only lower mass resonances can be produced
- Babayaga
  - Used to model QED processes:  $e^+e^- \to \{e^+e^-,\ \mu^+\mu^-,\ \gamma\gamma\}$
  - ullet Very accurate results; estimated theoretical uncertainty of 0.1 %
    - High precision required for determination of integrated luminosity

#### Selection Cuts

$\pi^\pm$ and ${\mathcal K}^\pm$ Selection			
Vertex $(xy)$ $V_{xy} < 1  \text{cm}$			
Vertex $(z)$ $ Vz  < 10 \mathrm{cm}$			
MDC Angle $ \cos \theta  < 0.93$			
Pion Probability	$P(\pi) > 0$ ,	$P(\pi) > P(K)$	
Kaon Probability	P(K) > 0	$P(K) > P(\pi)$	

#### $\gamma$ Selection

Min. Energy (Barrel)	$E_{EMC} > 25MeV$	$( \cos\theta <0.80)$
Min. Energy (Endcap)	$E_{EMC} > 50MeV$	$(0.84 <  \cos \theta  < 0.92)$
TDC Timing	$(0 \le t \le 14) \times 50  \mathrm{ns}$	

	$\pi^0  o \gamma \gamma$ Selection	$K_S^0  o \pi^+\pi^-$ Selection
Nominal Mass	$115 < m_{\pi^0} [{ m MeV}] < 150$	$487 < m_{K_c^0}[{ m MeV}] < 511$
Fit Quality	$\chi^2 <$ 200, Converged	$\chi^2 < 100$ , Converged

#### Hadronic Selection Event Cuts

Vertex (xy)	$V_{xy} < 1  \mathrm{cm}$
Vertex $(z)$	$ Vz  < 10  \mathrm{cm}$
MDC Angle	$ \cos  heta  < 0.93$

	$(0 \le t \le 14) \times 50 \mathrm{ns}$	
Minimum Energy (Endcap)	$F_{\text{EMC}} > 50 \text{MeV}$	$(0.86 <  \cos \theta  < 0.92)$
Minimum Energy (Barrel)	$E_{EMC} > 25MeV$	$( \cos \theta  < 0.80)$

Highest Energy	$\cos  heta_+^{ ext{max}} < 0.8$ $\cos  heta^{ ext{max}} > -0.8$	$(N_{\text{tracks}} = 2)$
	$\cos  heta_+^{ m max} < 0.8 \ { m or} \ (p/E_{ m cm})_+^{ m max} \leq 0.3 \ { m cos} \  heta^{ m max} > -0.8 \ { m or} \ (p/E_{ m cm})_+^{ m max} \leq 0.3$	$(N_{\text{tracks}} = 3, 4)$
Highest Momentum	$0.8 \le (E_{\text{EMC}}/p)_{+}^{\text{max}} \le 1.1$ $0.8 \le (E_{\text{EMC}}/p)_{-}^{\text{max}} \le 1.1$	

## Hadronic Selection Group Cuts (SHAD)

Number of Tracks	$N_{ m tracks} > 2$	
Visible Energy	$(E_{\rm vis}/E_{\rm cm})>0.3$	
Visible Momentum	$(p_{z\mathrm{vis}}/E_{\mathrm{vis}}) < 0.6$	$(N_{\text{tracks}}=3,4)$
Maximum Shower Energy	$(E_{ m EMC}^{ m max}/E_{ m beam}) < 0.75$	$(N_{tracks} = 3, 4)$
Total Shower Energy	$0.25 < (E_{ m EMC}^{ m tot}/E_{ m cm}) < 0.75$	$(N_{\text{tracks}} = 3)$
Total Shower Ellergy	$0.15 < (E_{ m EMC}^{ m tot}/E_{ m cm}) < 0.75$	$(N_{tracks} = 4)$

## Hadronic Selection Group Cuts (LHAD)

$N_{tracks} > 1$	
$(E_{ m vis}/E_{ m cm})>0.4$	$(N_{tracks} = 2)$
$(E_{ m vis}/E_{ m cm})>0.3$	$(N_{tracks} \geq 3)$
$(p_{z \text{ vis}}/E_{\text{vis}}) < 0.3$	$(N_{tracks} = 2)$
$(p_{z\mathrm{vis}}/E_{\mathrm{vis}}) < 0.6$	$(N_{tracks} = 3, 4)$
$(E_{ m EMC}^{ m max}/E_{ m beam}) < 0.50$	$(N_{tracks} = 2)$
$(E_{ m EMC}^{ m max}/E_{ m beam}) < 0.75$	$(N_{tracks} = 3, 4)$
$0.25 < (E_{ m EMC}^{ m tot}/E_{ m cm}) < 0.75$	$(N_{tracks} = 2, 3)$
$0.15 < (E_{ m EMC}^{ m tot}/E_{ m cm}) < 0.75$	$(N_{tracks} = 4)$
	$(E_{\rm vis}/E_{\rm cm}) > 0.4$ $(E_{\rm vis}/E_{\rm cm}) > 0.3$ $(p_{z{ m vis}}/E_{ m vis}) < 0.3$ $(p_{z{ m vis}}/E_{ m vis}) < 0.6$ $(E_{ m EMC}^{\rm max}/E_{ m beam}) < 0.50$ $(E_{ m EMC}^{\rm max}/E_{ m beam}) < 0.75$

## Hadronic Selection Group Cuts (THAD)

Number of Tracks	$N_{\rm tracks} > 3$	
Visible Energy	$(E_{ m vis}/E_{ m cm})>0.4$	
Visible Momentum	$(p_{z\mathrm{vis}}/E_{\mathrm{vis}}) < 0.6$	$(N_{\text{tracks}} = 4)$
Maximum Shower Energy	$(E_{ m EMC}^{ m max}/E_{ m beam}) < 0.75$	$(N_{tracks} = 4, 5)$
Total Shower Energy	$0.15 < (E_{ m EMC}^{ m  tot}/E_{ m cm}) < 0.75$	$(N_{\text{tracks}} = 4)$
Total Shower Ellergy	$0.00 < (E_{ m EMC}^{ m tot}/E_{ m cm}) < 0.75$	$(N_{tracks} = 5)$