



# Klotski Solver

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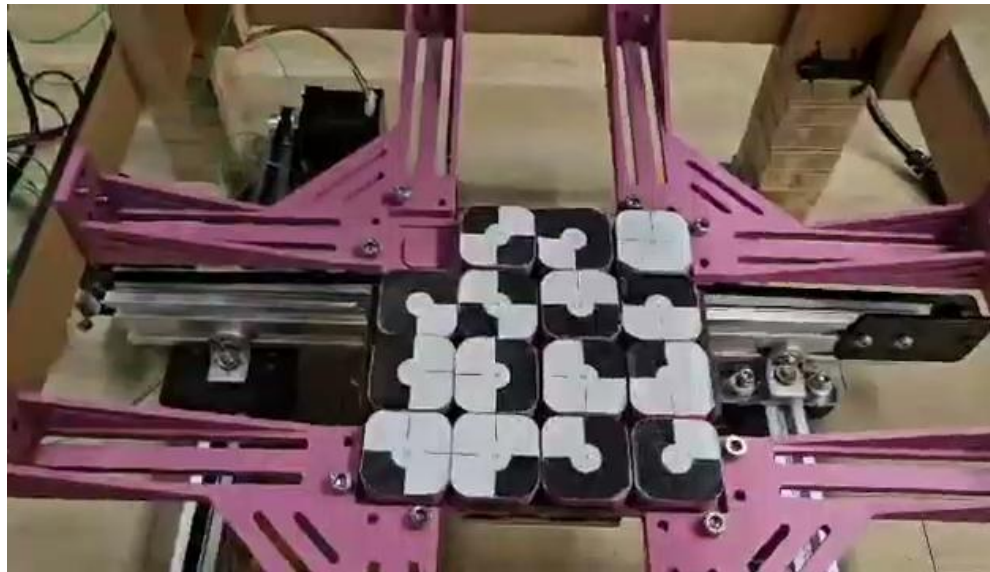
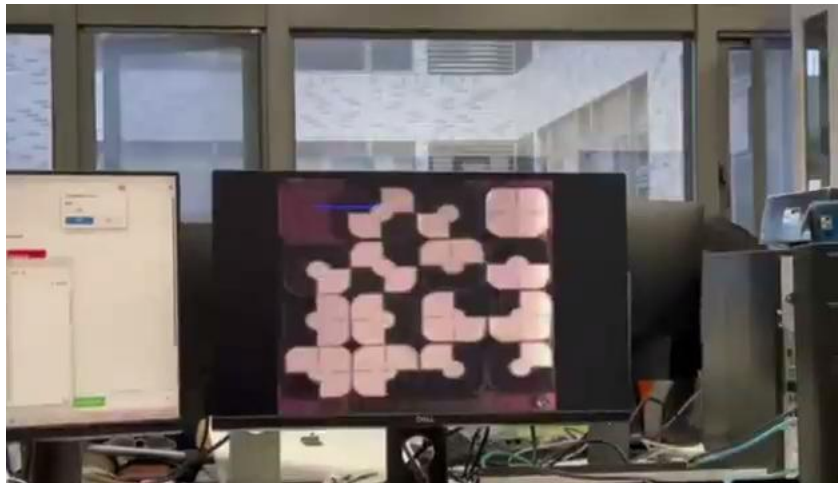
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# Objective

# Objective



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# Algorithm



# Overview

1	2		



## Overview

1	2		
			4



## Overview

1	2		3
			4





## Overview

1	2		3
			4



## Overview

1	2	3	4



## Overview

1	2	3	4
5	6		



## Overview

1	2	3	4
5	6		
			8



## Overview

1	2	3	4
5	6		7
			8



## Overview

1	2	3	4
5	6		7
			8



## Overview

1	2	3	4
5	6	7	8



## Overview

1	2	3	4
5	6	7	8
			13





## Overview

1	2	3	4
5	6	7	8
9			13



## Overview

1	2	3	4
5	6	7	8
9	13		



## Overview

1	2	3	4
5	6	7	8
9			
13			



## Overview

1	2	3	4
5	6	7	8
9			
13			14



## Overview

1	2	3	4
5	6	7	8
9			
13	10		14



## Overview

1	2	3	4
5	6	7	8
9			
13	10	14	



## Overview

1	2	3	4
5	6	7	8
9	10		
13	14		



## Overview

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	



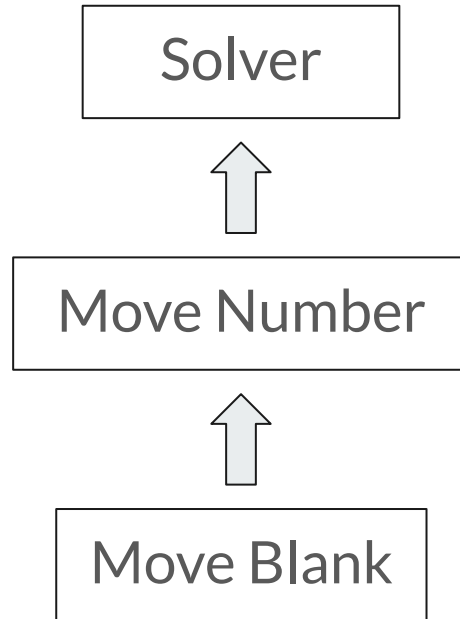


## Problem Formulation

- Instead of moving blocks, considering to move the blank.
- The blank has 4 possible moves.
- Divide and conquer by bottom-up method.

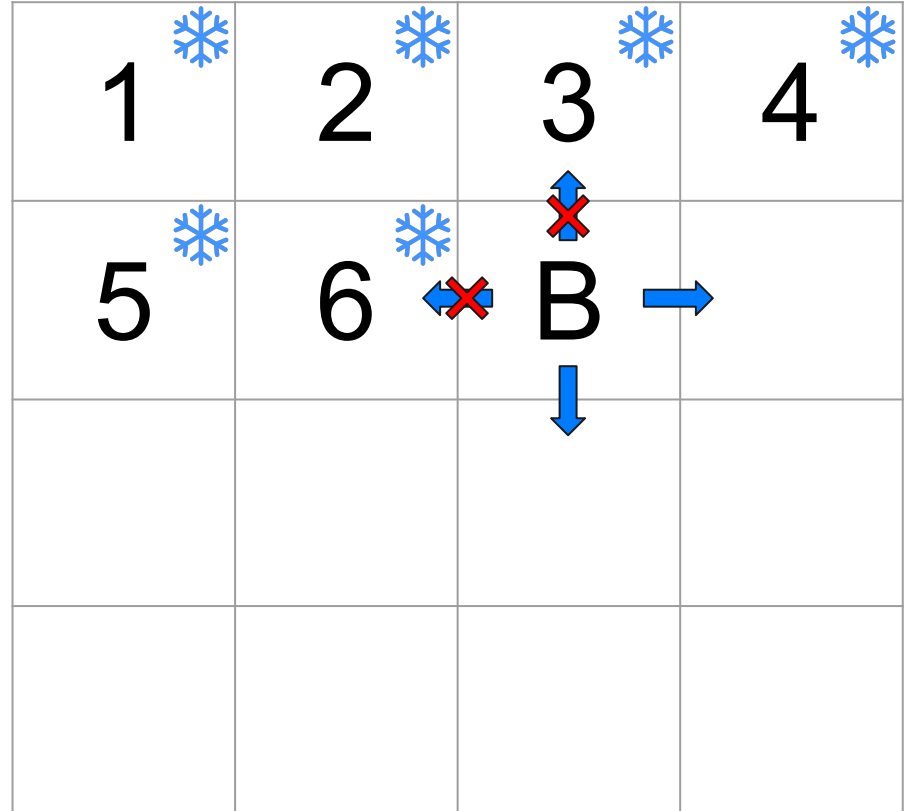


## Bottom-Up Method



## Move Blank

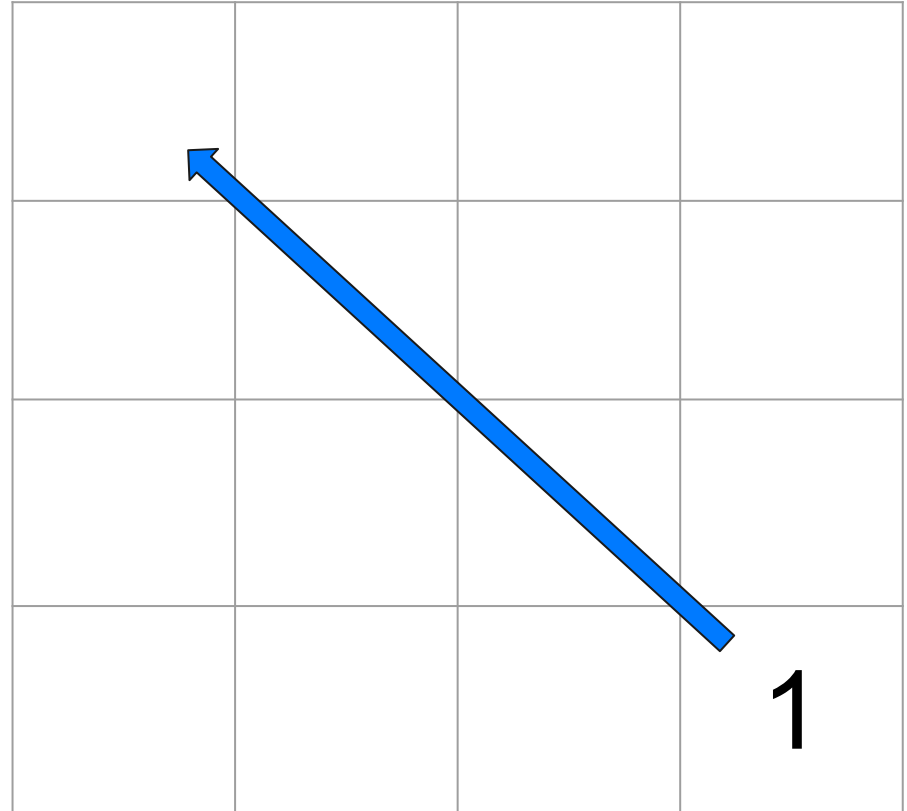
- 4 possible directions.
- Blocks at correct positions can't not be moved.  
-> Using mask to freeze blocks.





## Move Number

- Reuse “Move Blank”.





## Move Number

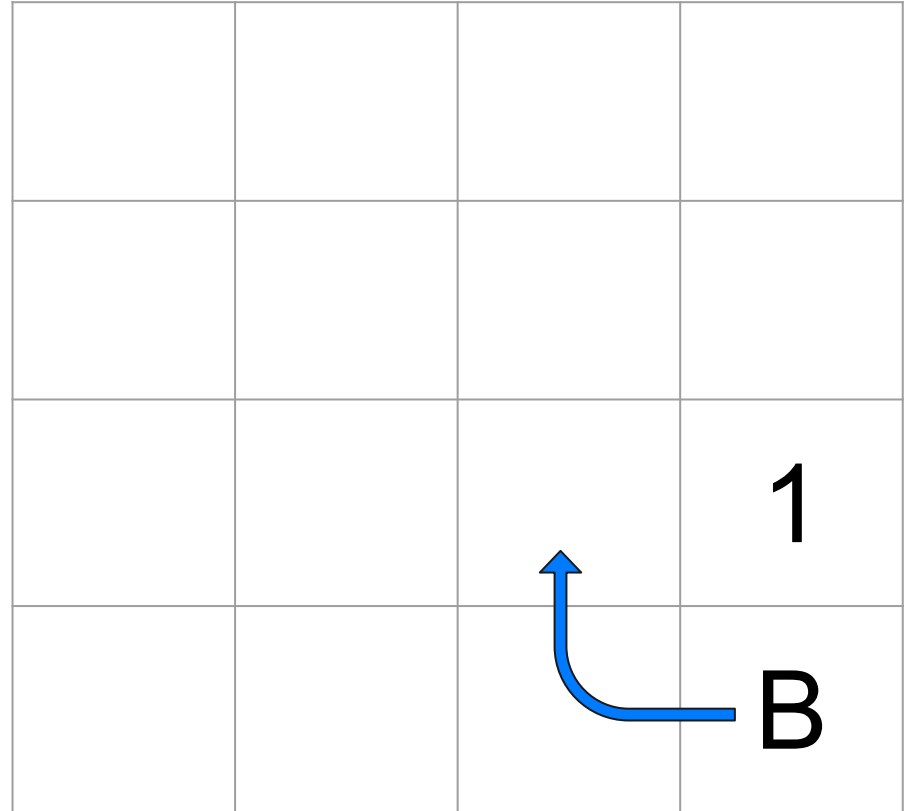
- Reuse “Move Blank”.

			B
			↓ 1



## Move Number

- Reuse “Move Blank”.





## Move Number

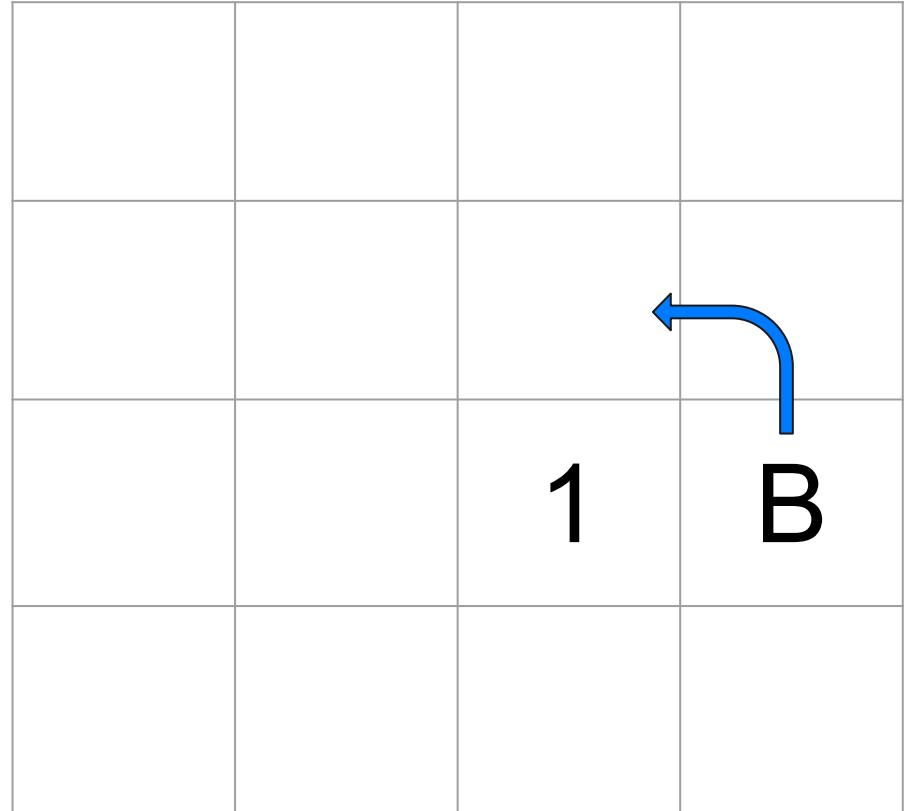
- Reuse “Move Blank”.

		B → 1	



## Move Number

- Reuse “Move Blank”.







## Move Number

- Reuse “Move Blank”.

		B	
		↓	
		1	



## Move Number

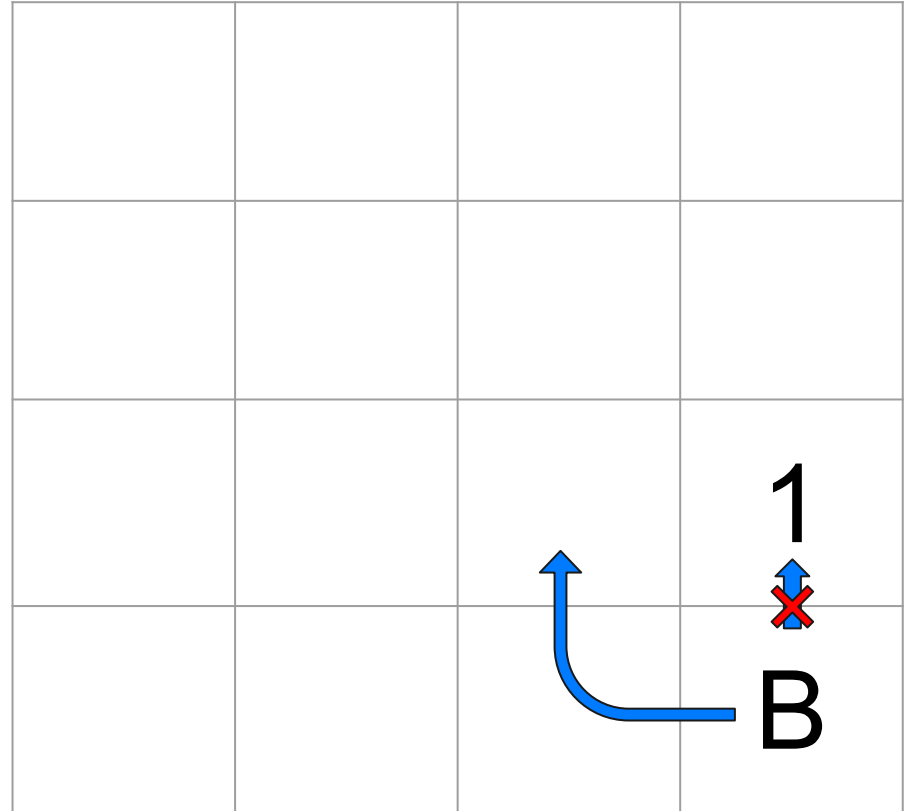
- Reuse “Move Blank”.

		1	
		B	



## Move Number: Issue 1

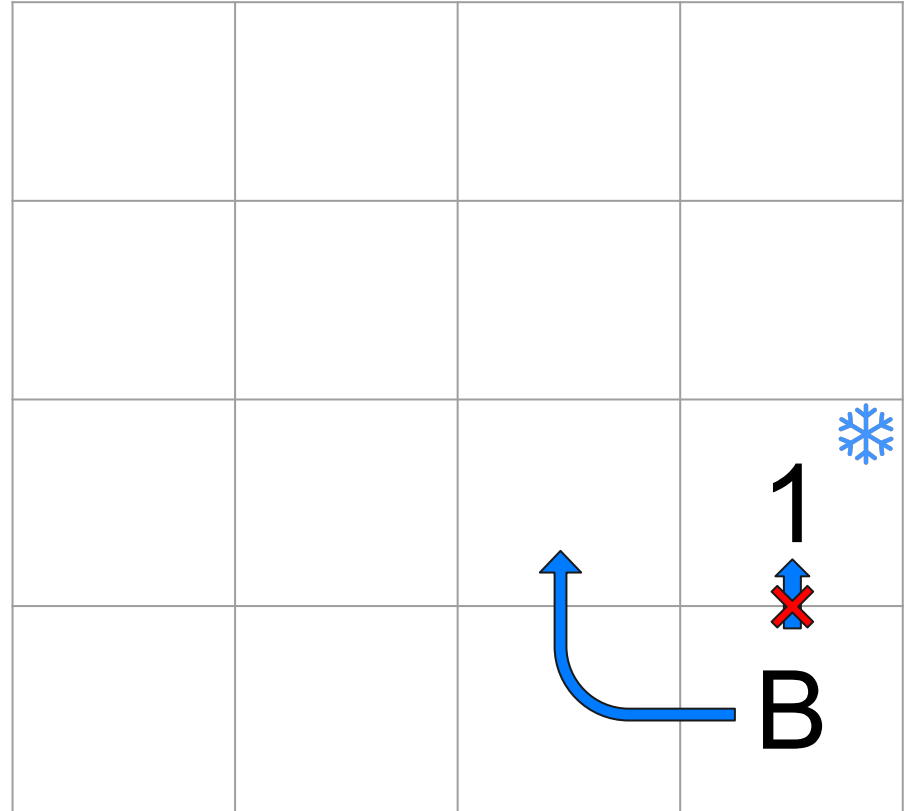
- The blank may move through  
The target number





## Move Number: Sol 1

- Freeze the target.





## Move Number: Sol 1-1

- Freeze the target.  
Then unfreeze it.

		B → 1	🔥



## Move Number: Sol 1-1





- Freeze the target.  
Then unfreeze it.

		1	B



## Move Number: Issue 2-1

- Mask may hinder other blocks.

1 	2 	3 	4 
5 	6 	7 	X
			
			B
			8



## Move Number: Sol 2-1

- Preserve space for others.







1 	2 	3 	4 
5 	6 		7 
			8 

Diagram illustrating a move sequence on a 4x4 grid. The grid contains numbers 1 through 8, each accompanied by a blue snowflake icon. A blue arrow points from the cell containing the number 7 to the cell containing the number 6, indicating a move.





## Move Number: Issue 2-2

- Blocks may be captured.

1 	2 	3 	4 
5 	6 	8 	7 
		 	
		B	















## Move Number: Sol 2-2

- Prevent the target blocks to be captured.

1 	2 	3 	4 
5 	6 		7 
			 8  

## Move Number: Issue 3













- At least two not frozen rows are needed for moving numbers.

1 	2 	3 	4 
5 	6 	7 	8 
9 	10 		
11 		13	



## Move Number: Sol 3

- Sort columns first.

1 	2 	3 	4 
5 	6 	7 	8 
9 			
13 	 10	 14	



## Solver

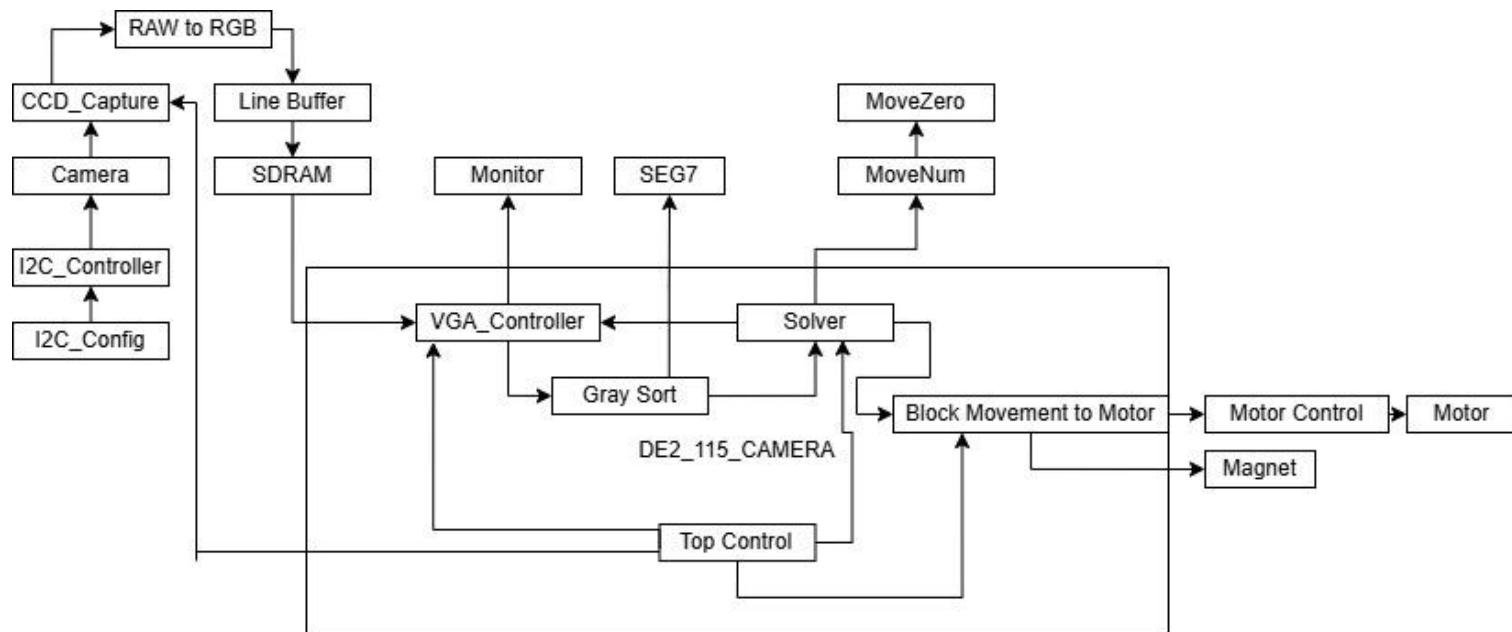
- From 1 to 15.
- Reuse “Move Number”.

3	12	9	5
7	13	14	1
15	4	6	2
10	11	8	

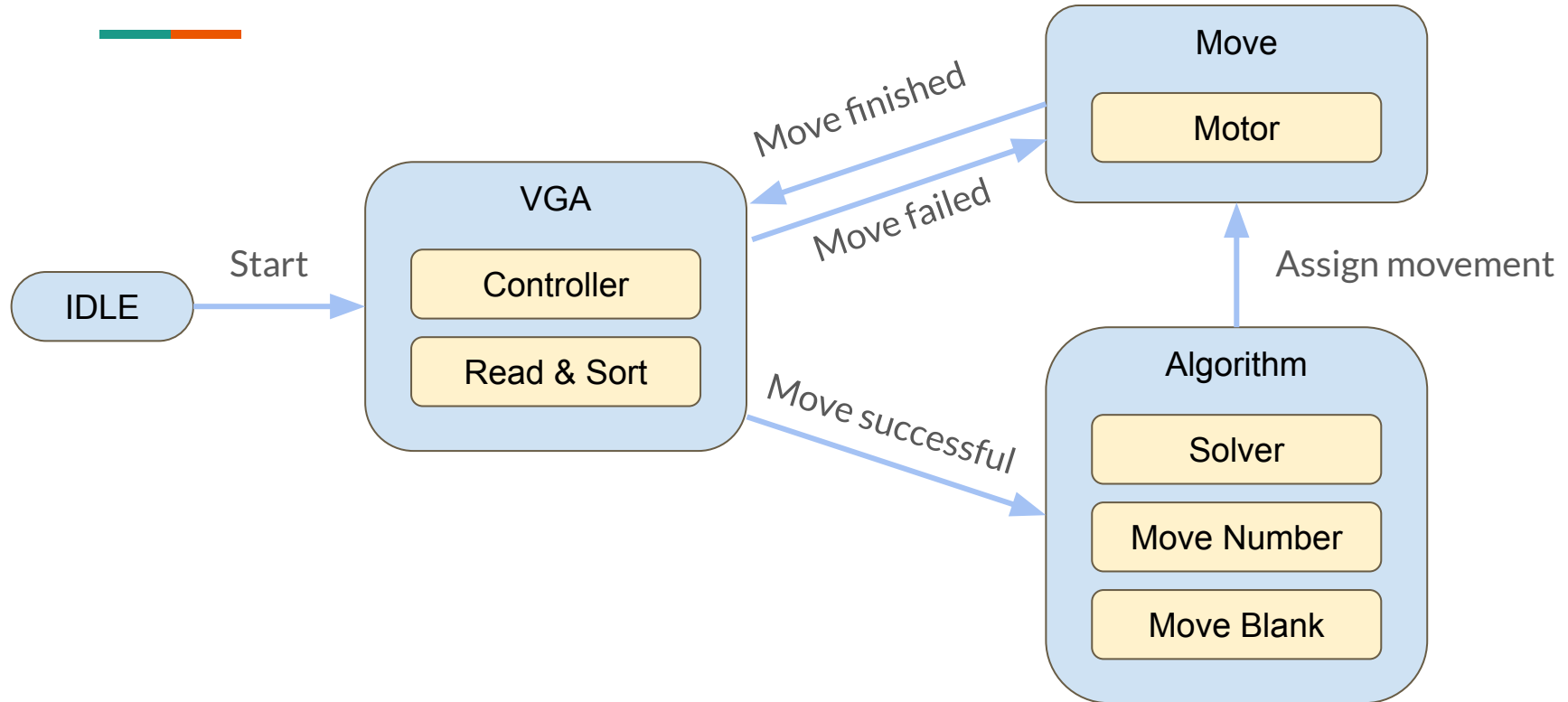


# Architecture

# Architecture

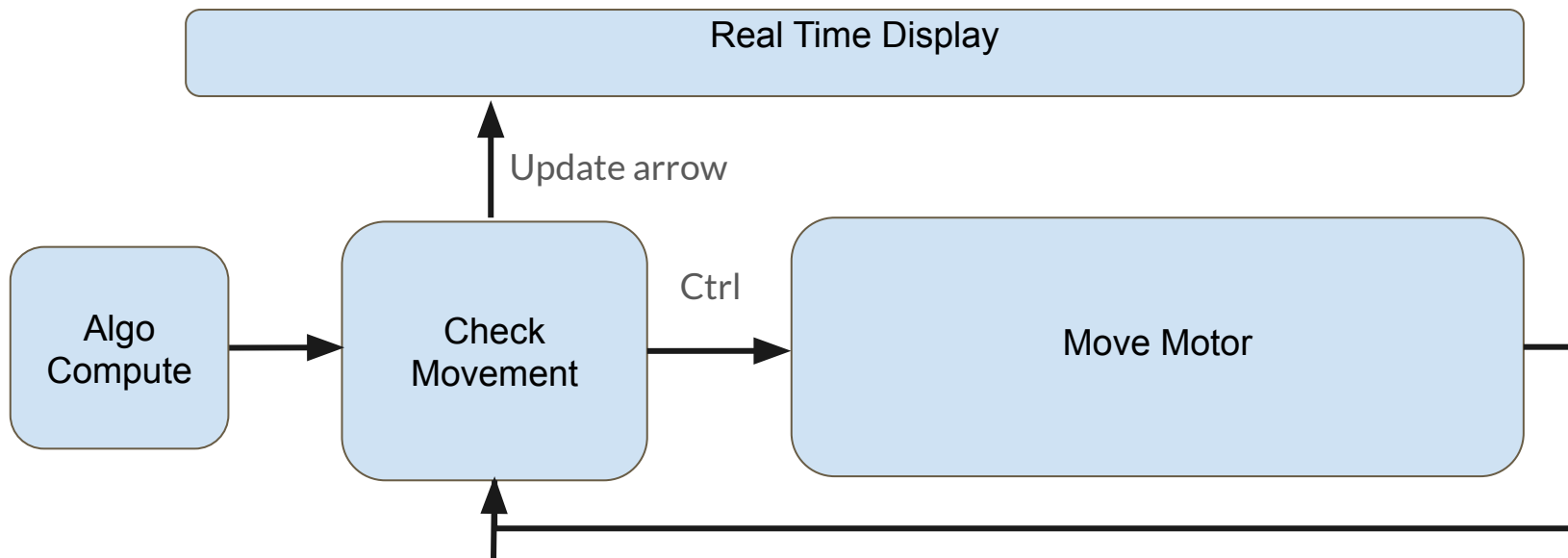


# Finite State Machine





# Time Flow



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# Testing



# Workflow



## Python

Use python to simulate the algorithm.

## Submodule

Use several testbenches to check the function.

## Top Module

## FPGA



## Python approach

```
# run "python solver.py for 1000 times"
for i in {1..1000}
do
    python solver.py
done
```

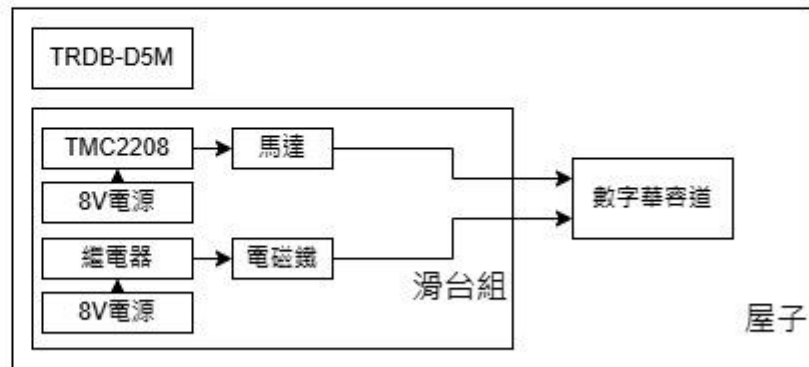
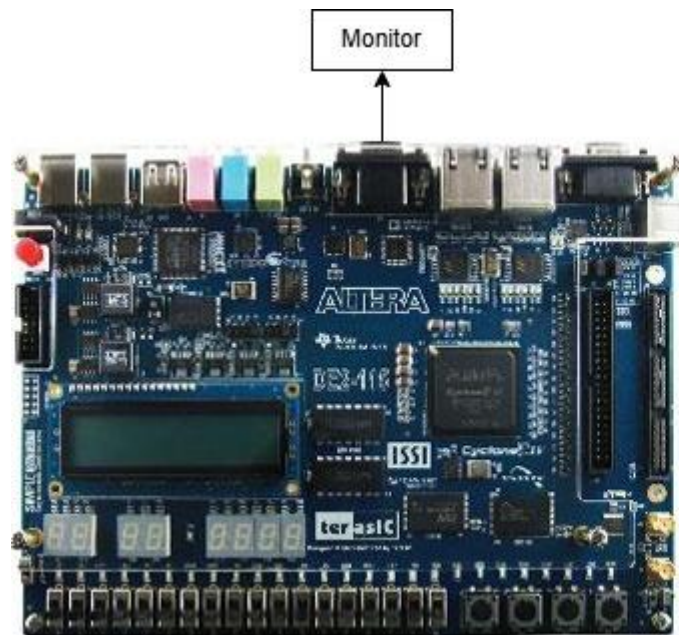
```
def main():
    # generate a random klotski
    klotski = np.random.permutation(16).reshape(4, 4)
    solve(klotski)
    print(klotski)

if __name__ == "__main__":
    main()
```

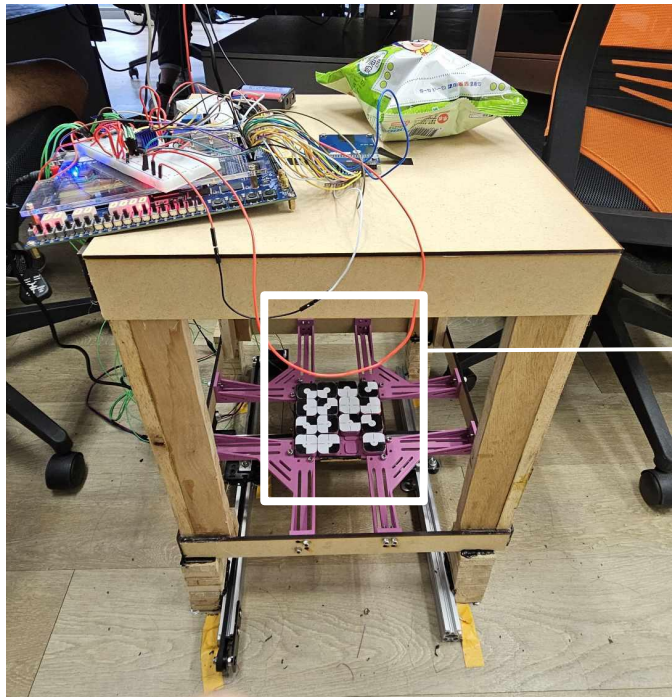
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# Implementation

# Hardware Resources

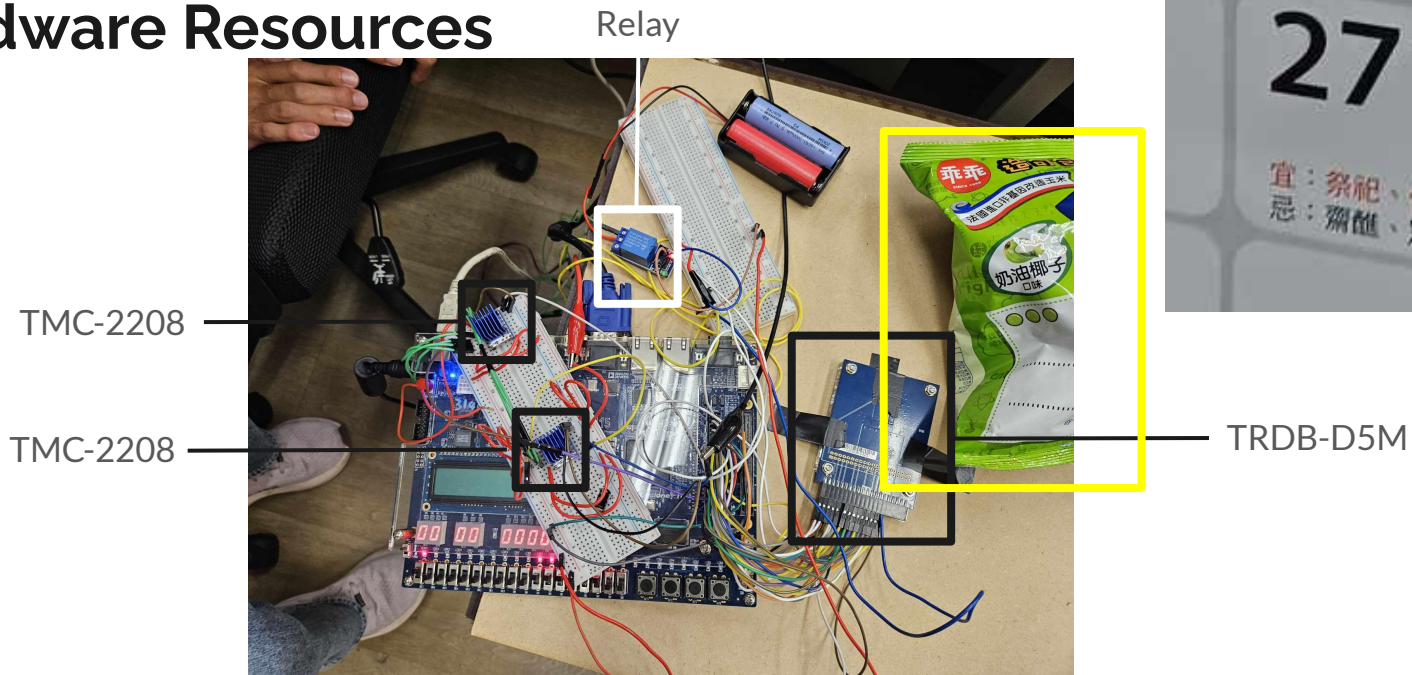


# Hardware Resources



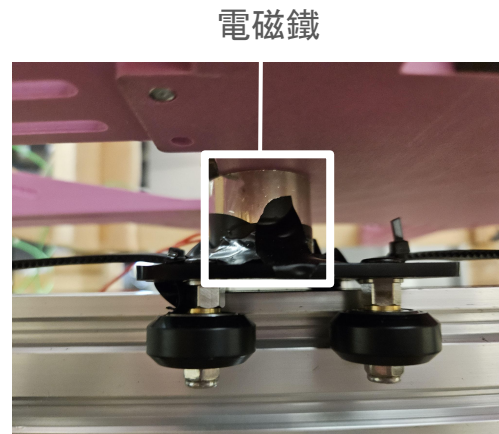
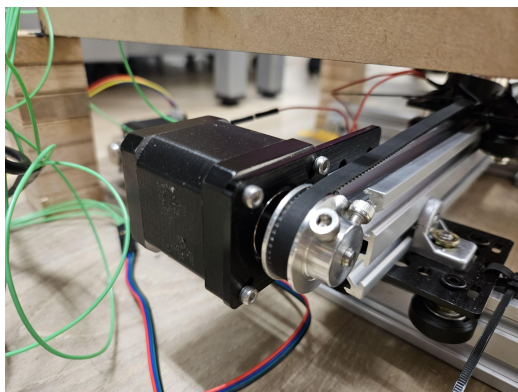
Klotski

# Hardware Resources



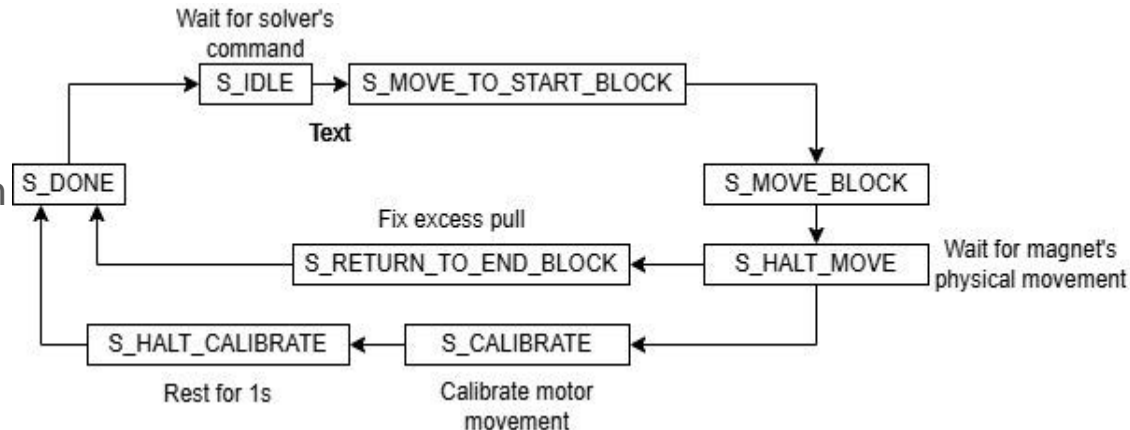


# Hardware Resources



# Function of Motor

1. Receive start block & end block from solver
2. Route Planning(avoid intervention between different movement)
3. Signal conversion
4. Excess tow & Rest
5. Automatic movement calibration





# klotski

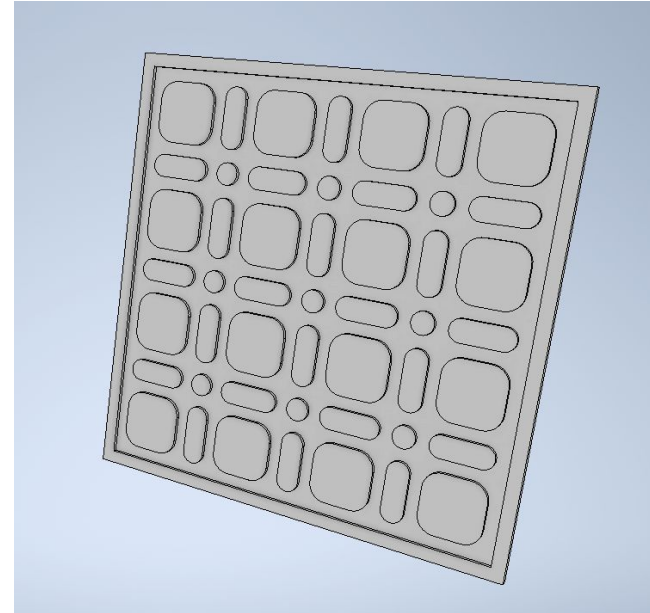
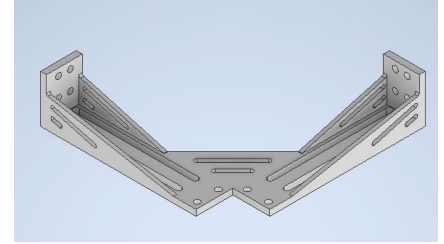
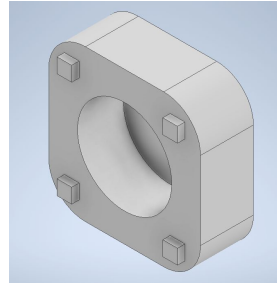
Issue 1: Rotation of cube when moving

Solve 1: Moving along the rail

Issue 2: Cubes stuck with each other

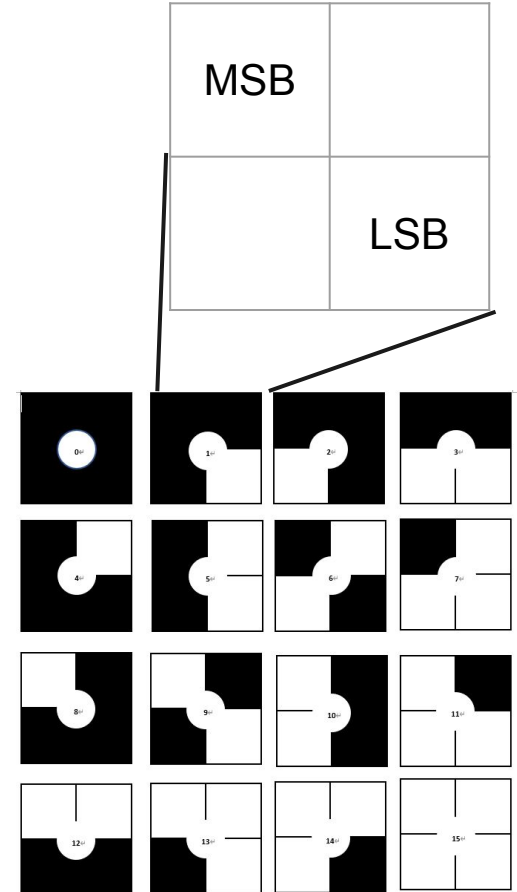
Solve 2: Corner rounded,

Sense whether a movement is correctly executed



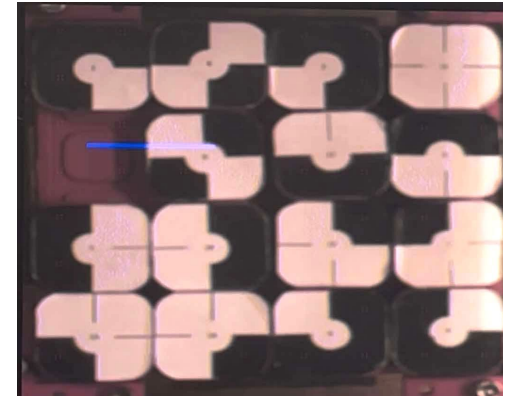
## Block Sensing

- Issue:  
Relative color is sensitive to relative brightness
- Use black and white to encode  
4 sample points in a session to increase accuracy
- Shift before Addition to reduce required register



## Block Sensing

- Use black and white to decode
  - Bayer pattern -> RGB
- Read **Green signal** to represent the block
- Use **blue arrow**, and thus no interference





## Novelty

- We proposed the algorithm for klotski.
- To handle failed moves, we use VGA to check if the position of the number is correct after every move.



## 參考資料

- DE2-115 User Manual: [https://www.terasic.com.tw/attachment/archive/502/DE2\\_115\\_User\\_manual.pdf](https://www.terasic.com.tw/attachment/archive/502/DE2_115_User_manual.pdf)
- TRDB-D5M User Manual : [https://www.terasic.com.tw/attachment/archive/281/TRDB\\_D5M\\_UserGuide.pdf](https://www.terasic.com.tw/attachment/archive/281/TRDB_D5M_UserGuide.pdf)
- A4988驱动NEMA步进电机(42步进电机)<http://www.taichi-maker.com/homepage/reference-index/motor-reference-index/arduino-a4988-nema-stepper-motor/>
- Arduino控制電磁鐵繼電器正確使用 | 智慧工廠專題 <https://www.youtube.com/watch?v=A4OWrq6dQNA>
- Real-Time-Image-Video-Dehazing <https://github.com/DCLAB08/Real-Time-Image-Video-Dehazing/tree/main>
- alhaitham-hardware <https://github.com/aabdelfattah/alhaitham-hardware>
- [Arduino 範例] 繼電器(Relay)的使用 <https://blog.imaker.com.tw/arduino-relay/>