

# APPENDIX A

## Statistical Tables

**Table 1: z Scores**

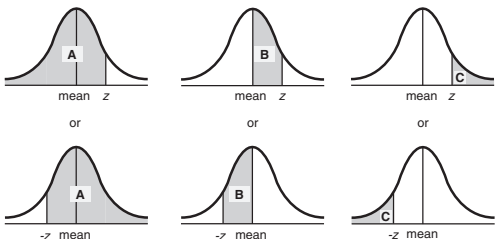
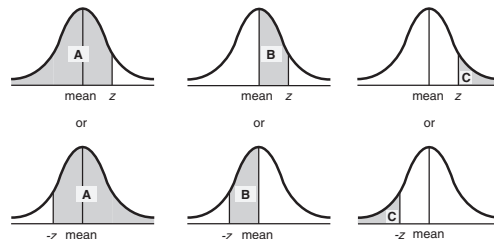
Area under the normal curve				Area under the normal curve			
							
A	B	C		A	B	C	
Below +z	From mean	Above +z		Below +z	From mean	Above +z	
z score	Above -z	to z or to -z	Below -z	z score	Above -z	to z or to -z	Below -z
0.00	50.00%	0.00%	50.00%	0.25	59.87%	9.87%	40.13%
0.01	50.40%	0.40%	49.60%	0.26	60.26%	10.26%	39.74%
0.02	50.80%	0.80%	49.20%	0.27	60.64%	10.64%	39.36%
0.03	51.20%	1.20%	48.80%	0.28	61.03%	11.03%	38.97%
0.04	51.60%	1.60%	48.40%	0.29	61.41%	11.41%	38.59%
0.05	51.99%	1.99%	48.01%	0.30	61.79%	11.79%	38.21%
0.06	52.39%	2.39%	47.61%	0.31	62.17%	12.17%	37.83%
0.07	52.79%	2.79%	47.21%	0.32	62.55%	12.55%	37.45%
0.08	53.19%	3.19%	46.81%	0.33	62.93%	12.93%	37.07%
0.09	53.59%	3.59%	46.41%	0.34	63.31%	13.31%	36.69%
0.10	53.98%	3.98%	46.02%	0.35	63.68%	13.68%	36.32%
0.11	54.38%	4.38%	45.62%	0.36	64.06%	14.06%	35.94%
0.12	54.78%	4.78%	45.22%	0.37	64.43%	14.43%	35.57%
0.13	55.17%	5.17%	44.83%	0.38	64.80%	14.80%	35.20%
0.14	55.57%	5.57%	44.43%	0.39	65.17%	15.17%	34.83%
0.15	55.96%	5.96%	44.04%	0.40	65.54%	15.54%	34.46%
0.16	56.36%	6.36%	43.64%	0.41	65.91%	15.91%	34.09%
0.17	56.75%	6.75%	43.25%	0.42	66.28%	16.28%	33.72%
0.18	57.14%	7.14%	42.86%	0.43	66.64%	16.64%	33.36%
0.19	57.53%	7.53%	42.47%	0.44	67.00%	17.00%	33.00%
0.20	57.93%	7.93%	42.07%	0.45	67.36%	17.36%	32.64%
0.21	58.32%	8.32%	41.68%	0.46	67.72%	17.72%	32.28%
0.22	58.71%	8.71%	41.29%	0.47	68.08%	18.08%	31.92%
0.23	59.10%	9.10%	40.90%	0.48	68.44%	18.44%	31.56%
0.24	59.48%	9.48%	40.52%	0.49	68.79%	18.79%	31.21%

Table 1: z Scores (continued)

z score	A	B	C	z score	A	B	C
	Below +z Above -z	From mean to z or to -z	Above +z Below -z		Below +z Above -z	From mean to z or to -z	Above +z Below -z
0.50	69.15%	19.15%	30.85%	0.87	80.78%	30.78%	19.22%
0.51	69.50%	19.50%	30.50%	0.88	81.06%	31.06%	18.94%
0.52	69.85%	19.85%	30.15%	0.89	81.33%	31.33%	18.67%
0.53	70.19%	20.19%	29.81%	0.90	81.59%	31.59%	18.41%
0.54	70.54%	20.54%	29.46%	0.91	81.86%	31.86%	18.14%
0.55	70.88%	20.88%	29.12%	0.92	82.12%	32.12%	17.88%
0.56	71.23%	21.23%	28.77%	0.93	82.38%	32.38%	17.62%
0.57	71.57%	21.57%	28.43%	0.94	82.64%	32.64%	17.36%
0.58	71.90%	21.90%	28.10%	0.95	82.89%	32.89%	17.11%
0.59	72.24%	22.24%	27.76%	0.96	83.15%	33.15%	16.85%
0.60	72.57%	22.57%	27.43%	0.97	83.40%	33.40%	16.60%
0.61	72.91%	22.91%	27.09%	0.98	83.65%	33.65%	16.35%
0.62	73.24%	23.24%	26.76%	0.99	83.89%	33.89%	16.11%
0.63	73.57%	23.57%	26.43%	1.00	84.13%	34.13%	15.87%
0.64	73.89%	23.89%	26.11%	1.01	84.38%	34.38%	15.62%
0.65	74.22%	24.22%	25.78%	1.02	84.61%	34.61%	15.39%
0.66	74.54%	24.54%	25.46%	1.03	84.85%	34.85%	15.15%
0.67	74.86%	24.86%	25.14%	1.04	85.08%	35.08%	14.92%
0.68	75.17%	25.17%	24.83%	1.05	85.31%	35.31%	14.69%
0.69	75.49%	25.49%	24.51%	1.06	85.54%	35.54%	14.46%
0.70	75.80%	25.80%	24.20%	1.07	85.77%	35.77%	14.23%
0.71	76.11%	26.11%	23.89%	1.08	85.99%	35.99%	14.01%
0.72	76.42%	26.42%	23.58%	1.09	86.21%	36.21%	13.79%
0.73	76.73%	26.73%	23.27%	1.10	86.43%	36.43%	13.57%
0.74	77.04%	27.04%	22.96%	1.11	86.65%	36.65%	13.35%
0.75	77.34%	27.34%	22.66%	1.12	86.86%	36.86%	13.14%
0.76	77.64%	27.64%	22.36%	1.13	87.08%	37.08%	12.92%
0.77	77.94%	27.94%	22.06%	1.14	87.29%	37.29%	12.71%
0.78	78.23%	28.23%	21.77%	1.15	87.49%	37.49%	12.51%
0.79	78.52%	28.52%	21.48%	1.16	87.70%	37.70%	12.30%
0.80	78.81%	28.81%	21.19%	1.17	87.90%	37.90%	12.10%
0.81	79.10%	29.10%	20.90%	1.18	88.10%	38.10%	11.90%
0.82	79.39%	29.39%	20.61%	1.19	88.30%	38.30%	11.70%
0.83	79.67%	29.67%	20.33%	1.20	88.49%	38.49%	11.51%
0.84	79.95%	29.95%	20.05%	1.21	88.69%	38.69%	11.31%
0.85	80.23%	30.23%	19.77%	1.22	88.88%	38.88%	11.12%
0.86	80.51%	30.51%	19.49%	1.23	89.07%	39.07%	10.93%

	<b>A</b>				<b>A</b>		
	<b>Below +z</b>	<b>From mean</b>	<b>Above +z</b>		<b>Below +z</b>	<b>From mean</b>	<b>Above +z</b>
<b>z score</b>	<b>Above -z</b>	<b>to z or to -z</b>	<b>Below -z</b>	<b>z score</b>	<b>Above -z</b>	<b>to z or to -z</b>	<b>Below -z</b>
<b>1.24</b>	89.25%	39.25%	10.75%	<b>1.61</b>	94.63%	44.63%	5.37%
<b>1.25</b>	89.44%	39.44%	10.56%	<b>1.62</b>	94.74%	44.74%	5.26%
<b>1.26</b>	89.62%	39.62%	10.38%	<b>1.63</b>	94.84%	44.84%	5.16%
<b>1.27</b>	89.80%	39.80%	10.20%	<b>1.64</b>	94.95%	44.95%	5.05%
<b>1.28</b>	89.97%	39.97%	10.03%	<b>1.65</b>	95.05%	45.05%	4.95%
<b>1.29</b>	90.15%	40.15%	9.85%	<b>1.66</b>	95.15%	45.15%	4.85%
<b>1.30</b>	90.32%	40.32%	9.68%	<b>1.67</b>	95.25%	45.25%	4.75%
<b>1.31</b>	90.49%	40.49%	9.51%	<b>1.68</b>	95.35%	45.35%	4.65%
<b>1.32</b>	90.66%	40.66%	9.34%	<b>1.69</b>	95.45%	45.45%	4.55%
<b>1.33</b>	90.82%	40.82%	9.18%	<b>1.70</b>	95.54%	45.54%	4.46%
<b>1.34</b>	90.99%	40.99%	9.01%	<b>1.71</b>	95.64%	45.64%	4.36%
<b>1.35</b>	91.15%	41.15%	8.85%	<b>1.72</b>	95.73%	45.73%	4.27%
<b>1.36</b>	91.31%	41.31%	8.69%	<b>1.73</b>	95.82%	45.82%	4.18%
<b>1.37</b>	91.47%	41.47%	8.53%	<b>1.74</b>	95.91%	45.91%	4.09%
<b>1.38</b>	91.62%	41.62%	8.38%	<b>1.75</b>	95.99%	45.99%	4.01%
<b>1.39</b>	91.77%	41.77%	8.23%	<b>1.76</b>	96.08%	46.08%	3.92%
<b>1.40</b>	91.92%	41.92%	8.08%	<b>1.77</b>	96.16%	46.16%	3.84%
<b>1.41</b>	92.07%	42.07%	7.93%	<b>1.78</b>	96.25%	46.25%	3.75%
<b>1.42</b>	92.22%	42.22%	7.78%	<b>1.79</b>	96.33%	46.33%	3.67%
<b>1.43</b>	92.36%	42.36%	7.64%	<b>1.80</b>	96.41%	46.41%	3.59%
<b>1.44</b>	92.51%	42.51%	7.49%	<b>1.81</b>	96.49%	46.49%	3.51%
<b>1.45</b>	92.65%	42.65%	7.35%	<b>1.82</b>	96.56%	46.56%	3.44%
<b>1.46</b>	92.79%	42.79%	7.21%	<b>1.83</b>	96.64%	46.64%	3.36%
<b>1.47</b>	92.92%	42.92%	7.08%	<b>1.84</b>	96.71%	46.71%	3.29%
<b>1.48</b>	93.06%	43.06%	6.94%	<b>1.85</b>	96.78%	46.78%	3.22%
<b>1.49</b>	93.19%	43.19%	6.81%	<b>1.86</b>	96.86%	46.86%	3.14%
<b>1.50</b>	93.32%	43.32%	6.68%	<b>1.87</b>	96.93%	46.93%	3.07%
<b>1.51</b>	93.45%	43.45%	6.55%	<b>1.88</b>	96.99%	46.99%	3.01%
<b>1.52</b>	93.57%	43.57%	6.43%	<b>1.89</b>	97.06%	47.06%	2.94%
<b>1.53</b>	93.70%	43.70%	6.30%	<b>1.90</b>	97.13%	47.13%	2.87%
<b>1.54</b>	93.82%	43.82%	6.18%	<b>1.91</b>	97.19%	47.19%	2.81%
<b>1.55</b>	93.94%	43.94%	6.06%	<b>1.92</b>	97.26%	47.26%	2.74%
<b>1.56</b>	94.06%	44.06%	5.94%	<b>1.93</b>	97.32%	47.32%	2.68%
<b>1.57</b>	94.18%	44.18%	5.82%	<b>1.94</b>	97.38%	47.38%	2.62%
<b>1.58</b>	94.29%	44.29%	5.71%	<b>1.95</b>	97.44%	47.44%	2.56%
<b>1.59</b>	94.41%	44.41%	5.59%	<b>1.96</b>	97.50%	47.50%	2.50%
<b>1.60</b>	94.52%	44.52%	5.48%	<b>1.97</b>	97.56%	47.56%	2.44%

Table 1: z Scores (continued)

z score	A	B	C	z score	A	B	C
	Below +z Above -z	From mean to z or to -z	Above +z Below -z		Below +z Above -z	From mean to z or to -z	Above +z Below -z
1.98	97.61%	47.61%	2.39%	2.35	99.06%	49.06%	0.94%
1.99	97.67%	47.67%	2.33%	2.36	99.09%	49.09%	0.91%
2.00	97.72%	47.72%	2.28%	2.37	99.11%	49.11%	0.89%
2.01	97.78%	47.78%	2.22%	2.38	99.13%	49.13%	0.87%
2.02	97.83%	47.83%	2.17%	2.39	99.16%	49.16%	0.84%
2.03	97.88%	47.88%	2.12%	2.40	99.18%	49.18%	0.82%
2.04	97.93%	47.93%	2.07%	2.41	99.20%	49.20%	0.80%
2.05	97.98%	47.98%	2.02%	2.42	99.22%	49.22%	0.78%
2.06	98.03%	48.03%	1.97%	2.43	99.25%	49.25%	0.75%
2.07	98.08%	48.08%	1.92%	2.44	99.27%	49.27%	0.73%
2.08	98.12%	48.12%	1.88%	2.45	99.29%	49.29%	0.71%
2.09	98.17%	48.17%	1.83%	2.46	99.31%	49.31%	0.69%
2.10	98.21%	48.21%	1.79%	2.47	99.32%	49.32%	0.68%
2.11	98.26%	48.26%	1.74%	2.48	99.34%	49.34%	0.66%
2.12	98.30%	48.30%	1.70%	2.49	99.36%	49.36%	0.64%
2.13	98.34%	48.34%	1.66%	2.50	99.38%	49.38%	0.62%
2.14	98.38%	48.38%	1.62%	2.51	99.40%	49.40%	0.60%
2.15	98.42%	48.42%	1.58%	2.52	99.41%	49.41%	0.59%
2.16	98.46%	48.46%	1.54%	2.53	99.43%	49.43%	0.57%
2.17	98.50%	48.50%	1.50%	2.54	99.45%	49.45%	0.55%
2.18	98.54%	48.54%	1.46%	2.55	99.46%	49.46%	0.54%
2.19	98.57%	48.57%	1.43%	2.56	99.48%	49.48%	0.52%
2.20	98.61%	48.61%	1.39%	2.57	99.49%	49.49%	0.51%
2.21	98.64%	48.64%	1.36%	2.58	99.51%	49.51%	0.49%
2.22	98.68%	48.68%	1.32%	2.59	99.52%	49.52%	0.48%
2.23	98.71%	48.71%	1.29%	2.60	99.53%	49.53%	0.47%
2.24	98.75%	48.75%	1.25%	2.61	99.55%	49.55%	0.45%
2.25	98.78%	48.78%	1.22%	2.62	99.56%	49.56%	0.44%
2.26	98.81%	48.81%	1.19%	2.63	99.57%	49.57%	0.43%
2.27	98.84%	48.84%	1.16%	2.64	99.59%	49.59%	0.41%
2.28	98.87%	48.87%	1.13%	2.65	99.60%	49.60%	0.40%
2.29	98.90%	48.90%	1.10%	2.66	99.61%	49.61%	0.39%
2.30	98.93%	48.93%	1.07%	2.67	99.62%	49.62%	0.38%
2.31	98.96%	48.96%	1.04%	2.68	99.63%	49.63%	0.37%
2.32	98.98%	48.98%	1.02%	2.69	99.64%	49.64%	0.36%
2.33	99.01%	49.01%	0.99%	2.70	99.65%	49.65%	0.35%
2.34	99.04%	49.04%	0.96%	2.71	99.66%	49.66%	0.34%

z score	A	B	C	z score	A	B	C
	Below +z Above -z	From mean to z or to -z	Above +z Below -z		Below +z Above -z	From mean to z or to -z	Above +z Below -z
2.72	99.67%	49.67%	0.33%	3.09	99.900%	49.900%	0.100%
2.73	99.68%	49.68%	0.32%	3.10	99.903%	49.903%	0.097%
2.74	99.69%	49.69%	0.31%	3.11	99.906%	49.906%	0.094%
2.75	99.702%	49.702%	0.298%	3.12	99.910%	49.910%	0.090%
2.76	99.711%	49.711%	0.289%	3.13	99.913%	49.913%	0.087%
2.77	99.720%	49.720%	0.280%	3.14	99.916%	49.916%	0.084%
2.78	99.728%	49.728%	0.272%	3.15	99.918%	49.918%	0.082%
2.79	99.736%	49.736%	0.264%	3.16	99.921%	49.921%	0.079%
2.80	99.744%	49.744%	0.256%	3.17	99.924%	49.924%	0.076%
2.81	99.752%	49.752%	0.248%	3.18	99.926%	49.926%	0.074%
2.82	99.760%	49.760%	0.240%	3.19	99.929%	49.929%	0.071%
2.83	99.767%	49.767%	0.233%	3.20	99.931%	49.931%	0.069%
2.84	99.774%	49.774%	0.226%	3.21	99.934%	49.934%	0.066%
2.85	99.781%	49.781%	0.219%	3.22	99.936%	49.936%	0.064%
2.86	99.788%	49.788%	0.212%	3.23	99.938%	49.938%	0.062%
2.87	99.795%	49.795%	0.205%	3.24	99.940%	49.940%	0.060%
2.88	99.801%	49.801%	0.199%	3.25	99.942%	49.942%	0.058%
2.89	99.807%	49.807%	0.193%	3.26	99.944%	49.944%	0.056%
2.90	99.813%	49.813%	0.187%	3.27	99.946%	49.946%	0.054%
2.91	99.819%	49.819%	0.181%	3.28	99.948%	49.948%	0.052%
2.92	99.825%	49.825%	0.175%	3.29	99.950%	49.950%	0.050%
2.93	99.831%	49.831%	0.169%	3.30	99.952%	49.952%	0.048%
2.94	99.836%	49.836%	0.164%	3.31	99.953%	49.953%	0.047%
2.95	99.841%	49.841%	0.159%	3.32	99.955%	49.955%	0.045%
2.96	99.846%	49.846%	0.154%	3.33	99.957%	49.957%	0.043%
2.97	99.851%	49.851%	0.149%	3.34	99.958%	49.958%	0.042%
2.98	99.856%	49.856%	0.144%	3.35	99.960%	49.960%	0.040%
2.99	99.861%	49.861%	0.139%	3.36	99.961%	49.961%	0.039%
3.00	99.865%	49.865%	0.135%	3.37	99.962%	49.962%	0.038%
3.01	99.869%	49.869%	0.131%	3.38	99.964%	49.964%	0.036%
3.02	99.874%	49.874%	0.126%	3.39	99.965%	49.965%	0.035%
3.03	99.878%	49.878%	0.122%	3.40	99.966%	49.966%	0.034%
3.04	99.882%	49.882%	0.118%	3.41	99.968%	49.968%	0.032%
3.05	99.886%	49.886%	0.114%	3.42	99.969%	49.969%	0.031%
3.06	99.889%	49.889%	0.111%	3.43	99.970%	49.970%	0.030%
3.07	99.893%	49.893%	0.107%	3.44	99.971%	49.971%	0.029%
3.08	99.896%	49.896%	0.104%	3.45	99.972%	49.972%	0.028%

Table 1: z Scores (continued)

A				A			
Below +z		From mean	Above +z	Below +z		From mean	Above +z
z score	Above -z	to z or to -z	Below -z	z score	Above -z	to z or to -z	Below -z
3.46	99.973%	49.973%	0.027%	3.79	99.9925%	49.9925%	0.0075%
3.47	99.974%	49.974%	0.026%	3.80	99.9928%	49.9928%	0.0072%
3.48	99.975%	49.975%	0.025%	3.81	99.9931%	49.9931%	0.0069%
3.49	99.976%	49.976%	0.024%	3.82	99.9933%	49.9933%	0.0067%
3.50	99.9767%	49.9767%	0.0233%	3.83	99.9936%	49.9936%	0.0064%
3.51	99.9776%	49.9776%	0.0224%	3.84	99.9938%	49.9938%	0.0062%
3.52	99.9784%	49.9784%	0.0216%	3.85	99.9941%	49.9941%	0.0059%
3.53	99.9792%	49.9792%	0.0208%	3.86	99.9943%	49.9943%	0.0057%
3.54	99.9800%	49.9800%	0.0200%	3.87	99.9946%	49.9946%	0.0054%
3.55	99.9807%	49.9807%	0.0193%	3.88	99.9948%	49.9948%	0.0052%
3.56	99.9815%	49.9815%	0.0185%	3.89	99.9950%	49.9950%	0.0050%
3.57	99.9822%	49.9822%	0.0178%	3.90	99.9952%	49.9952%	0.0048%
3.58	99.9828%	49.9828%	0.0172%	3.91	99.9954%	49.9954%	0.0046%
3.59	99.9835%	49.9835%	0.0165%	3.92	99.9956%	49.9956%	0.0044%
3.60	99.9841%	49.9841%	0.0159%	3.93	99.9958%	49.9958%	0.0042%
3.61	99.9847%	49.9847%	0.0153%	3.94	99.9959%	49.9959%	0.0041%
3.62	99.9853%	49.9853%	0.0147%	3.95	99.9961%	49.9961%	0.0039%
3.63	99.9858%	49.9858%	0.0142%	3.96	99.9963%	49.9963%	0.0037%
3.64	99.9864%	49.9864%	0.0136%	3.97	99.9964%	49.9964%	0.0036%
3.65	99.9869%	49.9869%	0.0131%	3.98	99.9966%	49.9966%	0.0034%
3.66	99.9874%	49.9874%	0.0126%	3.99	99.9967%	49.9967%	0.0033%
3.67	99.9879%	49.9879%	0.0121%	4.00	99.9968%	49.9968%	0.0032%
3.68	99.9883%	49.9883%	0.0117%	4.10	99.99793%	49.99793%	0.00207%
3.69	99.9888%	49.9888%	0.0112%	4.20	99.99867%	49.99867%	0.00133%
3.70	99.9892%	49.9892%	0.0108%	4.30	99.99915%	49.99915%	0.00085%
3.71	99.9896%	49.9896%	0.0104%	4.40	99.99946%	49.99946%	0.00054%
3.72	99.9900%	49.9900%	0.0100%	4.50	99.99966%	49.99966%	0.00034%
3.73	99.9904%	49.9904%	0.0096%	4.60	99.99979%	49.99979%	0.00021%
3.74	99.9908%	49.9908%	0.0092%	4.70	99.99987%	49.99987%	0.00013%
3.75	99.9912%	49.9912%	0.0088%	4.80	99.99992%	49.99992%	0.00008%
3.76	99.9915%	49.9915%	0.0085%	4.90	99.99995%	49.99995%	0.00005%
3.77	99.9918%	49.9918%	0.0082%	5.00	99.99997%	49.99997%	0.00003%
3.78	99.9922%	49.9922%	0.0078%				

**Table 2:** Random Number Table

	<b>A</b>	<b>B</b>	<b>C</b>	<b>D</b>	<b>E</b>	<b>F</b>
<b>1</b>	8607	1887	5432	2039	5502	3174
<b>2</b>	5574	4576	5273	8582	1424	9439
<b>3</b>	5515	8367	6317	6974	3452	2639
<b>4</b>	0296	8870	3197	4853	4434	1571
<b>5</b>	0149	1919	8684	9082	0335	6276
<b>6</b>	8211	4653	2421	8635	8388	2544
<b>7</b>	2848	7715	5620	2649	7561	0766
<b>8</b>	3007	3419	4373	6721	2428	1532
<b>9</b>	2221	4703	7265	4061	9277	0900
<b>10</b>	8670	0480	0672	8572	9597	7785
<b>11</b>	5475	9133	5481	7966	8873	3147
<b>12</b>	7294	5418	1795	5198	4946	1615
<b>13</b>	3498	1061	4566	0370	3225	8464
<b>14</b>	3186	8239	8706	8345	2373	4830
<b>15</b>	7037	6540	9220	6516	0370	8777
<b>16</b>	3953	0689	3746	6861	4949	3386
<b>17</b>	2136	4209	8825	2571	6623	7126
<b>18</b>	3761	0535	4566	6536	9985	5070
<b>19</b>	8048	6079	2496	9461	2638	9390
<b>20</b>	4275	6909	5832	9159	4191	1325
<b>21</b>	2092	1191	7593	4784	9688	0476
<b>22</b>	8545	4468	8530	8935	1195	6530
<b>23</b>	4863	2618	9081	7876	8383	0235
<b>24</b>	8354	8405	4918	4851	6941	4597
<b>25</b>	8010	5343	3199	3236	6898	2562
<b>26</b>	5158	9039	8902	0905	2472	0704
<b>27</b>	9943	8717	2530	0421	1351	7920
<b>28</b>	0540	9804	7933	2358	8892	4633
<b>29</b>	9761	0723	3059	5386	5249	8290
<b>30</b>	1276	9555	5058	5119	1543	2066
<b>31</b>	3625	7693	3127	5576	4385	0356
<b>32</b>	7543	6216	2586	6012	7964	9972
<b>33</b>	5065	2734	6829	6362	6208	1577
<b>34</b>	7910	8629	7253	3425	4733	9927
<b>35</b>	9080	8616	4977	0703	3784	2608
<b>36</b>	4142	9849	7180	0053	6437	4342
<b>37</b>	5633	2804	4612	0386	2020	8173
<b>38</b>	5371	2571	1339	4213	1945	4844
<b>39</b>	1440	2099	5031	6049	5047	6239
<b>40</b>	6914	5610	2821	8760	5634	7445

■ A-8 Appendix A

**Table 3:** Critical Values of t

df	$\alpha = .05$ , one-tailed -or- $\alpha = .10$ , two-tailed	$\alpha = .025$ , one-tailed -or- $\alpha = .05$ , two-tailed	$\alpha = .01$ , one-tailed -or- $\alpha = .02$ , two-tailed	$\alpha = .005$ , one-tailed -or- $\alpha = .01$ , two-tailed
1	6.314	<b>12.706</b>	31.821	63.657
2	2.920	<b>4.303</b>	6.965	9.925
3	2.353	<b>3.182</b>	4.541	5.841
4	2.132	<b>2.776</b>	3.747	4.604
5	2.015	<b>2.571</b>	3.365	4.032
6	1.943	<b>2.447</b>	3.143	3.707
7	1.895	<b>2.365</b>	2.998	3.499
8	1.860	<b>2.306</b>	2.896	3.355
9	1.833	<b>2.262</b>	2.821	3.250
10	1.812	<b>2.228</b>	2.764	3.169
11	1.796	<b>2.201</b>	2.718	3.106
12	1.782	<b>2.179</b>	2.681	3.055
13	1.771	<b>2.160</b>	2.650	3.012
14	1.761	<b>2.145</b>	2.624	2.977
15	1.753	<b>2.131</b>	2.602	2.947
16	1.746	<b>2.120</b>	2.583	2.921
17	1.740	<b>2.110</b>	2.567	2.898
18	1.734	<b>2.101</b>	2.552	2.878
19	1.729	<b>2.093</b>	2.539	2.861
20	1.725	<b>2.086</b>	2.528	2.845
21	1.721	<b>2.080</b>	2.518	2.831
22	1.717	<b>2.074</b>	2.508	2.819
23	1.714	<b>2.069</b>	2.500	2.807
24	1.711	<b>2.064</b>	2.492	2.797
25	1.708	<b>2.060</b>	2.485	2.787
26	1.706	<b>2.056</b>	2.479	2.779
27	1.703	<b>2.052</b>	2.473	2.771
28	1.701	<b>2.048</b>	2.467	2.763
29	1.699	<b>2.045</b>	2.462	2.756
30	1.697	<b>2.042</b>	2.457	2.750
31	1.696	<b>2.040</b>	2.453	2.744
32	1.694	<b>2.037</b>	2.449	2.738
33	1.692	<b>2.035</b>	2.445	2.733
34	1.691	<b>2.032</b>	2.441	2.728
35	1.690	<b>2.030</b>	2.438	2.724
36	1.688	<b>2.028</b>	2.434	2.719
37	1.687	<b>2.026</b>	2.431	2.715
38	1.686	<b>2.024</b>	2.429	2.712
39	1.685	<b>2.023</b>	2.426	2.708



<b>df</b>	<b><math>\alpha = .05</math>, one-tailed -or- <math>\alpha = .10</math>, two-tailed</b>	<b><math>\alpha = .025</math>, one-tailed -or- <math>\alpha = .05</math>, two-tailed</b>	<b><math>\alpha = .01</math>, one-tailed -or- <math>\alpha = .02</math>, two-tailed</b>	<b><math>\alpha = .005</math>, one-tailed -or- <math>\alpha = .01</math>, two-tailed</b>
40	1.684	<b>2.021</b>	2.423	2.704
41	1.683	<b>2.020</b>	2.421	2.701
42	1.682	<b>2.018</b>	2.418	2.698
43	1.681	<b>2.017</b>	2.416	2.695
44	1.680	<b>2.015</b>	2.414	2.692
45	1.679	<b>2.014</b>	2.412	2.690
46	1.679	<b>2.013</b>	2.410	2.687
47	1.678	<b>2.012</b>	2.408	2.685
48	1.677	<b>2.011</b>	2.407	2.682
49	1.677	<b>2.010</b>	2.405	2.680
50	1.676	<b>2.009</b>	2.403	2.678
55	1.673	<b>2.004</b>	2.396	2.668
60	1.671	<b>2.000</b>	2.390	2.660
65	1.669	<b>1.997</b>	2.385	2.654
70	1.667	<b>1.994</b>	2.381	2.648
75	1.665	<b>1.992</b>	2.377	2.643
80	1.664	<b>1.990</b>	2.374	2.639
85	1.663	<b>1.988</b>	2.371	2.635
90	1.662	<b>1.987</b>	2.368	2.632
95	1.661	<b>1.985</b>	2.366	2.629
100	1.660	<b>1.984</b>	2.364	2.626
120	1.658	<b>1.980</b>	2.358	2.617
140	1.656	<b>1.977</b>	2.353	2.611
160	1.654	<b>1.975</b>	2.350	2.607
180	1.653	<b>1.973</b>	2.347	2.603
200	1.653	<b>1.972</b>	2.345	2.601
250	1.651	<b>1.969</b>	2.341	2.596
300	1.650	<b>1.968</b>	2.339	2.592
350	1.649	<b>1.967</b>	2.337	2.590
400	1.649	<b>1.966</b>	2.336	2.588
450	1.648	<b>1.965</b>	2.335	2.587
500	1.648	<b>1.965</b>	2.334	2.586
600	1.647	<b>1.964</b>	2.333	2.584
700	1.647	<b>1.963</b>	2.332	2.583
800	1.647	<b>1.963</b>	2.331	2.582
900	1.647	<b>1.963</b>	2.330	2.581
1000	1.646	<b>1.962</b>	2.330	2.581
$\infty$	1.645	<b>1.960</b>	2.326	2.576

**Table 4a:** Critical Values of  $F$ ,  $\alpha = .05$

		Numerator degrees of freedom						
		1	2	3	4	5	6	7
Denominator degrees of freedom	1	161.448	199.500	215.707	224.583	230.162	233.986	236.768
	2	18.513	19.000	19.164	19.247	19.296	19.330	19.353
	3	10.128	9.552	9.277	9.117	9.013	8.941	8.887
	4	7.709	6.944	6.591	6.388	6.256	6.163	6.094
	5	6.608	5.786	5.409	5.192	5.050	4.950	4.876
	6	5.987	5.143	4.757	4.534	4.387	4.284	4.207
	7	5.591	4.737	4.347	4.120	3.972	3.866	3.787
	8	5.318	4.459	4.066	3.838	3.687	3.581	3.500
	9	5.117	4.256	3.863	3.633	3.482	3.374	3.293
	10	4.965	4.103	3.708	3.478	3.326	3.217	3.135
	11	4.844	3.982	3.587	3.357	3.204	3.095	3.012
	12	4.747	3.885	3.490	3.259	3.106	2.996	2.913
	13	4.667	3.806	3.411	3.179	3.025	2.915	2.832
	14	4.600	3.739	3.344	3.112	2.958	2.848	2.764
	15	4.543	3.682	3.287	3.056	2.901	2.790	2.707
	16	4.494	3.634	3.239	3.007	2.852	2.741	2.657
	17	4.451	3.592	3.197	2.965	2.810	2.699	2.614
	18	4.414	3.555	3.160	2.928	2.773	2.661	2.577
	19	4.381	3.522	3.127	2.895	2.740	2.628	2.544
	20	4.351	3.493	3.098	2.866	2.711	2.599	2.514
	21	4.325	3.467	3.072	2.840	2.685	2.573	2.488
	22	4.301	3.443	3.049	2.817	2.661	2.549	2.464
	23	4.279	3.422	3.028	2.796	2.640	2.528	2.442
	24	4.260	3.403	3.009	2.776	2.621	2.508	2.423
	25	4.242	3.385	2.991	2.759	2.603	2.490	2.405
	26	4.225	3.369	2.975	2.743	2.587	2.474	2.388
	27	4.210	3.354	2.960	2.728	2.572	2.459	2.373
	28	4.196	3.340	2.947	2.714	2.558	2.445	2.359
	29	4.183	3.328	2.934	2.701	2.545	2.432	2.346
	30	4.171	3.316	2.922	2.690	2.534	2.421	2.334
	31	4.160	3.305	2.911	2.679	2.523	2.409	2.323
	32	4.149	3.295	2.901	2.668	2.512	2.399	2.313
	33	4.139	3.285	2.892	2.659	2.503	2.389	2.303
	34	4.130	3.276	2.883	2.650	2.494	2.380	2.294
	35	4.121	3.267	2.874	2.641	2.485	2.372	2.285
	36	4.113	3.259	2.866	2.634	2.477	2.364	2.277
	37	4.105	3.252	2.859	2.626	2.470	2.356	2.270
	38	4.098	3.245	2.852	2.619	2.463	2.349	2.262

Numerator degrees of freedom								
8	9	10	11	12	13	14	15	16
238.883	240.543	241.882	242.983	243.906	244.690	245.364	245.950	246.464
19.371	19.385	19.396	19.405	19.413	19.419	19.424	19.429	19.433
8.845	8.812	8.786	8.763	8.745	8.729	8.715	8.703	8.692
6.041	5.999	5.964	5.936	5.912	5.891	5.873	5.858	5.844
4.818	4.772	4.735	4.704	4.678	4.655	4.636	4.619	4.604
4.147	4.099	4.060	4.027	4.000	3.976	3.956	3.938	3.922
3.726	3.677	3.637	3.603	3.575	3.550	3.529	3.511	3.494
3.438	3.388	3.347	3.313	3.284	3.259	3.237	3.218	3.202
3.230	3.179	3.137	3.102	3.073	3.048	3.025	3.006	2.989
3.072	3.020	2.978	2.943	2.913	2.887	2.865	2.845	2.828
2.948	2.896	2.854	2.818	2.788	2.761	2.739	2.719	2.701
2.849	2.796	2.753	2.717	2.687	2.660	2.637	2.617	2.599
2.767	2.714	2.671	2.635	2.604	2.577	2.554	2.533	2.515
2.699	2.646	2.602	2.565	2.534	2.507	2.484	2.463	2.445
2.641	2.588	2.544	2.507	2.475	2.448	2.424	2.403	2.385
2.591	2.538	2.494	2.456	2.425	2.397	2.373	2.352	2.333
2.548	2.494	2.450	2.413	2.381	2.353	2.329	2.308	2.289
2.510	2.456	2.412	2.374	2.342	2.314	2.290	2.269	2.250
2.477	2.423	2.378	2.340	2.308	2.280	2.256	2.234	2.215
2.447	2.393	2.348	2.310	2.278	2.250	2.225	2.203	2.184
2.420	2.366	2.321	2.283	2.250	2.222	2.197	2.176	2.156
2.397	2.342	2.297	2.259	2.226	2.198	2.173	2.151	2.131
2.375	2.320	2.275	2.236	2.204	2.175	2.150	2.128	2.109
2.355	2.300	2.255	2.216	2.183	2.155	2.130	2.108	2.088
2.337	2.282	2.236	2.198	2.165	2.136	2.111	2.089	2.069
2.321	2.265	2.220	2.181	2.148	2.119	2.094	2.072	2.052
2.305	2.250	2.204	2.166	2.132	2.103	2.078	2.056	2.036
2.291	2.236	2.190	2.151	2.118	2.089	2.064	2.041	2.021
2.278	2.223	2.177	2.138	2.104	2.075	2.050	2.027	2.007
2.266	2.211	2.165	2.126	2.092	2.063	2.037	2.015	1.995
2.255	2.199	2.153	2.114	2.080	2.051	2.026	2.003	1.983
2.244	2.189	2.142	2.103	2.070	2.040	2.015	1.992	1.972
2.235	2.179	2.133	2.093	2.060	2.030	2.004	1.982	1.961
2.225	2.170	2.123	2.084	2.050	2.021	1.995	1.972	1.952
2.217	2.161	2.114	2.075	2.041	2.012	1.986	1.963	1.942
2.209	2.153	2.106	2.067	2.033	2.003	1.977	1.954	1.934
2.201	2.145	2.098	2.059	2.025	1.995	1.969	1.946	1.926
2.194	2.138	2.091	2.051	2.017	1.988	1.962	1.939	1.918

**Table 4a:** Critical Values of  $F$ ,  $\alpha = .05$  (continued)

	Numerator degrees of freedom						
	1	2	3	4	5	6	7
<b>39</b>	4.091	3.238	2.845	2.612	2.456	2.342	2.255
<b>40</b>	4.085	3.232	2.839	2.606	2.449	2.336	2.249
<b>41</b>	4.079	3.226	2.833	2.600	2.443	2.330	2.243
<b>42</b>	4.073	3.220	2.827	2.594	2.438	2.324	2.237
<b>43</b>	4.067	3.214	2.822	2.589	2.432	2.318	2.232
<b>44</b>	4.062	3.209	2.816	2.584	2.427	2.313	2.226
<b>45</b>	4.057	3.204	2.812	2.579	2.422	2.308	2.221
<b>46</b>	4.052	3.200	2.807	2.574	2.417	2.304	2.216
<b>47</b>	4.047	3.195	2.802	2.570	2.413	2.299	2.212
<b>48</b>	4.043	3.191	2.798	2.565	2.409	2.295	2.207
<b>49</b>	4.038	3.187	2.794	2.561	2.404	2.290	2.203
<b>50</b>	4.034	3.183	2.790	2.557	2.400	2.286	2.199
<b>55</b>	4.016	3.165	2.773	2.540	2.383	2.269	2.181
<b>60</b>	4.001	3.150	2.758	2.525	2.368	2.254	2.167
<b>65</b>	3.989	3.138	2.746	2.513	2.356	2.242	2.154
<b>70</b>	3.978	3.128	2.736	2.503	2.346	2.231	2.143
<b>75</b>	3.968	3.119	2.727	2.494	2.337	2.222	2.134
<b>80</b>	3.960	3.111	2.719	2.486	2.329	2.214	2.126
<b>85</b>	3.953	3.104	2.712	2.479	2.322	2.207	2.119
<b>90</b>	3.947	3.098	2.706	2.473	2.316	2.201	2.113
<b>95</b>	3.941	3.092	2.700	2.467	2.310	2.196	2.108
<b>100</b>	3.936	3.087	2.696	2.463	2.305	2.191	2.103
<b>120</b>	3.920	3.072	2.680	2.447	2.290	2.175	2.087
<b>140</b>	3.909	3.061	2.669	2.436	2.279	2.164	2.076
<b>160</b>	3.900	3.053	2.661	2.428	2.271	2.156	2.067
<b>180</b>	3.894	3.046	2.655	2.422	2.264	2.149	2.061
<b>200</b>	3.888	3.041	2.650	2.417	2.259	2.144	2.056
<b>250</b>	3.879	3.032	2.641	2.408	2.250	2.135	2.046
<b>300</b>	3.873	3.026	2.635	2.402	2.244	2.129	2.040
<b>350</b>	3.868	3.022	2.630	2.397	2.240	2.125	2.036
<b>400</b>	3.865	3.018	2.627	2.394	2.237	2.121	2.032
<b>450</b>	3.862	3.016	2.625	2.392	2.234	2.119	2.030
<b>500</b>	3.860	3.014	2.623	2.390	2.232	2.117	2.028
<b>600</b>	3.857	3.011	2.620	2.387	2.229	2.114	2.025
<b>700</b>	3.855	3.009	2.618	2.385	2.227	2.112	2.023
<b>800</b>	3.853	3.007	2.616	2.383	2.225	2.110	2.021
<b>900</b>	3.852	3.006	2.615	2.382	2.224	2.109	2.020
<b>1000</b>	3.851	3.005	2.614	2.381	2.223	2.108	2.019
$\infty$	3.841	2.996	2.605	2.372	2.214	2.099	2.010

Denominator degrees of freedom

Numerator degrees of freedom								
<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>	<b>12</b>	<b>13</b>	<b>14</b>	<b>15</b>	<b>16</b>
2.187	2.131	2.084	2.044	2.010	1.981	1.954	1.931	1.911
2.180	2.124	2.077	2.038	2.003	1.974	1.948	1.924	1.904
2.174	2.118	2.071	2.031	1.997	1.967	1.941	1.918	1.897
2.168	2.112	2.065	2.025	1.991	1.961	1.935	1.912	1.891
2.163	2.106	2.059	2.020	1.985	1.955	1.929	1.906	1.885
2.157	2.101	2.054	2.014	1.980	1.950	1.924	1.900	1.879
2.152	2.096	2.049	2.009	1.974	1.945	1.918	1.895	1.874
2.147	2.091	2.044	2.004	1.969	1.940	1.913	1.890	1.869
2.143	2.086	2.039	1.999	1.965	1.935	1.908	1.885	1.864
2.138	2.082	2.035	1.995	1.960	1.930	1.904	1.880	1.859
2.134	2.077	2.030	1.990	1.956	1.926	1.899	1.876	1.855
2.130	2.073	2.026	1.986	1.952	1.921	1.895	1.871	1.850
2.112	2.055	2.008	1.968	1.933	1.903	1.876	1.852	1.831
2.097	2.040	1.993	1.952	1.917	1.887	1.860	1.836	1.815
2.084	2.027	1.980	1.939	1.904	1.874	1.847	1.823	1.802
2.074	2.017	1.969	1.928	1.893	1.863	1.836	1.812	1.790
2.064	2.007	1.959	1.919	1.884	1.853	1.826	1.802	1.780
2.056	1.999	1.951	1.910	1.875	1.845	1.817	1.793	1.772
2.049	1.992	1.944	1.903	1.868	1.837	1.810	1.786	1.764
2.043	1.986	1.938	1.897	1.861	1.830	1.803	1.779	1.757
2.037	1.980	1.932	1.891	1.856	1.825	1.797	1.773	1.751
2.032	1.975	1.927	1.886	1.850	1.819	1.792	1.768	1.746
2.016	1.959	1.910	1.869	1.834	1.803	1.775	1.750	1.728
2.005	1.947	1.899	1.858	1.822	1.791	1.763	1.738	1.716
1.997	1.939	1.890	1.849	1.813	1.782	1.754	1.729	1.707
1.990	1.932	1.884	1.842	1.806	1.775	1.747	1.722	1.700
1.985	1.927	1.878	1.837	1.801	1.769	1.742	1.717	1.694
1.976	1.917	1.869	1.827	1.791	1.759	1.732	1.707	1.684
1.969	1.911	1.862	1.821	1.785	1.753	1.725	1.700	1.677
1.965	1.907	1.858	1.816	1.780	1.748	1.720	1.695	1.672
1.962	1.903	1.854	1.813	1.776	1.745	1.717	1.691	1.669
1.959	1.901	1.852	1.810	1.774	1.742	1.714	1.689	1.666
1.957	1.899	1.850	1.808	1.772	1.740	1.712	1.686	1.664
1.954	1.895	1.846	1.805	1.768	1.736	1.708	1.683	1.660
1.952	1.893	1.844	1.802	1.766	1.734	1.706	1.681	1.658
1.950	1.892	1.843	1.801	1.764	1.732	1.704	1.679	1.656
1.949	1.890	1.841	1.799	1.763	1.731	1.703	1.678	1.655
1.948	1.889	1.840	1.798	1.762	1.730	1.702	1.676	1.654
1.938	1.880	1.831	1.789	1.752	1.720	1.692	1.666	1.644

**Table 4b:** Critical Values of  $F_{\alpha} = .01$

		Numerator degrees of freedom						
		1	2	3	4	5	6	7
Denominator degrees of freedom	1	4052.18	4999.50	5403.35	5624.58	5763.65	5858.99	5928.36
	2	98.503	99.000	99.166	99.249	99.299	99.333	99.356
	3	34.116	30.817	29.457	28.710	28.237	27.911	27.672
	4	21.198	18.000	16.694	15.977	15.522	15.207	14.976
	5	16.258	13.274	12.060	11.392	10.967	10.672	10.456
	6	13.745	10.925	9.780	9.148	8.746	8.466	8.260
	7	12.246	9.547	8.451	7.847	7.460	7.191	6.993
	8	11.259	8.649	7.591	7.006	6.632	6.371	6.178
	9	10.561	8.022	6.992	6.422	6.057	5.802	5.613
	10	10.044	7.559	6.552	5.994	5.636	5.386	5.200
	11	9.646	7.206	6.217	5.668	5.316	5.069	4.886
	12	9.330	6.927	5.953	5.412	5.064	4.821	4.640
	13	9.074	6.701	5.739	5.205	4.862	4.620	4.441
	14	8.862	6.515	5.564	5.035	4.695	4.456	4.278
	15	8.683	6.359	5.417	4.893	4.556	4.318	4.142
	16	8.531	6.226	5.292	4.773	4.437	4.202	4.026
	17	8.400	6.112	5.185	4.669	4.336	4.102	3.927
	18	8.285	6.013	5.092	4.579	4.248	4.015	3.841
	19	8.185	5.926	5.010	4.500	4.171	3.939	3.765
	20	8.096	5.849	4.938	4.431	4.103	3.871	3.699
	21	8.017	5.780	4.874	4.369	4.042	3.812	3.640
	22	7.945	5.719	4.817	4.313	3.988	3.758	3.587
	23	7.881	5.664	4.765	4.264	3.939	3.710	3.539
	24	7.823	5.614	4.718	4.218	3.895	3.667	3.496
	25	7.770	5.568	4.675	4.177	3.855	3.627	3.457
	26	7.721	5.526	4.637	4.140	3.818	3.591	3.421
	27	7.677	5.488	4.601	4.106	3.785	3.558	3.388
	28	7.636	5.453	4.568	4.074	3.754	3.528	3.358
	29	7.598	5.420	4.538	4.045	3.725	3.499	3.330
	30	7.562	5.390	4.510	4.018	3.699	3.473	3.304
	31	7.530	5.362	4.484	3.993	3.675	3.449	3.281
	32	7.499	5.336	4.459	3.969	3.652	3.427	3.258
	33	7.471	5.312	4.437	3.948	3.630	3.406	3.238
	34	7.444	5.289	4.416	3.927	3.611	3.386	3.218
	35	7.419	5.268	4.396	3.908	3.592	3.368	3.200
	36	7.396	5.248	4.377	3.890	3.574	3.351	3.183
	37	7.373	5.229	4.360	3.873	3.558	3.334	3.167
	38	7.353	5.211	4.343	3.858	3.542	3.319	3.152

Numerator degrees of freedom								
8	9	10	11	12	13	14	15	16
5981.07	6022.47	6055.85	6083.32	6106.32	6125.86	6142.67	6157.28	6170.10
99.374	99.388	99.399	99.408	99.416	99.422	99.428	99.433	99.437
27.489	27.345	27.229	27.133	27.052	26.983	26.924	26.872	26.827
14.799	14.659	14.546	14.452	14.374	14.307	14.249	14.198	14.154
10.289	10.158	10.051	9.963	9.888	9.825	9.770	9.722	9.680
8.102	7.976	7.874	7.790	7.718	7.657	7.605	7.559	7.519
6.840	6.719	6.620	6.538	6.469	6.410	6.359	6.314	6.275
6.029	5.911	5.814	5.734	5.667	5.609	5.559	5.515	5.477
5.467	5.351	5.257	5.178	5.111	5.055	5.005	4.962	4.924
5.057	4.942	4.849	4.772	4.706	4.650	4.601	4.558	4.520
4.744	4.632	4.539	4.462	4.397	4.342	4.293	4.251	4.213
4.499	4.388	4.296	4.220	4.155	4.100	4.052	4.010	3.972
4.302	4.191	4.100	4.025	3.960	3.905	3.857	3.815	3.778
4.140	4.030	3.939	3.864	3.800	3.745	3.698	3.656	3.619
4.004	3.895	3.805	3.730	3.666	3.612	3.564	3.522	3.485
3.890	3.780	3.691	3.616	3.553	3.498	3.451	3.409	3.372
3.791	3.682	3.593	3.519	3.455	3.401	3.353	3.312	3.275
3.705	3.597	3.508	3.434	3.371	3.316	3.269	3.227	3.190
3.631	3.523	3.434	3.360	3.297	3.242	3.195	3.153	3.116
3.564	3.457	3.368	3.294	3.231	3.177	3.130	3.088	3.051
3.506	3.398	3.310	3.236	3.173	3.119	3.072	3.030	2.993
3.453	3.346	3.258	3.184	3.121	3.067	3.019	2.978	2.941
3.406	3.299	3.211	3.137	3.074	3.020	2.973	2.931	2.894
3.363	3.256	3.168	3.094	3.032	2.977	2.930	2.889	2.852
3.324	3.217	3.129	3.056	2.993	2.939	2.892	2.850	2.813
3.288	3.182	3.094	3.021	2.958	2.904	2.857	2.815	2.778
3.256	3.149	3.062	2.988	2.926	2.871	2.824	2.783	2.746
3.226	3.120	3.032	2.959	2.896	2.842	2.795	2.753	2.716
3.198	3.092	3.005	2.931	2.868	2.814	2.767	2.726	2.689
3.173	3.067	2.979	2.906	2.843	2.789	2.742	2.700	2.663
3.149	3.043	2.955	2.882	2.820	2.765	2.718	2.677	2.640
3.127	3.021	2.934	2.860	2.798	2.744	2.696	2.655	2.618
3.106	3.000	2.913	2.840	2.777	2.723	2.676	2.634	2.597
3.087	2.981	2.894	2.821	2.758	2.704	2.657	2.615	2.578
3.069	2.963	2.876	2.803	2.740	2.686	2.639	2.597	2.560
3.052	2.946	2.859	2.786	2.723	2.669	2.622	2.580	2.543
3.036	2.930	2.843	2.770	2.707	2.653	2.606	2.564	2.527
3.021	2.915	2.828	2.755	2.692	2.638	2.591	2.549	2.512

**Table 4b:** Critical Values of  $F, \alpha = .01$  (continued)

		Numerator degrees of freedom						
		1	2	3	4	5	6	7
Denominator degrees of freedom	39	7.333	5.194	4.327	3.843	3.528	3.305	3.137
	40	7.314	5.179	4.313	3.828	3.514	3.291	3.124
	41	7.296	5.163	4.299	3.815	3.501	3.278	3.111
	42	7.280	5.149	4.285	3.802	3.488	3.266	3.099
	43	7.264	5.136	4.273	3.790	3.476	3.254	3.087
	44	7.248	5.123	4.261	3.778	3.465	3.243	3.076
	45	7.234	5.110	4.249	3.767	3.454	3.232	3.066
	46	7.220	5.099	4.238	3.757	3.444	3.222	3.056
	47	7.207	5.087	4.228	3.747	3.434	3.213	3.046
	48	7.194	5.077	4.218	3.737	3.425	3.204	3.037
	49	7.182	5.066	4.208	3.728	3.416	3.195	3.028
	50	7.171	5.057	4.199	3.720	3.408	3.186	3.020
	55	7.119	5.013	4.159	3.681	3.370	3.149	2.983
	60	7.077	4.977	4.126	3.649	3.339	3.119	2.953
	65	7.042	4.947	4.098	3.622	3.313	3.093	2.928
	70	7.011	4.922	4.074	3.600	3.291	3.071	2.906
	75	6.985	4.900	4.054	3.580	3.272	3.052	2.887
	80	6.963	4.881	4.036	3.563	3.255	3.036	2.871
	85	6.943	4.864	4.021	3.548	3.240	3.022	2.857
	90	6.925	4.849	4.007	3.535	3.228	3.009	2.845
	95	6.909	4.836	3.995	3.523	3.216	2.998	2.833
	100	6.895	4.824	3.984	3.513	3.206	2.988	2.823
	120	6.851	4.787	3.949	3.480	3.174	2.956	2.792
	140	6.819	4.760	3.925	3.456	3.151	2.933	2.769
	160	6.796	4.740	3.906	3.439	3.134	2.917	2.753
	180	6.778	4.725	3.892	3.425	3.120	2.904	2.740
	200	6.763	4.713	3.881	3.414	3.110	2.893	2.730
	250	6.737	4.691	3.861	3.395	3.091	2.875	2.711
	300	6.720	4.677	3.848	3.382	3.079	2.862	2.699
	350	6.708	4.666	3.838	3.373	3.070	2.854	2.691
	400	6.699	4.659	3.831	3.366	3.063	2.847	2.684
	450	6.692	4.653	3.825	3.361	3.058	2.842	2.679
	500	6.686	4.648	3.821	3.357	3.054	2.838	2.675
	600	6.677	4.641	3.814	3.351	3.048	2.832	2.669
	700	6.671	4.636	3.810	3.346	3.043	2.828	2.665
	800	6.667	4.632	3.806	3.343	3.040	2.825	2.662
	900	6.663	4.629	3.803	3.340	3.038	2.822	2.659
	1000	6.660	4.626	3.801	3.338	3.036	2.820	2.657
	∞	6.635	4.605	3.782	3.319	3.017	2.802	2.639



Numerator degrees of freedom								
8	9	10	11	12	13	14	15	16
3.006	2.901	2.814	2.741	2.678	2.624	2.577	2.535	2.498
2.993	2.888	2.801	2.727	2.665	2.611	2.563	2.522	2.484
2.980	2.875	2.788	2.715	2.652	2.598	2.551	2.509	2.472
2.968	2.863	2.776	2.703	2.640	2.586	2.539	2.497	2.460
2.957	2.851	2.764	2.691	2.629	2.575	2.527	2.485	2.448
2.946	2.840	2.754	2.680	2.618	2.564	2.516	2.475	2.437
2.935	2.830	2.743	2.670	2.608	2.553	2.506	2.464	2.427
2.925	2.820	2.733	2.660	2.598	2.544	2.496	2.454	2.417
2.916	2.811	2.724	2.651	2.588	2.534	2.487	2.445	2.408
2.907	2.802	2.715	2.642	2.579	2.525	2.478	2.436	2.399
2.898	2.793	2.706	2.633	2.571	2.517	2.469	2.427	2.390
2.890	2.785	2.698	2.625	2.562	2.508	2.461	2.419	2.382
2.853	2.748	2.662	2.589	2.526	2.472	2.424	2.382	2.345
2.823	2.718	2.632	2.559	2.496	2.442	2.394	2.352	2.315
2.798	2.693	2.607	2.534	2.471	2.417	2.369	2.327	2.289
2.777	2.672	2.585	2.512	2.450	2.395	2.348	2.306	2.268
2.758	2.653	2.567	2.494	2.431	2.377	2.329	2.287	2.249
2.742	2.637	2.551	2.478	2.415	2.361	2.313	2.271	2.233
2.728	2.623	2.537	2.464	2.401	2.347	2.299	2.257	2.219
2.715	2.611	2.524	2.451	2.389	2.334	2.286	2.244	2.206
2.704	2.600	2.513	2.440	2.378	2.323	2.275	2.233	2.195
2.694	2.590	2.503	2.430	2.368	2.313	2.265	2.223	2.185
2.663	2.559	2.472	2.399	2.336	2.282	2.234	2.192	2.154
2.641	2.536	2.450	2.377	2.314	2.260	2.212	2.169	2.131
2.624	2.520	2.434	2.360	2.298	2.243	2.195	2.153	2.114
2.611	2.507	2.421	2.348	2.285	2.230	2.182	2.140	2.102
2.601	2.497	2.411	2.338	2.275	2.220	2.172	2.129	2.091
2.583	2.479	2.392	2.319	2.257	2.202	2.154	2.111	2.073
2.571	2.467	2.380	2.307	2.244	2.190	2.142	2.099	2.061
2.562	2.458	2.372	2.299	2.236	2.181	2.133	2.090	2.052
2.556	2.452	2.365	2.292	2.229	2.175	2.126	2.084	2.045
2.551	2.447	2.360	2.287	2.224	2.170	2.121	2.079	2.040
2.547	2.443	2.356	2.283	2.220	2.166	2.117	2.075	2.036
2.541	2.437	2.351	2.277	2.214	2.160	2.111	2.069	2.030
2.537	2.433	2.346	2.273	2.210	2.155	2.107	2.064	2.026
2.533	2.429	2.343	2.270	2.207	2.152	2.104	2.061	2.023
2.531	2.427	2.341	2.267	2.204	2.150	2.101	2.058	2.020
2.529	2.425	2.339	2.265	2.203	2.148	2.099	2.056	2.018
2.511	2.407	2.321	2.248	2.185	2.130	2.082	2.039	2.000

**Table 5a:** Studentized Range (*q*) Values,  $\alpha = .05$

	<i>k</i>										
	2	3	4	5	6	7	8	9	10	11	12
<b>1</b>	17.97	26.98	32.82	37.08	40.41	43.12	45.40	47.36	49.07	50.59	51.96
<b>2</b>	6.09	8.33	9.80	10.88	11.73	12.43	13.03	13.54	13.99	14.40	14.76
<b>3</b>	4.50	5.91	6.83	7.50	8.04	8.48	8.85	9.18	9.46	9.72	9.95
<b>4</b>	3.93	5.04	5.76	6.29	6.71	7.05	7.35	7.60	7.83	8.03	8.21
<b>5</b>	3.64	4.60	5.22	5.67	6.03	6.33	6.58	6.80	7.00	7.17	7.32
<b>6</b>	3.46	4.34	4.90	5.31	5.63	5.90	6.12	6.32	6.49	6.65	6.79
<b>7</b>	3.34	4.17	4.68	5.06	5.36	5.61	5.82	6.00	6.16	6.30	6.43
<b>8</b>	3.26	4.04	4.53	4.89	5.17	5.40	5.60	5.77	5.92	6.05	6.18
<b>9</b>	3.20	3.95	4.42	4.76	5.02	5.24	5.43	5.60	5.74	5.87	5.98
<b>10</b>	3.15	3.88	4.33	4.65	4.91	5.12	5.30	5.46	5.60	5.72	5.83
<b>11</b>	3.11	3.82	4.26	4.57	4.82	5.03	5.20	5.35	5.49	5.61	5.71
<b>12</b>	3.08	3.77	4.20	4.51	4.75	4.95	5.12	5.27	5.40	5.51	5.62
<b>13</b>	3.06	3.73	4.15	4.45	4.69	4.88	5.05	5.19	5.32	5.43	5.53
<b>14</b>	3.03	3.70	4.11	4.41	4.64	4.83	4.99	5.13	5.25	5.36	5.46
<b>15</b>	3.01	3.67	4.08	4.37	4.60	4.78	4.94	5.08	5.20	5.31	5.40
<b>16</b>	3.00	3.65	4.05	4.33	4.56	4.74	4.90	5.03	5.15	5.26	5.35
<b>17</b>	2.98	3.63	4.02	4.30	4.52	4.71	4.86	4.99	5.11	5.21	5.31
<b>18</b>	2.97	3.61	4.00	4.28	4.49	4.67	4.82	4.96	5.07	5.17	5.27
<b>19</b>	2.96	3.59	3.98	4.25	4.47	4.65	4.79	4.92	5.04	5.14	5.23
<b>20</b>	2.95	3.58	3.96	4.23	4.45	4.62	4.77	4.90	5.01	5.11	5.20
<b>24</b>	2.92	3.53	3.90	4.17	4.37	4.54	4.68	4.81	4.92	5.01	5.10
<b>30</b>	2.89	3.49	3.85	4.10	4.30	4.46	4.60	4.72	4.82	4.92	5.00
<b>40</b>	2.86	3.44	3.79	4.04	4.23	4.39	4.52	4.63	4.74	4.82	4.90
<b>60</b>	2.83	3.40	3.74	3.98	4.16	4.31	4.44	4.55	4.65	4.73	4.81
<b>120</b>	2.80	3.36	3.69	3.92	4.10	4.24	4.36	4.47	4.56	4.64	4.71
<b>∞</b>	2.77	3.31	3.63	3.86	4.03	4.17	4.29	4.39	4.47	4.55	4.62

<i>k</i>												
<b>13</b>	<b>14</b>	<b>15</b>	<b>16</b>	<b>17</b>	<b>18</b>	<b>19</b>	<b>20</b>	<b>30</b>	<b>40</b>	<b>60</b>	<b>80</b>	<b>100</b>
53.20	54.33	55.36	56.32	57.22	58.04	58.83	59.56	65.15	68.92	73.97	77.40	79.98
15.09	15.39	15.65	15.92	16.14	16.38	16.57	16.78	18.27	19.28	20.66	21.59	22.29
10.15	10.35	10.52	10.69	10.84	10.98	11.11	11.24	12.21	12.86	13.76	14.36	14.82
8.37	8.52	8.66	8.79	8.91	9.03	9.13	9.23	10.00	10.53	11.24	11.73	12.10
7.47	7.60	7.72	7.83	7.93	8.03	8.12	8.21	8.88	9.33	9.95	10.37	10.69
6.92	7.03	7.14	7.24	7.34	7.43	7.51	7.59	8.19	8.60	9.16	9.55	9.84
6.55	6.66	6.76	6.85	6.94	7.02	7.10	7.17	7.73	8.11	8.63	8.99	9.26
6.29	6.39	6.48	6.57	6.65	6.73	6.80	6.87	7.40	7.76	8.25	8.59	8.84
6.09	6.19	6.28	6.36	6.44	6.51	6.58	6.64	7.14	7.49	7.96	8.28	8.53
5.94	6.03	6.11	6.19	6.27	6.34	6.41	6.47	6.95	7.28	7.73	8.04	8.28
5.81	5.90	5.98	6.06	6.13	6.20	6.27	6.33	6.79	7.11	7.55	7.85	8.08
5.71	5.80	5.88	5.95	6.02	6.09	6.15	6.21	6.66	6.97	7.39	7.69	7.91
5.63	5.71	5.79	5.86	5.93	6.00	6.06	6.11	6.55	6.85	7.27	7.55	7.77
5.55	5.64	5.71	5.79	5.85	5.92	5.97	6.03	6.46	6.75	7.16	7.44	7.65
5.49	5.57	5.65	5.72	5.79	5.85	5.90	5.96	6.38	6.67	7.07	7.34	7.55
5.44	5.52	5.59	5.66	5.73	5.79	5.84	5.90	6.31	6.59	6.98	7.25	7.46
5.39	5.47	5.54	5.61	5.68	5.73	5.79	5.84	6.25	6.53	6.91	7.18	7.38
5.35	5.43	5.50	5.57	5.63	5.69	5.74	5.79	6.20	6.47	6.85	7.11	7.31
5.31	5.39	5.46	5.53	5.59	5.65	5.70	5.75	6.15	6.42	6.79	7.05	7.24
5.28	5.36	5.43	5.49	5.55	5.61	5.66	5.71	6.10	6.37	6.74	6.99	7.19
5.18	5.25	5.32	5.38	5.44	5.49	5.55	5.59	5.97	6.23	6.58	6.82	7.01
5.08	5.15	5.21	5.27	5.33	5.38	5.43	5.48	5.83	6.08	6.42	6.65	6.83
4.98	5.04	5.11	5.16	5.22	5.27	5.31	5.36	5.70	5.93	6.26	6.48	6.65
4.88	4.94	5.00	5.06	5.11	5.15	5.20	5.24	5.57	5.79	6.09	6.30	6.46
4.78	4.84	4.90	4.95	5.00	5.04	5.09	5.13	5.43	5.64	5.93	6.13	6.28
4.69	4.74	4.80	4.85	4.89	4.93	4.97	5.01	5.30	5.50	5.76	5.95	6.09

Kind permission has been granted to reproduce this table from: Gleason, J. R. 1998. A Table of the Upper Quantile Points of the Studentized Range Distribution. *Stata Technical Bulletin*, 46: 6–10.

**Table 5b:** Studentized Range (*q*) Values,  $\alpha = .01$

	<i>k</i>										
	2	3	4	5	6	7	8	9	10	11	12
<b>1</b>	90.02	135.00	164.30	185.60	202.20	215.80	227.20	237.00	245.60	253.20	260.00
<b>2</b>	14.04	19.02	22.29	24.72	26.63	28.20	29.53	30.68	31.69	32.59	33.40
<b>3</b>	8.26	10.62	12.17	13.32	14.24	15.00	15.65	16.21	16.69	17.13	17.53
<b>4</b>	6.51	8.12	9.17	9.96	10.58	11.10	11.54	11.92	12.26	12.57	12.84
<b>5</b>	5.70	6.98	7.80	8.42	8.91	9.32	9.67	9.97	10.24	10.48	10.70
<b>6</b>	5.24	6.33	7.03	7.56	7.97	8.32	8.61	8.87	9.10	9.30	9.49
<b>7</b>	4.95	5.92	6.54	7.01	7.37	7.68	7.94	8.17	8.37	8.55	8.71
<b>8</b>	4.75	5.64	6.20	6.63	6.96	7.24	7.47	7.68	7.86	8.03	8.18
<b>9</b>	4.60	5.43	5.96	6.35	6.66	6.92	7.13	7.33	7.49	7.65	7.78
<b>10</b>	4.48	5.27	5.77	6.14	6.43	6.67	6.88	7.05	7.21	7.36	7.49
<b>11</b>	4.39	5.15	5.62	5.97	6.25	6.48	6.67	6.84	6.99	7.13	7.25
<b>12</b>	4.32	5.05	5.50	5.84	6.10	6.32	6.51	6.67	6.81	6.94	7.06
<b>13</b>	4.26	4.96	5.40	5.73	5.98	6.19	6.37	6.53	6.67	6.79	6.90
<b>14</b>	4.21	4.90	5.32	5.63	5.88	6.09	6.26	6.41	6.54	6.66	6.77
<b>15</b>	4.17	4.84	5.25	5.56	5.80	5.99	6.16	6.31	6.44	6.56	6.66
<b>16</b>	4.13	4.79	5.19	5.49	5.72	5.92	6.08	6.22	6.35	6.46	6.56
<b>17</b>	4.10	4.74	5.14	5.43	5.66	5.85	6.01	6.15	6.27	6.38	6.48
<b>18</b>	4.07	4.70	5.09	5.38	5.60	5.79	5.94	6.08	6.20	6.31	6.41
<b>19</b>	4.05	4.67	5.05	5.33	5.55	5.74	5.89	6.02	6.14	6.25	6.34
<b>20</b>	4.02	4.64	5.02	5.29	5.51	5.69	5.84	5.97	6.09	6.19	6.29
<b>24</b>	3.96	4.55	4.91	5.17	5.37	5.54	5.69	5.81	5.92	6.02	6.11
<b>30</b>	3.89	4.46	4.80	5.05	5.24	5.40	5.54	5.65	5.76	5.85	5.93
<b>40</b>	3.83	4.37	4.70	4.93	5.11	5.27	5.39	5.50	5.60	5.69	5.76
<b>60</b>	3.76	4.28	4.59	4.82	4.99	5.13	5.25	5.36	5.45	5.53	5.60
<b>120</b>	3.70	4.20	4.50	4.71	4.87	5.01	5.12	5.21	5.30	5.38	5.44
<b>∞</b>	3.64	4.12	4.40	4.60	4.76	4.88	4.99	5.08	5.16	5.23	5.29

<i>k</i>													
<b>13</b>	<b>14</b>	<b>15</b>	<b>16</b>	<b>17</b>	<b>18</b>	<b>19</b>	<b>20</b>	<b>30</b>	<b>40</b>	<b>60</b>	<b>80</b>	<b>100</b>	
90.02	135.00	164.30	185.60	202.20	215.80	227.20	237.00	245.60	253.20	260.00	77.40	79.98	
14.04	19.02	22.29	24.72	26.63	28.20	29.53	30.68	31.69	32.59	33.40	21.59	22.29	
8.26	10.62	12.17	13.32	14.24	15.00	15.65	16.21	16.69	17.13	17.53	14.36	14.82	
6.51	8.12	9.17	9.96	10.58	11.10	11.54	11.92	12.26	12.57	12.84	11.73	12.10	
5.70	6.98	7.80	8.42	8.91	9.32	9.67	9.97	10.24	10.48	10.70	10.37	10.69	
5.24	6.33	7.03	7.56	7.97	8.32	8.61	8.87	9.10	9.30	9.49	9.55	9.84	
4.95	5.92	6.54	7.01	7.37	7.68	7.94	8.17	8.37	8.55	8.71	8.99	9.26	
4.75	5.64	6.20	6.63	6.96	7.24	7.47	7.68	7.86	8.03	8.18	8.59	8.84	
4.60	5.43	5.96	6.35	6.66	6.92	7.13	7.33	7.49	7.65	7.78	8.28	8.53	
4.48	5.27	5.77	6.14	6.43	6.67	6.88	7.05	7.21	7.36	7.49	8.04	8.28	
4.39	5.15	5.62	5.97	6.25	6.48	6.67	6.84	6.99	7.13	7.25	7.85	8.08	
4.32	5.05	5.50	5.84	6.10	6.32	6.51	6.67	6.81	6.94	7.06	7.69	7.91	
4.26	4.96	5.40	5.73	5.98	6.19	6.37	6.53	6.67	6.79	6.90	7.55	7.77	
4.21	4.90	5.32	5.63	5.88	6.09	6.26	6.41	6.54	6.66	6.77	7.44	7.65	
4.17	4.84	5.25	5.56	5.80	5.99	6.16	6.31	6.44	6.56	6.66	7.34	7.55	
4.13	4.79	5.19	5.49	5.72	5.92	6.08	6.22	6.35	6.46	6.56	7.25	7.46	
4.10	4.74	5.14	5.43	5.66	5.85	6.01	6.15	6.27	6.38	6.48	7.18	7.38	
4.07	4.70	5.09	5.38	5.60	5.79	5.94	6.08	6.20	6.31	6.41	7.11	7.31	
4.05	4.67	5.05	5.33	5.55	5.74	5.89	6.02	6.14	6.25	6.34	7.05	7.24	
4.02	4.64	5.02	5.29	5.51	5.69	5.84	5.97	6.09	6.19	6.29	6.99	7.19	
3.96	4.55	4.91	5.17	5.37	5.54	5.69	5.81	5.92	6.02	6.11	6.82	7.01	
3.89	4.46	4.80	5.05	5.24	5.40	5.54	5.65	5.76	5.85	5.93	6.65	6.83	
3.83	4.37	4.70	4.93	5.11	5.27	5.39	5.50	5.60	5.69	5.76	6.48	6.65	
3.76	4.28	4.59	4.82	4.99	5.13	5.25	5.36	5.45	5.53	5.60	6.30	6.46	
3.70	4.20	4.50	4.71	4.87	5.01	5.12	5.21	5.30	5.38	5.44	6.13	6.28	
3.64	4.12	4.40	4.60	4.76	4.88	4.99	5.08	5.16	5.23	5.29	5.95	6.09	

Kind permission has been granted to reproduce this table from: Gleason, J. R. 1998. A Table of the Upper Quantile Points of the Studentized Range Distribution. *Stata Technical Bulletin*, 46: 6–10.

■ A-22 Appendix A

**Table 6:** Critical Values of  $r$

df	$\alpha = .05$ , one-tailed -or- $\alpha = .10$ , two-tailed	$\alpha = .025$ , one-tailed -or- $\alpha = .05$ , two-tailed	$\alpha = .01$ , one-tailed -or- $\alpha = .02$ , two-tailed	$\alpha = .005$ , one-tailed -or- $\alpha = .01$ , two-tailed
1	.988	<b>.997</b>	1.000	1.000
2	.900	<b>.950</b>	.980	.990
3	.805	<b>.878</b>	.934	.959
4	.729	<b>.811</b>	.882	.917
5	.669	<b>.754</b>	.833	.875
6	.621	<b>.707</b>	.789	.834
7	.582	<b>.666</b>	.750	.798
8	.549	<b>.632</b>	.715	.765
9	.521	<b>.602</b>	.685	.735
10	.497	<b>.576</b>	.658	.708
11	.476	<b>.553</b>	.634	.684
12	.458	<b>.532</b>	.612	.661
13	.441	<b>.514</b>	.592	.641
14	.426	<b>.497</b>	.574	.623
15	.412	<b>.482</b>	.558	.606
16	.400	<b>.468</b>	.543	.590
17	.389	<b>.456</b>	.529	.575
18	.378	<b>.444</b>	.516	.561
19	.369	<b>.433</b>	.503	.549
20	.360	<b>.423</b>	.492	.537
21	.352	<b>.413</b>	.482	.526
22	.344	<b>.404</b>	.472	.515
23	.337	<b>.396</b>	.462	.505
24	.330	<b>.388</b>	.453	.496
25	.323	<b>.381</b>	.445	.487
26	.317	<b>.374</b>	.437	.479
27	.311	<b>.367</b>	.430	.471
28	.306	<b>.361</b>	.423	.463
29	.301	<b>.355</b>	.416	.456
30	.296	<b>.349</b>	.409	.449
31	.291	<b>.344</b>	.403	.442
32	.287	<b>.339</b>	.397	.436
33	.283	<b>.334</b>	.392	.430
34	.279	<b>.329</b>	.386	.424
35	.275	<b>.325</b>	.381	.418
36	.271	<b>.320</b>	.376	.413
37	.267	<b>.316</b>	.371	.408
38	.264	<b>.312</b>	.367	.403

<b>df</b>	<b><math>\alpha = .05</math>, one-tailed -or- <math>\alpha = .10</math>, two-tailed</b>	<b><math>\alpha = .025</math>, one-tailed -or- <math>\alpha = .05</math>, two-tailed</b>	<b><math>\alpha = .01</math>, one-tailed -or- <math>\alpha = .02</math>, two-tailed</b>	<b><math>\alpha = .005</math>, one-tailed -or- <math>\alpha = .01</math>, two-tailed</b>
39	.260	<b>.308</b>	.362	.398
40	.257	<b>.304</b>	.358	.393
41	.254	<b>.301</b>	.354	.389
42	.251	<b>.297</b>	.350	.384
43	.248	<b>.294</b>	.346	.380
44	.246	<b>.291</b>	.342	.376
45	.243	<b>.288</b>	.338	.372
46	.240	<b>.285</b>	.335	.368
47	.238	<b>.282</b>	.331	.365
48	.235	<b>.279</b>	.328	.361
49	.233	<b>.276</b>	.325	.358
50	.231	<b>.273</b>	.322	.354
55	.220	<b>.261</b>	.307	.339
60	.211	<b>.250</b>	.295	.325
65	.203	<b>.240</b>	.284	.313
70	.195	<b>.232</b>	.274	.302
75	.189	<b>.224</b>	.265	.292
80	.183	<b>.217</b>	.257	.283
85	.178	<b>.211</b>	.249	.275
90	.173	<b>.205</b>	.242	.267
95	.168	<b>.200</b>	.236	.260
100	.164	<b>.195</b>	.230	.254
120	.150	<b>.178</b>	.210	.232
140	.139	<b>.165</b>	.195	.216
160	.130	<b>.154</b>	.183	.202
180	.122	<b>.146</b>	.172	.190
200	.116	<b>.138</b>	.164	.181
250	.104	<b>.124</b>	.146	.162
300	.095	<b>.113</b>	.134	.148
350	.088	<b>.105</b>	.124	.137
400	.082	<b>.098</b>	.116	.128
450	.077	<b>.092</b>	.109	.121
500	.073	<b>.088</b>	.104	.115
600	.067	<b>.080</b>	.095	.105
700	.062	<b>.074</b>	.088	.097
800	.058	<b>.069</b>	.082	.091
900	.055	<b>.065</b>	.077	.086
1000	.052	<b>.062</b>	.073	.081

**Table 7:** Fisher’s  $r$  to  $z$  Transformation

		Second digit of $r$									
		.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
First digit of $r$	.0	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
	.1	0.10	0.11	0.12	0.13	0.14	0.15	0.16	0.17	0.18	0.19
	.2	0.20	0.21	0.22	0.23	0.24	0.26	0.27	0.28	0.29	0.30
	.3	0.31	0.32	0.33	0.34	0.35	0.37	0.38	0.39	0.40	0.41
	.4	0.42	0.44	0.45	0.46	0.47	0.48	0.50	0.51	0.52	0.54
	.5	0.55	0.56	0.58	0.59	0.60	0.62	0.63	0.65	0.66	0.68
	.6	0.69	0.71	0.73	0.74	0.76	0.78	0.79	0.81	0.83	0.85
	.7	0.87	0.89	0.91	0.93	0.95	0.97	1.00	1.02	1.05	1.07
	.8	1.10	1.13	1.16	1.19	1.22	1.26	1.29	1.33	1.38	1.42
	.9	1.47	1.53	1.59	1.66	1.74	1.83	1.95	2.09	2.30	2.65



Table 8: Fisher’s z to r Transformation

		Final digit of z value									
		.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
First 2 digits of z value	0.0	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
	0.1	.10	.11	.12	.13	.14	.15	.16	.17	.18	.19
	0.2	.20	.21	.22	.23	.24	.24	.25	.26	.27	.28
	0.3	.29	.30	.31	.32	.33	.34	.35	.35	.36	.37
	0.4	.38	.39	.40	.41	.41	.42	.43	.44	.45	.45
	0.5	.46	.47	.48	.49	.49	.50	.51	.52	.52	.53
	0.6	.54	.54	.55	.56	.56	.57	.58	.58	.59	.60
	0.7	.60	.61	.62	.62	.63	.64	.64	.65	.65	.66
	0.8	.66	.67	.68	.68	.69	.69	.70	.70	.71	.71
	0.9	.72	.72	.73	.73	.74	.74	.74	.75	.75	.76
	1.0	.76	.77	.77	.77	.78	.78	.79	.79	.79	.80
	1.1	.80	.80	.81	.81	.81	.82	.82	.82	.83	.83
	1.2	.83	.84	.84	.84	.85	.85	.85	.85	.86	.86
	1.3	.86	.86	.87	.87	.87	.87	.88	.88	.88	.88
	1.4	.89	.89	.89	.89	.89	.90	.90	.90	.90	.90
	1.5	.91	.91	.91	.91	.91	.91	.92	.92	.92	.92
	1.6	.92	.92	.92	.93	.93	.93	.93	.93	.93	.93
	1.7	.94	.94	.94	.94	.94	.94	.94	.94	.94	.95
	1.8	.95	.95	.95	.95	.95	.95	.95	.95	.95	.96
	1.9	.96	.96	.96	.96	.96	.96	.96	.96	.96	.96
	2.0	.96	.96	.97	.97	.97	.97	.97	.97	.97	.97
	2.1	.97	.97	.97	.97	.97	.97	.97	.97	.97	.98
	2.2	.98	.98	.98	.98	.98	.98	.98	.98	.98	.98
	2.3	.98	.98	.98	.98	.98	.98	.98	.98	.98	.98
	2.4	.98	.98	.98	.98	.98	.99	.99	.99	.99	.99
	2.5	.99	.99	.99	.99	.99	.99	.99	.99	.99	.99
	2.6	.99	.99	.99	.99	.99	.99	.99	.99	.99	.99
	2.7	.99	.99	.99	.99	.99	.99	.99	.99	.99	.99
	2.8	.99	.99	.99	.99	.99	.99	.99	.99	.99	.99
	2.9	.99	.99	.99	.99	.99	.99	.99	.99	.99	.99
	3.0	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00

**Table 9:** Power for a Given  $N$  and a Given Observed or Hypothesized Correlation Value,  $\alpha = .05$ , Two-Tailed

$N$	.05	.10	.15	.20	.25	.30	.35	.40	.45	.50
5	.02	.03	.04	.04	.05	.06	.07	.08	.10	.11
6	.03	.03	.04	.05	.06	.07	.09	.11	.13	.15
7	.03	.03	.04	.06	.07	.08	.10	.13	.16	.19
8	.03	.04	.05	.06	.08	.10	.12	.15	.19	.23
9	.04	.04	.05	.07	.09	.11	.14	.17	.21	.26
10	.03	.04	.05	.07	.09	.12	.16	.20	.24	.30
11	.03	.04	.06	.08	.10	.13	.17	.22	.27	.34
12	.03	.04	.06	.08	.11	.15	.19	.24	.30	.37
13	.03	.05	.06	.09	.12	.16	.21	.26	.33	.41
14	.03	.05	.07	.09	.13	.17	.22	.28	.36	.44
15	.03	.05	.07	.10	.14	.18	.24	.31	.38	.47
16	.03	.05	.07	.10	.14	.19	.26	.33	.41	.50
17	.03	.05	.08	.11	.15	.21	.27	.35	.44	.53
18	.03	.05	.08	.12	.16	.22	.29	.37	.46	.56
19	.03	.05	.08	.12	.17	.23	.30	.39	.49	.59
20	.03	.06	.09	.13	.18	.24	.32	.41	.51	.61
21	.04	.06	.09	.13	.19	.25	.34	.43	.53	.64
22	.04	.06	.09	.14	.19	.27	.35	.45	.56	.66
23	.04	.06	.09	.14	.20	.28	.37	.47	.58	.69
24	.04	.06	.10	.15	.21	.29	.38	.49	.60	.71
25	.04	.06	.10	.15	.22	.30	.40	.51	.62	.73
26	.04	.06	.10	.16	.23	.31	.41	.52	.64	.74
27	.04	.07	.11	.16	.23	.32	.43	.54	.66	.76
28	.04	.07	.11	.17	.24	.34	.44	.56	.67	.78
29	.04	.07	.11	.17	.25	.35	.46	.57	.69	.79
30	.04	.07	.12	.18	.26	.36	.47	.59	.71	.81
32	.04	.07	.12	.19	.27	.38	.50	.62	.74	.84
34	.04	.08	.13	.20	.29	.40	.52	.65	.76	.86
36	.04	.08	.13	.21	.31	.42	.55	.68	.79	.88
38	.04	.08	.14	.22	.32	.44	.58	.70	.81	.90
40	.04	.08	.14	.23	.34	.46	.60	.73	.83	.91
42	.04	.09	.15	.24	.35	.48	.62	.75	.85	.92
44	.05	.09	.16	.25	.37	.50	.64	.77	.87	.94
46	.05	.09	.16	.26	.38	.52	.66	.79	.88	.94
48	.05	.09	.17	.27	.40	.54	.68	.81	.90	.95
50	.05	.10	.17	.28	.41	.56	.70	.82	.91	.96
55	.05	.10	.19	.30	.45	.60	.75	.86	.93	.97
60	.05	.11	.20	.33	.48	.64	.78	.89	.95	.98

NOTE: If cell is blank, power is greater than .99.

Beta ( $\beta$ ) = probability of a Type II error = 1 – power.

<b>.55</b>	<b>.60</b>	<b>.65</b>	<b>.70</b>	<b>.75</b>	<b>.80</b>	<b>.85</b>	<b>.90</b>	<b>.95</b>
.13	.16	.19	.23	.27	.34	.42	.54	.73
.18	.22	.26	.32	.39	.47	.58	.72	.88
.23	.28	.34	.41	.49	.59	.70	.83	.95
.28	.34	.41	.49	.58	.69	.80	.90	.98
.32	.39	.47	.56	.66	.76	.86	.95	
.37	.44	.53	.63	.73	.82	.91	.97	
.41	.50	.59	.68	.78	.87	.94	.98	
.45	.54	.64	.73	.83	.90	.96		
.49	.59	.68	.78	.86	.93	.97		
.53	.63	.72	.82	.89	.95	.98		
.57	.67	.76	.85	.92	.96			
.60	.70	.79	.87	.93	.97			
.63	.73	.82	.90	.95	.98			
.66	.76	.85	.91	.96	.98			
.69	.79	.87	.93	.97				
.72	.81	.89	.94	.97				
.74	.83	.90	.95	.98				
.76	.85	.92	.96	.98				
.78	.87	.93	.97					
.80	.88	.94	.97					
.82	.90	.95	.98					
.84	.91	.96	.98					
.85	.92	.96	.98					
.87	.93	.97						
.88	.94	.97						
.89	.94	.98						
.91	.96	.98						
.93	.97							
.94	.97							
.95	.98							
.96	.98							
.97								
.97								
.98								
.98								
.98								

**Table 9:** Power for a Given  $N$  and a Given Observed or Hypothesized Correlation Value,  $\alpha = .05$ , Two-Tailed (continued)

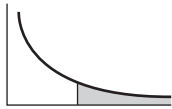
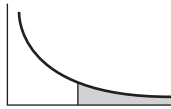
$N$	.05	.10	.15	.20	.25	.30	.35	.40	.45	.50
65	.05	.12	.22	.35	.52	.68	.82	.91	.96	
70	.06	.12	.23	.38	.55	.71	.84	.93	.97	
75	.06	.13	.24	.40	.58	.74	.87	.94	.98	
80	.06	.14	.26	.42	.61	.77	.89	.96	.98	
85	.06	.14	.27	.45	.63	.80	.91	.96		
90	.06	.15	.29	.47	.66	.82	.92	.97		
95	.06	.15	.30	.49	.68	.84	.93	.98		
100	.07	.16	.31	.51	.71	.86	.94	.98		
110	.07	.17	.34	.55	.75	.89	.96			
120	.07	.19	.37	.59	.78	.91	.97			
130	.08	.20	.39	.62	.82	.93	.98			
140	.08	.21	.42	.66	.84	.95	.98			
150	.08	.22	.44	.69	.87	.96				
160	.09	.24	.47	.71	.89	.97				
170	.09	.25	.49	.74	.90	.97				
180	.09	.26	.52	.76	.92	.98				
190	.10	.27	.54	.79	.93	.98				
200	.10	.29	.56	.81	.94					
220	.11	.31	.60	.84	.96					
240	.11	.33	.64	.87	.97					
260	.12	.36	.67	.90	.98					
280	.12	.38	.71	.92	.98					
300	.13	.40	.74	.93						
400	.16	.51	.85	.98						
500	.19	.60	.92							
600	.23	.68	.95							
700	.26	.75	.97							
800	.29	.80	.98							
900	.32	.85								
1000	.35	.88								
1500	.49	.97								
2000	.60									
3000	.78									
4000	.88									
5000	.94									
6000	.97									
7000	.98									
8000										

NOTE: If cell is blank, power is greater than .99.

Beta ( $\beta$ ) = probability of a Type II error = 1 – power.



**Table 10:** Critical Values of Chi-Square

							
$\alpha$ level				$\alpha$ level			
df	.10	.05	.001	df	.10	.05	.001
1	2.706	<b>3.841</b>	10.828	24	33.196	<b>36.415</b>	51.179
2	4.605	<b>5.991</b>	13.816	25	34.382	<b>37.652</b>	52.620
3	6.251	<b>7.815</b>	16.266	26	35.563	<b>38.885</b>	54.052
4	7.779	<b>9.488</b>	18.467	27	36.741	<b>40.113</b>	55.476
5	9.236	<b>11.070</b>	20.515	28	37.916	<b>41.337</b>	56.892
6	10.645	<b>12.592</b>	22.458	29	39.087	<b>42.557</b>	58.301
7	12.017	<b>14.067</b>	24.322	30	40.256	<b>43.773</b>	59.703
8	13.362	<b>15.507</b>	26.124	31	41.422	<b>44.985</b>	61.098
9	14.684	<b>16.919</b>	27.877	32	42.585	<b>46.194</b>	62.487
10	15.987	<b>18.307</b>	29.588	33	43.745	<b>47.400</b>	63.870
11	17.275	<b>19.675</b>	31.264	34	44.903	<b>48.602</b>	65.247
12	18.549	<b>21.026</b>	32.909	35	46.059	<b>49.802</b>	66.619
13	19.812	<b>22.362</b>	34.528	36	47.212	<b>50.998</b>	67.985
14	21.064	<b>23.685</b>	36.123	37	48.363	<b>52.192</b>	69.346
15	22.307	<b>24.996</b>	37.697	38	49.513	<b>53.384</b>	70.703
16	23.542	<b>26.296</b>	39.252	39	50.660	<b>54.572</b>	72.055
17	24.769	<b>27.587</b>	40.790	40	51.805	<b>55.758</b>	73.402
18	25.989	<b>28.869</b>	42.312	41	52.949	<b>56.942</b>	74.745
19	27.204	<b>30.144</b>	43.820	42	54.090	<b>58.124</b>	76.084
20	28.412	<b>31.410</b>	45.315	43	55.230	<b>59.304</b>	77.419
21	29.615	<b>32.671</b>	46.797	44	56.369	<b>60.481</b>	78.750
22	30.813	<b>33.924</b>	48.268	45	57.505	<b>61.656</b>	80.077
23	32.007	<b>35.172</b>	49.728				