

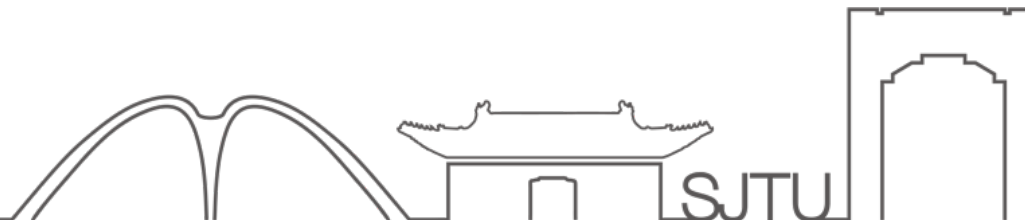


JOINT INSTITUTE
交大密西根学院

ECE2700J SU24 RC5

FSM Optimization

Wenyue Li
7/15/2024

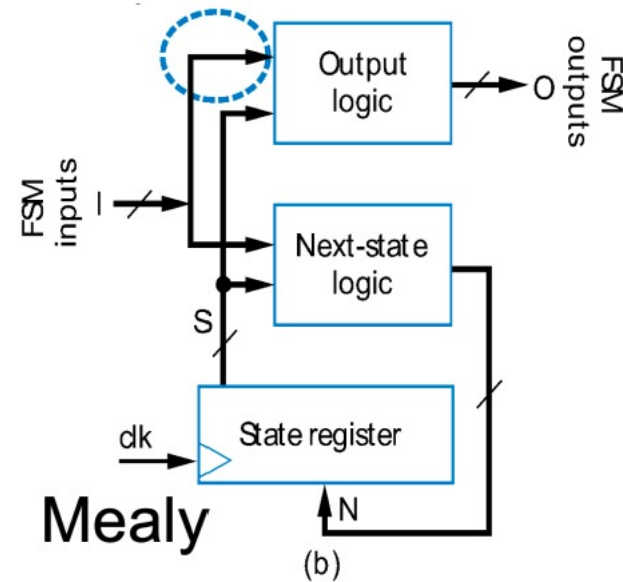
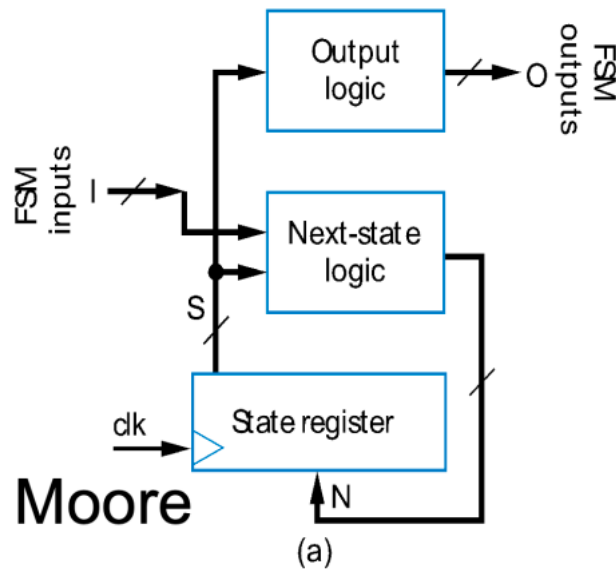


JOINT INSTITUTE
交大密西根学院

FSM

Moore vs. Mealy FSMs

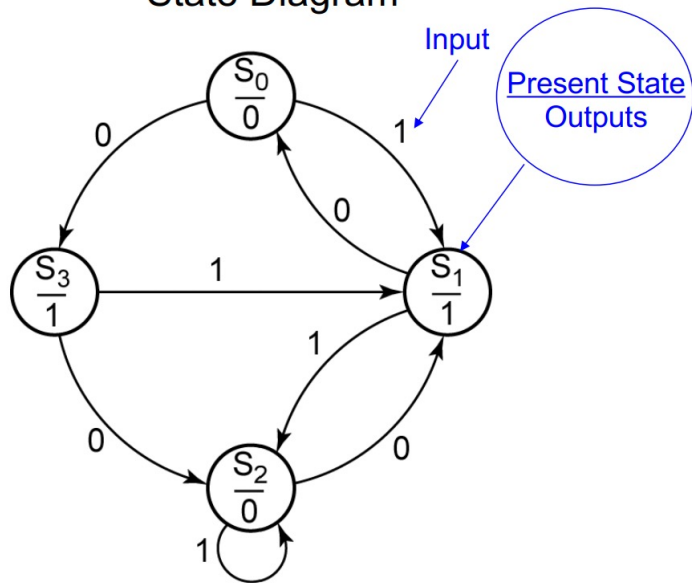
- Output logic
- Depends on present state only – Moore FSM
- Depends on present state and FSM inputs – Mealy FSM



FSM

Moore vs Mealy FSMs

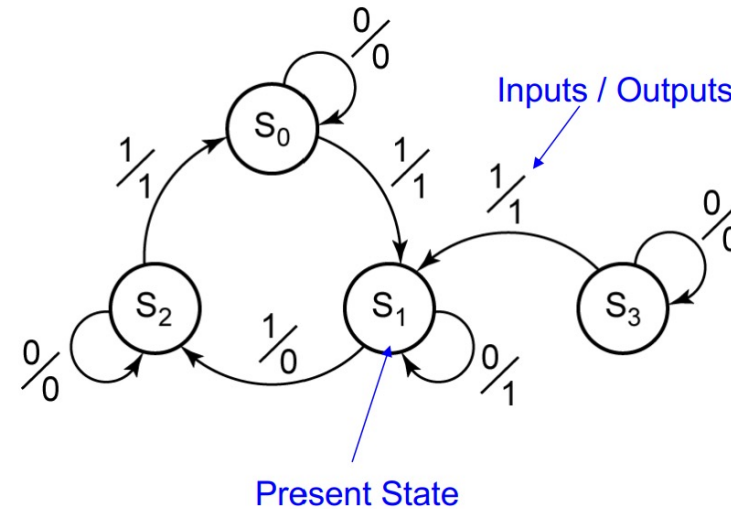
State Diagram



Or
Present State
State Table

In	P.S.	N.S.	Out
0	S0	S3	0
1	S0	S1	1
0	S1	S0	0
1	S1	S2	1
0	S2	S1	0
1	S2	S2	0
0	S3	S2	0
1	S3	S1	1

State Diagram



State Table

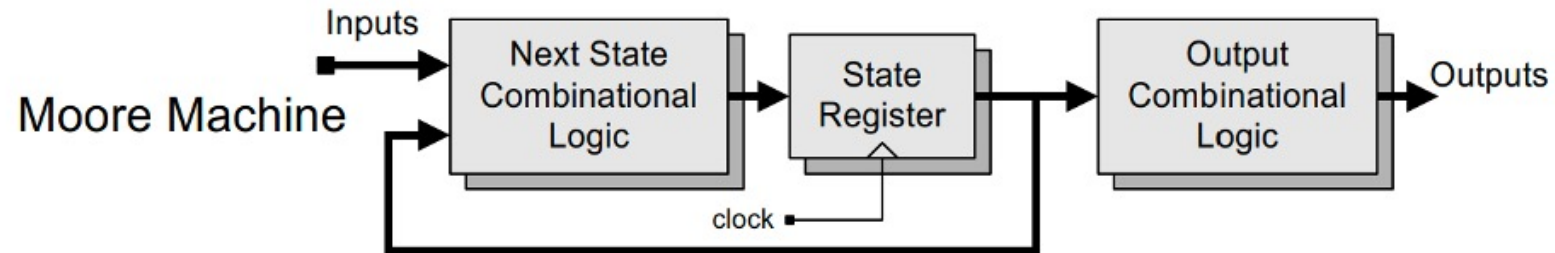
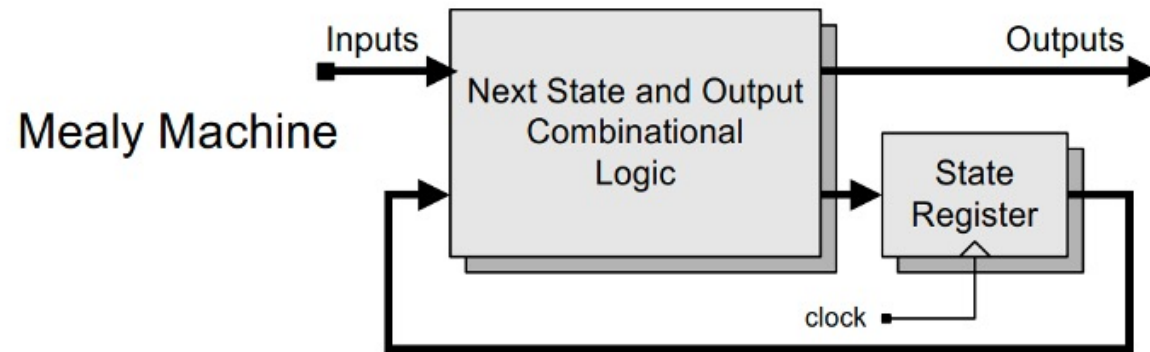
In	P.S.	N.S.	Out
0	S0	S0	0
1	S0	S1	1
0	S1	S1	1
1	S1	S2	0
0	S2	S2	0
1	S2	S0	1
0	S3	S3	0
1	S3	S1	1

Moore vs Mealy FSMs

- Output
 - Mealy: depends on both inputs and presents
 - Moore: doesn't depend on inputs
- State Diagram
 - Mealy: less states -> potentially less number of flip-flops
 - Moore: more states than Mealy -> possibly bigger circuit
- Speed of output response to the inputs
 - Mealy: quick, as soon as input changes
 - Moore: as long as one clock cycle delay
- TIMING ISSUE
 - Mealy: asynchronous, may cause serious problem
 - Moore: synchronous, more stable

FSM

Standard architecture of FSMs



FSM Optimization

State reduction with Implication tables

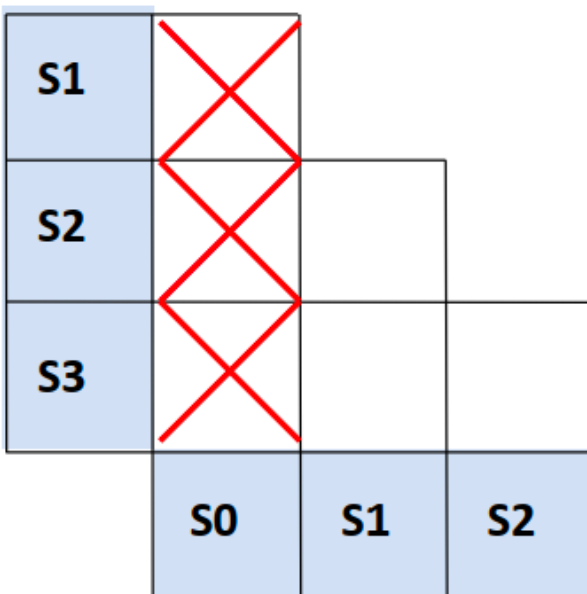
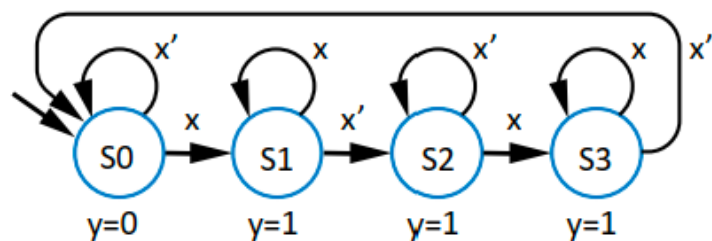
Step	Description
1 <i>Mark state pairs having different outputs as nonequivalent</i>	States having different outputs obviously cannot be equivalent.
2 <i>For each unmarked state pair, write the next state pairs for the same input values</i>	
3 <i>For each unmarked state pair, mark state pairs having nonequivalent next-state pairs as nonequivalent. Repeat this step until no change occurs, or until all states are marked.</i>	States with nonequivalent next states for the same input values can't be equivalent. Each time through this step is called a <i>pass</i> .
4 <i>Merge remaining state pairs</i>	Remaining state pairs must be equivalent.



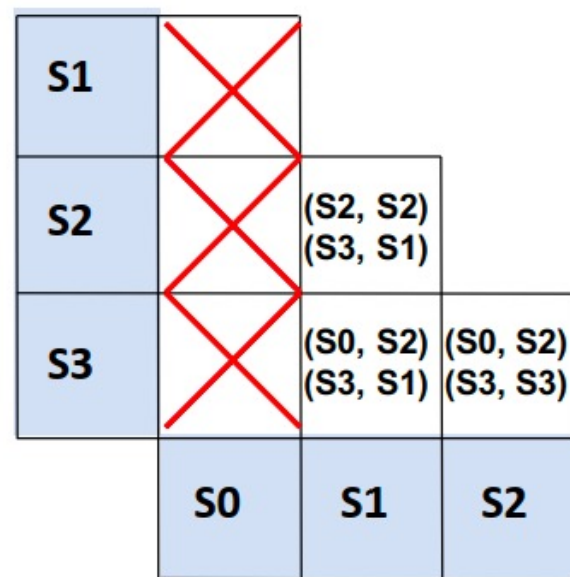
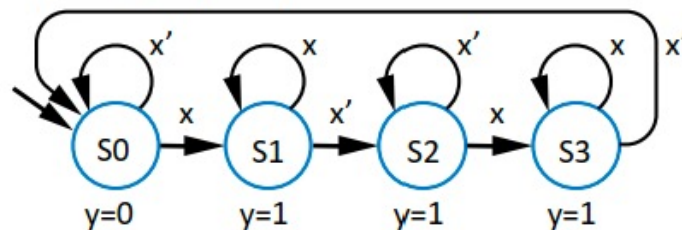
FSM

FSM Optimization

Inputs: x ; Outputs: y



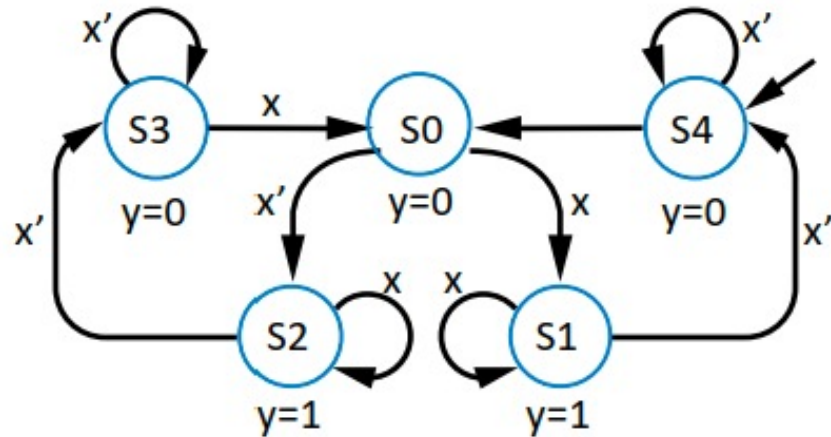
Inputs: x ; Outputs: y



FSM

FSM Optimization

Inputs: x ; Outputs: y

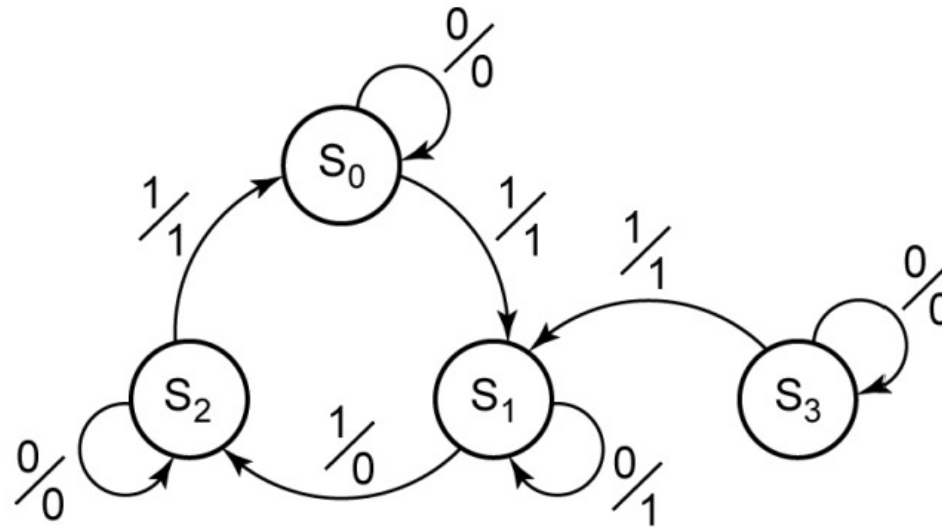


Exercise: Use the implication tables to optimize the example in the slide by yourself step by step.

FSM

FSM Optimization of Mealy FSM

- Example:



- Should have both next state pairs and output pairs in a cell for comparison

S1	Out: (0, 1) (1, 0) NS: (S0, S1) (S1, S2)		
	Out: (0, 0) (1, 1) NS: (S0, S2) (S1, S0)	Out: (1, 0) (0, 1) NS: (S1, S2) (S2, S0)	
	Out: (0, 0) (1, 1) NS: (S0, S3) (S1, S1)	Out: (1, 0) (0, 1) NS: (S1, S3) (S2, S1)	Out: (0, 0) (1, 1) NS: (S2, S3) (S0, S1)
	S0	S1	S2