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ECE2700J SU24 RC5

FSM Optimization

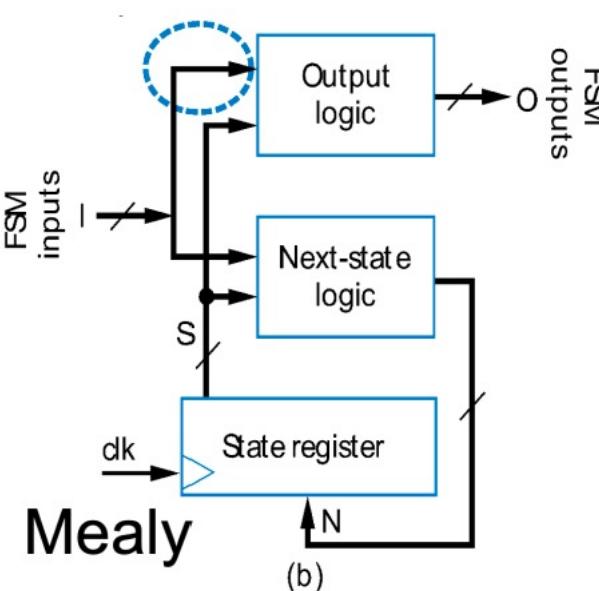
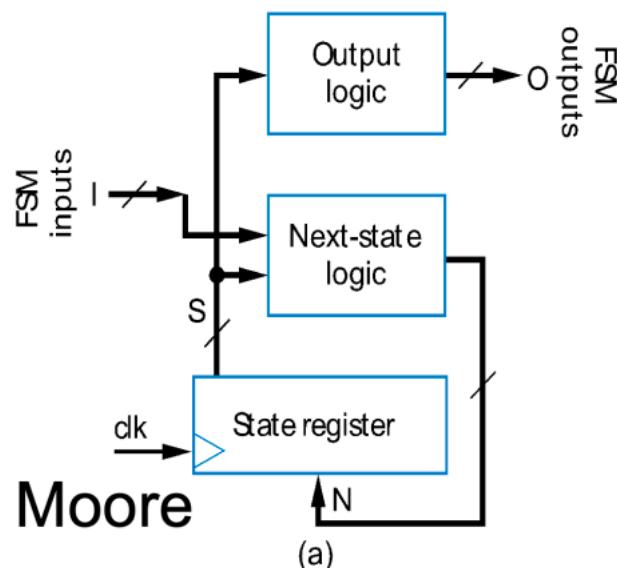
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Moore vs. Mealy FSMs

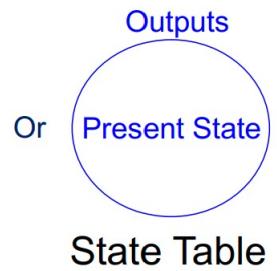
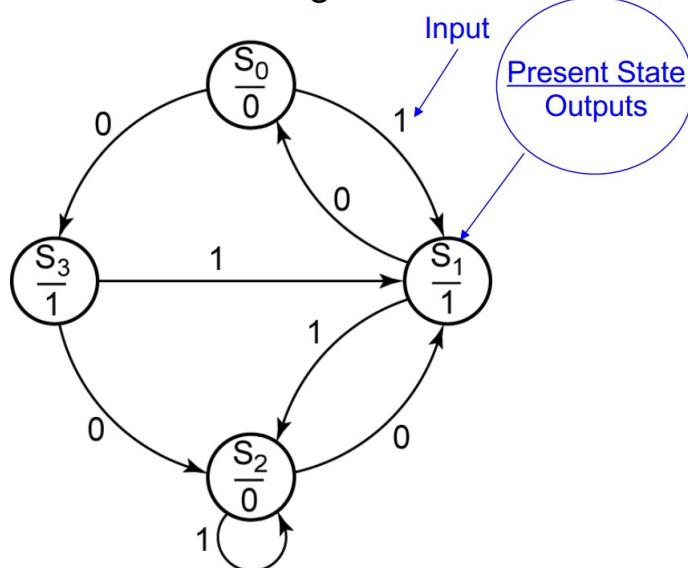
- Output logic
 - Depends on present state only – Moore FSM
 - Depends on present state and FSM inputs – Mealy FSM



FSM

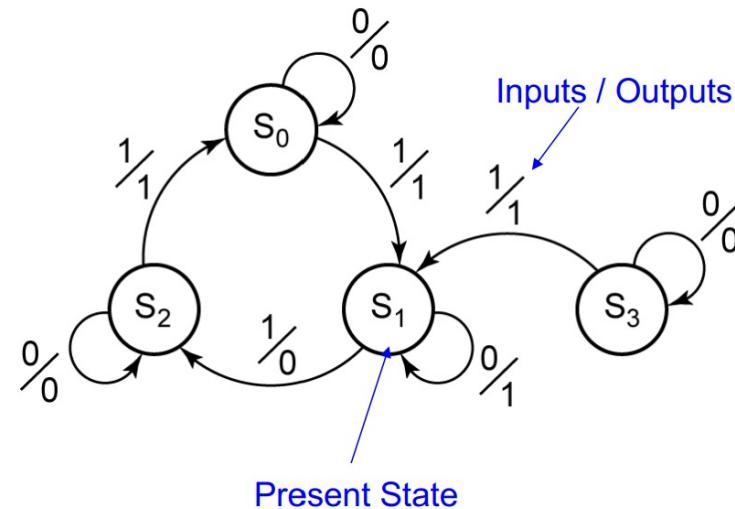
Moore vs Mealy FSMs

State Diagram



In	P.S.	N.S.	Out
0	S_0	S_3	0
1	S_0	S_1	
0	S_1	S_0	1
1	S_1	S_2	
0	S_2	S_1	0
1	S_2	S_2	
0	S_3	S_2	1
1	S_3	S_1	

State Diagram



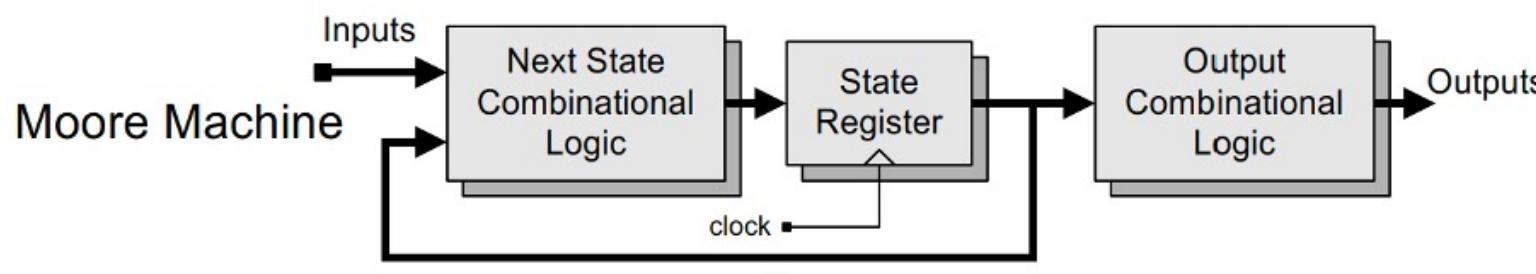
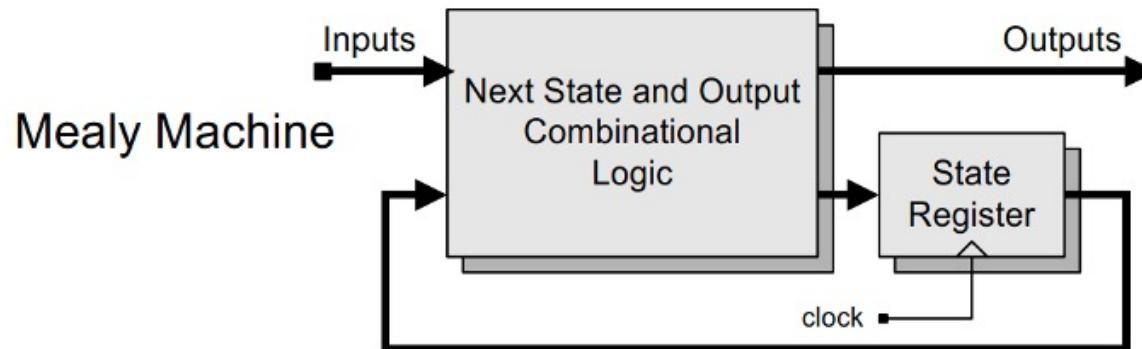
State Table

In	P.S.	N.S.	Out
0	S_0	S_0	0
1	S_0	S_1	1
0	S_1	S_1	1
1	S_1	S_2	0
0	S_2	S_2	0
1	S_2	S_0	1
0	S_3	S_3	0
1	S_3	S_1	1

Moore vs Mealy FSMs

- Output
 - Mealy: depends on both inputs and presents
 - Moore: doesn't depend on inputs
- State Diagram
 - Mealy: less states -> potentially less number of flip-flops
 - Moore: more states than Mealy -> possibly bigger circuit
- Speed of output response to the inputs
 - Mealy: quick, as soon as input changes
 - Moore: as long as one clock cycle delay
- TIMING ISSUE
 - Mealy: asynchronous, may cause serious problem
 - Moore: synchronous, more stable

Standard architecture of FSMs



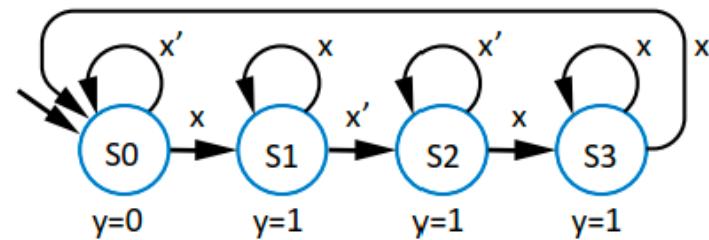
FSM Optimization

State reduction with Implication tables

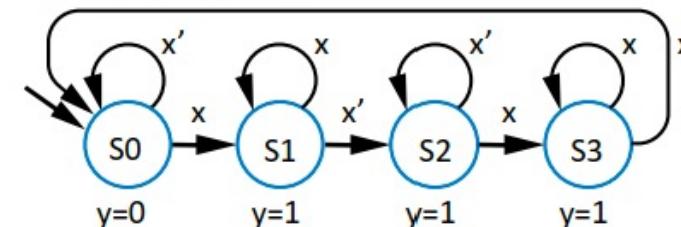
Step	Description
1 <i>Mark state pairs having different outputs as nonequivalent</i>	States having different outputs obviously cannot be equivalent.
2 <i>For each unmarked state pair, write the next state pairs for the same input values</i>	
3 <i>For each unmarked state pair, mark state pairs having nonequivalent next-state pairs as nonequivalent. Repeat this step until no change occurs, or until all states are marked.</i>	States with nonequivalent next states for the same input values can't be equivalent. Each time through this step is called a <i>pass</i> .
4 <i>Merge remaining state pairs</i>	Remaining state pairs must be equivalent.



FSM Optimization

Inputs: x ; Outputs: y 

S1		
S2		
S3		
S0	S1	S2

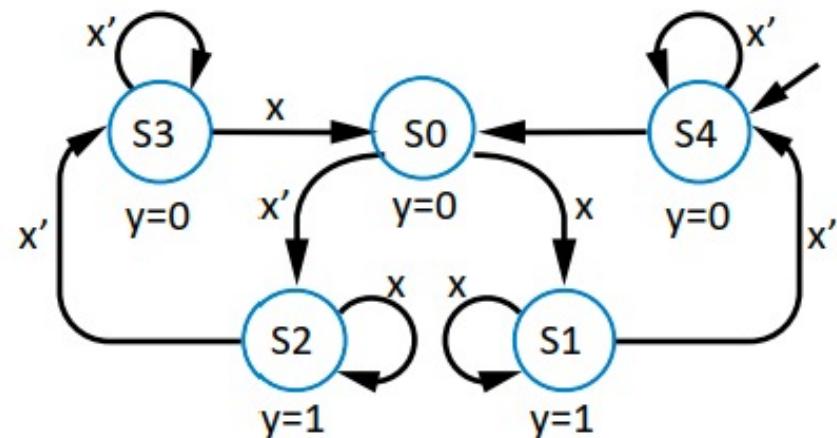
Inputs: x ; Outputs: y 

,

S1		
S2		(S2, S2) (S3, S1)
S3	(S0, S2) (S3, S1)	(S0, S2) (S3, S3)
S0	S1	S2

FSM Optimization

Inputs: x ; Outputs: y

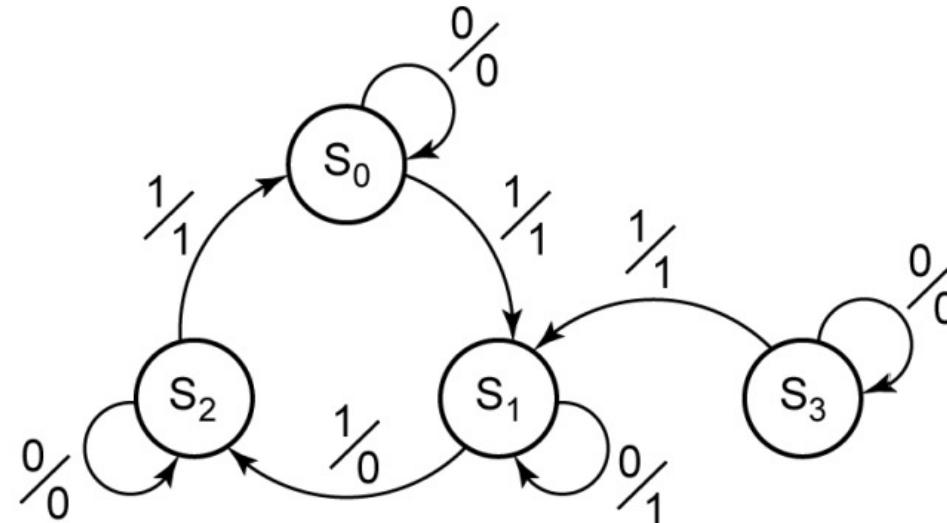


Exercise: Use the implication tables to optimize the example in the slide by yourself step by step.

FSM

FSM Optimization of Mealy FSM

- Example:



- Should have both next state pairs and output pairs in a cell for comparison

S1	Out: (0, 1) (1, 0) NS: (S0, S1) (S1, S2)	
S2	Out: (0, 0) (1, 1) NS: (S0, S2) (S1, S0)	Out: (1, 0) (0, 1) NS: (S1, S2) (S2, S0)
S3	Out: (0, 0) (1, 1) NS: (S0, S3) (S1, S1)	Out: (1, 0) (0, 1) NS: (S1, S3) (S2, S1)
S0		