

---

**Question 1:**

---

Given two strings  $S$  and  $T$ , and an integer  $n$ , find the number of times  $S$  occurs as a subsequence of  $T^n$  ( $T$  concatenated with itself  $n$  times).

$1 \leq |S| \leq 50$ ,  $1 \leq |T| \leq 1000$ ,  $1 \leq n \leq 10^{18}$ , and  $S$  and  $T$  only contain characters from **a** through **e**.

---

**Question 2:**

---

For a weighted, undirected graph  $G$  with  $n$  nodes, for all  $1 \leq i, j \leq n$ , define  $D(G, i, j)$  as the shortest path in  $G$  between nodes  $i$  and  $j$ . Also, define  $S(G) = \sum_{1 \leq i < j \leq n} D(G, i, j)$ ; i.e. the sum of shortest distances between all (unordered) pairs of nodes in  $G$ .

Given a weighted, undirected  $G$  with  $n$  nodes, find the smallest possible of  $S(T)$ , where  $T$  is a spanning tree of  $G$ .

$1 \leq n \leq 15$ .