HOMEWORK 0

Econ 501: Macroeconomic Analysis and Policy

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Spring 2016

- 1. Determine the concavity/convexity of $f(x) = -\frac{1}{3}x^2 + 8x 3$
- 2. Let $f(x) = Ax^{\alpha}$, where A > 0 and α are parameters. For what values of α is f (which is twice differentiable) non-decreasing and concave on the interval $[0, \infty)$?
- 3. A competitive firm receives the price p > 0 for each unit of its output, and pays the price w > 0 for each unit of its single input. Its output from using x units of the variable input is $f(x) = x^{\frac{1}{4}}$. Is this production function concave? Is the firm's profit concave in x?
- 4. A firm uses two inputs to produce a single output. Its production function f is homogeneous of degree 1. An implication of the homogeneity of f, which you are not asked to prove, is that the partial derivatives f_x and f_y with respect to the two inputs are homogeneous of degree zero. Use Euler's theorem to find an expression for the cross partial derivative $f_{xy}(x,y)$ in terms of x, y, and $f_{xx}(x,y)$.
- 5. Determine whether or not each of the following functions is homogeneous, and if so of what degree.

a.
$$2x^2 + xy$$

b.
$$x^2 + x^3$$

c. $g[(x_1, x_2,...,x_n)]^p$, where g is homogeneous of degree n.