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Master thesis



The effects of word segmentation quality on word alignments

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Abstract

An *abstract* is a brief summary of a research article, thesis, review, conference proceeding or any in-depth analysis of a particular subject or discipline, and is often used to help the reader quickly ascertain the paper's purpose. When used, an abstract always appears at the beginning of a manuscript, acting as the point-of-entry for any given academic paper or patent application. Abstracting and indexing services for various academic disciplines are aimed at compiling a body of literature for that particular subject.

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1 Introduction

2 Goals of the thesis

The goal of this thesis has been primarily to analyse the BPE algorithm, as a way to tokenize raw text and as opposed to other tokenization methods such as word tokenization, or other subword tokenizations. After reading this thesis the reader should have no doubts as to how the BPE algorithm works, given the extensive array of examples and codes that are presented throughout the thesis. This thesis also aims to replicate the BPE algorithm and obtain satisfactory performance results.

In order to evaluate the performance of the BPE algorithm, an alignment method from statistical machine translation is transferred into this scenario, to compare the difference between aligning words and subword units.

An additional goal is to analyse, understand and replicate an improvement over BPE called BPE dropout. The intricacies of the algorithm improvement, the motivation stemming from some of BPE's drawbacks will be explained, and examples and codes included as well. By iterating on some of the hyperparameters used to obtain BPE dropout results, this thesis will attempt to improve BPE dropout's results.

This thesis will also intend to improve the original BPE learning algorithm, making a dramatic improvement in performance. Furthermore, a new paradigm to obtain BPE units will be presented, namely removing the space boundary between words to admit creating BPE units among different words. This will be integrated into the algorithm, so that the end user can choose which mode to use, either the traditional space separated version employed in the BPE and BPE dropout paper, or the new one.

The pipeline will be automated and easy to tweak in the sense that by changing some parameters in a global file, such as dropout rate, number of merges, space mode on or off, etc. the pipeline will automatically adapt to the specific scenario.

3 Literature review

3.1 Tokenization

3.1.1 Introduction

Tokenization is the first major step in language processing. The main idea is simplifying or compressing the input text into meaningful units, called tokens, creating a big vocabulary of tokens and shorter sequences, as illustrated in Figure 3.1. [1]

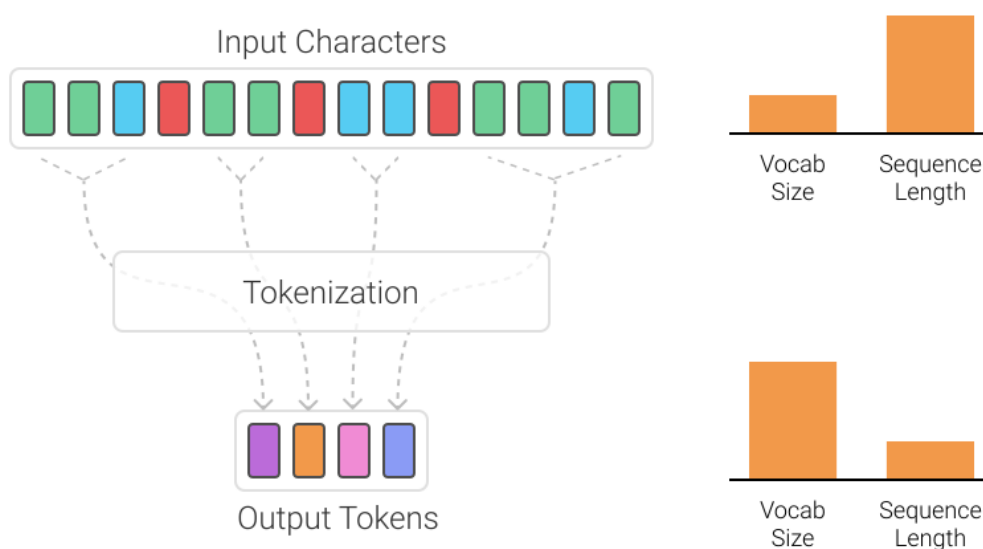


Figure 3.1: Tokenization of a sequence of text

Tokens in language are defined as units which have a semantic meaning, be it words, phrases, symbols or other elements. Here is an example of a simple way to tokenize text:

Raw text: I ate a burger today, and it was good.

Text after tokenization: ['I', 'ate', 'a', 'burger', 'today', 'and', 'it', 'was', 'good']

In this example, the tokenization process is simple. First, locate the word boundaries and split words by whitespaces. Next, remove symbols and punctuation marks as both contain no definitive meaning. However, tokenization in real life is not always that easy: some punctuation marks are relevant to the meaning of the words around them.

How to deal with punctuation marks?

Every language has its challenges. In English for example, there are possessors such as *aren't*, and contractions such as *Sarah's* and *O'Neill*. Because of this, it is imperative to know the language of the input text. *Language identification* is the task of identifying the language of the input text. Methods

ranging from the initial k-gram algorithms used in cryptography (Konnheim, 1981), to more modern n-gram methods (Dunning, 1994) are commonly used. Once the language is identified, we can follow the rules for each case and deal with punctuation marks appropriately.

Other types of tokens

In the simple example above, tokens were words. Alternatively, tokens can be groups of words, characters or subwords (parts of a word). For example, take the word *smarter*:

- Sentence: the smarter computer
- Word tokens: the, smarter, computer
- Character tokens: t, h, e, s, m, a, r, t, e, r, c, o, m, p, u, t, e, r
- Subword tokens: the, smart, er, comput, er
- Subword tokens without word boundaries: the smart, er comput, er

The major question in the tokenization phase is: **what are the correct tokens to use?**. The following section explores these 4 types of tokenization methods and delves into the algorithms and code libraries available.

3.1.2 Tokenization algorithm types

The tokenization method depends heavily on the targeted application. This results in different applications requiring different tokenization algorithms. Nowadays, most deep learning architectures in NLP process raw text at the token level and as a first step, create embeddings for these tokens, which will be explained in more detail in the following section. In short, *the type of tokenization depends on the type of embedding*. Advantages and drawbacks of several tokenization methods are further explained in the following sections.

Word level tokenization

Word level tokenization is the first established type of tokenization. It is the most basic and also the most common form of tokenization. It splits a piece of text into individual words based on word boundaries; usually a specific delimiter consisting mostly of whitespace ' ' or other punctuation signs.

Conceptually, splitting on whitespace can also split an element which should be regarded as a single token, for example New York. This is mostly the case with names, borrowed foreign phrases, and compounds that are sometimes written as multiple words. Tokenization without word boundaries aims to address that problem. 3.1.2 on page 13

Word level algorithms

The simplest way to obtain word level tokenization is by splitting the sentence on the desired delimiter; most commonly this is whitespace. The `sentence.split()` function in Python or a Regex command `re.findall("[\w']+", text)` achieves this in a simple way.

The natural language toolkit (NLTK) in Python provides a tokenize package which includes a `word_tokenize` function. The user can provide the language of the text, whereby if none is given, English is taken as default.

```
1 from nltk.tokenize import word_tokenize
2 sentence = u'I spent $2 yesterday'
3 sentence_tokenized = word_tokenize(sentence, language='English')
4 >>> sentence_tokenized = ['I', 'spent', '$', '2', 'yesterday']
```

Comparatively, SpaCy offers a similar functionality. It is possible to load the language model for different languages and model size. In this case, the English language (en) and small model size (sm) was loaded.

```
1 import spacy
2 sp = spacy.load('en_core_web_sm')
3 sentence = u'I spent $2 yesterday'
4 sentence_tokenized = sp(sentence)
5 >>> sentence_tokenized = ['I', 'spent', '$', '2', 'yesterday']
```

Other word level tokenization functions include Keras:

```
1 from keras.preprocessing.text import text_to_word_sequence
2 sentence_tokenized = text_to_word_sequence(sentence)
```

And Gensim:

```
1 from gensim.utils import tokenize
2 sentence_tokenized = list(tokenize(sentence))
```

Depending on the target application and framework, one might favor an algorithm over the other.

Word embeddings

As stated before, the goal of tokenization is to split the text into units with meaning. Typically, each token is assigned an embedding vector. Word2vec (Mikolov et al., 2013 [2]) is a way of transforming a word into a fixed-size vector representation, as shown in Figure 3.2.

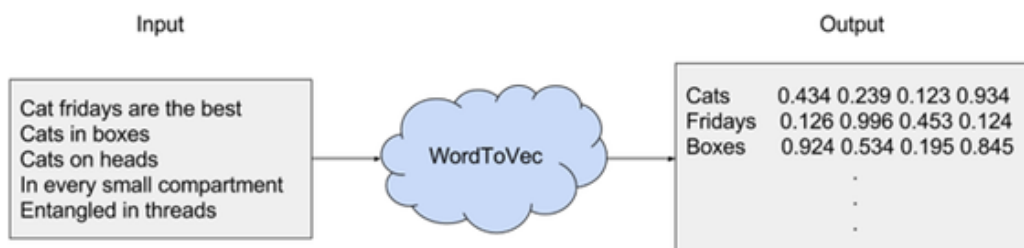


Figure 3.2: Representation of word embeddings

Apart from word2vec, there are other word embedding algorithms, namely *GloVe* or *fasttext*. When words are translated into a multi-dimensional (N) plane, each word can be compared relative to another. As such, words with similar context will appear closer to one another. Here is a simplified example to illustrate the concept of word embeddings.

- Word: smart. Embedding: [2, 3, 1, 4]

- Word: intelligent. Embedding: [2, 3, 2, 3]
- Word: stupid. Embedding: [-2, -4, -1, -3]

In the example, the embeddings of *smart* and *intelligent* have a distance of 2, since the last two numbers in the vector differ by one respectively. If this was plotted in a four dimensional space, these words would be very close together. On the other hand, *stupid* is almost the opposite of *smart*. The distance in this case is much larger. In the plot, these words would sit roughly in opposite directions. Thus, with word embeddings, a sentence is transformed into a sequence of embedding vectors, which is very useful for NLP tasks.

Word level tokenization drawbacks

Word embeddings have some drawbacks. In many cases, a word can have more than one meaning: *well*, for example, can be used in these two scenarios.

I'm doing quite well.

The well was full of water.

In the first case, *well* is an adverb and in the second it is a noun. *well*'s embedding will probably be a mixture of the two, since word embeddings do not generalize to **homonyms**. Consequently, the true meaning of both words cannot be represented.

Another drawback is that word embeddings are not well equipped to deal with **out of vocabulary (oov) words**. Word embeddings are created based on limited vocabulary size known to the system. If a foreign or misspelled word is detected, it will be given a universal unknown <UNK> embedding, that will be the same for all unknown words. Therefore, all unknown words in NLP will be treated similarly as if they have the same meaning. The information within these words is lost due to the mapping from OOV to UNK.

Another issue with word tokens is related to the **vocabulary size**. Generally, pre-trained models are trained on a large volume of the text corpus. As such, if the vocabulary is built with all the unique words in such a large corpus, it creates a huge vocabulary. This opens the door to *character tokenization*, since in this case the vocabulary depends on the number of characters, which is significantly lower than the number of all different words.

These problems are not to be mistaken with tokenization problems, tokenization is merely a way to an end. In most cases however, they are used to create embeddings. And if embeddings from word tokens have drawbacks, the tokenization method is changed in order to create different tokens, in order to create other types of embeddings.

Character level tokenization

In this type of tokenization, instead of splitting a text into words, the splitting is done into characters, whereby *smarter* becomes *s-m-a-r-t-e-r* for instance. Karpathy, 2015 was the first to introduce a character level language model.

OOV words, misspellings or rare words are handled better, since they are broken down into characters and these characters are usually known in the vocabulary. In addition, the size of the vocabulary is significantly lower, namely 26 in the simple case where only the English characters are considered,

though one might as well include all ASCII characters. Zhang et al. (2015) [3], who introduced the character CNN, consider all the alphanumeric character, in addition to punctuation marks and some special symbols.

Character level models are unrestricted in their vocabulary and see the input "as-is". Since the vocabulary is much lower, the model's performance is much better than in the word tokens case. Tokenizing sequences at the character level has shown some impressive results.

Radfor et al. (2017) [4] from OpenAI showed that character level models can capture the semantic properties of text. Kalchbrenner et al.(2016) [5] from Deepmind and Leet et al. (2017) [6] both demonstrated translation at the character level. These are particularly compelling results as the task of translation captures the semantic understanding of the underlying text.

Character level algorithms

The previous libraries explored in the case of word tokenization (native python libraries, nltk, spacy, keras) have their own version for character level tokenization.

Character level tokenization drawbacks

When tokenizing a text at the character level, the sequences are longer, which takes longer to compute since the neural network needs to have significantly more parameters to allow the model to perform the conceptual grouping internally, instead of being handed the groups from the beginning.

It becomes challenging to learn the relationship between the characters to form meaningful words and, given that there is no semantic information among characters, characters are semantically void. This makes it complicated to generate character embeddings.

Sometimes the NLP task does not need processing at the character level, such as when doing a sequence tagging task or name entity recognition, the character level model will output characters, which requires post processing.

As an in-betweenener between word and character tokenization, subword tokenization produces subword units, smaller than words but bigger than just characters.

Subword level tokenization

Subword tokenization is the task of splitting the text into subwords or n-gram characters. For example, words like *lower* can be segmented as *low-er*, *smartest* as *smart-est*, and so on. In the event of an OOV word such as *corner*, this tokenizer will divide it into *corn-er* and effectively obtain some semantic information. Very common subwords such as *ing*, *ion*, usually with a morphological sense, are learnt through repetition. The word *unfriendly* would be split into *un-friend-ly*.

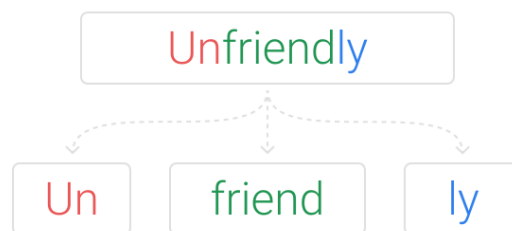


Figure 3.3: Representation of the word 'unfriendly' in subword units

At the time of writing (2020), the most powerful deep learning architectures are based on Transformers (Vaswani et al., 2017 [7]), and these rely on subword tokenization algorithms to prepare the vocabulary.

Subword level algorithms

Since Transformers are a relatively new architecture in 2020, subword tokenization is an active area of research. Nowadays four algorithms stand out: byte-pair encoding (BPE), unigram LM, WordPiece and SentencePiece.

Since BPE is the basis of the thesis, it will be explained in depth in the following section. A simple explanation of BPE and the rest of the algorithms follow below.

Huggingface, an open source NLP company, released Transformers and Tokenizers (Wolf et al., 2019 [8]), two popular NLP framework which include several subword tokenizers such as *ByteLevelBPETokenizer*, *CharBPETokenizer*, *SentencePieceBPETokenizer* and *BertWordPieceTokenizer*. The first refer to the first subword level algorithm, BPE, in addition to WordPiece and SentencePiece.

BPE

BPE (Sennrich et al., 2016 [9]) merges the most frequently occurring character or character sequences iteratively. This is roughly how the algorithm works:

1. Get a large enough corpus.
2. Define a desired subword vocabulary size.
3. Split word to sequence of characters and append a special token showing the beginning-of-word or end-of-word affix/suffix respectively.
4. Calculate pairs of sequences in the text and their frequencies. For example, ('t', 'h') has frequency X, ('h', 'e') has frequency Y.
5. Generate a new subword according to the pairs of sequences that occurs most frequently. For example, if ('t', 'h') has the highest frequency in the set of pairs, the new subword unit would become 'th'.
6. Repeat from step 3 until reaching subword vocabulary size (defined in step 2) or the next highest frequency pair is 1. Following the example, ('t', 'h') would be replaced by 'th' in the corpus, the pairs calculated again, the most frequent pair obtained again, and merged again.

BPE is based on a greedy and deterministic symbol replacement and can not provide multiple segmentations.

Unigram LM

Unigram language modelling (Kudo, 2018 [10]) is based on the assumption that all subword occurrences are independent and therefore subword sequences are produced by the product of subword occurrence probabilities. These are the steps of the algorithm:

1. Get a large enough corpus.
2. Define a desired subword vocabulary size.

3. Optimize the probability of word occurrence by giving a word sequence.
4. Compute the loss of each subword.
5. Sort the symbol by loss and keep top X % of word (X=80% for example). To avoid OOV instances, character level is recommended to be included as a subset of subwords.
6. Repeat step 3–5 until reaching the subword vocabulary size (defined in step 2) or there are no changes (step 5).

Kudo argues that the unigram LM model is more flexible than BPE because it is based on a probabilistic LM and can output multiple segmentations with their probabilities.

WordPiece

WordPiece (Schuster and Nakajima, 2012 [11]) was initially used to solve Japanese and Korean voice problem. It is similar to BPE in many ways, except that it forms a new subword based on likelihood, not on the next highest frequency pair. These are the steps of the algorithm:

1. Get a large enough corpus.
2. Define a desired subword vocabulary size.
3. Split word to sequence of characters.
4. Initialize the vocabulary with all the characters in the text.
5. Build a language model based on the vocabulary.
6. Generate a new subword unit by combining two units out of the current vocabulary to increment the vocabulary by one. Choose the new subword unit out of all the possibilities that increases the likelihood on the training data the most when added to the model.
7. Repeat step 5 until reaching subword vocabulary size (defined in step 2) or the likelihood increase falls below a certain threshold.

WordPiece and BPE only differ in step 6, since BPE merges the token combination that has the maximum frequency. This frequency stems from the combination of the tokens and not previous individual tokens. In WordPiece, the frequency of the two tokens are separately taken into account. If there are 2 tokens A and B, the score of this combination will be the following:

$$\text{Score}(A,B) = \text{Frequency}(A,B) / \text{Frequency}(A) * \text{Frequency}(B)$$

The token pair with the highest score will be selected. It might be the case that $\text{Frequency}('so', 'on')$ is very high but their individual frequencies are also high. Hence with the WordPiece algorithm, 'soon' will not be merged as the overall score is low. In another example, $\text{Frequency}('Jag', 'gery')$ might be low but if their individual frequencies are also low, 'Jag' and 'gery' might be joined to form 'Jaggery'.

BERT (Devlin et al., 2018 [12]) uses WordPiece as its tokenization method, yet the precise tokenization algorithm and/or code has not been made public. This example shows the tokenization step and how it handles OOV words.

original tokens = ["John", "Johanson", "'s", "house"] bert tokens = ["[CLS]", "john", "johan",
"##son", "'", "s", "house", "[SEP]"]

SentencePiece

SentencePiece (Kudo et al. 2018 [13]) is a subword tokenization type that has an extensive Github repository with freely available code.

As the repository states, it is an unsupervised text tokenizer and detokenizer where the vocabulary size is predetermined prior to the neural model training. It implements subword units (e.g., BPE 3.1.2) and unigram LM 3.1.2) with the extension of direct training from raw sentences. It does not depend on language-specific pre or post-processing.

While conceptually similar to BPE, it does not use the greedy encoding strategy, thus achieving higher quality tokenization while reducing error induced by location-dependent factors as seen in BPE. SentencePiece sees ambiguity in character grouping as a source of regularization for downstream models during training, and uses a simple language model to evaluate the most likely character groupings instead of greedily picking the longest recognized strings like BPE does.

Approaching ambiguity in text as a regularization parameter for downstream models results in higher tokenization quality but adversely reduces the performance of the pipeline, at times making it the slowest part or bottleneck of an NLP system. While the assumption of ambiguity in tokenization seems natural, it appears the performance trade-off is not worth it, as Google itself opted not to use this strategy in their BERT language model. 3.1.2

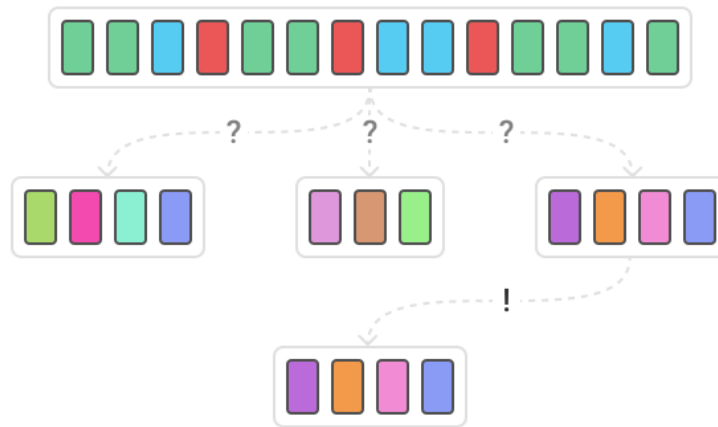


Figure 3.4: Representation of the SentencePiece tokenization in a sequence of text

The number of unique tokens in SentencePiece is predetermined, the segmentation model is trained such that the final vocabulary size is fixed, e.g., 8k, 16k, or 32k. This is different from BPE (Sennrich et al., 2015 [9]) which uses the number of merge operations instead. The number of merge operations is a BPE-specific parameter and not applicable to other segmentation algorithms, including unigram, word and character level algorithms.

Tokenization without word boundaries

Another type of tokenization, beyond word, character or subword, is tokenization without word boundaries. The three types of tokenization explored until now cannot create units among words, that is, they consider words separately.

When dealing with languages that do not include space tokenization, such as several Asian languages,

an individual symbol can resemble a syllable rather than a word or letter. Most words are short (the most common length is 2 characters), and given the lack of standardization of word breaks in the writing system or lack of punctuation in certain languages, it is not always clear where word boundaries should be placed. As an example, in English:

Input sentence: the smarter computer

Subword tokens without word boundaries: the smart, er comput, er

An approach to handle this has been to abandon word-based indexing, and do all indexing from just short subsequences of characters (character n-grams), regardless of whether particular sequences cross word boundaries or not. Hence, at times, each character used is taken as a token in Chinese tokenization.

3.1.3 BPE

Byte Pair Encoding (BPE) (Sennrich et al., 2015 [9]), is a widely used tokenization method among Transformer-based models. The code is open source and there is an active repository on Github. It merges the most frequently occurring character or character sequences iteratively.

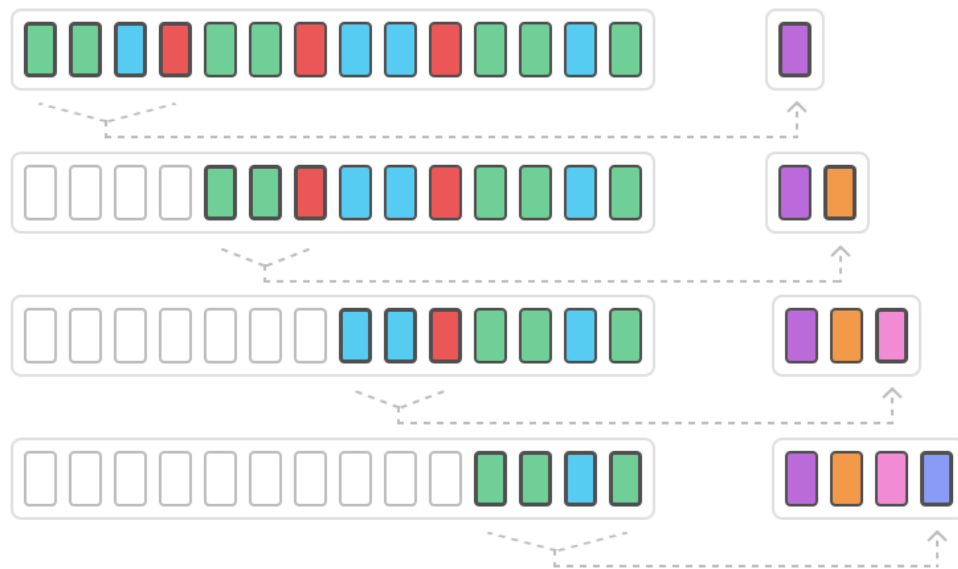


Figure 3.5: Representation of the BPE tokenization in a sequence of text

BPE enables the encoding of rare or OOV words with appropriate subword tokenization without introducing any 'unknown' tokens. One of the performance aspects in tokenization is the length of output sequences. Here, BPE is superior as it produces shorter sequences compared to character tokenization.

Minimal algorithm to learn BPE segmentations

Subsection 3.1.2 showed a simple algorithm to build subword units. In this section it will be explained in depth with an example. These are the steps of the algorithm:

1. Get a large enough corpus.
2. Define a desired subword vocabulary size.

3. Split word to sequence of characters and append a special token showing the beginning-of-word or end-of-word affix/suffix respectively.
4. Calculate pairs of sequences in the text and their frequencies.
5. Generate a new subword according to the pairs of sequences that occurs most frequently, and save it to the vocabulary.
6. Merge the most frequent pair in corpus.
7. Repeat from step 4 until reaching subword vocabulary size (defined in step 2) or the next highest frequency pair is 1.

Considering a simple corpus with a single line, and a desired subword vocabulary size of 10. The character '_' marks the beginning of each word. The following code shows the steps 1-3.

```

1 def read_corpus(corpus):
2     tokens = ["_" + " ".join(token) for token in corpus]
3     return tokens
4
5 corpus = ['this is this.']
6 vocab_size = 10
7 tokens = read_corpus(corpus)
8 >>> tokens = ['_t h i s _i s _t h i s .']

```

Now we can calculate the pairs of characters and their frequencies, as well as the most popular pair. These are the steps 4-5 in the algorithm above.

```

1 from collections import Counter
2
3 def get_stats(tokens):
4     pairs = Counter()
5     for sent in tokens:
6         for word in sent[1:].split(' _'):
7             symbols = ('_' + word).split()
8             for j in range(len(symbols) - 1):
9                 pairs[symbols[j], symbols[j+1]] += 1
10    return pairs
11
12 pairs = get_stats(tokens)
13 >>> pairs = Counter({'_t', 'h'): 2, ('h', 'i'): 2, ('i', 's'): 2,
14                     ('_i', 's'): 1, ('i', 's,'): 1, ('_', 'i'): 1,
15                     ('_i', 't'): 1, ('t', '?'): 1})
16
17 most_frequent_pair = pairs.most_common(1)[0][0]
18 >>> most_frequent_pair = ('_t', 'h')
19
20 vocab = []
21 vocab.append(most_frequent_pair)

```

There we can see each bigram and its frequency. For example, ('_t', 'h') occurs twice in the corpus, and it is taken as the most frequently occurring bigram, which we can save into the merge_list. Now it is the time to merge this pair in the corpus as stated in step 6.

```

1 import re
2
3 def merge_pair_in_corpus(tokens, pair):
4     # convert list of sentences into one big string
5     # in order to do the substitution once
6     tokens = '\n'.join(tokens)
7
8     # regex to capture the pair
9     p = re.compile(r'(?<!\S)' + re.escape(' '.join(pair)) + r'(?!\S)')
10
11     # substitute the unmerged pair by the merged pair
12     tokens = p.sub(' '.join(pair), tokens)
13
14     tokens = tokens.split('\n')
15     return tokens
16
17 tokens = merge_pair_in_corpus(tokens, most_frequent_pair)
18 >>> tokens = ['_th i s _i s _th i s .']

```

The subword unit '_th' has been created, saved in the vocabulary and merged in the corpus. The last step is iterating until the subword vocabulary size has been reached or until there are no pairs with bigger than 1. At each step, the object *pairs* is computed again since there might be new pairs such as ('_th', 'i') in this example. The whole minimal code would look like this:

```

1 corpus = ['this is this.']
2 vocab_size = 10
3 vocab = []
4
5 tokens = read_corpus(corpus)
6
7 for _ in range(vocab_size):
8
9     pairs = get_stats(tokens)
10
11     # frequency of the most common pair is 1, break loop
12     if pairs.most_common(1)[0][1] == 1:
13         break
14
15     most_frequent_pair = pairs.most_common(1)[0][0]
16     vocab.append(most_frequent_pair)
17     tokens = merge_pair_in_corpus(tokens, most_frequent_pair)
18
19 >>> tokens = ['_this _i s _this .']

```

In each step of the iteration, the *get_stats* function iterates all the characters in the corpus, so the complexity is $O(\text{len}(\text{corpus}) * \text{length of sentence})$, for an average sentence length. Obtaining the most frequent pair takes constant time, since the object *pairs* is a Counter object and includes a function to retrieve the most frequent item. At the step of *merge_pair_in_corpus*, the corpus is iterated in its entirety again, with a complexity of $O(\text{len}(\text{corpus}) * \text{len}(\text{sent}))$. Therefore, the algorithm has a complexity of $O(\text{num_merges} * \text{len}(\text{corpus}) * \text{len}(\text{sent}))$. Iterating *num_merges* amount of times cannot be avoided, but operating through all the characters in the corpus is computationally very expensive.

One of the contributions of this thesis is an optimization of this algorithm, as will be shown in the following chapters.

Applying BPE to OOV words

In the event of an OOV word, such as 'these', which the corpus used in the previous example does not know, the BPE algorithm can create some subword units from the corpus used before.

1. Split the OOV word into characters after inserting ' _ ' in the beginning.
2. Compute the pair of character or character sequences in the OOV word.
3. Select the pairs present in the learned operations.
4. Merge the most frequent pair.
5. Repeat steps 2-4 until merging is possible.

And this is the code in Python for such an algorithm:

```
1 oov = 'these'
2 oov = ['_ ' + ' '.join(list(oov))]
3
4 i = 0
5 while True:
6     pairs = get_stats(oov)
7     # find the pairs available in the vocab learnt before
8     idx = [vocab.index(i) for i in pairs if i in vocab]
9
10    if len(idx) == 0:
11        print("BPE completed")
12        break
13
14    # choose the most frequent pair which appears in the OOV word
15    best = merges[min(idx)]
16
17    # merge the best pair
18    oov = merge_vocab(best, oov)
19
20 >>> oov = '_th e s e'
```

'_th' is the only known merge in the vocabulary, the rest of the characters ('e', 's', 'e') are unknown to the vocabulary so it does not know how to create any subword units.

BPE dropout

BPE dropout (Provilkov et al., 2019 [14]) changes the BPE algorithm by stochastically corrupting the segmentation procedure of BPE, producing multiple segmentations within the same fixed BPE framework.

It exploits the innate ability of BPE to be stochastic: the merge table remains the same, but when applying it to the corpus, at each merge step some merges are randomly dropped with probability p ,

hence the name of BPE dropout. In the paper $p=0.1$ is used during training and $p=0$ during inference. For the Chinese and Japanese languages, $p=0.6$ is used in order to match the increase in length of segmented sentences as other languages.

It is hypothesized in the paper that exposing a model to different segmentations might result in better understanding of the whole words as well as their subword units. The performance improvement with respect to normal BPE is consistent no matter the vocabulary size, but it is shown that the impact from using BPE-Dropout vanishes when a corpora size gets bigger. These results are replicated and confirmed in later chapters.

Sentences segmented with BPE-Dropout are longer. There is a danger that models trained with BPE-Dropout might use more fine-grained segmentation during inference and hence slow down the process.

BPE drawbacks

Kudo (2018) [10] showed that BPE is a **greedy algorithm** that keeps the most frequent words intact, while splitting the rare ones into multiple tokens. BPE splits words into unique sequences, meaning that for each word, a model observes **only one segmentation**, meaning that if there is a segmentation error, all the following steps are erroneous. Additionally, subwords into which rare words are segmented end up poorly understood.

Although the problem of unique segmentation can be improved with the BPE Dropout method, it is still susceptible to the common problems of BPE, namely, the greediness of the algorithm and fragility regarding segmentation errors, problems which are explored in the following chapters.

3.2 Translation

A significant component of this thesis is the use of word alignments, a method employed in statistical machine translation in order to gauge how good a translation is. If a word in French gets aligned to its equivalent word in English, for example *maison-house*, then the translation is correct. It is a metric to evaluate if a translation has been successful.

This thesis is not related to translation, not SMT nor its more modern approach neural machine translation. But the word alignment algorithm is used in order to compare word alignments against BPE alignments. Taking word alignments as the basis, alignment algorithms are used to see if these BPE units are also correctly aligned to the BPE units in the other language. For example, ideally the English suffix *ment* would be aligned to the German word ending of *keit*. But before diving deep into word alignments and how they work, it is important to understand the background of this algorithm, as well as its original purpose and a general notion of how statistical machine translation works.

3.2.1 Statistical machine translation (SMT)

SMT is a machine translation approach where translations are generated based on statistical models, whose parameters are derived from the analysis of bilingual text corpora. It can be done with rule-based approaches in a supervised way, or example-based approaches, in an unsupervised way. A document is translated according to the probabilistic distribution $P(e/s)$ that a word e in the target language (for example English) is the translation of a word s in the source language (for example, Spanish).

- Suppose that $s = \text{gracias}$
- $P(\text{thanks}|\text{gracias}) = 0.45$
- $P(\text{appreciate}|\text{gracias}) = 0.13$
- $P(\text{water}|\text{gracias}) = 0.00001$

Given the word *gracias*, the translation algorithm would give a higher probability that it is aligned with *thanks*, and lower probabilities to other alignments. For each word, there usually is a list with alignment possibilities and its probabilities, and the one with the highest probability is taken as alignment. Note that since this translation method is statistical, there is no direct translation, there is no direct approval of one alignment and dismissal of the rest, since all is based on probabilities.

Typically, a translation model first translates the source language into a broken version of the target language, using an algorithm such as the expectation-maximization algorithm. Afterwards, a language model in the target language makes the broken language look more natural, in the way native speakers would speak it. A good language model will for example assign a higher probability to the sentence "the house is small" than to "small the is house". An example of a translation system from Spanish to English can be seen in Figure 3.6. In the first step, the translation model needs to know which words to align in a source-target sentence pair, which is handled by the word alignment step.

3.2.2 Word alignments

Word alignment between a parallel corpora is the NLP task of identifying translation relationships among the words in a parallel text, resulting in a graph between the two sides of the texts, with an arc

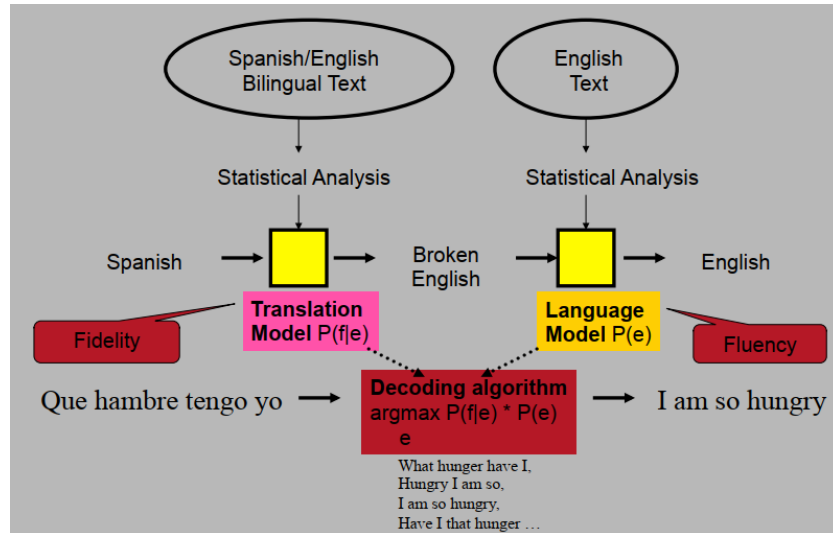


Figure 3.6: Example of Spanish-English SMT system.

between two words if they are translations of one another. Figure 3.7. shows an alignment example between a sentence in English and its counterpart in French. Alternatively, the alignments can also be displayed in a matrix as shown in Figure 3.8.

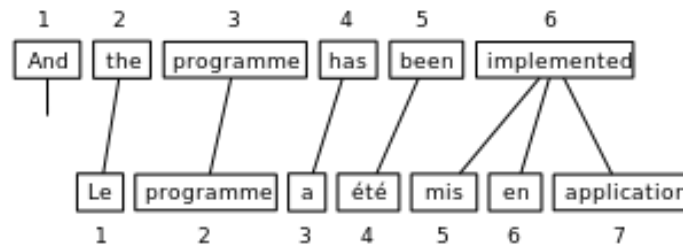


Figure 3.7: Word alignments between an English and French sentence.

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | |
|-------------|----|-----------|---|-----|-----|----|-------------|---|
| implemented | | | | | ● | ● | ● | 6 |
| been | | | | ● | | | | 5 |
| has | | | ● | | | | | 4 |
| programme | | ● | | | | | | 3 |
| the | ● | | | | | | | 2 |
| And | | | | | | | | 1 |
| | Le | programme | a | été | mis | en | application | |

Figure 3.8: Word alignments between an English and French sentence in matrix form.

The most basic words usually have one-to-one alignments, such as *the-le* in this example, and words with the same root, *programme-programme* since they both come from Latin. However, in many cases one language might express something using one word but another might express with with many words, distributed throughout the sentence. Besides, as seen in this example, some words do not even have an

alignment (*And*), and some have multiple alignments, in this case one-to-many: *implemented-mis en application*. There can also be many-to-one and many-to-many alignments.

The parameters of word alignment methods are usually estimated by observing word-aligned texts [15], and automatic word alignment is typically done by choosing that alignment which best fits a statistical machine translation model. A popular algorithm to find word alignments is the **expectation-maximization algorithm** [16]

For training, historically IBM models have been used. [17] These models are used in statistical machine translation to train a translation model, as well as an alignment model. They make use of the expectation-maximization algorithm explained above: in the expectation step, the translation probabilities within each sentence are computed; in the maximization step, these probabilities are accumulated to global translation probabilities.

This approach is an example of unsupervised learning, meaning that the system has no knowledge of the kind of output it is expected to produce, but tries to find values for the unobserved model and alignments which best explain the observed parallel text. In some cases, a small number of manually aligned sentences is used to help the model, as a way to explore supervised learning. [18] These models are able to more easily take advantage of combining many features within the data, such as context, syntactic structure, part-of-speech or translation lexicon information, which are difficult to integrate into the unsupervised models generally used.

Fastalign algorithm

Fastalign algorithm [19] is a simple log-linear reparametrization of IBM Model 2 that overcomes problems from both Model 1 and Model 2. Training this model is consistently ten times faster than Model 4. An open-source implementation of the alignment model described in this paper is available in Github.

Fastalign is a variation of the lexical translation. Lexical translation works as follows: given a source sentence f with length n , first generate the length of the target sentence m , where the target sentence is e . Then generate an alignment vector of length m that indicates which source word (or null token) each target word will be a translation of. Lastly, generate the m output words, where each word in e depends only on the word in f it is aligned with.

Fastalign's modification is that the distribution over alignments is parametrized by a null alignment probability and a precision parameter, which controls how strongly the model favors alignment points close to the diagonal (if we use the word alignment matrix like in the example above). It also adds a symmetrization step called GDFA.

The paper [19] has more detailed information on training, inference and results.

Eflomal algorithm

The Eflomal alignment algorithm [20], presented in 2016, defines itself as an *Efficient Low-Memory Aligner*. Its code is available on Github, and it is a word alignment tool based on *Efmaral*, with some improvements, such as more compact data structures, yielding a lower memory requirement, and the fact that the estimation of alignment variable marginals is done one sentence at a time, which also saves a lot of memory at no detectable cost in accuracy. Eflomal differs from Fastalign in the sense that it is based on a hidden Markov Model, as opposite to Fastalign which is based on an IBM model. Eflomal also

requires the symmetrization step GDFA, and has historically had better results than Fastalign. Technical details relevant to both *Efmaral* and *Eflomal* can be found in the cited article.

3.2.3 Alignment metrics

Evaluating alignments is usually done by the following metrics: precision, recall, F1 score and accuracy. It is assumed that the actual results are at a disposal, in this case, that the correct alignments are known. The system then makes a prediction for certain alignments. This confusion matrix shows the table for true positives, true negatives, false positives and false negatives.

| | | Predicted | |
|--------|----------|----------------|----------------|
| | | Negative | Positive |
| Actual | Negative | True Negative | False Positive |
| | Positive | False Negative | True Positive |

Figure 3.9: Confusion matrix for actual and predicted results

If an alignment is predicted and is also correct, that constitutes a true positive. If an alignment is predicted but is not correct, that constitutes a false positive. If a correct alignment was not predicted, it constitutes a false negative. And an alignment that is not present in the actual alignment list nor in the prediction list is a true negative. These are the formulas to calculate the precision, recall and F1 score:

- Precision = true positives / (true positives + false positives) = true positives / (total predicted positives)
- Recall = true positives / (true positives + false negatives) = true positives / (total actual positives)
- F1 score = 2 x precision x recall / (precision + recall)

In a nutshell, precision evaluates the following: out of all the predicted items, how many are correct? And recall: out of all the correct items, how many were predicted? The F1 score is a balance between the two, so that a system with a high precision but low recall might have a decent F1 score.

This is the traditional use of precision and recall. When talking specifically about alignments however, a slightly different definition is commonly provided:

- Precision = test alignments x possible alignments / test alignments
- Recall = test alignments x sure alignments / sure alignments
- AER = 1 - (test x sure + test x possible) / (test + sure)

AER, Alignment Error Rate [21] [17], is a commonly used metric for assessing sentence alignments. It combines precision and recall metrics together such that a perfect alignment must have all of the sure alignments and may have some possible alignments.

4 Methodology

This chapter explains the technical content of this thesis in broad strokes, the methodology used and the general idea of each method employed. For a more in-depth analysis and code snippets and explanations, refer to the Development chapter 5. The results, plots and graphs are displayed in the Results chapter 6. This thesis, first of all, aims to replicate the results of BPE and BPE dropout.

4.1 Replication of BPE

Using Sennrich et al.'s [9] code on Github, the first goal of the thesis is to replicate the BPE algorithm, and gauge how good the BPE units are by using an alignment algorithm and matching it against a gold standard. For that, these steps are undertaken:

1. Write learn-BPE from corpus algorithm
2. Write apply-BPE to corpus algorithm
3. Write extract alignment script
4. Write calculate alignment scores script

The corpus employed in this thesis is a 10k sentence English-German corpus. As an excerpt of three sentences from the corpora:

English

21 The Committee on Transport and Tourism has adopted four amendments for the second reading .

22 They will certainly enhance the feeling of the right of movement by EU citizens and they will also certainly benefit disabled drivers .

23 The initial Commission proposal was adopted unamended by Parliament on first reading .

German

21 Der Transportausschuß hat für die zweite Lesung vier Änderungsanträge beschlossen .

22 Sie werden bei den EU-Bürgern gewiß das Gefühl für das Recht auf Freizügigkeit stärken , und sie werden gewiß auch behinderten Fahrern Vorteile bringen .

23 Der ursprüngliche Vorschlag der Kommission wurde vom Parlament in erster Lesung ohne Änderungen verabschiedet .

Each step of the pipeline will be detailed as follows.

4.1.1 Learn-BPE algorithm

Sennrich's repository's code has some additional parameters that were not relevant for a minimal implementation of the BPE algorithm, so the script was adapted. These are the steps for a minimal algorithm to learn-BPE units:

1. Read corpus into tokens, parse index.
2. Count pair frequencies.
3. Start loop from 1 until desired vocabulary size. In this case, 10k merges.
 - a) Get most frequent pair.
 - b) Append most frequent pair to vocabulary.
 - c) Merge pair in corpus.
 - d) Count pair frequencies in corpus.
4. Write vocabulary to a file.

This step of the pipeline only has to be done once for each corpus, afterwards the vocabulary can be used in different ways. But this minimal algorithm, since it has to count all the pairs in the whole corpus in each iteration, takes a long time. One of the improvements of this thesis is optimizing the runtime of this algorithm, which will be explained in the subsequent sections of this chapter. With the given corpus, these are the 10 most frequent merges in the English language: `_t h`, `_th e`, `o n`, `r e`, `t i`, `e n`, `e r`, `i n`, `i s`, `n d`. And the 10 most frequent merges in German: `e n`, `e r`, `c h`, `i e`, `e i`, `n d`, `n g`, `_d ie`, `s t`, `i ch`.

4.1.2 Apply-BPE algorithm

The learnt vocabulary can be applied to a corpus. In the case of this thesis, this corpus is the same as the one used to learn the BPE units. Different `num_merges` are declared. For example, for 500 merges, only the first 500 merges of the vocabulary are taken, and there are barely any recognizable BPE units in the corpus. For bigger merge values, more and more subword units get merged. In this thesis, merges range from 500 up to 8000. These are the steps for applying BPE merges to a corpus:

1. Load data, corpus and BPE vocabulary.
2. Start loop for all numbers of merges: 500 merges, 2000 merges, 8000 merges.
 - a) Start loop from 1 until desired amount of merges: from 1 to 500 for example.
 - i. Merge the current most frequent pair in corpus.
 - b) Write merged corpus to `.bpe` file.

This is what the excerpts from the example corpora above look like after 100 merges, that is, after the 100 most common units in the language have been merged:

English

_the _Comm it t e e _on _T ran s p ort _and _T ouris m _has _a d o p t ed _f our _a
m end ment s _for _the _sec ond _re a d ing _.
_the y _w ill _cer t a in ly _en h an ce _the _f e e ling _of _the _ri g h t _of _m o ve
ment _b y _E U _citi z en s _and _the y _w ill _al s o _cer t a in ly _ben e f it _d is a
bled _d ri ver s _.
_the _in iti al _Commission _pro p o s al _w as _a d o p t ed _u n a m end ed _b y _P
ar li a ment _on _f ir st _re a d ing _.

German

_der _T ran s p or t a ussch u ß _h at _für _die _z w eite _L es ung _v ier _Ä nder ung s
ant r ä ge _besch l o ss en _.
_s ie _wer den _bei _den _E U - B ür ger n _ge w i ß _das _G e f ü h l _für _das _Re
ch t _auf _F r ei z ü g i g k eit _st ä r k en _, _und _s ie _wer den _ge w i ß _au ch
_beh inder ten _F a hr er n _V or tei l e _b r ing en _.
_der _ur s p r ü ng lich e _V or sch la g _der _Ko mm iss ion _w ur de _v o m _P ar la
ment _in _er ster _L es ung _o h n e _Ä nder ungen _vera b sch ie det _.

In English, *_the*, *_and*, *ment* and other very common words and affix/suffixes have been merged. As for German, we can see very common words being merged such as *_die*, *_das*, *_bei* and so on. The same sentences after 1000 merges:

English

_the _Committee _on _T ran s p ort _and _T ourism _has _adop ted _four _amendments
_for _the _second _reading _.
_they _will _certain ly _en h an ce _the _feeling _of _the _right _of _mo vement _by
_EU _citizens _and _they _will _also _certain ly _bene f it _dis abled _d rivers _.
_the _initi al _Commission _proposal _was _adop ted _un amended _by _Parliament
_on _first _reading _.

German

_der _T ran s p or t aussch u ß _hat _für _die _zweite _L esung _v ier _Ä nderungsant r ä ge
_beschlossen _.
_sie _werden _bei _den _EU - B ür gern _gew iß _das _Ge fü hl _für _das _Recht _auf
_Freiz ü g igkeit _st ä r ken _, _und _sie _werden _gew iß _auch _beh inderten _F ahrrn
_Vorteile _b ringen _.
_der _ur sp r ü ngliche _Vorschlag _der _Kommission _wurde _vom _Parlament _in
_erster _L esung _ohne _Ä nderungen _verab schiedet _.

We can see bigger subwords being merged, such as *reading*, *first*, *zweite* and so on. And the sentences after 4000 merges:

English

_the _Committee _on _Transport _and _Tourism _has _adopted _four _amendments
_for _the _second _reading _.

_they _will _certainly _enhance _the _feeling _of _the _right _of _movement _by _EU
_citizens _and _they _will _also _certainly _benefit _dis abled _drivers _.

_the _initial _Commission _proposal _was _adopted _un amended _by _Parliament _on
_first _reading _.

German

_der _T ransp ortausschuß _hat _für _die _zweite _Lesung _vier _Änderungsanträge
_beschlossen _.

_sie _werden _bei _den _EU-B ür gern _gew iß _das _Ge fü hl _für _das _Recht _auf
_Freizügigkeit _stärken _, _und _sie _werden _gew iß _auch _behinderten _Fahrern
_Vorteile _bringen _.

_der _ursprüngliche _Vorschlag _der _Kommission _wurde _vom _Parlament _in _erster
_Lesung _ohne _Änderungen _verabschiedet _.

Most words are merged, except *_dis abled* in English, and *_T ransp ortausschuß* in German for instance. At this point, the corpus is not composed of words anymore, but rather of subwords.

4.1.3 Extract alignments

To evaluate if the BPE units are good, bilingual corpora are aligned and then compared against a gold standard. The motivation behind alignment and how it works can be found in 3.2. The challenge here lies in the fact that if the BPEs are of good quality, the alignment algorithm will align subword items correctly, and therefore in the subword-to-word mapping, the word alignments will have a high score relative to the gold standard.

On the first step, alignment, two algorithms have been used, namely *Fastalign* and *Eflomal*. The software installation guides can be found in the development section 5. These algorithms take English text and German as input and create an alignment file as output. For the example above:

English sentence: The Committee on Transport and Tourism has adopted four amendments
for the second reading .

German sentence: Der Transportausschuß hat für die zweite Lesung vier Änderungsanträge
beschlossen .

Alignment output: 0-0 1-1 2-1 3-1 4-1 5-1 6-2 7-9 8-7 9-8 10-3 11-4 12-5 13-6 14-10

English sentence: The initial Commission proposal was adopted unamended by Parliament
on first reading .

German sentence: Der ursprüngliche Vorschlag der Kommission wurde vom Parlament in
erster Lesung ohne Änderungen verabschiedet .

Alignment output: 0-0 1-1 2-4 3-2 3-3 4-5 5-13 6-11 6-12 7-6 8-7 9-8 10-9 11-10 12-14

Many words have one-to-one alignment, such as *four-vier* and *adopted-verabschiedet*. Some others have many-to-one alignments, such as *Committee on Transport and Tourism-Transportausschuß* and one-to-many alignments such as *unamended-ohne Änderungen*. In our case however, the input files are not composed by words, but rather by subwords. And the alignments are done among subwords. Using the example above but with subwords instead of words:

English sentence: _the _Committee _on _Transport _and _Tourism _has _adopted _four
_amendments _for _the _second _reading _.
German sentence: _der _T ransp ortausschuß _hat _für _die _zweite _Lesung _vier
_Änderungsanträge _beschlossen _.
Alignment output: 0-0 1-1 2-1 3-1 4-1 5-1 1-2 2-2 3-2 4-2 5-2 1-3 2-3 3-3 4-3 5-3 6-4 7-11 8-9
9-10 10-5 11-6 12-7 13-8 14-12

Now there are subword alignments as opposed to word alignments. For instance, since the German word *Transportausschuß* is divided into three words, namely *T ransp ortausschuß*, the many-to-one alignment from the previous case is now a many-to-many alignment. The number of alignment has grown from last example. Because the gold standard against which the system is being evaluated consists of word alignments, it is necessary to map subword alignments into word alignments, which is the second step in this algorithm. Using English and German corpora and the alignment file as input files, this algorithm gives a word alignment file as output.

English sentence: _the _Committee _on _Transport _and _Tourism _has _adopted _four
_amendments _for _the _second _reading _.
German sentence: _der _T ransp ortausschuß _hat _für _die _zweite _Lesung _vier
_Änderungsanträge _beschlossen _.
Subword alignment: 0-0 1-1 2-1 3-1 4-1 5-1 1-2 2-2 3-2 4-2 5-2 1-3 2-3 3-3 4-3 5-3 6-4 7-11
8-9 9-10 10-5 11-6 12-7 13-8 14-12
Word alignment output: 0-0 1-1 2-1 3-1 4-1 5-1 6-2 7-9 8-7 9-8 10-3 11-4 12-5 13-6 14-10

4.1.4 Calculate alignment scores

In the final step, the alignment scores are computed against the gold standard. After loading the gold dataset, each alignment file is matched against this dataset, obtaining precision, recall, F1 score and AER metrics. In the case of 100 learnt symbols, there will be an associated score and so on for other numbers of learnt symbols. Additionally, the gold standard's scores are also computed as a baseline. To make it more visual, the scores are plotted and saved into a *.png* image file as well as *.csv* file with the exact numbers.

4.2 Replication of BPE-dropout

BPE-dropout is difference with regards to normal BPE is the fact that some merges do not take place. Based on this random factor, each time this system is carried out, new BPE merges are created. For example, if the most merge in English ($_t, h$) is not merged, the resulting file of BPE merges is vastly different than if the 10th most frequent merge does not take place. In order to obtain different instances, the dropout algorithm is run a number of times, in this case 10 times, the alignments extracted 10 times, and then the alignments aggregated. Regarding each specific step, the algorithm to create the merge list (`learn_bpe`) remains unchanged, the first slight change occurs when applying the BPE algorithm to the corpus.

In the apply-BPE algorithm, a random variable is created for every merge: if it falls below a threshold, the dropout threshold, the merge in question is discarded. Apart from this, the whole algorithm is run a number of times, creating a number of BPE files, usually ten throughout this thesis. When extracting alignments, since now there are ten BPE files instead of a single one, the whole algorithm is run ten times, and alignments for all numbers of merges multiplied by all dropout repetitions are saved. At this point, there are ten alignments for each sentence. Which alignments to pick, is the next step to be resolved. Three methods are selected:

- Create the union of all alignments.
- Create the intersection of all alignments.
- Create a threshold parameter, for example 0.5. If an alignment is present in 50% of all alignments for that sentence, it is added to the aggregated file.

To illustrate this with a example. Files 1, 2 and 3 are three alignment files for a given sentence pair.

- File 1: 0-0 0-1 1-1 1-2 2-3
- File 2: 0-0 0-1 1-2
- File 3: 0-0 1-1 1-3
- Union file: 0-0 0-1 1-1 1-2 1-3 2-3
- Intersection file: 0-0
- Aggregated file: 0-0 0-1 1-1 1-2

As it is visible in the example, the **union** case takes all alignments into account. By brute force, possibly most of the correct alignments will be present in the alignment, yielding a high recall, but the majority of the alignments in the union file will be incorrect, that is, it will have low precision. By contrast, the **intersection** case is the opposite. The file is much shorter since only the alignments present in *all* files are considered, which means that these alignments will mostly be correct. But also many of the actually correct alignments will not be present, because they might have been skipped, and therefore are not present in the intersection.

The method of creating an **aggregated file** with the threshold aims to alleviate this problem by creating a sort of middle point between union and intersection. Taking a threshold value closer to 0 will

mean that almost all alignments will be accepted, and therefore the score will be closer to the score of the union. In the opposite end of the spectrum, a threshold value close to 1 means that only alignments present in most alignment files will be accepted, and this resembles the intersection. Many experiments have been done with threshold values ranging from 0.3 to 0.9, and the corresponding scores can be found in the Results chapter.

4.3 Improvement of learn-BPE algorithm

One of the drawbacks of the algorithm to learn-BPE units is that every time a pair of sequences is merged in the corpus, all sequence pairs and their frequencies has to be computed from scratch. This requires iterating over all characters from each sentence in the corpus, and for each iteration, a pair of sequences gets merged.

4.3.1 Updating only neighboring sequences

In order to understand the magnitude of this computation, let us explore the step of merging a pair in the corpus. We can use this small corpus as an example:

```
0 A start and the end .
1 The index of a document .
2 My name is Bob .
```

In the foremost step, all characters are separated into individual tokens, and the beginning of the work is marked:

```
0 _A _s t a r t _a n d _t h e _e n d .
1 _T h e _i n d e x _o f _a _d o c u m e n t .
2 _M y _n a m e _i s _B o b .
```

For the sake of the example, let us assume that ('n', 'd') is the most frequent pair of tokens. When merging them, the corpus is altered in the following way:

```
0 _A _s t a r t _a n d _t h e _e n d .
1 _T h e _i n d e x _o f _a _d o c u m e n t .
2 _M y _n a m e _i s _B o b .
```

In the brute force approach, each pair's frequency is computed again: the sequence pairs ('_T', 'h'), ('h', 'e'), etc. are all revisited and their frequencies counted from scratch. But this does not have to be the case, actually the only pairs that need to be updated are the ones surrounding ('n', 'd'). When viewing this merge from a different perspective, these are the changes that occur in the pairs of tokens:

- ('_a', 'n') in sentence 0 now becomes ('_a', 'nd')
- ('_e', 'n') in sentence 0 now becomes ('_e', 'nd')
- ('i', 'n') in sentence 1 now becomes ('i', 'nd')

- ('d', 'e') in sentence 1 now becomes ('nd', 'e')

The pair of tokens in the word 'and' which previously was ('_a', 'n'), now becomes ('_a', 'nd') since 'n' and 'd' have been merged. In this instance, the pair ('_a', 'n') no longer exists, and a new pair has been created: ('_a', 'nd'). And so on for the rest of the tokens. As a result, only the following frequency updates must be made:

- Reduce frequency of ('_a', 'n') by 1, increase frequency of ('_a', 'nd') by 1.
- Reduce frequency of ('_e', 'n') by 1, increase frequency of ('_e', 'nd') by 1.
- Reduce frequency of ('i', 'n') by 1, increase frequency of ('i', 'nd') by 1.
- Reduce frequency of ('d', 'e') by 1, increase frequency of ('n', 'de') by 1.

All the other pairs remain unchanged. This is the major improvement of this thesis regarding the learn-BPE algorithm, **the fact that only neighboring tokens of the merged pair need to be updated**. Now, instead of updating each pair in each sentence, it is only necessary to update the merge pair's surrounding tokens. The way to do this is by locating the merged pair in the sentence, and updating the previous and next tokens.

4.3.2 Saving indexes of pairs

If a pair is very frequent, it is safe to assume that it will be present in the majority of the sentences in the corpus. In the example above, the last sentence does not contain the ('n', 'd') pair. In a bigger corpus, the more merges are done, the rarer they become. It is therefore useful to only visit those sentences where the pair is present. If the merged pair only appears in 10% of the corpus' sentences, it is a waste of resources to visit all sentences. This can be solved by saving the index where each pair appears. This way, each pair has its frequency associated to it, as well as a list of indexes where it is present. Creating this index list can be done in the initial step of the algorithm when the corpus is read and iterated completely, each pair's frequency computed for the first time, and the indexes recorded.

This way, when accessing the most frequent pair in the corpus, we can also access to the sentences they are present in, and iterate only those.

4.4 BPE without word boundaries

Up until this point, the underlying principle of creating BPE units is that merges between words are not considered. But given the existence of languages without any clear word boundaries, this thesis also explores what would happen if merges between different words were allowed, which has not been done before in literature, to the knowledge of the author. Regarding the algorithm pipeline, all remains the same except the algorithm to create BPE merges. Now, instead of having a special token to mark the beginning of each word, the same token is used to replace whitespace. For instance, the space mode tokenization used until now and the new no-space mode tokenization:

- Raw sentence: The cake is delicious .
- Sentence after space mode tokenization: _T h e _c a k e _i s _d e l i c i o u s .
- Sentence after no-space mode tokenization: T h e _c a k e _i s _d e l i c i o u s _ .

This way, merges with whitespace are possible, as well as merges between endings of some words and beginnings of the next. After learning BPE units using this method, these are the most common merges in English: e _, t h, s _, t _, n _, d _, t h e_, e r, i n, y _. The most common BPE unit between words is *of_ the_*. As for German, the most common merges are: n _, e r, e n_, c h, e _, _ d, e i, u n, t _, e r _. And the most common BPE unit between words is , _*da*.

Since now merges between words are possible, there are many more possible merges, and the algorithm is not as fast as in the space mode. The rest of the algorithms, namely applying BPE units to a corpus, extracting alignments, and calculating scores remain the same. However, it is important to consider that when aligning units this way, a unit containing multiple words might get aligned to a unit containing also multiple words, so the mapping subword to word is slightly altered, relative to the previous case where only parts of words were aligned.

5 Development

This chapter explains the development of the thesis in a deeper way, adding more detailed explanations, the code and algorithms previously explained in the Methodology section. 4 This chapter includes coding practices, how global variables are stored and treated, the tree directory of the project, and the various tasks that have been undertaken during this thesis, which include the following:

1. Replication of the BPE algorithm and results
2. Replication of the BPE-dropout algorithm and results
3. Improvement of the learn BPE algorithm
4. Study and implementation of BPE without word boundaries

5.1 Coding practices

To ensure consistency, the parameters for the pipeline, called global variables, such as num_symbols, dropout, file paths, etc. have been written in *settings.py*. The word separator is a special Unicode character. The languages used as source and target languages are English and German respectively. The number of symbols to be learnt in the learn-BPE phase is set as 20000. When applying these merges to the corpus, in order to have different variants and explore the differences between merging few symbols or more, a number of key numbers are selected for these experiments, as seen in the variable *all_symbols*.

```
1  # settings.py
2  import os
3  import glob
4  from os.path import join
5
6  word_sep = u'\u2581'
7  source, target = 'eng', 'deu'
8  learn_merges = 20000
9  merges = [100, 200, 500, 1000, 2000, 4000, 6000, 8000]
10
11 rootdir = os.getcwd()
12 if rootdir.split(os.sep)[-1] == 'src':
13     rootdir = os.sep.join(rootdir.split(os.sep)[: -1])
14 datadir = join(rootdir, 'data')
15 inputdir = join(datadir, 'input', source+'-'+target)
16 bpedir = join(datadir, 'normal_bpe')
17 baselinedir = join(rootdir, 'reports', 'scores_normal_bpe')
18 scoredir = join(rootdir, 'reports', 'scores_normal_bpe')
19 goldpath = join(inputdir, source+'_'+target+'.gold')
20 inputpath = {}
21 for filename in glob.glob(join(inputdir, "*.txt")):
22     inputpath[filename.split(os.sep)[-1].split('_')[0]] = filename
```

Regarding directories and paths, the tree view of the project is displayed in the following figure. The input data is saved into *data/input*, the rest of the intermediate data files such as *.bpe*, *.wgdfa* and others are saved into their respective folder depending on the dropout parameter. The models are saved in the general *data* folder with the *.model* extension. The LaTeX files for writing this thesis are saved in the *doc* folder, the score figures and csv files in *reports*, all Python scripts in *src*, the *Fastalign* and *Eflomal* installation files in *tools*, and README, requirements, gitignore and the global variable file *settings.py* are saved in the root folder.

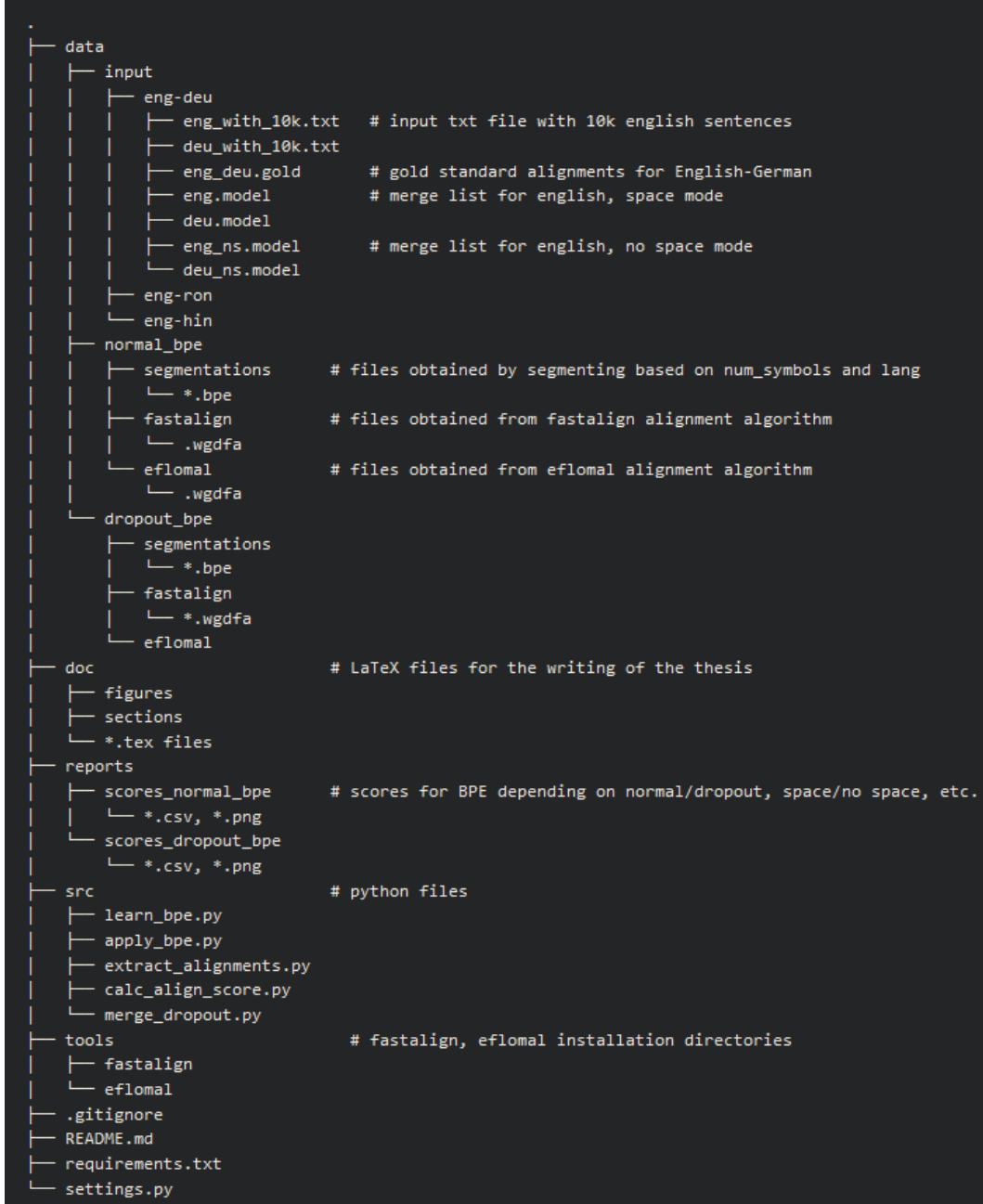


Figure 5.1: Project directories in tree mode

5.2 Replication of BPE results

The first programming task in this thesis has been to replicate the BPE results from Sennrich et al. [9]. In order to modularize the code in clear units, these have been the steps:

1. Write the learn-BPE from corpus algorithm
2. Write the apply-BPE to corpus algorithm
3. Write extract alignments script
4. Write calculate alignment scores script

In the following sections, each step will be explained in detail, with comments and examples for each function.

5.2.1 Learn-BPE algorithm

In learning BPE units, the first step is to read the corpus into an appropriate format. All the libraries and global variables imported are also added here for simplicity.

```

1  # learn_bpe.py
2  import os
3  import re
4  import sys
5  import codecs
6  from os.path import join
7  from collections import defaultdict, Counter
8  # import global variables from settings.py
9  sys.path.insert(1, os.path.join(sys.path[0], '..'))
10 from settings import *
11
12 def read_corpus(corpus: list) -> list:
13     '''
14     Read corpus, strip index and new line characters.
15     A word_sep symbol is added at the beginning of each word.
16     example:
17     tokens = [
18         '\_w e \_d o \_n o t \_b e l i e v e
19         \_t h a t \_w e \_s h o u l d
20         \_c h e r r y - p i c k \_.' ,
21         ...
22     ]
23     '''
24     tokens = []
25     for line in corpus:
26         line = line.split('\t')[1].strip('\r\n ')
27         line = line.split()
28         line[0] = str.lower(line[0])
29
30         # add word_sep to each beginning of word and join by space
31         tokens.append(' '.join([word_sep + ' '.join(word) for word in line]))
32     return tokens

```

Once the corpus is parsed, all pairs and their frequencies are computed and saved in a suitable data structure.

```

1  # learn_bpe.py
2  def get_stats(tokens: list) -> Counter:
3      '''
4      Count frequency of all bigrams and the frequency per index.
5      pairs = {
6          ('s', 'h'): 5,
7          ('h', 'e'): 6
8      }
9      The last token '.' or word_sep. is not merged with anything.
10     '''
11     pairs = Counter()
12     for i, sent in enumerate(tokens):
13         # get stats for each word independently,
14         # no bigrams between different words
15         for word in sent[1:].split(' ' + word_sep):
16             symbols = symbols.split()
17             for j in range(len(symbols) - 1):
18                 pairs[symbols[j], symbols[j + 1]] += 1
19     return pairs

```

Following the algorithm explained in the previous chapter, 4.1.1, the big/outer loop iterates between extraction of highest frequency pairs and merging of corpus until the maximum number of merges is reached.

```

1  # learn_bpe.py
2  def merge_token(corpus: list, most_frequent: tuple) -> list:
3      str_corpus = '\n'.join(corpus)
4      str_corpus = str_corpus.replace(' '.join(most_frequent), ''.join(most_frequent))
5      return str_corpus.split('\n')
6
7  def learn_bpe(argsinput: str) -> list:
8      '''
9      Learn BPE operations from vocabulary. Steps:
10     1. split corpus into characters, count frequency
11     2. count bigrams in corpus
12     3. merge most frequent symbols
13     4. Update bigrams in corpus
14     '''
15     corpus = read_corpus(argsinput)
16     most_frequent_merges = []
17     for i in range(learn_merges):
18         pairs = get_stats(corpus)
19         try:
20             most_frequent = pairs.most_common(1)[0][0]
21         except:
22             # pairs is empty
23             break
24         most_frequent_merges.append(most_frequent)
25         corpus = merge_token(corpus, most_frequent)
26     return most_frequent_merges

```

After the loop ends, the merge list is saved into a *.bpe* file. The following code includes this function as well as the main function that calls out all functions.

```

1  #learn_bpe.py
2  def write_bpe(lang: str, most_freq_merges: list):
3      bpe_file = codecs.open(join(datadir, lang+'.model'), 'w', encoding='utf-8')
4      bpe_file.write(f"{lang} {len(most_freq_merges)}\n")
5      bpe_file.write('\n'.join(' '.join(item) for item in most_freq_merges))
6      return
7
8  if __name__ == '__main__':
9      for lang in [source, target]:
10         argsinput = codecs.open(inputpath[lang], encoding='utf-8')
11         most_freq_merges = learn_bpe(argsinput)
12         write_bpe(lang, most_freq_merges)

```

5.2.2 Apply-BPE algorithm

After learning BPE units, there is already a merge list written into the project data directory, which can now be loaded into memory in order to apply these merges to the corpus. The following function returns a list of the languages present in the project, BPE models and corpora for each language.

```

1  # apply_bpe.py
2  import os
3  from os.path import join
4  import sys
5  import codecs
6  # import global variables from settings.py
7  sys.path.insert(1, os.path.join(sys.path[0], '..'))
8  from settings import *
9  from learn_bpe import read_bpe_model, read_corpus
10
11 def load_data() -> (list, list, list):
12     langs = [source, target]
13     bpe_models = []
14     corpora = []
15     for lang in langs:
16         argsinput = codecs.open(inputpath[lang], encoding='utf-8')
17         corpora.append(read_corpus(argsinput))
18         bpe_model = codecs.open(join(datadir, lang+'.model'), encoding='utf-8').readlines()
19         bpe_model = [tuple(item.strip('\r\n ').split(' ')) for item in bpe_model]
20         bpe_models.append(bpe_model[1:])
21     return langs, bpe_models, corpora

```

Once this data is available, the merge list is applied to the corpus iteratively, for the symbols present in the global variable *all_symbols*. To avoid repetition, when aiming for 8000 merges, the loop is halted at 100, 500 merges respectively, in order to save the state of the corpus into the *.bpe* file. After writing the file in the system, the loop resumes again. A less efficient approach would be making the loop run until 100 merges, then start from scratch and run until 500, and so on. This method is equally effective but not nearly as efficient.

```

1 # apply_bpe.py
2 def write_bpe(lang: str, num_symbols: int, merged_corpus: str):
3     outputpath = join(bpedir, 'segmentations', f"{lang}_{num_symbols}.bpe")
4     argsoutput = codecs.open(outputpath, 'w', encoding='utf-8')
5     argsoutput.write(merged_corpus)
6     return
7
8 def apply_bpe(langs: list, bpe_models: list, corpora: list):
9     for lang, bpe_model, corpus in zip(langs, bpe_models, corpora):
10         bpe_model = bpe_model[:max(merges)]
11         k = 0
12         str_corpus = '\n'.join(corpus)
13         for j, bigram in enumerate(bpe_model):
14             str_corpus = str_corpus.replace(' '.join(bigram), ''.join(bigram))
15             if j + 1 == merges[k]:
16                 write_bpe(lang, merges[k], str_corpus)
17                 k += 1
18     return
19
20 if __name__ == "__main__":
21     os.makedirs(join(bpedir, 'segmentations'), exist_ok=True)
22     langs, bpe_models, corpora = load_data()
23     apply_bpe(langs, bpe_models, corpora)

```

After this step, in the directory `../data/normal_bpe/segmentations/` various files exist with the following format:

- eng_100.bpe
- eng_200.bpe
- ...
- deu_100.bpe
- deu_200.bpe
- ...

deu or *eng* refers to the language, and the numbers are the amount of merges that have been applied into this file. For examples, see 4.1.2.

5.2.3 Extract alignments

This step requires some prior installation of the alignment software. The thesis has been conducted in a Linux environment, so the installation guide is adapted to this case. The installation of the software in any other OS is however possible, as long as the user adapts the commands to their OS. Initially, if not present in the system, it is mandatory to install Cmake. The installation steps for *Fastalign* are as follows, in bash. The path *path/to/project* should be the path to where the README, data folders and so on are present. Here, a new folder named *tools* is created to save the alignment algorithms.

```
sudo apt-get install libgoogle-perftools-dev libsparsehash-dev
cd /path/to/project
mkdir tools
cd tools
git clone https://github.com/clab/fast_align.git
cd fast_align
mkdir build
cd build
cmake ..
make
```

And for *Eflomal*:

```
cd /path/to/project/tools
git clone https://github.com/robertostling/eflomal.git
cd eflomal
make
sudo make install
python3 setup.py install
```

The paths for the installation are then saved in the global variable file, as well as the *mode* to make the alignments, either of the two algorithms.

```
1 # settings.py
2 mode = "fastalign" #fastalign, eflomal
3 fastalign_path = join(rootdir, "tools/fast_align/build/fast_align")
4 atools_path = join(rootdir, "tools/fast_align/build/atools")
5 eflomal_path = join(rootdir, "tools/eflomal")
```

In this step, as a general notion, the extract alignments script takes two files as input: English BPE file, German BPE file, and outputs an alignment file, with the extension *.wgdfa*. First of all, it is necessary to iterate through the different merge types that have been done before. There are BPE files with 100 merges, 200, 500, etc for both languages. At each iteration, a different alignment file is created. Regarding alignment algorithms, they work on parallel data, that is, they expect text in the following format:

Hello from England ||| Hallo aus Deutschland

Since the BPE files do not have this format, they are actually separated into two files, namely *deu* and *eng* files, first of all the function *create_parallel_text* creates a *.txt* file in the appropriate parallel format.

```
1 # extract_alignments.py
2 from os.path import join
3 import os
4 import sys
5 import codecs
6 # import global variables from settings.py
7 sys.path.insert(1, os.path.join(sys.path[0], '..'))
```



```

8 from settings import *
9 from subword_word import *
10
11 def create_parallel_text(sourcepath: str, targetpath: str, outpath: str):
12     fa_file = codecs.open(outpath + '.txt', "w", "utf-8")
13     fsrc = codecs.open(sourcepath, "r", "utf-8")
14     ftrg = codecs.open(targetpath, "r", "utf-8")
15     for sl, tl in zip(fsrc, ftrg):
16         sl = sl.strip().split("\t")[-1]
17         tl = tl.strip().split("\t")[-1]
18         fa_file.write(f"{sl} ||| {tl}\n")
19     fa_file.close()
20     return

```

Fastalign and *eflomal* work by issuing a command on the OS terminal, and they generate forward and reverse alignments. This is handled by the *create_fwd_rev_files* function, which creates *.fwd* and *.rev* files with the corresponding file name.

```

1 # extract_alignments.py
2 def create_fwd_rev_files(outpath: str):
3     if mode == "fastalign":
4         os.system(f"{fastalign_path} -i {outpath}.txt -v -d -o > {outpath}.fwd")
5         os.system(f"{fastalign_path} -i {outpath}.txt -v -d -o -r > {outpath}.rev")
6     elif mode == "eflomal":
7         os.system(f"cd {eflomal_path}; python align.py -i {outpath}.txt --model 3 -f {
8                                     outpath}.fwd -r {outpath}.rev")
9     return

```

Given these *.fwd* and *.rev* files, the alignment algorithm creates a type of union between these two, called *grow-diag-final-and*, handled by the *create_gdfa_file* function, creating files with the extension *.gdfa*. The previously generated files, *.fwd*, *.rev*, *.txt* and the intermediate file *_unnum.gdfa* are deleted from the system.

```

1 # extract_alignments.py
2 def create_gdfa_file(outpath: str):
3     # create gdfa file from .fwd and .rev
4     comm = f"{atools_path} -i {outpath}.fwd -j {outpath}.rev -c grow-diag-final-and > {
5                                     outpath}_unnum.gdfa"
6
7     os.system(comm)
8
9     # parse _unnum.gdfa to .gdfa with "\t" separator
10    with codecs.open(f"{outpath}_unnum.gdfa", "r", "utf-8") as fi:
11        with codecs.open(f"{outpath}.gdfa", "w", "utf-8") as fo:
12            for i, line in enumerate(fi):
13                fo.write(f"{i}\t{line.strip()}\n")
14
15    # delete unnecessary files
16    comm = f"rm {outpath}_unnum.gdfa; rm {outpath}.fwd; rm {outpath}.rev; rm {outpath}.
17                                     txt"
18
19    os.system(comm)
20    return

```

As explained in the *Extract alignment* subsection in the Methodology chapter 4.1.3, the alignment aligns whitespace-separated units, which are generally words but in this case are subword, or BPE units. In order to actually make alignments between words, the subword alignments need to be transformed into word alignments. The function `load_and_map_segmentations` loads the BPE files and maps each BPE unit to its corresponding word. The comments on the function display a simple example to illustrate this concept. This is an auxiliary function in order to map the alignments later. Afterwards, by calling `bpe_word_align`, the mapping from subword alignments to word alignments is made. Lastly, the new alignments are saved in a file with the extension `.wgdfa`.

```

1  # extract_alignments.py
2  def load_and_map_segmentations(num_symbols: int):
3      '''
4      Given a .bpe file composed of the corpus made of subword units such as
5      corpus_eng = [
6          '_We _do _no t _be li eve _.',
7          '_Thi s _is _a _sent ence _.',
8          ...
9      ]
10     Output: dictionary of each language and
11     a list of indexes pointing to which word each element (_do) belongs to
12     bpes = {
13         'eng':[
14             [0, 1, 2, 2, 3, 3, 3, 4],
15             [0, 0, 1, 2, 3, 4, 5],
16             ...
17         ],
18         ...
19     }
20     '''
21     bpes = {}
22     for lang in [source, target]:
23         bpes[lang] = []
24         corpus = codecs.open(lang+'_'+str(num_symbols)+'.bpe', encoding='utf-8')
25         for sent in corpus:
26             mapping = [0]
27             i = 0
28             for subw in sent.split()[1:]:
29                 if subw[0] == word_sep:
30                     i += 1
31                 mapping.append(i)
32             bpes[lang].append(mapping)
33     return bpes
34
35 def bpe_word_align(bpes: dict, bpe_aligns: list) -> str:
36     '''
37     Input: dictionary of bpes obtained as output of map_subword_to_word()
38     Output: list of word alignments and their indexes
39     "
40         0    0-0 0-1 1-1 1-2 3-1 2-4 \n
41         1    0-0 1-0 1-1 2-1 \n
42         ...

```

```

43     "
44     ' ' '
45     all_word_aligns = ''
46     for i, (sent1, sent2, bpe_al) in enumerate(zip(bpes[source], bpes[target],
47                                                    bpe_aligns)):
48         word_aligns = set()
49         # iterate each alignment
50         for al in bpe_al.split('\t')[1].split():
51             firstal, secondal = al.split('-')
52             new_al = str(sent1[int(firstal)]) + '-' + str(sent2[int(secondal)])
53             word_aligns.add(new_al)
54         all_word_aligns += str(i) + "\t" + ' '.join(word_aligns) + "\n"
55     return all_word_aligns

```

The alignment algorithm is executed for two types of files. Firstly, for the raw corpus itself, the alignment algorithm is executed to align the English raw corpus with the German raw corpus, which will serve as baseline to check how good the BPE merges are. And then, the alignment algorithm is executed for the BPE files themselves.

```

1  # extract_alignments.py
2  def extract_alignments(input_mode=False: bool):
3      for num_symbols in merges:
4          if input_mode:
5              print("Alignments for input files")
6              sourcepath = inputpath[source]
7              targetpath = inputpath[target]
8              outpath = join(bpedir, mode, "input")
9          else:
10             print(f"Alignments for {num_symbols} symbols")
11             sourcepath = join(bpedir, 'segmentations', f"{source}_{num_symbols}.bpe")
12             targetpath = join(bpedir, 'segmentations', f"{target}_{num_symbols}.bpe")
13             outpath = join(bpedir, mode, str(num_symbols))
14             create_parallel_text(sourcepath, targetpath, outpath)
15             create_fwd_rev_files(outpath)
16             create_gdfa_file(outpath)
17             # map alignment from subword to word
18             bpes = load_and_map_segmentations(num_symbols)
19             all_word_aligns = bpe_word_align(bpes, codecs.open(o+'.gdfa', encoding='utf-8'))
20             os.system(f"rm {outpath}.gdfa")
21             codecs.open(outpath+'.wgdfa', 'w', encoding='utf-8').write(all_word_aligns)
22         return
23
24  if __name__ == "__main__":
25      os.makedirs(join(bpedir, mode), exist_ok=True)
26      if not os.path.isfile(join(bpedir, mode, 'input.wgdfa')):
27          extract_alignments(input_mode=True)
28      extract_alignments()

```

5.2.4 Calculate alignment scores

At this point in the pipeline, the alignments between subword units are obtained, mapped into word alignments, and the last step to be performed is to calculate the alignment scores. First of all, the gold

alignment file is loaded and its alignments extracted.

```

1  # calc_align_scores.py
2  import os
3  from os.path import join
4  import sys
5  import glob
6  import random
7  import collections
8  import pandas as pd
9  import matplotlib.pyplot as plt
10 import seaborn as sns
11 # import global variables from settings.py
12 sys.path.insert(1, os.path.join(sys.path[0], '..'))
13 from settings import *
14
15 def load_gold(g_path: str) -> (dict, dict, float):
16     gold_f = open(g_path, "r")
17     pros = {}
18     surs = {}
19     all_count = 0.
20     surs_count = 0.
21     for line in gold_f:
22         line = line.strip().split("\t")
23         line[1] = line[1].split()
24         pros[line[0]] = set()
25         surs[line[0]] = set()
26         for al in line[1]:
27             pros[line[0]].add(al.replace('p', '-'))
28             if 'p' not in al:
29                 surs[line[0]].add(al)
30         all_count += len(pros[line[0]])
31         surs_count += len(surs[line[0]])
32     return pros, surs, surs_count

```

The next function, given an input path, calculates the precision, recall, F1 and AER score based on the gold standard.

```

1  # calc_align_scores.py
2  def calc_score(input_path: str, probs: dict, surs: dict, surs_count: float) -> (float,
                                                                                   float, float, float):
3
4     total_hit, p_hit, s_hit = 0., 0., 0.
5     target_f = open(input_path, "r")
6     for line in target_f:
7         line = line.strip().split("\t")
8         if line[0] not in probs: continue
9         if len(line) < 2: continue
10        line[1] = line[1].split()
11        for pair in line[1]:
12            if pair in probs[line[0]]:
13                p_hit += 1
14            if pair in surs[line[0]]:
15                s_hit += 1
16        total_hit += 1

```

```

16 target_f.close()
17 y_prec = round(p_hit / max(total_hit, 1.), 3)
18 y_rec = round(s_hit / max(surs_count, 1.), 3)
19 y_f1 = round(2. * y_prec * y_rec / max((y_prec + y_rec), 0.01), 3)
20 aer = round(1 - (s_hit + p_hit) / (total_hit + surs_count), 3)
21 return y_prec, y_rec, y_f1, aer

```

This step is done for the baseline, to obtain a measure of the standard version of the system, that is, the raw English and German corpora, and then for the BPE files itself.

```

1 # calc_align_scores.py
2 columns = ['num_symbols', 'prec', 'rec', 'f1', 'AER']
3
4 def get_baseline_score(probs: dict, surs: dict, surs_count: int) -> pd.DataFrame:
5     alfile = join(bpedir, mode, 'input.wgdfa')
6     score = [0]
7     score.extend(list(calc_score(alfile, probs, surs, surs_count)))
8     baseline_df = pd.DataFrame([score], columns=columns).round(decimals=3)
9     return baseline_df
10
11 def calc_align_scores(probs: dict, surs: dict, surs_count: int):
12     scores = []
13     for num_symbols in merges:
14         alfile = join(bpedir, mode, f"{num_symbols}.wgdfa")
15         score = [int(num_symbols)]
16         score.extend(list(calc_score(alfile, probs, surs, surs_count)))
17         scores.append(score)
18     df = pd.DataFrame(scores, columns=columns).round(decimals=3)
19     return df

```

The scores for the baseline and the corresponding BPE files are obtained and stored in a DataFrame data structure. Next, this data is plotted and saved into *.png* and *.csv* files.

```

1 # calc_align_scores.py
2 def plot_scores(df: pd.DataFrame, baseline_df: pd.DataFrame, scoredir: str):
3     # Use plot styling from seaborn.
4     sns.set(style='darkgrid')
5     # Increase the plot size and font size.
6     sns.set(font_scale=1.5)
7     plt.rcParams["figure.figsize"] = (12, 6)
8     plt.clf()
9     ax = plt.gca() # gca stands for 'get current axis'
10    colors = ['magenta', 'tab:blue', 'tab:green', 'tab:red']
11    df = df.sort_values('num_symbols')
12    columns = list(df)
13    for column, color in zip(columns[1:], colors):
14        df.plot(kind='line', x=columns[0], y=column, color=color, ax=ax)
15    for baseline_results, color in zip(list(baseline_df.iloc[0][1:]), colors):
16        plt.axhline(y=baseline_results, color=color, linestyle='dashed')
17    plt.savefig(join(scoredir+'.png'))
18    return
19
20

```

```

21 if __name__ == "__main__":
22     # Calculate alignment quality scores based on the gold standard.
23     # The output contains Precision, Recall, F1, and AER.
24     probs, surs, surs_count = load_gold(goldpath)
25     baseline_df = get_baseline_score(probs, surs, surs_count)
26     df = calc_align_scores(probs, surs, surs_count, baseline_df)
27     scorename = join(scoredir, 'scores')
28     print(f"Scores saved into {scorename}")
29     df.to_csv(scorename+'.csv', index=False)
30     plot_scores(df, baseline_df, scorename)

```

5.3 Replication of BPE-dropout

The previous section has laid the backbone of the algorithms, the various files and functions. In this and the following sections, some modifications and improvements are introduced to the already existing Python scripts. For the sake of simplicity, the code snippets that follow only include the new changes, or the functions from the last section with new modifications, and the modifications are introduced by signalling the line numbers from previous scripts in which changes are introduced. For example, it might be mentioned that a certain line is added to line 21 of a certain function in a specific script. This refers to the function introduced in the previous section, and it will be referred as such. In the case that a function is altered in a significant way, the new version of the function will be shown, which overrules the previous version. The functions that remain unaltered are not shown.

When adding dropout to BPE, three new parameters come into play in the project, namely **dropout** rate, **dropout_samples**, that is, how many samples of the dropout system are considered, and **merge_threshold**, which serves its function with alignments later on. These values are saved into *settings.py*, as well as new data directories to store files resulting from BPE-dropout.

```

1 # settings.py
2
3 dropout = 0.1
4 dropout_samples = 10
5 merge_threshold = [0.3, 0.5, 0.7, 0.9]
6
7 bpedir = join(datadir, 'dropout_bpe' if dropout > 0 else 'normal_bpe')
8 scoredir = join(rootdir, 'reports', 'scores_' + ('dropout_bpe' if dropout > 0 else 'normal_bpe'))

```

5.3.1 Apply-BPE to corpus with dropout

The first modifications in the project occur in *apply_bpe.py*, where some merges are skipped, and the process is repeated 10 times. More theoretical insights regarding this approach can be found in the Methodology section 4.2. The function *apply_bpe* includes two new lines where a random number between 0 and 1 is generated. If this number is smaller than the *dropout* rate saved in *settings.py*, then that merge is not considered and the loop skips it. This means that if the *dropout* variable has the value of 0.1, 10% of merges are skipped.

Additionally, in the main function, the function *apply_bpe* is called *dropout_samples* times. To save the files accordingly, a new variable is introduced, namely *i*, that does nothing in the case where

dropout=0, but when repeating the process, for instance if lang=eng, num_symbols=2000, and first iteration of dropout, that is, i=0, the files are saved as *eng_2000_0.bpe* instead, and so on for further iterations. This is effectively achieved by changing the variable *outputpath*. In the function *write_bpe* in the general pipeline 5.2.2, the following modifications are made:

```

1  # apply_bpe.py
2  import random
3
4  def write_bpe(lang: str, num_symbols: int, merged_corpus: str, i: int ==-1):
5      outputpath = join(bpedir, 'segmentations', f"{lang}_{num_symbols}_{f'_{i}' if i != -1
6                                     else ''}.bpe")
7      argsoutput = codecs.open(outputpath, 'w', encoding='utf-8')
8      argsoutput.write(merged_corpus)
9      return
10
11 def apply_bpe(langs: list, bpe_models: list, corpora: list, i: int ==-1):
12     for lang, bpe_model, corpus in zip(langs, bpe_models, corpora):
13         bpe_model = bpe_model[:max(merges)]
14         merges_copy = merges.copy()
15         str_corpus = '\n'.join(corpus)
16         for j, bigram in enumerate(bpe_model):
17             if random.uniform(0, 1) < dropout:
18                 continue
19             str_corpus = str_corpus.replace(' '.join(bigram), ''.join(bigram))
20             if j + 1 == merges_copy[0]:
21                 write_bpe(lang, merges_copy.pop(0), str_corpus, i)
22         return
23
24 if __name__ == "__main__":
25     langs, bpe_models, corpora = load_data()
26     if dropout > 0:
27         for i in range(dropout_samples):
28             apply_bpe(i)
29     else:
30         apply_bpe()

```

5.3.2 Extract alignments with dropout

The only change in this step is that the *extract_alignment* 5.2.3 function is called *dropout_samples* times, which changes the function to write the alignments in the new format, namely, changing the variables *sourcepath* and *targetpath*. Additionally, the gold standard's alignments do not need to be calculated since the baseline are the BPE scores rather than the gold standard scores. The rest of the alignment algorithm remains unchanged.

```

1  # extract_alignments.py
2  # change line 2
3  def extract_alignments(i: int ==-1, input_mode: bool =False):
4
5  # change lines 11 and 12
6  sourcepath = join(bpedir, 'segmentations', f"{source}_{num_symbols}_{f'_{i}' if
7                                     dropout else ''}.bpe")

```

```

7 targetpath = join(bpedir, 'segmentations', f"{target}_{num_symbols}_{'_' + str(i) if
                                dropout else ''}.bpe")
8
9 # change line 30
10 if dropout > 0:
11     for i in range(dropout_samples):
12         extract_alignments(i)
13 else:
14     extract_alignments()

```

5.3.3 Calculate alignment scores with dropout

As explained in the Methodology section 4.2, variants of union, intersection and threshold are created. This is introduced with a new script, namely *merge_dropout.py*. First of all, the function *merge_dropout_alignments* opens all alignment files and creates a dictionary data structure with the union, intersection and threshold alignment files and saves them into *X_union.wgdfa*, *X_inter.wgdfa*, *X_thres.wgdfa* respectively.

```

1 # merge_dropout.py
2 import os
3 from os.path import join
4 import sys
5 import codecs
6 import pandas as pd
7 from tqdm import tqdm
8 from collections import Counter
9 # import global variables from settings.py
10 sys.path.insert(1, os.path.join(sys.path[0], '..'))
11 from settings import *
12 from calc_align_score import *
13
14 def merge_dropout_alignments():
15     union_merge, inter_merge, thres_merge = {}, {}, {}
16     for num_symbols in tqdm(merges, desc=f"merge_dropout: dropout={dropout}, union,
                                inter, thres"):
17         union_merge[num_symbols], inter_merge[num_symbols], thres_merge[num_symbols] = [],
                                [], []
18         for i in range(dropout_samples):
19             for j, line in enumerate(open(f'{num_symbols}_{i}.wgdfa', 'r').readlines()):
20                 al = frozenset(line.strip().split("\t")[1].split())
21
22                 # at the first iteration, just append the alignment
23                 if i == 0:
24                     union_merge[num_symbols].append(al)
25                     inter_merge[num_symbols].append(al)
26                     thres_merge[num_symbols].append(Counter(al))
27                     continue
28
29                 # do union, intersection or frequency addition
30                 union_merge[num_symbols][j] |= al
31                 inter_merge[num_symbols][j] &= al

```



```

32     thres_merge[num_symbols][j] += Counter(al)
33
34     # write to output
35     unionfile = codecs.open(f'{num_symbols}_union.wgdfa', 'w')
36     interfile = codecs.open(f'{num_symbols}_inter.wgdfa', 'w')
37     thresfiles = {merge_t: codecs.open(f'{num_symbols}_thres_{merge_t}.wgdfa', 'w')
38                   for merge_t in merge_threshold}
39
40     for i in range(len(union_merge[num_symbols])):
41         unionfile.write(f"{i}\t{' '.join(union_merge[num_symbols][i])}\n")
42         interfile.write(f"{i}\t{' '.join(inter_merge[num_symbols][i])}\n")
43         # get alignments more common than the merge_threshold %
44         for merge_t in merge_threshold:
45             common_aligns = [k for k in thres_merge[num_symbols][i]
46                              if thres_merge[num_symbols][i][k] > merge_t * dropout_samples]
47             thresfiles[merge_t].write(f"{i}\t{' '.join(common_aligns)}\n")
48
49     return

```

Afterwards, the function `calc_score_merges` opens these files and calculates the score, much in the way as the `calc_align_score` algorithm from the previous section.

```

1  # merge_dropout.py
2  def calc_score_merges():
3      probs, surs, surs_count = load_gold(goldpath)
4      baseline_df = pd.read_csv(join(basedir, f'scores_{source}_{target}.csv'))
5      scorespath = join(scoresdir, str(dropout))
6      if not os.path.isdir(scorespath):
7          os.mkdir(scorespath)
8
9      for merge_type in ['union', 'inter']:
10         scores = []
11         for num_symbols in merges:
12             mergefilepath = join(bpedir, mode, f'{num_symbols}_{merge_type}.wgdfa')
13             score = [int(num_symbols)]
14             score.extend(list(calc_score(mergefilepath, probs, surs, surs_count)))
15             scores.append(score)
16
17         df = pd.DataFrame(scores, columns=columns).round(decimals=3)
18         scorename = join(scorespath, 'scores', merge_type)
19
20         print(f"Scores saved into {scorename}")
21         df.to_csv(scorename+'.csv', index=False)
22         plot_scores(df, baseline_df, scorename)
23
24     # threshold case, iterate all merge_thresholds saved
25     for merge_t in merge_threshold:
26         scores = []
27         for num_symbols in merges:
28             mergefilepath = join(bpedir, mode, f'{num_symbols}_thres_{merge_t}.wgdfa')
29             score = [int(num_symbols)]
30             score.extend(list(calc_score(mergefilepath, probs, surs, surs_count)))
31             scores.append(score)
32
33     df = pd.DataFrame(scores, columns=columns).round(decimals=3)

```

```

34     scorename = join(scorespath, 'scores', f"{merge_t}_thres")
35
36     print(f"Scores saved into {scorename}")
37     df.to_csv(scorename+'.csv', index=False)
38     plot_scores(df, baseline_df, scorename)
39     return
40
41 if __name__ == "__main__":
42     merge_dropout_alignments()
43     calc_score_merges()

```

5.4 Improvement of learn-BPE algorithm

As explained in the methodology 4.3, the main improvement in the learn-BPE algorithm is to only update previous and next tokens to the merged pair, as well as saving the indexes where each pair occurs. These improvements are built on top of the code shown in 5.2.1.

In the *learn_bpe* function, the new *update_tokens* returns the updated pairs and the merged tokens, all in one step. The function *get_stats*, which is the function that iterates the whole corpus, only has to be performed once. This is however a modification of the previous *get_stats* function, since it computes the indexes of the pairs as well.

```

1  # learn_bpe.py
2  def learn_bpe(corpus: list, bpe_model: list): list:
3      '''
4      Learn BPE operations from vocabulary.
5      Steps:
6      1. split corpus into characters, count frequency
7      2. count bigrams in corpus
8      3. merge most frequent symbols
9      4. Update bigrams in corpus
10     '''
11     tokens = read_corpus(corpus)
12     pairs, idx = get_stats(tokens)
13     most_frequent_merges = []
14     for i in range(learn_merges):
15         try:
16             most_frequent = pairs.most_common(1)[0][0]
17         except:
18             # pairs is empty
19             break
20         most_freq_merges.append(most_frequent)
21         tokens, idx, pairs = update_tokens(tokens, idx, pairs, most_frequent)
22     return most_freq_merges

```

These are the modifications introduced in the *get_stats* function so that it saves the pair indexes. In the *idx* data structure, not only is the index saved, but also the amount of appearances of each pair in that sentence. This is done to ensure that if the pair ('t', 'h') in index 0 now becomes ('t', 'he') because of the ('h', 'e') merge, and the frequency of ('t', 'h') is reduced by one, it might be assumed that ('t', 'h') no longer appears in that sentence. But this would be a mistake, since there might be other instances of

('t', 'h') in the sentence that are not altered by this merge. We only want to say that ('t', 'h') no longer appears in index 0 when all instances of ('t', 'h') have been merged with other sequences. This is the motivation behind storing the amount of appearances of each pair in a sentence.

```

1 # learn_bpe.py
2 def get_stats(tokens: list) -> (Counter, dict):
3     """
4     Count frequency of all bigrams, their indexes and the frequency per index.
5     pairs = {
6         ('s', 'h'): 5,
7         ('h', 'e'): 6
8     }
9     idx = {
10         ('t', 'h'): {
11             # keys are indexes in corpus, values are frequency of appearance
12             0: 2,
13             1: 3,
14         }
15     }
16     """
17 def get_pairs_idx(pairs, idx, symbols):
18     symbols = symbols.split()
19     for j in range(len(symbols) - 1):
20         new_pair = symbols[j], symbols[j + 1]
21         pairs[new_pair] += 1
22         idx[new_pair][j] += 1
23     return pairs, idx
24
25 pairs = Counter()
26 idx = defaultdict(lambda: defaultdict(int))
27 for i, sent in enumerate(tokens):
28     # get stats for each word independently, no bigrams between different words
29     for word in sent[1:].split(' ' + word_sep):
30         pairs, idx = get_pairs_idx(pairs, idx, word_sep + word)
31 return pairs, idx

```

The `update_tokens` function handles the situation where only the previous and after tokens are updated for each merged pair. Comments are included in the code for readability.

```

1 # learn_bpe.py
2 def update_tokens(tokens, idx, pairs, pair):
3
4     def update_freqs(pairs, idx, pair, new_pair=-1):
5         # decrease freq from pairs
6         pairs[pair] -= 1
7         if pairs[pair] <= 0: del pairs[pair]
8         # decrease freq from idx
9         idx[pair][i] -= 1
10        if idx[pair][i] <= 0: del idx[pair][i]
11        if len(idx[pair]) <= 0: del idx[pair]
12        if new_pair != -1:
13            pairs[new_pair] += 1
14            idx[new_pair][i] += 1

```

```

15     return pairs, idx
16
17 merged_pair = ''.join(pair)
18 p = re.compile(r'(?<!\S)' + re.escape(''.join(pair)) + r'(?!\S)')
19 # only iterate the corpus indexes where the pair to be merged is present
20 for i in list(idx[pair]).copy():
21
22     # merge pair in the sentence
23     sent = p.sub(merged_pair, tokens[i])
24     # sentence remains unchanged. Delete pair from pairs and idx and continue
25     if sent == tokens[i]:
26         del pairs[pair]
27         del idx[pair][i]
28         if len(idx[pair]) <= 0:
29             del idx[pair]
30         continue
31     tokens[i] = sent
32     '''
33     iterate sent by the position the merged_pair occurs.
34     in each position, we need to reduce freq of previous and after tokens
35     sentence before merge: 'h e l l o', pair: ('e', 'l')
36     merged sent = 'h e l l o'
37     sent.split(merged_pair) -> ['h ', ' l o']
38     we iterate the splitted sentence and in each occasion
39     * decrease freq of previous token ('h', 'e')
40     * create new token ('h', 'el')
41     * decrease freq of after token ('l', 'l')
42     * create new token ('el', 'l')
43     * decrease freq of merged pair ('e', 'l')
44     '''
45     sent = sent.split(merged_pair)
46     for k in range(len(sent[:-1])):
47         if sent[k].split() and sent[k][-1] == ' ' and word_sep not in pair[0][0]:
48             '''
49             conditions to update the **previous** token:
50             * if sent[k] is not empty. if it is, there's no previous token to update.
51             * if the merged_pair is not the beginning of the word.
52             * in this case, discard the last letter from the prev word to be merged with
53             ...
54             * our current pair. ... e _t h ... ('e', '_t') is discarded
55             '''
56             prev = (sent[k].split()[-1], pair[0])
57             new_pair = (prev[0], merged_pair)
58             pairs, idx = update_freqs(pairs, idx, prev, new_pair)
59
60         if not sent[k+1].split() and word_sep not in pair[0][0]:
61             '''
62             conditions to update the **after** token when merged bigrams are consecutive:
63             * when the pair's first character is not the beginning of the word
64             * and when the next token is empty
65             * there are consecutive merged pairs, merged_pair=('ssi'), sent='m i ssi ssi p
66                                     p i'

```

```

65         * in this case, delete the token between the merged_pair: ('i', 's')
66         * and create a new pair ('ssi', 'ssi')
67     '''
68     if sent[k] and sent[k][-1] == word_sep:
69         after = (word_sep+merged_pair, pair[0])
70         new_pair = -1
71     else:
72         after = (pair[1], pair[0])
73         new_pair = (merged_pair, merged_pair)
74         pairs, idx = update_freqs(pairs, idx, after, new_pair)
75     elif sent[k+1].split() and word_sep not in sent[k+1].split()[0]:
76         '''
77         conditions to update the **after** token in a more general case:
78         * if sent[k] is not empty. if it is, there's no after token to update.
79         * if the after token is a new word, we do not want to consider it.
80         '''
81         after = (pair[1], sent[k+1].split()[0])
82         new_pair = (merged_pair, after[1])
83         pairs, idx = update_freqs(pairs, idx, after, new_pair)
84         # decrease freq of merged bigram
85         pairs, idx = update_freqs(pairs, idx, pair)
86     return tokens, idx, pairs

```

The performance improvements of this approach can be seen in the Results section.

5.5 BPE without word boundaries

As explained in the Methodology chapter, this addition considers BPE units between different words. The only change occurs when learning these BPE units and mapping multiple-word-units to multiple-word-units, the rest of the pipeline remains as is, other than changing the filenames and paths of the alignments and scores. A new Boolean variable is introduced in *settings.py*, so that by changing it to a positive value will make the whole pipeline act in space mode, that is, setting the space boundary and only allowing merges between words. On the contrary, no space mode allows merges between different words.

```

1 # settings.py
2 space = False

```

The following scripts for learning BPEs and extracting and mapping alignments are generalized in the sense that just by changing the Boolean variable in the settings file, the pipeline runs automatically and no further changes need to be done. The code snippets below display these functionality, accepting both modes.

In *learn_bpe.py*, the way to parse and tokenize the corpus is slightly different, now instead of having a special token to denote the beginning of a word, the special token denotes the whitespace.

```

1 # learn_bpe.py
2 def read_corpus(corpus: list) -> list:
3     '''
4     Read corpus, strip index and new line characters.
5     In space mode, each word has a word_sep symbol at the beginning of the word.
6     tokens = [

```

```

7     'w e \_ d o \_ n o t \_ b e l i e v e \_ t h a t \_ w e \_ s h o u l d .',
8 ]
9 In no space mode, words are joined by word_sep.
10 tokens = [
11     'w e \_ d o \_ n o t \_ b e l i e v e \_ t h a t \_ w e \_ s h o u l d .',
12 ]
13 '''
14 tokens = []
15 for line in corpus:
16     line = line.split('\t')[1].strip('\r\n ')
17     line = line.split()
18     line[0] = str.lower(line[0])
19     if space:
20         # add word_sep to each beginning of word and join by space
21         tokens.append(' '.join([word_sep + ' '.join(word) for word in line]))
22     else:
23         # join all words by word_sep
24         tokens.append(u' \u2581 '.join([' '.join(word) for word in line]))
25 return tokens

```

When analysing pairs and their frequencies, each word's last character and the following whitespace has to be considered, as well as this whitespace and the following word's first character. This changes the `get_stats` function slightly.

```

1 # learn_bpe.py
2 def get_stats(tokens: list) -> (Counter, dict):
3     '''
4     Count frequency of all bigrams, their indexes and the frequency per index.
5     pairs = {
6         ('s', 'h'): 5,
7         ('h', 'e'): 6
8     }
9     idx = {
10         ('t', 'h'): {
11             # keys are indexes in corpus, values are frequency of appearance
12             0: 2,
13             1: 3,
14         }
15     }
16 In space mode, the last token '.' or word_sep. is not merged with anything.
17     '''
18 def get_pairs_idx(pairs, idx, symbols):
19     symbols = symbols.split()
20     for j in range(len(symbols) - 1):
21         new_pair = symbols[j], symbols[j + 1]
22         pairs[new_pair] += 1
23         idx[new_pair][j] += 1
24     return pairs, idx
25
26 pairs = Counter()
27 idx = defaultdict(lambda: defaultdict(int))
28 for i, sent in enumerate(tokens):
29     if space:

```

```

30     # get stats for each word independently, no bigrams between different words
31     for word in sent[1:].split(u' \u2581'):
32         pairs, idx = get_pairs_idx(pairs, idx, word_sep + word)
33     else:
34         # get bigram stats for the whole sentence
35         pairs, idx = get_pairs_idx(pairs, idx, sent)
36     return pairs, idx

```

And finally, after merging a pair in the corpus, when updating the tokens and the pairs, the fact that space boundaries exist or not also plays a role. Specifically, the no space mode enjoys more freedom, in the sense that no matter which pair is merged, the pair immediately before and the pair immediately after are merged, no matter what. In space mode however, this cannot be done if the previous or next pair belong to another word, which puts some restrictions. Only modified lines with respect to the code in the previous improve learn BPE algorithm 5.4. There are comments in the code for readability.

```

1  # learn_bpe.py
2  def update_tokens(tokens: list, idx: dict, pairs: Counter, pair: tuple) -> (list, dict
                                     , Counter):
3
4  # change line 46
5  if sent[k].split() and (sent[k][-1] == ' ' and word_sep not in pair[0][0] if space
                           else True):
6
7      '''
8      conditions to update the **previous** token:
9      * in space mode, if the merged_pair is not the beginning of the word.
10     * in this case, discard the last letter from the prev word to be merged ...
11     * with our current pair. ... e _t h ... ('e', '_t') is discarded
12     '''
13
14 # change line 58
15 if space and not sent[k+1].split() and word_sep not in pair[0][0]:
16
17     conditions to update the **after** token when merged bigrams are consecutive:
18     * in space mode, when the pair's first character is not the beginning of the word
19     '''
20
21 # change line 74
22 elif sent[k+1].split() and (word_sep not in sent[k+1].split()[0] if space else True):
23
24     '''
25     * in space mode, if the after token is a new word, we do not want to consider it.
26     '''

```

The *apply_bpe.py* remains unchanged, aligning BPE files as well with the *Fastalign* or *Eflomal* algorithm as well. However, since now the alignments are among many words, the mapping is different than in the space case. The mapping is divided into subword to word mapping (`map_subword_to_word` function) and multiword to word (`map_multiword_to_word`).

```

1  # extract_alignments.py
2  def map_subword_to_word(corpus, bpes, lang):
3      '''
4      SPACE MODE
5      Input: list of sentences with subword separation

```

```

6 corpus = [
7     '_We _do _no t _be li eve _.',
8     '_Thi s _is _a _sent ence _.',
9 ]
10 Output: dictionary of each language and
11 a list of indexes pointing to which word each element (_do) belongs to
12 bpe = {
13     source:
14     [
15         [0, 1, 2, 2, 3, 3, 3, 4],
16         [0, 0, 1, 2, 3, 4, 5],
17     ],
18 }
19 '''
20 bpes[lang] = []
21 for sent in corpus:
22     mapping = [0]
23     i = 0
24     for subw in sent.split()[1:]:
25         if subw[0] == word_sep:
26             i += 1
27         mapping.append(i)
28     bpes[lang].append(mapping)
29 return bpes

```

And the new *map_multiword_to_word* function.

```

1 # extract_alignments.py
2 def map_multiple_to_word(corpus, bpes, lang):
3     '''
4     NO SPACE MODE
5     Input: list of sentences with subword separation
6     corpus = [
7         'b u t_this_is_no t_w hat_hap pen s_.',
8         'th e_ ice_cre am_.',
9     ]
10    Output: dictionary of each language and
11    a list of indexes pointing to which word each element (t\_w) belongs to
12    bpes = {
13        source:
14        [
15            [[0], [0], [0,1,2,3], [3,4], [4,5], [5], [5,6]],
16            [[0], [0], [1,2], [2]],
17        ],
18    }
19    '''
20    bpes[lang] = []
21    for sent in corpus:
22        sent_bpes = []
23        j = 0
24        for word in sent.split():
25            if word == word_sep:
26                # word is simply '_', doesn't belong to anything

```



```

27     j += 1
28     sent_bpes.append([])
29     continue
30 word_count = word.count(word_sep)
31 if word_count == 0:
32     sent_bpes.append([j])
33     continue
34 # multiple words in the element: t_this_is_no -> [0,1,2,3]
35 if word[0] == word_sep:
36     # word starts with '_' but there are no elements of the previous word in it
37     j += 1
38     word_count -= 1
39 if word[-1] == word_sep:
40     # word ends with '_' but there are no elements of the next word in it
41     sent_bpes.append(list(range(j, j + word_count)))
42 else:
43     sent_bpes.append(list(range(j, j + word_count + 1)))
44 j += word_count
45 bpes[lang].append(sent_bpes)
46 return bpes

```

Consequently, the function *load_and_map_segmentations* is altered in the following way:

```

1 # extract_alignments.py
2 def load_and_map_segmentations(num_symbols, i=-1):
3     bpes = {}
4     for lang in [source, target]:
5         segmentpath = lang+'_'+str(num_symbols)+'_'+str(i) if i != -1 else ''+'.bpe'
6         argsinput = codecs.open(segmentpath, encoding='utf-8')
7         if space:
8             bpes = map_subword_to_word(argsinput, bpes, lang)
9         else:
10            bpes = map_multiple_to_word(argsinput, bpes, lang)
11     return bpes

```

Besides, the function *bpe_word_align* is also altered to account for the fact that if a multiword unit such as *from_the* is aligned with *aus_dem*, each one-to-one alignment must be considered, that is, from-aus, from-dem, the-aus, and the-dem.

```

1 def bpe_word_align(bpes, bpe_aligns):
2     '''
3     Input: dictionary of bpes obtained as output of map_subword_to_word()
4     Output: list of word alignments and their indexes
5     '''
6     """
7     0    0-0 0-1 1-1 1-2 3-1 2-4 \n
8     1    0-0 1-0 1-1 2-1 \n
9     """
10    all_word_aligns = ''
11    for i, (sent1, sent2, bpe_al) in enumerate(zip(bpes[source], bpes[target],
12                                                    bpe_aligns)):
13        word_aligns = set()
14        # iterate each alignment

```

```
14     for al in bpe_al.split('\t')[1].split():
15         firstal, secondal = al.split('-')
16         if space:
17             new_al = str(sent1[int(firstal)]) + '-' + str(sent2[int(secondal)])
18             word_aligns.add(new_al)
19         else:
20             for el1 in sent1[int(firstal)]:
21                 for el2 in sent2[int(secondal)]:
22                     new_al = str(el1) + '-' + str(el2)
23                     word_aligns.add(new_al)
24     all_word_aligns += str(i) + "\t" + ' '.join(word_aligns) + "\n"
25     return all_word_aligns
```

The final step of calculating scores does not change.

6 Results

This chapter shows the results and analysis for each step of the development of this thesis, ranging from score plots for BPE alignments, to algorithm runtimes. The scores display four different metrics, namely precision, recall, F1 score and AER, which have been explained previously in the Translation chapter. 3.2.3

6.1 Replication of BPE

When replicating BPE, the best BPE result using *Fastalign* as alignment algorithm is a F1 score of 0.609, obtained after 1000 BPE merges. The baseline has a F1 score of 0.6. Baseline in this situation refers to the scores when aligning the raw corpus, leaving the words untouched and with no BPE units.

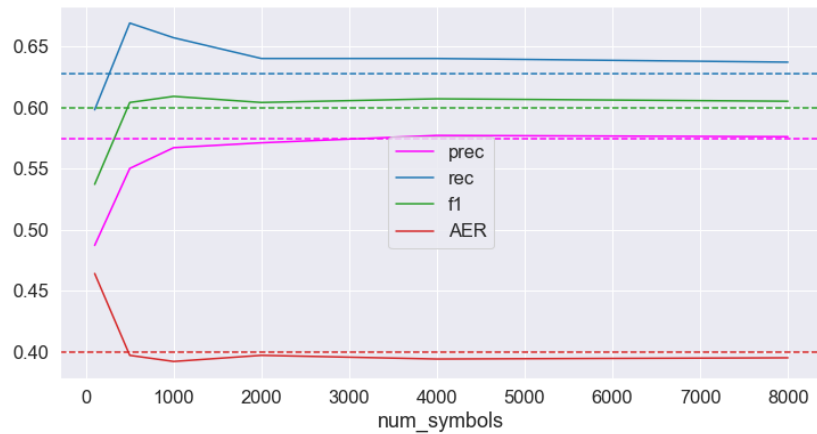


Figure 6.1: Scores of BPE over baseline, using Fastalign

In the case of *Eflomal*, the baseline F1 score is 0.72, and the best F1 score is 0.701, obtained after 6000 merges. When using *Eflomal*, BPE does not improve the baseline.

The alignment algorithms, *Fastalign* and *Eflomal*, require one language to be given as source and the other as target, and perform the alignment based on this. Throughout the thesis, English has been taken as the source language and German as the target. It might have been interesting to see that swapping the languages would yield different results, by swapping the languages in the global variables file. The difference between these two cases is barely perceptible, a difference of 0.03% throughout the scores across all numbers of merges. Therefore, it is assumed that swapping the source and target language has no effect in the experiment result scores.

6.2 Replication of BPE-dropout

BPE-dropout is meant to be an improvement of BPE, therefore the desired score comparison is that of BPE-dropout with respect to BPE. The BPE scores are taken as baseline, instead of the gold standard

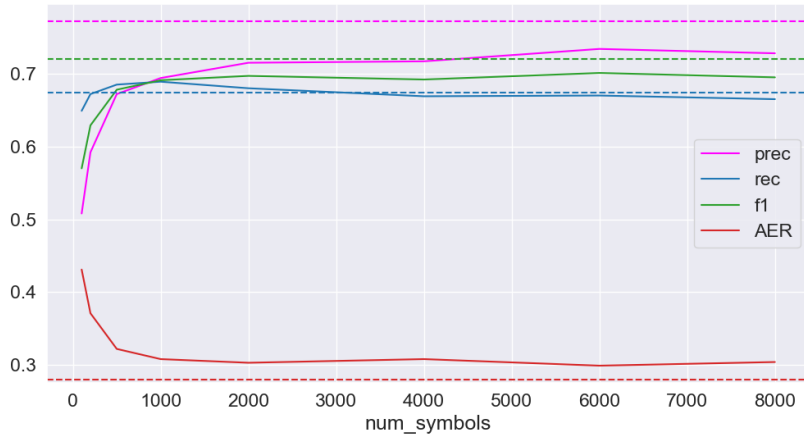


Figure 6.2: Scores of BPE over baseline, using Eflomal

scores as in the previous case. As explained in the Methodology chapter 4.2, the BPE dropout pipeline is run a number of times, resulting in many possible segmentations. Out of these, three types of results are obtained: union, intersection and threshold.

- The **union** case takes all alignments into account, resulting in a big list of alignments per sentence. These most probably include the correct alignments, but there are many other wrong alignments. This case has low precision and high recall.
- The **intersection** case takes only those alignments which are present in all alignment files, resulting in a few number of alignments per sentence. Most probably, these alignments are correct, but there are also be many alignments missing. This case has high precision and low recall.
- The **threshold** case is a mixture between union and intersection. Given a threshold, for instance 0.7, an alignment is accepted if it is present in 70% of the alignment files. Smaller values for this variable resemble the union case, since more alignments are accepted. Higher threshold numbers resemble the intersection case, where alignments must be present in more and more files in order to be accepted.

The following figures 6.3, 6.4 and 6.5. show the results for a *dropout* rate of 10%, and the union, intersection and threshold cases.

It can be seen that the F1 score improves consistently the more BPE units have been merged. Since there are more merges, there are fewer units, most words are completely merged and the uncertainty of aligning BPE units is lower, since the sentence looks more and more similar to the raw sentence where there are just words. Regarding the threshold case, the following two figures show the scores for threshold 0.3 and 0.7, **which achieves the best F1 score, namely 0.635**.

It is visible that the scores plot with the threshold at 0.3 resembles the union case more, and recall goes lower while the precision goes higher for larger threshold values. The optimal result is found at the threshold value of 0.7. This result is replicated when increasing the dropout rate up to 20% as well as 30%, and setting the alignment threshold at 0.5. **This shows that BPEs are robust to dropout.**

In the BPE dropout paper [14], the authors only use one dropout percentage, namely 10% for all languages and 60% specifically for Chinese and Japanese to match the increase in length of segmented

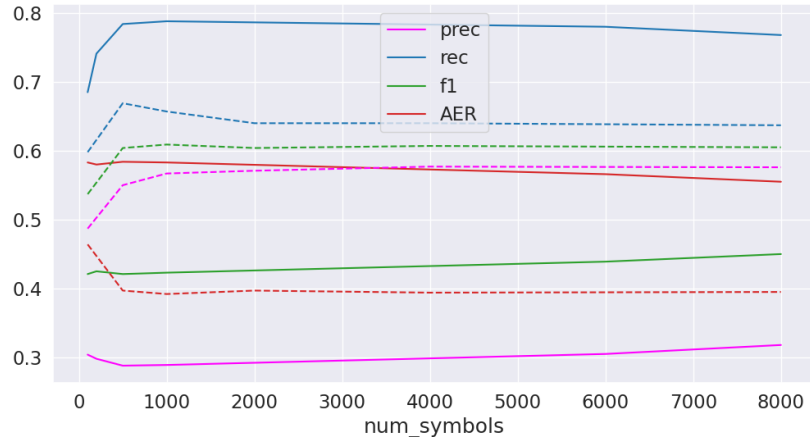


Figure 6.3: Scores for BPE-dropout with dropout rate 0.1, union mode

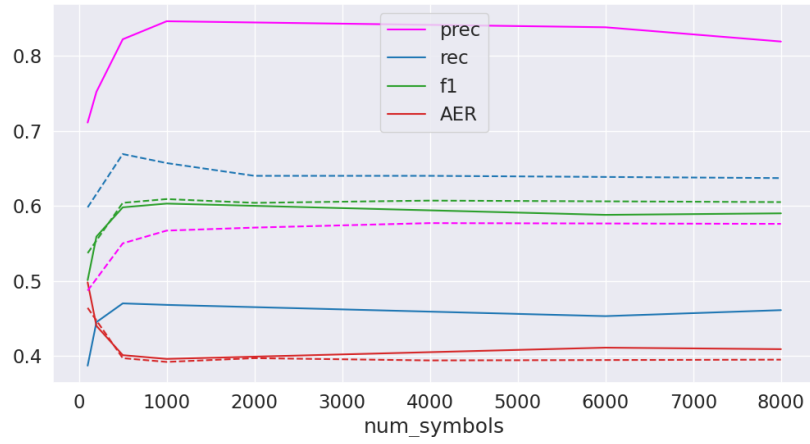


Figure 6.4: Scores for BPE-dropout with dropout rate 0.1, intersection mode

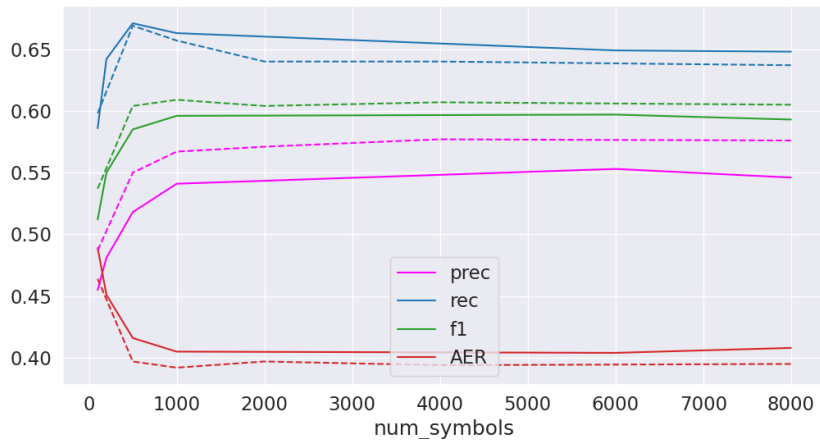


Figure 6.5: Scores for BPE-dropout with dropout rate 0.1, threshold mode at 0.3

sentences for other languages. The paper hypothesizes that exposing a model to different segmentations might result in better understanding of the whole words as well as their subword units, which is proven

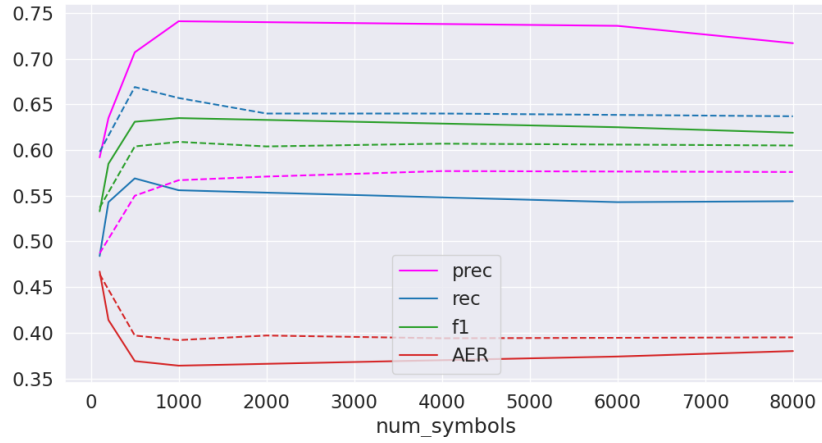


Figure 6.6: Scores for BPE-dropout with dropout rate 0.1, threshold mode at 0.7

by the paper and by this thesis as well. The paper authors also speculate the following:

Results indicate that using BPE-Dropout on the source side is more beneficial than using it on the target side. We speculate it is more important for the model to understand a source sentence, than being exposed to different ways to generate the same target sentence.

This theory is also confirmed in this thesis. As the experiment of only applying BPE in English in the English-German language pair shown in the Figure 6.7, the improvement of BPE-dropout over BPE in this case is 3%.

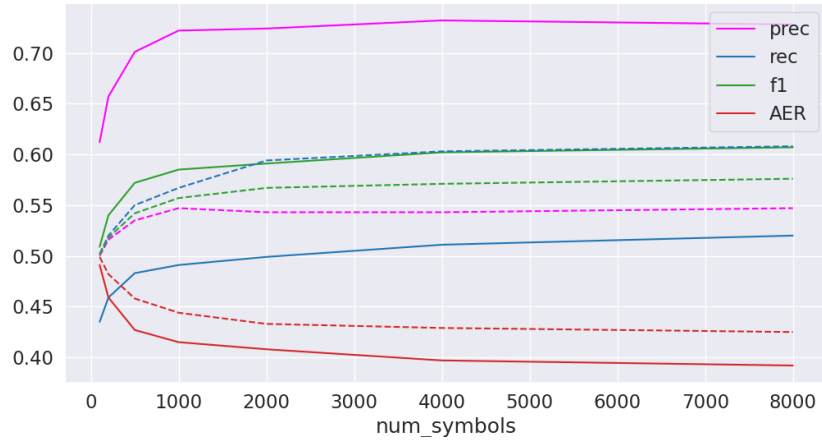


Figure 6.7: Scores for BPE-dropout with dropout rate 0.1, threshold at 0.7 and BPE only in source language

Regarding the improvements of BPE dropout over normal BPE, the authors conclude the following:

The improvement with respect to normal BPE are consistent no matter the vocabulary size.

But we see that the effect from using BPE-Dropout vanishes when a corpora size gets bigger.

This thesis has predominantly been run with a fixed size, relatively small corpus consisting of 10.000 sentences, whereas the paper authors have used much bigger corpora ranging from 133.000 sentences up

to 2 million. As a result, the effect of varying corpus size has not been replicated. However, it can be seen that for bigger number of merges, the effects of BPE dropout are smaller, since given the bigger number of merges, the segmentations resemble the case where no dropout is applied.

As the BPE dropout paper states, *BPE dropout improves BPE consistently no matter how many merges are performed*. This result is replicated in this paper. Additionally, in the paper they use a fixed dropout rate and they give no information as per the threshold used in determining how to aggregate alignments. **By experimenting with different dropout and threshold rates, it was possible to improve the F1 score by selecting a dropout rate of 30%, which is specific to the corpus, in this case English and German, creating 30 segmentations and selecting an alignment threshold of 0.5. This results in a F1 score of 0.685, an improvement of 2% from the previous case.**

6.3 BPE-dropout for other language pairs

The better results of BPE-dropout over BPE proves that BPE-dropout performs better than BPE, at least in the English-German case, and the optimal hyperparameters for this case were using a dropout rate of 10%, an alignment threshold of 0.7, and around 2000 merges. The 2000 merge hyperparameter might be dependent on the corpus, smaller corpora might not even have 2000 merges to make, while bigger corpora might obtain their optimal results for more merges. **But does BPE-dropout outperform BPE for other language pairs at a dropout rate of 10% and an alignment threshold of 0.7?**

A couple of other language pairs were tested, namely English-Romanian, consisting of 50.000 sentences, and English-Hindi, with 3.000 sentences. Merge lists were created for English, Romanian and Hindi, each according to the particular case. For instance, the English merge list in the English-Romanian case is much richer than the merge list in the English-Hindi case, because the former has a much bigger corpus from which to learn frequent sequence pairs. Instead of using the rich English merge list obtained from the 50.000 sentences and applying it to all language pairs, namely German, Romanian and Hindi, it was decided that each language pair would see its own merge list created from the available corpus. The Romanian case, being the corpus around 16 times bigger, takes longer to compute segmentations and alignments but the results are consistent. **BPE-dropout outperforms BPE in two other language pairs for a dropout rate of 10%, an alignment threshold of 0.7 and with vastly different corpus sizes.** The BPE-dropout scores are shown in the following figures, the F1 score improvement over BPE for English-Romanian is of 1.5%, obtained at 4000 merges, and the F1 score improvement over BPE for English-Hindi is of 2.8%. It is worth noting that given the small size of the English-Hindi corpora, the merge list is only around 5000 merges long.

6.4 Improvement of the learn-BPE algorithm

By modifying the algorithm to update the corpus after a merge, by introducing indexes and frequency counts to reduce iteration, the learn-BPE algorithm's runtime was dramatically accelerated. In the beginning, the algorithm starts by creating around 1.5 BPE merges per second, which is relatively slow because since the most frequent pairs are so frequent, most of the indexes in the corpus are visited and many update operations are done. The further down in the iterations, the less frequent merges are, the faster it is to merge them and update the corpus. The speed of merges per second gets faster and

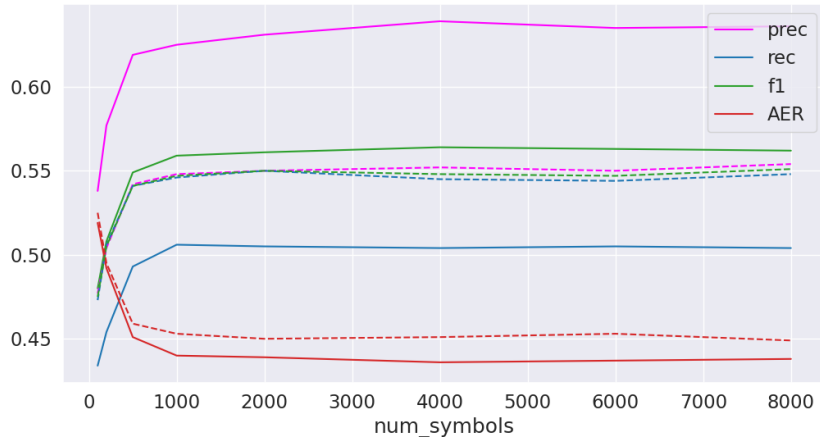


Figure 6.8: Scores for BPE-dropout on English-Romanian with dropout rate 0.1, threshold at 0.7

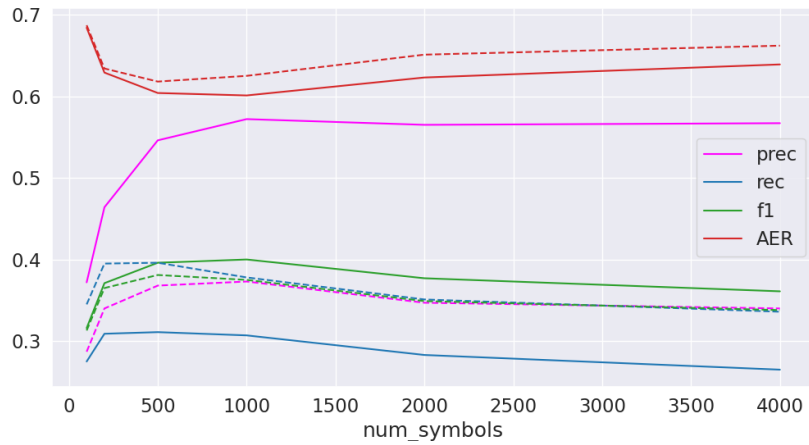


Figure 6.9: Scores for BPE-dropout on English-Hindi with dropout rate 0.1, threshold at 0.7

faster until by the time it is finished with the corpus, it is running at roughly 300 merges per second for English and 120 merges per second in German.

After the improvement, the algorithm, on average, needs **55s to learn BPE merges in English, and 1:25min in German on corpora composed of 10.000 sentences**. The time difference between English and German is due to the fact that the words in German are generally lower, with a higher variance, and there are therefore more merge possibilities. In contrast, Sennrich et al. [9]’s algorithm needs 2:15min for English and 3:20min for German. The algorithm presented here shows an improvement in speed of 2.5x for English and 2.4x for German. These tests have been performed on an Intel Core i5-7200U CPU at 2.5GHz, a 64-bit Windows OS with 8GB RAM.

A C++ implementation of the BPE algorithm from Sennrich et al. can be found on Github This package makes use of C++’s advantage to handle memory better than Python, for instance by memory mapping the input file to read it efficiently, and by using multi-threading to pre-compute the BPE splits of all words in the input file. When applied to this thesis’ dataset, it barely needs a few seconds to learn BPE codes, making it much faster than the algorithm developed in this thesis. However, this package does not include BPE-dropout or any other word separation rather than $</w>$ at the end of the word;

it is not possible to create BPE tokens without word boundaries using this method. It is assumed that it would not be very complicated to integrate these two aspects into the package, but given that this algorithm was created by a PhD student, there are no guarantees of maintenance in the future. In contrast, this thesis' algorithm takes more time but depending on *dropout* and *space* parameters, the algorithm is adapted to both scenarios.

6.5 No-space results

Learning BPE units that can handle merges among words takes more time, since there are more possibilities to merge; each end of the word and each beginning of the word can now be merged. In the previous case, there was only a fixed number of merges that could be done inside a word, once the whole word was merged into one unit, no other merges were possible. Now however, that word can be merged with its previous or subsequent tokens.

As with the space case, the algorithm starts relatively slow, at around 0.7 BPE merges per second. While the most frequent merge in the space case is `_t`, `h` for English and `e`, `n` for German, in the no-space case the most frequent merges are `e`, `_` for English and `e`, `n` again for German. In the English case, the pair `e`, `_` is much more frequent than the pair `_t`, `h`, and it takes more time for this pair to get merged. Afterwards, the number of merges per second increases until plateauing at 50 merges per second in English, and slightly lower in German. The runtime is **3:50min for 10.000 merges in English and 4:10min in German**. Since there are more merge possibilities, the algorithm was also run **for 20.000 merges, with a runtime of 9:30min in English and 10min in German**.

Further down the pipeline, alignments are performed without any notion of what words are, and *Fastalign* and *Eflomal* are not thought to handle multiword-to-multiword alignments. It is therefore expected that the scores will be lower than in the space case, and it is also expected that the more BPE merges, the bigger the segmentations, the more words will be merged together. For instance, if the multiword unit `in_the_street` is aligned to `auf_der_Strasse`, the following mapping would be performed: `in-auf`, `in-der`, `in-Strasse`, `the-auf`, `the-der` and so on. This brings the precision down dramatically, since most of these alignments are incorrect. For the case of no dropout, the best result for BPE without space separations is a F1 score of 0.477, obtained at 200 merges, which is a very low number of merges compared to the previous best scores. The F1 score is also poor relative to the case where merges between words are no allowed. Regardless, given that there is no notion as to what a word constitutes, this result cannot be poorly regarded.

As the following figures show, BPE-dropout outperforms BPE also in no-space mode, making this improvement consistent regardless if word boundaries are considered or not. It can be therefore concluded, that **BPE-dropout outperforms BPE in all experiments done in this thesis, with word boundaries or without**. For a dropout rate of 10%, results already improve with an F1 score of 0.523 for 200 merges and an alignment threshold of 0.7. The maximum F1 score is obtained at a dropout rate of 20%, with an **F1 score of 0.559 for 500 merges and an alignment threshold of 0.5**, which constitutes an improvement of 10.5% with respect to no-space BPE with no dropout.

Experiments with higher dropout rates have also been conducted, namely a dropout rate of 50% which is very large, half the merges are dropped, with a F1 score of 0.529 for 4000 merges and an alignment threshold of 0.3. These parameters are considerably different than the ones previously. The ideal score happens at 4000 merges, which makes sense that it is a bigger number since so many merges are dropped.

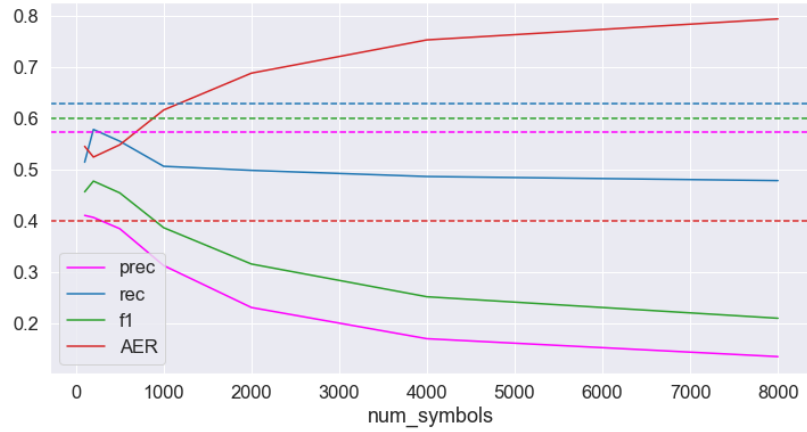


Figure 6.10: Scores for no-space BPE

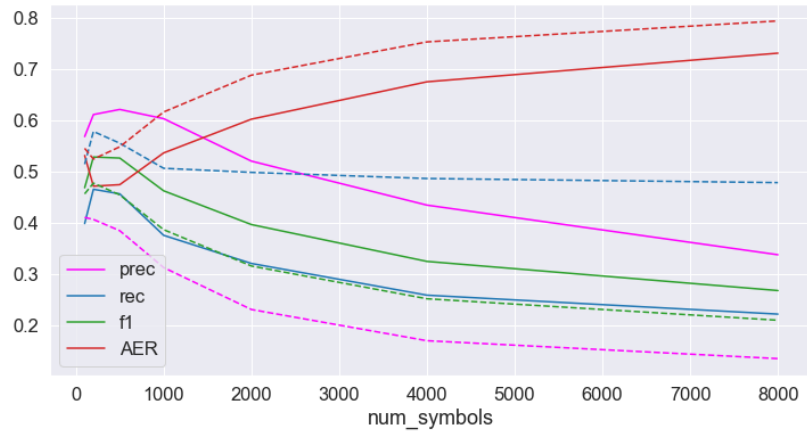


Figure 6.11: Scores for no-space BPE-dropout with dropout rate 0.1, threshold at 0.7

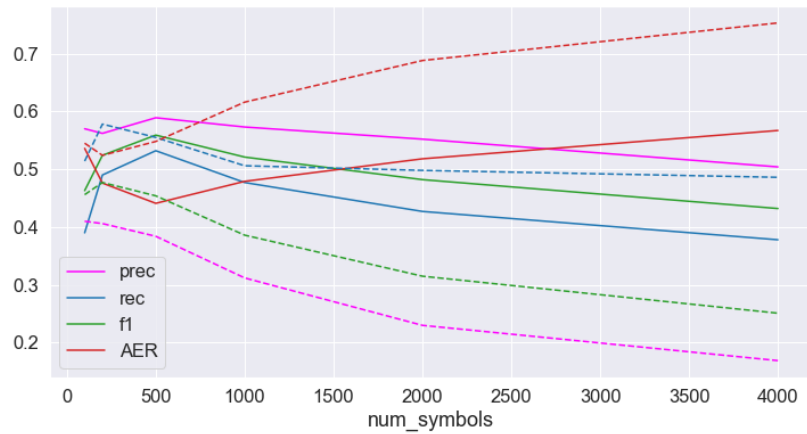


Figure 6.12: Scores for no-space BPE-dropout with dropout rate 0.2, threshold at 0.5

And the alignment threshold is also very low compared to previous cases, meaning that most alignments are accepted creating a sort of union.

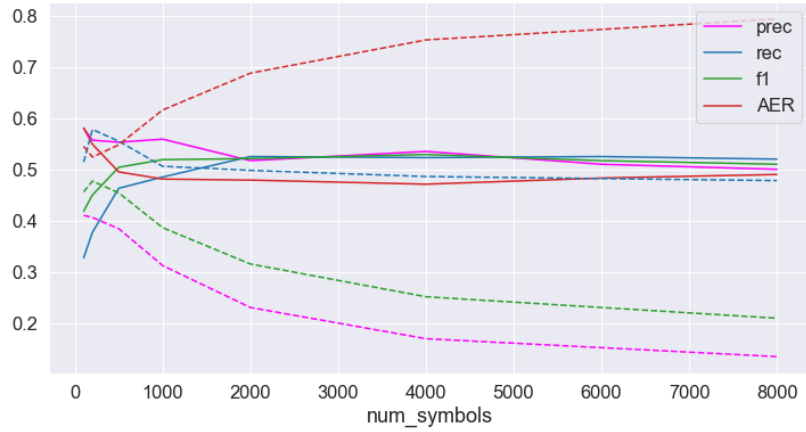


Figure 6.13: Scores for no-space BPE-dropout with dropout rate 0.5, threshold at 0.3

6.6 No-space results for other language pairs

Similarly to the case of BPE-dropout in space mode, where it was shown that BPE-dropout outperforms BPE with a dropout rate of 10% and an alignment threshold of 0.7, it is also interesting to see the performance of BPE-dropout in no-space mode in other language pairs, in this case with the optimal hyperparameters of no-space mode, namely a dropout rate of 20% and an alignment threshold of 0.5. The following figures show the performance of BPE-dropout given the baseline of BPE in no-space mode, for the language pairs English-Romanian and English-Hindi. At the ideal hyperparameter of 500 merges, the F1 score improvement of BPE-dropout over BPE in English-Hindi is of 6.2%, and 8.4% in English-Romanian.

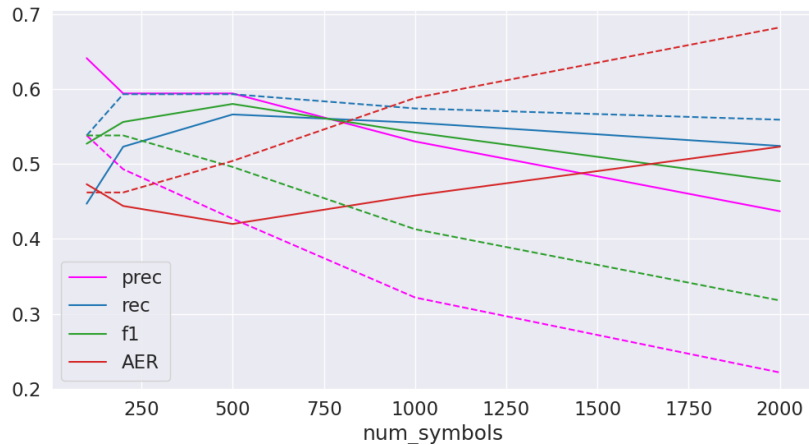


Figure 6.14: Scores for no-space BPE-dropout on English-Romanian with dropout rate 0.2, threshold at 0.5

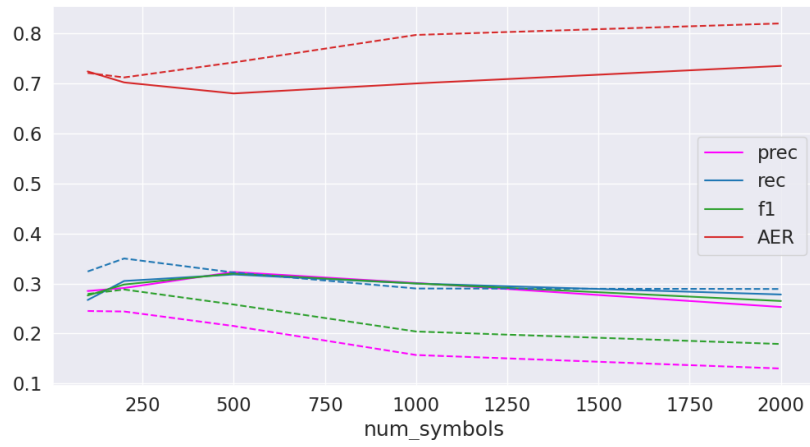


Figure 6.15: Scores for no-space BPE-dropout on English-Hindi with dropout rate 0.2, threshold at 0.5

7 Conclusion

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