Student Information

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Answer 1

a)

$$E(Blue) = \frac{1}{6}(1+2+3+4+5+6) = \frac{7}{2}$$

$$E(Yellow) = 1 * \frac{3}{8} + 3 * \frac{3}{8} + 4 * \frac{1}{8} + 8 * \frac{1}{8} = 3$$

E
$$(Red) = 2 * \frac{5}{10} + 3 * \frac{2}{10} + 4 * \frac{2}{10} + 6 * \frac{1}{10} = 3$$

b)

0.0.1 i)

Sum up Expected value of each of dice. E (Blue)+ E (Yellow) + E (Red)= 3.5+3+3=9.5

0.0.2 i)

Add up Expected Value of Blue 3 times. 3*E (Blue)= 10.5

So, by comparing cases i and ii, total expected value at ii is greater 10.5 > 9.5. therefore, answer is rolling 3 Blue dices.

 $\mathbf{c})$

In this question we apply the same logic with summing up the expected values of the dices given that E (Yellow)=8. So, the total expected value for i case in b part will be E (Blue)+ E (Yellow)+ E (Red)= 3.5+8+3=14.5

In this case, maximum total value will be obtained in the case of rolling three different dices, instead of three Blue dices because 14.5 > 10.5

 \mathbf{d}

Here Bayes Rule must be applied since we are working with conditional probability. $P\left(Red|Value=3\right)=\frac{P(Value=3|Red)P(Red)}{P(Value=3)}=\frac{\frac{1}{5}*\frac{1}{3}}{\frac{1}{6}*\frac{1}{3}+\frac{1}{8}*\frac{1}{3}+\frac{1}{5}*\frac{1}{3}}=\frac{24}{55}$

1

e)

Possible outcomes

Blue	Yellow
1	4
2	3
	3
	3
4	1
	1
	1

So the number of favourable outcomes is 7. There are total possible 6*8=48 outcomes. Answer is $\frac{7}{48}$

Answer 2

a)

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Using Binomial distribution n=80 p=0.025 q=1-0.025=0.975 x=4 P\left(X\geq 4\right)=1-P\left(X\leq 3\right)=1-\left(\binom{80}{0}*0.025^{0}*0.975^{80}+\binom{80}{1}*0.025^{1}*0.975^{79}+\binom{80}{2}*0.025^{2}*0.975^{78}+\binom{80}{3}*0.025^{3}*0.975^{77}\right)=0.14057
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b)

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A= no discount in all 80 shops of company A in either of 2 days B= no discount in 1 shop of company B in either of 2 days P(A)=(1-0.025)^2*80=0.0973 P(B)=(1-0.01)^2=0.81 P(not A)=1-0.0973=0.902 P(not B)=1-0.81=0.19 P(A union B)=0.902+0.19-(0.902*0.19)
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Answer 3

blue =
$$\begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 \end{bmatrix}$$
;
yellow = $\begin{bmatrix} 1 & 1 & 1 & 3 & 3 & 3 & 4 & 8 \end{bmatrix}$;
red = $\begin{bmatrix} 2 & 2 & 2 & 2 & 2 & 3 & 3 & 4 & 4 & 6 \end{bmatrix}$;

```
opt1\_total = 0;
opt2\_total = 0;
greater\_count = 0;
for i = 1:1000
    opt1_roll = [blue(randi(length(blue))), yellow(randi(length(yellow))), re
    opt1\_total = opt1\_total + sum(opt1\_roll);
    opt2_roll = [blue(randi(length(blue))), blue(randi(length(blue))), blue(r
    opt2\_total = opt2\_total + sum(opt2\_roll);
    if sum(opt2\_roll) > sum(opt1\_roll)
         greater_count = greater_count + 1;
    end
end
opt1_average_total = opt1_total / 1000;
opt2\_average\_total = opt2\_total / 1000;
greater_percentage = greater_count / 10;
plot(opt1_average_total);
plot(opt2_average_total);
plot(greater_percentage);
plot(opt1_average_total);
                            plot(opt2_average_total);
                                                        plot(greater_percentage);
```