

TONES KeyboardPitch Model, KeyboardNote, and KeyboardNoteGroup

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January 3, 2019

1 Who is this intended for?

It's intended for me. I might read this in a few months because I didn't know what the hell I was doing. Thus, it's written in a somewhat understandable way, but it won't try to explain ideas that aren't a product of this project.

2 KeyboardPitch

A keyboard pitch refers to a unique note “on the keyboard.” It does not refer to a specific pitch; this is important because then alternative/ microtonal tuning systems would be hard to implement and that would suck. Instead, it simply refers to something like “A4,” “F4,” etc.

We model a keyboard pitch as an integer from 0 to 144 inclusive, corresponding with the notes C-1 to C11. In the old TONES it was a special class, but this is such a simple egg that I don't think it deserves another class.

When we convert a note to a “name” like C1 or Db5, we can use the following formula:

$$\text{noteToName}(\text{note}) := \text{octaves}_{\text{note} \bmod 12} + \text{stringify}(\lfloor \text{note}/12 \rfloor - 1)$$

where octaves is [“C”, “C#”, “D”, “D#”, “E”, “F”, “F#”, “G”, “G#”, “A”, “A#”, “B”] and zero-indexed. For example, 69 gives us index 9 and $\lfloor 5.75 \rfloor - 1 = 4$, or A4.

The inverse of this function is the nameToNote function, which is a bit more complicated to deal with flats (b), double flats (bb), sharps (# or s), and double sharps (## or ss). We first apply the regex

$$\wedge([ABCDEFG])(\#|\#\#|B|BB|S|SS)?(-)?([0-9]+)\$$$

to an uppercased version of the input. The first (zero-indexed) group (letter name) we reference Dict 1 to get a semitone offset from the octave (l). The second group (accidental) we reference Dict 2 to get a semitone offset of the accidental (a). The third group we reference to get whether the octave number is negative as a true or false (b). Finally, the fourth group is parsed to an integer as the octave number itself (o). Then the note's value is

$$\text{nameToNote}(\text{name}) := l + a + (b ? -12 : 12) \cdot o + 12.$$

The relevant dicts:

Dict 1: `letter_nums` = {`"C"` : 0, `"D"` : 2, `"E"` : 4, `"F"` : 5, `"G"` : 7, `"A"` : 9, `"B"` : 11}; Dict 2: `accidental_offsets` = {`"#"` : 1, `"##"` : 2, `"B"` : -1, `"BB"` : -2, `"b"` : -1, `"bb"` : -2, `"s"` : 1, `"ss"` : 2, `"S"` : 1, `"SS"` : 2};

For utility and pitch estimation, there's the `noteTo12TET` function which converts a `KeyboardPitch` to its 12-TET frequency:

`noteTo12TET(n, a4 = 440)` := $a4 \cdot 2^{(n-69)/12}$.

There's also the concept of a `KeyboardInterval`, which is just a distance between two `KeyboardPitches`. Obviously, the `KeyboardInterval` between a and b is just $|a-b|$. For working with this there are the functions `nameToInterval` and `intervalToName`, but I don't expect them to be used and they are just an artifact from the old TONES, so I won't explain how they work here. Their algorithm is lengthy but straightforward. To get the value in cents of a `KeyboardInterval` in **12 TET**, multiply by 100.