Simulations based Inference

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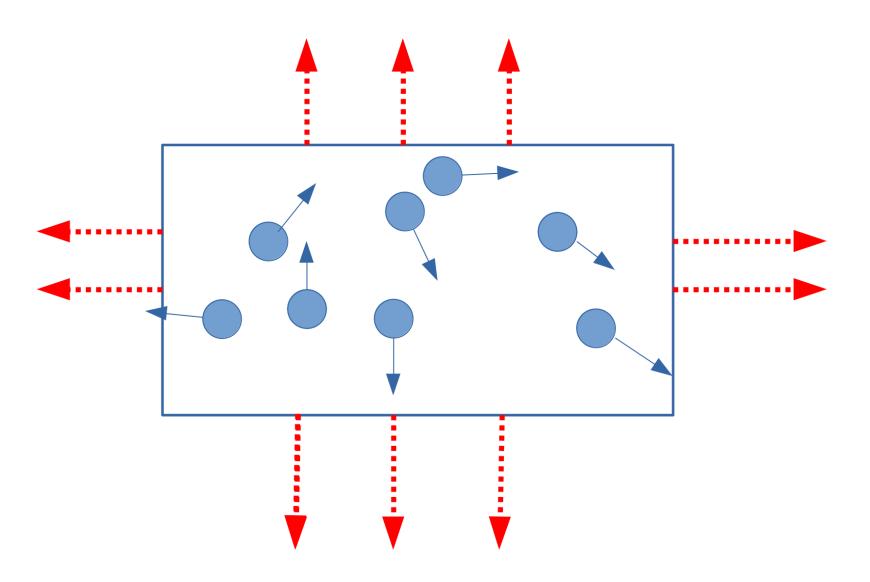
Simulation based Inference

- In this week's lab, we simulate particles moving and colliding with a 2 dimensional bounding box.
- Now, we will use this simulation to do some actual science.

Ideal Gas

- \bullet Imagine a $5m\times 5m$ 2-dimensional box filled with some kind of gas.
- We assume the gas is ideal.
 - No interaction/collision between gas molecules.
 - Gas molecules moves randomly.
- The walls of the box will feel **the pressure of the gas** since molecules collide with the walls.

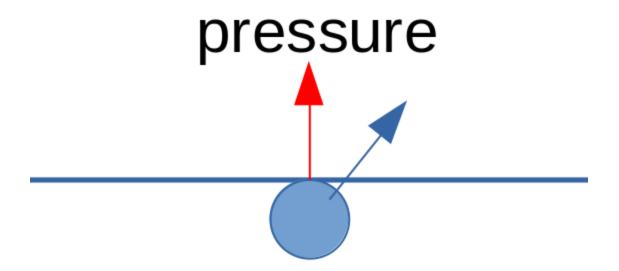
Ideal Gas



The Pressure

- The pressure to the wall is the average force applied perpendicular to the surface per unit area.
- Can we calculate the pressure of the wall using our simulation?
 - Suppose each "point" we plot using the lab code is an ideal gas molecule and the time interval between two update functions is exactly 1s.
 - Pressure created by a single wall-colliding molecule is the velocity perpendicular to the wall.
 - assuming each molecule has unit weight.
 - Adding up all pressures created by wall-colliding molecules, divide by the surface area, you get the average pressure.

The Pressure of a Single Wall-colliding Particle



 Hint: Pressure does not have directions, so you only need to take the magnitude of the perpendicular velocity.

Simulation based Inference

- Imagine the code we wrote during the lab is a simulation of ideal gas, where each "point" is an air molecule.
- Modify your lab code (for the 2nd task), so that it computes the average pressure received by the bounding box over the course of 500s.
- Run such simulations 100 times with randomly generated
 x and v.
- Plot the histogram of the average pressure computed from 100 simulations.
 - o Hint: ?hist

Simulation based Inference

- What is the relationship between the average pressure and number of molecules in the box?
- What is the relationship between the average pressure and velocities of molecules?
 - Hint: You can scale the velocities of molecules by
 v<-matrix(runif(n * 2, -.5, .5), nrow = n)*C,
 where c is a scaling factor.
- Is your finding consistent with Kinetic Theory?
 - \circ $PV=RNmv^{\overline{2}}$, where R is a constant, P is the average pressure, N is the number of molecules, V is the volume of the gas and $v^{\overline{2}}$ is the average of squared molecules velocities.