ass4

November 1, 2019

- 0.1 Assignment 4
- 0.1.1 Question 2] Coding: Classification with the decision tree model

Write a self-contained and fully functional Jupyter Notebook that:

0.1.2 a) Loads the necessary libraries to run (e.g., scikit-learn)

```
[281]: import matplotlib.pyplot as plt
from sklearn.datasets import load_digits
from sklearn.tree import DecisionTreeClassifier
import numpy as np
from sklearn import tree
from sklearn.model_selection import KFold
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score
from sklearn import svm
from sklearn.svm import SVC
from sklearn.neighbors import KNeighborsClassifier
from sklearn.model_selection import cross_val_score
```

0.1.3 b) Loads the dataset "digits" (see below for description) from the scikit-learn example datasets package.

digits is a dataset of a hadnwritten digits. Each feature is the intensity of one pixel of an 8x8 image

```
[284]: # loads digits dataset
digits = load_digits()
#print(digits)

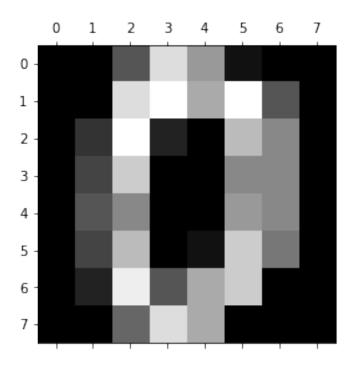
# create feature matrix
x = digits.data

# create target vector - what we are going to predict
y = digits.target
digits.target_names

# view the first observation's feature values
```

```
x[0]
     # view the first observation's feature values as matrix
     digits.images[0]
[284]: array([[ 0., 0., 5., 13., 9., 1.,
                                          0.,
                                               0.],
            [ 0., 0., 13., 15., 10., 15.,
                                          5.,
            [ 0., 3., 15., 2., 0., 11.,
            [ 0., 4., 12., 0., 0., 8.,
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            [0., 5., 8., 0., 0., 9.,
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            [0., 4., 11., 0., 1., 12., 7., 0.],
            [0., 2., 14., 5., 10., 12., 0., 0.],
            [0., 0., 6., 13., 10., 0., 0., 0.]])
[285]: #visualize the observation's feature values as image
     plt.gray()
     plt.matshow(digits.images[0])
     plt.show()
```

<Figure size 432x288 with 0 Axes>



0.1.4 c) Instantiates a sklearn.tree.DecisionTreeClassifier.

```
DecisionTreeClassifier(class_weight=None, criterion='gini', max_depth=None, max_features=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, presort=False, random_state=None, splitter='best')
```

0.1.5 d) Splits the dataset in training and testing sets using sklearn.model_selection.KFold cross validation (use K = 5).

```
[288]: kfold = KFold(n_splits=5)
kfold.get_n_splits(digits)
print(kf)
```

<generator object _BaseKFold.split at 0x000001932EA382A0>

0.1.6 e) Trains and tests the performance of the classifier in identifying the digits.

```
[289]: for train_index, test_index in kfold.split(x):
         print('Train: %s, Test: %s' % (train_index, test_index))
         x_train, x_test = x[train_index], x[test_index]
         y_train, y_test = y[train_index], y[test_index]
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```

```
[290]: # simulate splitting a dataset of 20 observations into 5 folds

kf = KFold(n_splits=5, shuffle=False).split(range(5))
# print the contents of each training and testing set
print('{} {:^14} {}'.format('Iteration', 'Training', 'Testing '))
for iteration, data in enumerate(kf, start=1):
    print('{:^10} {} {:^22}'.format(iteration, data[0], str(data[1])))
```

Iteration	Training	Testing
1	[1 2 3 4]	[0]
2	[0 2 3 4]	[1]
3	[0 1 3 4]	[2]
4	[0 1 2 4]	[3]
5	[0 1 2 3]	[4]

0.1.7 f) Computes and outputs the accuracy for each of the K folds of cross validation.

```
[291]: avg_accuracy = 0
for train_index, test_index in kfold.split(x):
    #print('Train: %s, Test: %s' % (train_index, test_index))
    x_train, x_test = x[train_index], x[test_index]
    y_train, y_test = y[train_index], y[test_index]

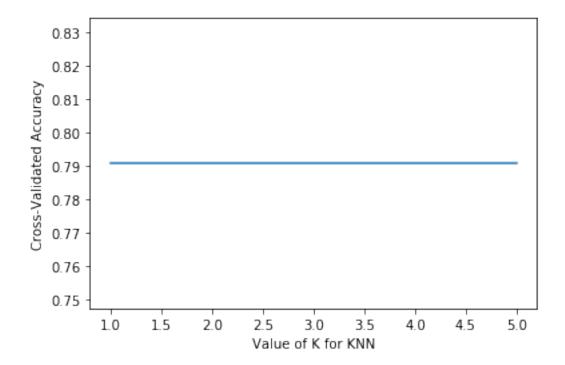
count = 0
    #clf = tree.DecisionTreeClassifier(random_state = 1)
    clf = clf.fit(x_train, y_train)
    predict = clf.predict (x_test)

for i in range (0, len(predict)):
```

```
if predict[i] == y_test[i]:
                  count +=1
          accuracy = count/len(predict)
          print("accuracy for the K folds of cross validation:", accuracy)
     accuracy for the K folds of cross validation: 0.758333333333333
     accuracy for the K folds of cross validation: 0.7416666666666667
     accuracy for the K folds of cross validation: 0.8161559888579387
     accuracy for the K folds of cross validation: 0.8495821727019499
     accuracy for the K folds of cross validation: 0.8022284122562674
[292]: Accuracy_score = cross_val_score(KNeighborsClassifier(n_neighbors=5), x, y,
      print(Accuracy_score )
     [0.9478022 0.9558011 0.96657382 0.98039216 0.96338028]
     0.1.8 g) Computes and outputs the average accuracy across the K folds.
[300]:
         avg_accuracy = (avg_accuracy + accuracy)
      Average = avg_accuracy / 5
      print("Average Accuracy:",Average)
     Average Accuracy: 0.962674094707521
[294]: # use average accuracy as an estimate of out-of-sample accuracy
      print(Accuracy_score .mean())
     0.9627899114966898
[295]: Score = cross_val_score(clf, x_train, y_train, cv=5, scoring = 'accuracy')
      print("Avg accuracy:", accuracy)
      print("Accuracy: %0.3f (+/- %0.3f)" %(Score.mean(), Score.std()*2))
     Avg accuracy: 0.8022284122562674
     Accuracy: 0.791 (+/- 0.073)
[301]: k_range = list(range(1, 6))
      k_scores = []
      for k in k_range:
         knn = KNeighborsClassifier(n_neighbors=k)
         Score = cross_val_score(clf, x_train, y_train, cv=5, scoring ='accuracy')
         k_scores.append(Score.mean())
      print(k_scores)
```

[0.7909259704254555, 0.7909259704254555, 0.7909259704254555, 0.7909259704254555, 0.7909259704254555]

[301]: Text(0, 0.5, 'Cross-Validated Accuracy')



0.1.9 Summary:

Commands: pip install scikit-learn or conda install scikit-learn

[]: []: