# RECOGNITION PERFORMANCE OF A STRUCTURED LANGUAGE MODEL[†]

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## ABSTRACT

A new language model for speech recognition inspired by linguistic analysis is presented. The model develops hidden hierarchical structure incrementally and uses it to extract meaningful information from the word history — thus enabling the use of extended distance dependencies — in an attempt to complement the locality of currently used trigram models. The structured language model, its probabilistic parameterization and performance in a two-pass speech recognizer are presented. Experiments on the SWITCHBOARD corpus show an improvement in both perplexity and word error rate over conventional trigram models.

## 1. INTRODUCTION

The main goal of the present work is to develop and evaluate a language model that uses syntactic structure to model long-distance dependencies. The model we present is closely related to the one investigated in [1], however different in a few important aspects:

• our model operates in a left-to-right manner, allowing the decoding of word lattices, as opposed to the one referred to previously, where only whole sentences could be processed, thus reducing its applicability to N-best list re-scoring; the syntactic structure is developed as a model component;

• our model is a factored version of the one in [1], thus enabling the calculation of the joint probability of words and parse structure; this was not possible in the previous case due to the huge computational complexity of that model.

The structured language model (SLM), its probabilistic parameterization and performance in a two-pass speech recognizer — we evaluate the model in a lattice decoding framework — are presented. Experiments on the SWITCHBOARD corpus show an improvement in both perplexity (PPL) and word error rate (WER) over conventional trigram models.

## 2. STRUCTURED LANGUAGE MODEL

An extensive presentation of the SLM can be found in [2]. The model assigns a probability $P(W, T)$ to every sentence $W$ and its every possible binary parse $T$. The terminals of $T$ are the words of $W$ with POStags, and the nodes of $T$ are annotated with phrase headwords and non-terminal labels. Let $W$ be a



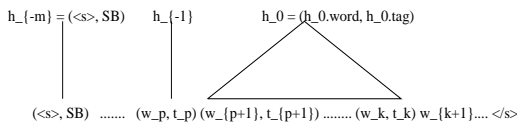Figure 1. A word-parse k-prefix

sentence of length $n$ words to which we have prepended <s> and appended </s> so that $w_0 =$ <s> and $w_{n+1} =$ </s>. Let $W_k$ be the word k-prefix $w_0 \ldots w_k$ of the sentence and $W_k T_k$
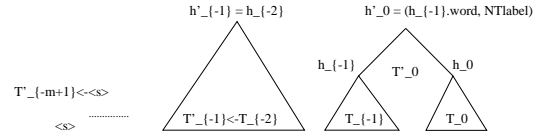
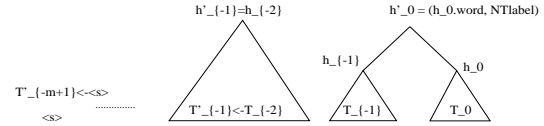Figure 2. Result of adjoin-left under NTlabel



Figure 3. Result of adjoin-right under NTlabel

the *word-parse k-prefix*. Figure 1 shows a word-parse k-prefix; h_0 .. h_{-m} are the *exposed heads*, each head being a pair(headword, non-terminal label), or (word, POStag) in the case of a root-only tree.

### 2.1. Probabilistic Model

The probability $P(W, T)$ of a word sequence $W$ and a complete parse $T$ can be broken into:

$$P(W, T) =$$
$$\prod_{k=1}^{n+1} [ \quad P(w_k/W_{k-1}T_{k-1}) \cdot P(t_k/W_{k-1}T_{k-1}, w_k) \cdot$$
$$\prod_{i=1}^{N_k} P(p_i^k/W_{k-1}T_{k-1}, w_k, t_k, p_1^k \ldots p_{i-1}^k)] \quad (1)$$

where:
• $W_{k-1}T_{k-1}$ is the word-parse $(k-1)$-prefix
• $w_k$ is the word predicted by WORD-PREDICTOR
• $t_k$ is the tag assigned to $w_k$ by the TAGGER
• $N_k - 1$ is the number of operations the PARSER executes at sentence position $k$ before passing control to the WORD-PREDICTOR (the $N_k$-th operation at position k is the null transition); $N_k$ is a function of $T$
• $p_i^k$ denotes the i-th PARSER operation carried out at position k in the word string; the operations performed by the PARSER are illustrated in Figures 2-3 and they ensure that all possible binary branching parses with all possible headword and non-terminal label assignments for the $w_1 \ldots w_k$ word sequence can be generated.

Our model is based on three probabilities, estimated using deleted interpolation [7], parameterized as follows:

$$P(w_k/W_{k-1}T_{k-1}) = P(w_k/h_0, h_{-1}) \quad (2)$$
$$P(t_k/w_k, W_{k-1}T_{k-1}) = P(t_k/w_k, h_0.tag, h_{-1}.tag) \quad (3)$$
$$P(p_i^k/W_kT_k) = P(p_i^k/h_0, h_{-1}) \quad (4)$$

It is worth noting that if the binary branching structure developed by the parser were always right-branching and we mapped

the POStag and non-terminal label vocabularies to a single type then our model would be equivalent to a trigram language model. Since the number of parses for a given word prefix $W_k$ grows exponentially with $k$, $|\{T_k\}| \sim O(2^k)$, the state space of our model is huge even for relatively short sentences so we had to use a search strategy that prunes it. Our choice was a synchronous multi-stack search algorithm which is very similar to a beam search.

The probability assignment for the word at position $k+1$ in the input sentence is made using:

$$P_{SLM}(w_{k+1}/W_k) = \sum_{T_k \in S_k} P(w_{k+1}/W_k T_k) \cdot \rho(W_k, T_k),$$

$$\rho(W_k, T_k) = P(W_k T_k)/\sum_{T_k \in S_k} P(W_k T_k) \qquad (5)$$

which ensures a proper probability over strings $W^*$, where $S_k$ is the set of all parses present in our stacks at the current stage $k$. An N-best EM [5] variant is employed to reestimate the model parameters such that the PPL on training data is decreased — the likelihood of the training data under our model is increased. The reduction in PPL is shown experimentally to carry over to the test data.

## 3.  $A^*$ DECODER FOR LATTICES

### 3.1.  $A^*$ Algorithm

The $A^*$ algorithm [8] is a tree search strategy that could be compared to depth-first tree-traversal: pursue the most promising path as deeply as possible.

To be more specific, let a set of hypotheses $L = \{h : x_1, \ldots, x_n\}, \; x_i \in \mathcal{W}^*$ — to be scored using the function $f(\cdot)$ — be organized as a prefix tree. We wish to obtain the hypothesis $h^* = \arg\max_{h \in L} f(h)$ without scoring all the hypotheses in $L$, if possible with a minimal computational effort.

To be able to pursue the most promising path, the algorithm needs to evaluate the possible continuations of a given prefix $x = w_1, \ldots, w_p$ that reach the end of the lattice. Let $C_L(x)$ be the set of complete continuations of $x$ in $L$ — they all reach the end of the lattice, see Figure 4. Assume we have an overestimate $g(x.y) = f(x) + h(y|x) \geq f(x.y)$ for the score of *complete* hypothesis $x.y$ — . denotes concatenation; imposing that $h(y|x) = 0$ for empty $y$, we have $g(x) = f(x), \forall \; complete \; x \in L$. This
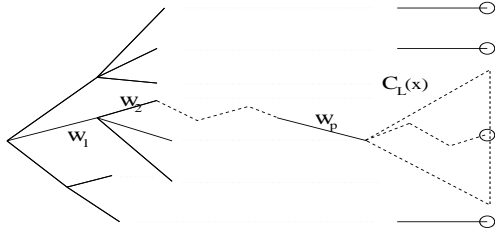


Figure 4. Prefix Tree Organization of a Set of Hypotheses

means that the quantity defined as:

$$g_L(x) \doteq \max_{y \in C_L(x)} g(x.y) = f(x) + h_L(x), \qquad (6)$$

$$h_L(x) \doteq \max_{y \in C_L(x)} h(y|x) \qquad (7)$$

is an overestimate of the most promising complete continuation of $x$ in $L$: $g_L(x) \geq f(x.y), \forall y \in C_L(x)$ and that $g_L(x) = f(x), \forall \; complete \; x \in L$.

The $A^*$ algorithm uses a potentially infinite stack[1] in which prefixes $x$ are ordered in decreasing order of $g_L(x)$; at each extension step the top-most prefix $x = w_1, \ldots, w_p$ is popped form

[1] The stack need not be larger than $|L| = n$

the stack, expanded with all possible one-symbol continuations of $x$ in $L$ and then all the resulting expanded prefixes — among which there may be complete hypotheses as well — are inserted back into the stack. The stopping condition is: whenever the popped hypothesis is a complete one, retain that one as the overall best hypothesis $h^*$.

### 3.2.  $A^*$ for Lattice Decoding

There are a couple of reasons that make $A^*$ appealing for our problem:
• the algorithm operates with whole prefixes $x$, making it ideal for incorporating language models whose memory is the entire prefix;
• a reasonably good overestimate $h(y|x)$ and an efficient way to calculate $h_L(x)$ (see Eq.6) are readily available using the n-gram model, as we will explain later.

The lattices we work with retain the following information after the first pass:
• time-alignment of each node;
• for each link connecting two nodes in the lattice we retain: word identity, acoustic model score and n-gram language model score. The lattice has a unique starting and ending node, respectively.

A lattice can be conceptually organized as a prefix tree of paths. When rescoring the lattice using a different language model than the one that was used in the first pass, we seek to find the complete path $p = l_0 \ldots l_n$ maximizing:

$$
\begin{aligned}
f(p) = \sum_{i=0}^{n} [ \; & logP_{AM}(l_i) \\
+ \; & LMweight \cdot logP_{LM}(w(l_i)|w(l_0) \ldots w(l_{i-1})) \\
- \; & logP_{IP} \; ] \qquad (8)
\end{aligned}
$$

where:
• $logP_{AM}(l_i)$ is the acoustic model log-likelihood assigned to link $l_i$;
• $logP_{LM}(w(l_i)|w(l_0) \ldots w(l_{i-1}))$ is the language model log-probability assigned to link $l_i$ given the previous links on the partial path $l_0 \ldots l_i$;
• $LMweight > 0$ is a constant weight which multiplies the language model score of a link; its theoretical justification is unclear but experiments show its usefulness;
• $logP_{IP} > 0$ is the "insertion penalty"; again, its theoretical justification is unclear but experiments show its usefulness.

To be able to apply the $A^*$ algorithm we need to find an appropriate stack entry scoring function $g_L(x)$ where $x$ is a partial path and $L$ is the set of complete paths in the lattice. Going back to the definition (6) of $g_L(\cdot)$ we need an overestimate $g(x.y) = f(x) + h(y|x) \geq f(x.y)$ for all possible $y = l_k \ldots l_n$ complete continuations of $x$ allowed by the lattice. We propose to use the heuristic:

$$
\begin{aligned}
h(y|x) = \sum_{i=k}^{n} [ & logP_{AM}(l_i) + LMweight \cdot (logP_{NG}(l_i) \\
& + logP_{COMP}) - logP_{IP}] \\
& + LMweight \cdot logP_{FINAL} \cdot \delta(k < n) \qquad (9)
\end{aligned}
$$

A simple calculation shows that if

$$logP_{NG}(l_i) + logP_{COMP} \geq logP_{LM}(l_i), \forall l_i$$

is satisfied then $g_L(x) = f(x) + max_{y \in C_L(x)} h(y|x)$ is a an appropriate choice for the $A^*$ search.

The justification for the $logP_{COMP}$ term is that it is supposed to compensate for the per word difference in log-probability between the n-gram model $NG$ and the superior model $LM$ with which we rescore the lattice — hence $logP_{COMP} > 0$. Its expected value can be estimated from the difference in perplexity between the two models $LM$ and $NG$. The $logP_{FINAL} > 0$

term is used for practical considerations as explained in the next section.

The calculation of $g_L(x)$ (6) is made very efficient after realizing that one can use the dynamic programming technique in the Viterbi algorithm [9]. Indeed, for a given lattice $L$, the value of $h_L(x)$ is completely determined by the identity of the ending node of $x$; a Viterbi backward pass over the lattice can store at each node the corresponding value of $h_L(x) = h_L(ending\_node(x))$ such that it is readily available in the $A^*$ search.

### 3.3. Some Practical Considerations

In practice one cannot maintain a potentially infinite stack. We chose to control the stack depth using two thresholds: one on the maximum number of entries in the stack, called *stack-depth-threshold* and another one on the maximum log-probability difference between the top most and the bottom most hypotheses in the stack, called *stack-logP-threshold*.

A gross overestimate used in connection with a finite stack may lure the search on a cluster of paths which is suboptimal — the desired cluster of paths may fall short of the stack if the overestimate happens to favor a wrong cluster.

Also, longer partial paths — thus having shorter suffixes — benefit less from the per word $logP_{COMP}$ compensation which means that they may fall out of a stack already full with shorter hypotheses — which have high scores due to compensation. This is the justification for the $logP_{FINAL}$ term in the compensation function $h(y|x)$: the variance $var[logP_{LM}(l_i|l_0 \dots l_{i-1}) - logP_{NG}(l_i)]$ is a finite positive quantity so the compensation is likely to be closer to the expected value $E[logP_{LM}(l_i|l_0 \dots l_{i-1}) - logP_{NG}(l_i)]$ for longer $y$ continuations than for shorter ones; introducing a constant $logP_{FINAL}$ term is equivalent to an adaptive $logP_{COMP}$ depending on the length of the $y$ suffix — smaller equivalent $logP_{COMP}$ for long suffixes $y$ for which $E[logP_{LM}(l_i|l_0 \dots l_{i-1}) - logP_{NG}(l_i)]$ is a better estimate for $logP_{COMP}$ than it is for shorter ones.

Because the structured language model is computationally expensive, a strong limitation is being placed on the width of the search — controlled by the `stack-depth` and the `stack-logP-threshold`. For an acceptable search width — runtime — one seeks to tune the compensation parameters to maximize performance measured in terms of WER. However, the correlation between these parameters and the WER is not clear and makes search problems diagnosis extremely difficult. Our method for choosing the search and compensation parameters was to sample a few complete paths $p_1, \dots, p_N$ from each lattice, rescore those paths according to the $f(\cdot)$ function (8) and then rank the $h^*$ path output by the $A^*$ search among the sampled paths. A correct $A^*$ search should result in average rank 0. In practice this doesn't happen but one can trace the topmost path $p^*$ — in the offending cases $p^* \neq h^*$ and $f(p^*) > f(h^*)$ — and check whether the search failed strictly because of insufficient compensation — a prefix of the $p^*$ hypothesis is present in the stack when $A^*$ returns — or because the path $p^*$ fell short of the stack during the search — in which case the compensation and the search-width interact.

The method we chose for sampling paths from the lattice was an N-best search using the n-gram language model scores; this is appropriate for pragmatic reasons — one prefers lattice rescoring to N-best list rescoring exactly because of the possibility to extract a path that is not among the candidates proposed in the N-best list — as well as practical reasons — they are among the "better" paths in terms of WER.

## 4. EXPERIMENTS

### 4.1. Experimental Setup

In order to train the structured language model (SLM) as described in [2] we need parse trees from which to initialize the parameters of the model. Fortunately a part of the Switchboard (SWB) [6] data has been manually parsed at UPenn ; let us refer to this corpus as the SWB-Treebank. The SWB training data

used for speech recognition — SWB-CSR — is different from the SWB-Treebank in two aspects:
- the SWB-Treebank is a subset of the SWB-CSR data;
- the SWB-Treebank tokenization is different from that of the SWB-CSR corpus; among other spurious small differences, the most frequent ones are of the type presented in Table 1.

| SWB-Treebank | SWB-CSR |
|--------------|---------|
| do n't | don't |
| it 's | it's |
| i 'm | i'm |
| i 'll | i'll |

Table 1. SWB-Treebank SWB-CSR tokenization mismatch

Our goal is to train the SLM on the SWB-CSR corpus.

#### 4.1.1. Training Setup

The training of the SLM model proceeded as follows:
- train SLM on SWB-Treebank — using the SWB-Treebank closed vocabulary — as described in [2]; this is possible because for this data we have parse trees from which we can gather initial statistics;
- process the SWB-CSR training data to bring it closer to the SWB-Treebank format. We applied the transformations suggested by Table 1; the resulting corpus will be called SWB-CSR-Treebank, although at this stage we only have words and no parse trees for it;
- transfer the SWB-Treebank parse trees onto the SWB-CSR-Treebank training corpus. To do so we parsed the SWB-CSR-Treebank using the SLM trained on the SWB-Treebank; the vocabulary for this step was the union between the SWB-Treebank and the SWB-CSR-Treebank closed vocabularies; at this stage SWB-CSR-Treebank is truly a "treebank";
- retrain the SLM on the SWB-CSR-Treebank training corpus using the parse trees obtained at the previous step for gathering initial statistics; the vocabulary used at this step was the SWB-CSR-Treebank closed vocabulary.

#### 4.1.2. Lattice Decoding Setup

To be able to run lattice decoding experiments we need to bring the lattices — SWB-CSR tokenization — to the SWB-CSR-Treebank format. The only operation involved in this transformation is splitting certain words into two parts, as suggested by Table 1. Each link whose word needs to be split is cut into two parts and an intermediate node is inserted into the lattice as shown in Figure 5. The acoustic and language model scores of the initial link are copied onto the second new link. *For all the*
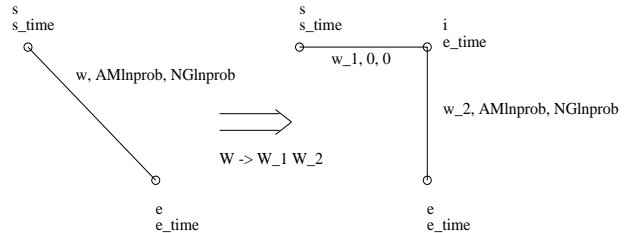


Figure 5. Lattice Processing

*decoding experiments we have carried out, the WER is measured after undoing the transformations highlighted above; the reference transcriptions for the test data were not touched and the NIST SCLITE package was used for measuring the WER.*

### 4.2. Perplexity Results

As a first step we evaluated the perplexity performance of the SLM relative to that of a deleted interpolation 3-gram model trained in the same conditions. We worked on the SWB-CSR-Treebank corpus. The size of the training data was 2.29 Mwds;

the size of the test data set aside for perplexity measurements was 28 Kwds — WS97 DevTest [4]. We used a closed vocabulary — test set words included in the vocabulary — of size 22Kwds. Similar to the experiments reported in [2], we built a deleted interpolation 3-gram model which was used as a baseline; we have also linearly interpolated the SLM with the 3-gram baseline showing a modest reduction in perplexity:

$$P(w_i|W_{i-1}) = \lambda \cdot P(w_i|w_{i-1}, w_{i-2}) + (1-\lambda) \cdot P_{SLM}(w_i|W_{i-1})$$

The results are presented in Table 2.

| Language Model | L2R Perplexity | | | | |
| | DEV set | | TEST set | | |
| $\lambda$ | 0.0 | 1.0 | 0.0 | 0.4 | 1.0 |
|---|---|---|---|---|---|
| 3-gram + Initl SLM | 23.9 | 22.5 | 72.1 | 65.8 | 68.6 |
| 3-gram + Reest SLM | 22.7 | 22.5 | 71.0 | 65.4 | 68.6 |

Table 2. Perplexity Results

### 4.3. Lattice Decoding Results

We proceeded to evaluate the WER performance of the SLM using the $A^*$ lattice decoder described previously. Before describing the experiments we need to make clear one point; there are two 3-gram language model scores associated with the each link in the lattice:

• the language model score assigned by the model that generated the lattice, referred to as the LAT3-gram; this model operates on text in the SWB-CSR tokenization;

• the language model score assigned by rescoring each link in the lattice with the deleted interpolation 3-gram built on the data in the SWB-CSR-Treebank tokenization, referred to simply as the 3-gram — used in the experiments reported in the previous section.

The perplexity results show that interpolation with the 3-gram model is beneficial for our model. Note that the interpolation:

$$P(l) = \lambda \cdot P_{LAT3-gram}(l) + (1 - \lambda) \cdot P_{SLM}(l)$$

between the LAT3-gram model and the SLM is illegitimate due to the tokenization mismatch.

As explained previously, due to the fact that the SLM's memory extends over the entire prefix we need to apply the $A^*$ algorithm to find the overall best path in the lattice. The parameters controlling the $A^*$ search were set to: $logP_{COMP} = 0.5$, $logP_{FINAL} = 2$, $LMweight = 12$, $logP_{IP} = 10$, stack-depth-threshold=30, stack-depth-logP-threshold=100 — see (8) and (9). The parameters controlling the SLM were the same as in [2]. The results for different interpolation coefficient values are shown in Table 3.

| Language Model | WER | | | |
| Search | $A^*$ | | | Vite |
| $\lambda$ | 0.0 | 0.4 | 1.0 | 1.0 |
|---|---|---|---|---|
| LAT-3gram + SLM | 42.4 | **40.3** | 41.6 | <u>41.3</u> |

Table 3. Lattice Decoding Results

The structured language model achieved an absolute improvement of 1% WER over the baseline; the improvement is statistically significant at the 0.002 level according to a sign test. In the 3-gram case, the $A^*$ search looses 0.3% over the Viterbi search due to finite stack and heuristic lookahead.

### 4.4. Search Evaluation Results

For tuning the search parameters we have applied the N-best lattice sampling technique described in Section 3.3. As a by-product, the WER performance of the structured language model on N-best list rescoring — N = 25 — was 40.9%. The average rank of the hypothesis found by the $A^*$ search among the N-best

ones — after rescoring them using the structured language model interpolated with the trigram — was 1.07 (minimum achievable value is 0). There were 585 offending sentences — out of a total of 2427 test sentences — in which the $A^*$ search led to a hypothesis whose score was lower than that of the top hypothesis among the N-best (1-best). In 310 cases the prefix of the rescored 1-best was still in the stack when $A^*$ returned — inadequate compensation — and in the other 275 cases the 1-best hypothesis was lost during the search due to the finite stack size.

One interesting experimental observation was that even though in the 585 offending cases the score of the 1-best was higher than that of the hypothesis found by $A^*$, the WER of those hypotheses — as a set — was *higher* than that of the set of $A^*$ hypotheses.

## 5. CONCLUSIONS

Similar experiments on the Wall Street Journal corpus are reported in [3] showing that the improvement holds even when the WER is much lower.

We believe we have presented an original approach to language modeling that takes into account the hierarchical structure in natural language. Our experiments showed improvement in both perplexity and word error rate over current language modeling techniques demonstrating the usefulness of syntactic structure for improved language models.

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