## Problem B

## Fun with Stones

Alice and Bob will play a game with 3 piles of stones. They take turns and, on each turn, a player must choose a pile that still has stones and remove a positive number of stones from it. Whoever removes the last stone from the last pile that still had stones wins. Alice makes the first move.

The *i*-th pile will have a random and uniformly distributed number of stones in the range  $[L_i, R_i]$ . What is the probability that Alice wins given that they both play optimally?

## Input

The input consists of a line with 6 integers, respectively,  $L_1, R_1, L_2, R_2, L_3, R_3$ . For each  $i, 1 \le L_i \le R_i \le 10^9$ .

## Output

Print an integer representing the probability that Alice wins modulo  $10^9 + 7$ .

It can be shown that the answer can be expressed as an irreducible fraction  $\frac{p}{q}$ , where p and q are integers and  $q \not\equiv 0 \pmod{10^9 + 7}$ , that is, we are interested in the integer  $p \times q^{-1} \pmod{10^9 + 7}$ .

Input example 1	Output example 1
3 3 4 4 5 5	1
Input example 2	Output example 2
4 4 8 8 12 12	0
Input example 3	Output example 3
1 10 1 10 1 10	580000005
Input example 4	Output example 4
5 15 2 9 35 42	1