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FMAT 8-BIT INSTRUCTION SET ARCHITECTURE

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1. INTRODUCTION

The FMAT Instruction Set Architecture is an 8-bit redesign of the standard MIPS Instruction Set. Our ISA is uniquely implemented to allow certain performance optimizations.

The FMAT ISA provides 8 bit wide instructions and 16 internal registers, which although is somewhat limited in instruction set breadth and memory, is sufficient for the implementation and execution of our three basic programs (product, string_match, and closest_pair). The FMAT Instruction Set supports essential operations including basic computational, logical, data control and transfer operations standard to the MIPS architecture as well as a few specialized instructions unique to the FMAT ISA that enables extended register functionality and use in light of the restricted width of our 8-bit processor. For instance, special operations such as **focus**, **otype rframe**, and **otype sframe** enables the user to effectively use more registers and thus handle more data than what a normal 8 bit instruction space would conservatively allow. In addition, FMAT aims to reduce overall dynamic instruction count thereby hopefully producing more efficient looped code and speedups.

2. INSTRUCTION FORMATS

	INSTRUCTION TYPES SPECIFICATION									
TVDE	NAME	ADDRESS FORMAT IN BITS					DESTINATION			
TYPE	NAME	7	6	5	4	3	2	1	0	DESTINATION
RR	REGISTER REGISTER		OPCODE		REG	i# REG#		G#	Reuse RS	
AF	ADDRESS FLAG	OPCODE		FRAME	RE	G#	FLAG	Specified		
Α	ADDRESS		OPCODE			FRA	ME	RE	G#	Implicit
I	IMMEDIATE		OPCODE				IM	M		Implicit
II	IMMEDIATE IMMEDIATE	OPCODE		IM	М	1 IMM		Implicit		
IF	IMMEDIATE FLAG		OPC	ODE			IMM		FLAG	Implicit

	INSTRUCTION TYPES EXAMPLES									
TVDE	EXAMPLE ADDRESS FORMAT IN BITS						DESTINATION			
TYPE	INSTRUCTION	7	6	5	4	3	2	1	0	DESTINATION
RR	ADD		00	001		0	0	C)1	reg[0][0]
AF	INCDEC		00	011		0	C	0	0	reg[0][0]
Α	FOCUS	1011			1	1	C	00	\$R	
ı	LOWER	1100				11	01		reg[\$R]	
II	JUMPIF	1111		0	0	1	0	N/A (\$PC)		
IF	SHIFT		11	110			100		0	reg[\$R]

3. OPERATIONS

	INSTRUCTIONS									
TVDE	ODCODE	INICTO	4 h:4	4 6:4	4 6:4	4 6:4	EVECODE	EVTINCED	FL	AG
TYPE	OPCODE	INSTR	1 bit	1 bit	1 bit	1 bit	EXTCODE EXTINSTR		if 0	if 1
IF	0000	OTYPE	(extin	str) <imm></imm>	•	(flag) <imm></imm>	000	NOP		
IF	0000	OTYPE	(extin	str) <imm></imm>	•	(flag) <imm></imm>	001	HALT		
IF	0000	OTYPE	(extin	str) <imm></imm>	•	(flag) <imm></imm>	010	TBD		
IF	0000	OTYPE	(extin	str) <imm></imm>	•	(flag) <imm></imm>	011	OVRFLW		
IF	0000	OTYPE	(extin	str) <imm></imm>	•	(flag) <imm></imm>	100	CLEAR	0s	1s
IF	0000	OTYPE	(extin	str) <imm></imm>	•	(flag) <imm></imm>	101	NSET	0	1
IF	0000	OTYPE	(extin	(extinstr) <imm></imm>		(flag) <imm></imm>	110	RFRAME	0	1
IF	0000	OTYPE	(extin	(extinstr) <imm></imm>		(flag) <imm></imm>	111	SFRAME	2	3
RR	0001	ADD	(reg#) <im< td=""><td colspan="2">#)<imm> (reg#)<in< td=""><td>t)<imm></imm></td><td></td><td></td><td></td><td></td></in<></imm></td></im<>	#) <imm> (reg#)<in< td=""><td>t)<imm></imm></td><td></td><td></td><td></td><td></td></in<></imm>		t) <imm></imm>				
RR	0010	SUB	(reg#) <im< td=""><td colspan="2">(reg#)<imm> (reg#</imm></td><td>*)<imm></imm></td><td></td><td></td><td></td><td></td></im<>	(reg#) <imm> (reg#</imm>		*) <imm></imm>				
AF	0011	INCDEC	(frame) <imm></imm>	(frame) <imm> (reg#)<imm></imm></imm>		(flag) <imm></imm>			inc	dec
RR	0100	AND	(reg#) <imm> (reg#</imm>		(reg#	*) <imm></imm>				
RR	0101	OR	(reg#) <im< td=""><td>M></td><td>(reg#</td><td>‡)<imm></imm></td><td></td><td></td><td></td><td></td></im<>	M>	(reg#	‡) <imm></imm>				
Α	0110	NOT	(frame#) <ii< td=""><td>MM></td><td>(reg#</td><td>‡)<imm></imm></td><td></td><td></td><td></td><td></td></ii<>	MM>	(reg#	‡) <imm></imm>				
AF	0111	SEED	(frame) <imm></imm>	(reg#)	<imm></imm>	(flag) <imm></imm>			\$CL	\$CR
RR	1000	MOVE	(reg#) <im< td=""><td>M></td><td>(reg#</td><td>*)<imm></imm></td><td></td><td></td><td></td><td></td></im<>	M>	(reg#	*) <imm></imm>				
RR	1001	LOAD	(reg#) <im< td=""><td>M></td><td>[(reg#</td><td>*)<imm>]</imm></td><td></td><td></td><td></td><td></td></im<>	M>	[(reg#	*) <imm>]</imm>				
RR	1010	STORE	[(reg#) <im< td=""><td colspan="2">[(reg#)<imm>] (reg#</imm></td><td>‡)<imm></imm></td><td></td><td></td><td></td><td></td></im<>	[(reg#) <imm>] (reg#</imm>		‡) <imm></imm>				
Α	1011	FOCUS	(frame) <imm> (reg#</imm>		‡) <imm></imm>					
I	1100	LOWER	<imm></imm>							
I	1101	UPPER		<imi></imi>	M>					
IF	1110	SHIFT	(amo	unt) <imm></imm>		(flag) <imm></imm>			left	right
II	1111	JUMPIF	(\$J#) <imi< td=""><td>M></td><td>(condit</td><td>on)<imm></imm></td><td></td><td></td><td></td><td></td></imi<>	M>	(condit	on) <imm></imm>				

FURTHER INSTRUCTION LISTING/ANALYSIS:

OTYPE NOP - Does not read, and does not write.

SYNTAX	MEANING	EXAMPLE
otype nop	zzz	otype nop # nothing happens

OTYPE HALT - Stop the machine from executing the current program.

SYNTAX	MEANING	EXAMPLE
otype halt	stop execution	otype halt # end of program

OTYPE TBD - It is a mystery.

SYNTAX	MEANING	EXAMPLE
otype tbd	???	otype tbd # ???

OTYPE OVRFLW - Adds the overflow bit to the focused register if flag is 1, subtracts if flag is 0.

SYNTAX	MEANING	EXAMPLE
otype ovrflw, 0	if flag = 0 (add): \$[\$R]++	# \$[0][0] = \$[0][1] = 200 add 0, 1 # result will overflow otype ovrflw, 0# \$[\$R]++
	<pre>if flag = 0 (substract): \$[\$R]</pre>	

OTYPE CLEAR - Clear the bits of \$[\$F][0] to 0s if flag is 0, or 1s if flag is 1.

SYNTAX	MEANING	EXAMPLE
otype clear, (fill) <imm></imm>	\$[\$R] <= 0 - fill	otype clear, 0 # \$[\$F][0] is now all zeros

OTYPE NSET - Set the \$N bit.

SYNTAX	MEANING	EXAMPLE
otype nset, 1	\$N <= 1	otype nset, 1 # \$N is now 1

OTYPE RFRAME - Changes the currently-focused-on registers to the specified REG FRAME.

SYNTAX	MEANING	EXAMPLE
otype rframe, (frame) <imm></imm>	\$F <= frame	otype rframe, 1 #\$F = 1

OTYPE SFRAME - Changes the currently-focused-on registers to the specified SYS FRAME.

SYNTAX	MEANING	EXAMPLE
otype sframe, (frame) <imm></imm>	\$F <= frame+2	otype sframe, 1 #\$F = 3

ADD: Adds the contents of two registers, rs and rt, and stores the result back into register rs.

SYNTAX	MEANING	EXAMPLE
add rs, rt	\$[rs] <= \$[rs] + \$[rt]	# \$1 = 1, \$2 = 2 add 1, 2 # \$1 = 1 + 2

SUB: Subtracts the contents of two registers, rs and rt, and stores the result back into register rs.

SYNTAX	MEANING	EXAMPLE
sub rs, rt	\$[rs] <= \$[rs] - \$[rt]	# \$1 = 2, \$2 = 1 sub 1, 2 # \$1 = 2 - 1

INCDEC: Increments or decrements (depending on flag) the contents of the register specified by the integer immediates. If flag = 0, the value of the register is incremented, else if flag = 1, the value of the register is decremented.

SYNTAX	MEANING	EXAMPLE
incdec (frame) <imm>, (reg)<imm>,</imm></imm>	if flag = 0 (Increment):	# \$[0][1] = 1
(flag) <imm></imm>	\$[frame][reg]++	incdec 0, 1, 0 # \$[0][1]++

<pre>if flag = 1 (Decrement): \$[frame][reg]</pre>	# \$[1][3] = 1 incdec 1, 3, 1 # \$[1][3]
--	---

AND: Performs a bitwise AND operation on the contents of registers rs and rt; stores the results back into register rs.

SYNTAX	MEANING	EXAMPLE
and rs, rt	\$[rs] <= \$[rs] & \$[rt]	# \$1 = 1, \$2 = 1 and \$1, \$2 # \$1 = 1 & 1

OR: Performs a bitwise OR operation on the contents of registers rs and rt; stores the results back into register rs.

SYNTAX	MEANING	EXAMPLE
or rs, rt	\$[rs] <= \$[rs] \$[rt]	# \$1 = 1, \$2 = 1 or \$1, \$2 # \$1 = 1 1

NOT: Performs a bitwise NOT operation on the contents of registers rs; stores the results back into register rs.

SYNTAX	MEANING	EXAMPLE
not rs	\$[rs] <= !(\$[rs])	# \$1 = 1 not \$1 # \$1 = 0

SEED - Sets \$CL or \$CR (depending on the value of the flag immediate) to be the register address or value (depends on whether \$CL or \$CR) of the register specified by the integer immediates - frame# and reg#. If flag = 0, register \$CL is set to the address of \$[frame#][reg#], else if flag = 1, the value of the register \$CR is set to value of \$[frame#][reg#]. This instruction is meant to optimize loop performance, by preemptively storing conditional comparison values beforehand.

SYNTAX	MEANING	EXAMPLE
<pre>seed (frame)<imm>, (reg)<imm>,</imm></imm></pre>	<pre>if flag = 0 (\$CL): \$CL <= (frame<<2) reg if flag = 1 (\$CR): \$CR <= \$[frame][reg]</pre>	seed 0, 1, 0 # \$CL = 0001 seed 1, 3, 1 # \$CR = \$[1][3]

MOVE: Copies the contents of register rt into register rs.

SYNTAX	MEANING	EXAMPLE
move rs, rt	\$[rs] <= \$[rt]	# \$1 = 0, \$2 = 1 move \$1, \$2 # \$1 = 1

LOAD: Loads Byte (8 Bits) from main memory into register rs from the address of register rt.

SYNTAX	MEANING	EXAMPLE
load rs, rt	R[rs] <= mem[offset]	load \$1, \$2 # \$1 = mem[\$2]

STORE: Store Byte (8 Bits) from contents of register rt into the memory address, rs

SYNTAX	MEANING	EXAMPLE
store rs, rt	mem[rs] <= \$[rt]	store \$1, \$2 # mem[\$1] = \$2

FOCUS: Sets \$F to the address of \$[frame#][reg#]

SYNTAX MEANING EXAMPLE		SYNTAX	MEANING	EXAMPLE
------------------------	--	--------	---------	---------

foci	us (frame) <imm>, (reg)<imm></imm></imm>	\$[\$F] = (frame<<2) reg	focus 3, 0	# \$F = 00001100	
------	--	----------------------------	------------	------------------	--

LOWER: Sets the lower four bits of the current "focused" register to the immediate value.

SYNTAX	MEANING	EXAMPLE					
lower <imm></imm>	\$[\$F] IMM	# \$[0][0] = 1111 1111 lower 5 # \$[0][0] = 1111 0101					

UPPER: Sets the upper four bits of the current "focused" register to the immediate value.

SYNTAX	MEANING	EXAMPLE				
upper <imm></imm>	\$[\$F] (IMM<<4)	# \$[0][0] = 1111 1111 upper 5# \$[0][0] = 0101 1111				

SHIFT: Shift the bits of the current "focused" register by the specified amount, in the specified (flag) direction. Left if a 0 flag, right is a 1 flag. An amount of 0 has a special meaning of 8, since we will never have a use for shifting a value by 0 places.

SYNTAX	MEANING	EXAMPLE					
shift (amount) <imm>, (direction)<imm></imm></imm>	\$[\$F] <= \$[\$F]< <amount< td=""><td># \$[0][0] = 1111 1111 shift 4, 1 # \$[0][0] = 0000 1111</td></amount<>	# \$[0][0] = 1111 1111 shift 4, 1 # \$[0][0] = 0000 1111					

JUMPIF: Jumps to the address stored in \$[3][reg] if \$CR is related to \$CL by the immediate comparison code. Comparison codes: 0: equal, 1: less than, 2: greater than, 3: will always return true. If you need to simply jump without checking for a condition, set #2 to be 3. If you want to negate the comparison, use otype nset to set \$N to 1.

SYNTAX	MEANING	EXAMPLE					
jumpif (reg) <imm>, (compare)<imm></imm></imm>	if (\$CL compare,\$C \$CR): \$PC <= \$[3][reg]	# \$CL > \$CR, \$C = 0 jumpif 3, 2 # jump to \$[3][3]					
		jumpif 3, 3 # jump to \$[3][3]					

4. Internal Registers

In our design, we utilize 16 registers: \$reg[0,1,2,3,4,5,6,7] are usable, \$reg[8,9,10,11] are implicitly used by the system, and only ever written to indirectly through otype instructions. \$reg[12,13,14,15] are usable, but should only be used for their specific purpose, to hold jump addresses. Each register holds 8 bits.

REGISTERS															
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
(FRAME 0 FRAME 1 REG FRAME 0) (REG FRAME 1)		FRAME 2 FRAME 3 (SYS FRAME 1))								
								N CL	CR	R	F	J0	J1	J2	J3

WHAT ARE REGISTER FRAMES?

The machine starts off in register frame 0. If you mention any 2-bit register address when in register frame 0, here are the registers you're talking about

00 register 0

01 register 1

10 register 2

11 register 3

It would be nice to have more registers. We obviously can't access more than 4 registers though, since we can only afford to support up to 2-parameter instructions if the register addresses can each fit in 2 bits. This is where register frames come in. You can change your register frame with the **otype rframe #1** and **otype sframe #1** instructions. If I issue **otype rframe 1**, then my register frame will now be 1 (frame number is stored in the \$F implicit register). NOW, if I mention 2-bit register addresses in any instructions, I will actually be talking about

00 register 4

01 register 5

10 register 6

11 register 7

There are certain instructions (instructions that can spare more bits for a single register address) that directly address registers.

REG FRAME REGISTERS

These are general-purpose registers that the programmer may use however they wish.

SYS FRAME REGISTERS

These are special registers that are written to ahead of time. Their values are called up to add extra information when we issue complex instructions later on. It's okay to read from and write to SYS FRAME 1 registers, but you really shouldn't be writing to SYS FRAME 0 registers. You *can*, but there shouldn't be a need to, since these values are written to implicitly after certain **otype** instructions are run; using the appropriate **otype** instruction, you may set these registers from anywhere in a program with only one instruction, but manually focusing on a SYS FRAME 0 register, setting its lower bits, and setting its upper bits would take three instructions. Because not all these values take up a full 8 bits, these registers are sometimes shared.

R [4bits] (Register): the address of the focused register, because the letter F was already taken.

N [1bit] (Negation): whether comparisons in jumpif #1, #2 instructions should be negated, 0 for normal, 1 for negated. We need this simply because we don't even have a single bit to spare in the jumpif #1, #2 instruction.

F [2bits] (Frame): the current frame, simply describes our current frame value: {0,1,2,3}

CL [4bits] (Compare Left): the address of the register used on the left side of the comparison (dynamic value). **CR [8bits] (Compare Right)**: the value used on the right side of the comparison (static value).

These values are primarily intended for use with the **jumpif #1**, **#2** instructions, so that (1) we have enough bits to specify the comparison we're making and (2) so that the comparison can be done in the same instruction as the jump, by specifying which values we wish to compare *outside of the loop*.

J0, J1, J2, J3 [each 8bits] (Jumps): 8-bit addresses, pointing to locations that we wish to jump to when using loops or conditionals. For example, when we want to write a loop, we would set \$J0 and \$J1 ahead of time so that we can save those bits for other purposes when we actually issue the **jumpif #1, #2** instruction.

"THAT'S TOO TROUBLESOME"

Our original design only used 4 registers. You may write programs that ignore REG FRAME 1. You might have to perform extra loads and stores than you otherwise would have had to perform, though. You must interact with the SYS FRAMEs. The SYS FRAMEs were included in order to make loops take up fewer instructions. You could, for example, use memory, through loads and stores, to keep track of everything you need, but instructions like jumpif will only pay attention to SYS FRAME 1 registers. These constructs are a necessity because we are unable to fit an adequate amount of information into the parameter slots of each 8-bit instruction. We must store some information beforehand.

5. CONTROL FLOW (BRANCHES)

WHAT TYPE OF BRANCHES ARE SUPPORTED

FMAT ISA does not support branches (in the conventional sense) rather it provides a different approach to controlling data flow. We support a **jumpif reg<IMM>**, **compare<IMM>** instruction that takes an immediate register value in order to designate which register address the operation will jump to, and a conditional comparison value that determines whether that jump should occur. In effect, FMAT's single **jumpif** operates as a **bg, bl, beq, ba** combined in a single statement and does so depending on the set comparison value. For instance, if the comparison flag is set to 0, we will be comparing \$CL == \$CR (similar to **beq**); if the comparison flag is set to 1, then we will be comparing \$CL < \$CR (similar to **bl**), etc. If the comparison flag is set to 3, no regard will be taken to the condition and we will be jumping directly to the specified register address (similar to **ba**). (Refer to Section 3 for a more detailed specification). The contents of registers \$CL and \$CR are seeded before the comparison / jump occurs.

HOW ARE TARGET ADDRESSES CALCULATED

Due to the bit constraints of our design, were not able to follow our **jumpif** operation with an immediate address; instead, we compute the target address of the jump by taking the address of \$[3][reg] (Frame 3, Register reg) as specified by the immediate register value, reg.

MAXIMUM BRANCH DISTANCE SUPPORTED

From any point in a program, you can branch to any other point from instruction 0 to instruction 255. Because we must specify the absolute jump address in 8 bits, we are limited to 256 addresses. If we find a need to jump farther in future programs, there are ways we could revise our ISA to allow different types of jumps.

6. ADDRESSING MODES

SUPPORTED MEMORY ADDRESSING MODES

Register Addressing: FMAT ISA supports register addressing for its operations in which the address of a single register is set or "focused" on beforehand. For instance, **focus 0, 1** designates the register to be used for an **incdec** operation. Register addressing is used in particular for instructions that require the movement or setting of a large amount of data (or more so that we can support for FMAT's 2-bit register).

Base (Memory) Addressing: Base addressing is used for FMAT's **load** and **store** instructions which each take in two register values, **rs** and **rt**. Here, the address is computed as address <= \$[rt], where **rt** is the base register.

HOW ARE MEMORY ADDRESSES CALCULATED?

Memory addresses are absolute, so if we load and pass in \$[0][0], we grab the value from \$[0][0], say 134, and access mem[134], which is the 134th Byte in memory.

7-16. QUESTIONS AND ANSWERS

7. How large is the main memory?

256 Bytes: main memory is byte-addressable with 2^8=256 addresses

8. In what ways did you optimize for dynamic instruction count?

The main goal of this ISA is to require as few operations inside a loop as possible. We've gotten loops down to very low line-count amount, which will make up for any setup required before the loop.

9. In what ways did you optimize for the ease of design?

To be honest, ease of design took a backseat on this one. Although we allow instruction names to be up to 6 characters (ease of readability) and we include common instructions found in 32-bit architectures (or at least

mimic them), we had to introduce some complexity in order to work successfully with a tiny 8-bit instruction space that was to still be capable of handling Bytes of data.

10. In what ways did you optimize for short cycle time?

We only include simple instructions. For example, we do *not* include a multiply, divide, or modulus instruction. Probably our slowest instruction (besides memory accesses) will be the jumpif instruction, which has to compare the values of two registers, a \$C flag, and write to the program counter. We only allow the load and the store instructions to access memory; every other instruction may only deal with parameters and register contents.

11. If you did optimize for anything else, what was optimized and how? (optional)

The only optimizations worth noting are the tight loop optimizations.

12. Why is your ISA better than a competitor's ISA (2 explicit operands =>1 source operand, 1 source/destination operand; 4 registers => 2-bit register specific; 16 instr =>4 opcode bits)

Our ISA matches the 2 explicit operands, and goes beyond. Certain instructions that are data-heavy accept one, large, 4-bit operand, while others accept three operands and contain flags. The format depends on the opcode. We offer 8 general purpose registers for our programmers. In total, we offer 16 registers, but of those, 8 are general purpose, 4 are implicit, and 4 are specialized. We offer 23 instructions; the 0000-opcode instruction has been extended to include, in actuality, 8 sub instructions, each of which either need no operands, or merely need a single, 1-bit flag operand.

13. What do you think will be the biggest general purpose weakness in your design?

Much setup is required before any real work can be done. Jump addresses must be seeded ahead of time. Comparative **jumpif #1**, **#2** instructions must have their operands seeded ahead of time. Although this leads to tight loops, it also shows quite obviously in a bulky static instruction count. Another weakness that must be mentioned is that we can only access 256 jump locations and 256 Bytes of main memory, because jump addressing and main memory addressing are both absolute.

14. What would you have done differently if you had 2 more bits for instructions/ 2 fewer bits?

The nice thing about this ISA is that it's ways of handling data can be generalized to even fewer bits. We could run the same system on a 6-bit instruction width, for example. Our ways of handling limited operand space include setting implicit registers ahead of time, and register frame shifting. If we had 2 more bits, not too much would have actually changed. Maybe a few instructions could have benefitted from not having to call upon implicit registers. We also would have had 4x more addressable jump locations and 4x more addressable main memory locations. If we had 4 more bits, everything would have changed. If we had 4 more bits, we would have actually been able to work directly with Bytes right in our instruction operands, so the majority of this ISA would be different; we might not have had a need for frame shifting at all.

15. Can you name/classify your machine in any of the classical ways (i.e stack machine, accumulator, register, load-store)?

Our machine is a load-store architecture.

16. Give an example of assembly language instruction in your machine, translate to machine code.

simple program to add mem[0] and mem[1], and place result in \$[0][0]

```
# we're dealing with REG FRAME 0 here
line01    otype rframe, 0  # $F = 0
line02    focus 1, 0  # $R = &$[1][0]

# seed mem[0] into $CL
line03    otype clear, 0  # $[1][0] = 0
```

```
line04
           load 0, 0
                            \# $[0][0] = mem[0]
# load mem[1] into $CR
line05
           incdec 1, 0, 0
                            # $[1][0]++ (now equals 1)
line06
           load 1, 0
                             # $[0][1] = mem[1]
                            # $[0][0] = $[0][0] + $[0][1]
line07
           add 0, 1
line08
           otype halt
                          # EOP, exit program
# machine code:
line01 0000 1100
line02 1011 0100
line03 0000 0110
line04 1001 0000
line05 0011 1000
line06 1001 0100
line07 0100 0001
```

line08 0000 0010

17. PROGRAM: PRODUCT

```
Example:
252 * 170 * 85 = 3641400
= (11 0111) 1001 0000 0011 1000 = 36920
A * B * C = (AB>>8 * C)<<8 + ((AB<<8)>>8 * C)
ok 11111100 * 10101010 * 01010101
ok 1010011101011000 * 01010101
ok (1010011100000000 + 01011000) * 01010101
ok (10100111 * 100000000 * 01010101) + (01011000 * 01010101)
ok (10100111 * 01010101) << 8 + (01011000 * 01010101)
ok 0011011101110011<<8 + 0001110100111000
(00110111)01110011000000000 + 0001110100111000
Register Assignment:
frame 0 0 0 0 1 1 1 1 reg 0 1 2 3 0 1 2
reg 0 1
_____
      ptr A,B,C ABlo prodlo i
                                     N/A ABhi
var
Math note: doing this calculation with 8-bit registers
A * B * C = (AB>>8 * C)<<8 + ((AB<<8)>>8 * C)
prodhi <= (ABhi * C)</pre>
prodlo <= (ABlo * C)</pre>
Pseudo Code:
AB = 0
for i from 0 to A
      ABlo += B (overflow into ABhi)
for i from 0 to C
      prodhi += ABhi
      prodlo += ABlo (overflow into prodhi)
FMAT Assembly:
      INIT:
             !-- Initialize variables and seed $CL and $CR
line001
            otype rframe, 0 # REG FRAME 0
           otype clear, 0  # $reg0(ptr) = 0
line002
line003
           move 2, 0
                               # $reg2(ABlo) = 0
line003
           move 3, 0
                               # $reg3(prodlo) = 0
line004
           incdec 0, 0, 0
                               \# points = 1
line005
           otype rframe, 1 # REG FRAME 1
          otype clear, 0  # $reg0(i) = 0

seed 1, 0, 0  # Seed $reg0(i) into $CL

move 2, 0  # $reg2(ABhi) = 0
line006
line007
line008
line009
           move 3, 0
                               # $reg3(prodhi) = 0
           otype rframe, 0 # REG FRAME 0
line010
           load 1,0
line011
                              # $reg1(A) <= MEM[ptr=1]</pre>
line012
           incdec 0, 0, 0
                               # ptr++
            seed 0, 1, 1
line013
                               # Seed $reg1(A) into $CR
line014
            load 1,0
                               # $reg1(B) <= MEM[ptr=2]
```

```
line015
             incdec 0, 0, 0
                                  # ptr++
             !-- Set up conditional negation flag
line016
             otype nset, 1
                                  # if the condition is NOT met, break
             !-- Set jump(to) addresses
line017
             focus 3, 0
                                  # $J0 store &LOOP1 (line024)
line018
             upper 1
line019
             lower 8
line020
             focus 3, 1
                                  # $J1 store &END1 (line030)
             upper 1
line021
line022
             lower 14
             !-- Set up overflow target
line023
             focus 1, 2
                                  # focus on ABhi
LOOP1($J0):
line024
             jumpif 1, 2
                                  # jump to $J1(END1) if NOT i < A</pre>
                                  # we can actually do without this, but it's clearer with it
line025
             otype nop
line026
             add
                    2, 1
                                  # ABlo += B (overflow into ABhi)
                                  # ABhi++ if overflow
line027
             otype ovrflw, 0
line028
             jumpif 0, 3
                                  # reloop
                                  # i++ (nop slot)
line029
             incdec 1, 0, 0
END1($J1):
line030
             load 1, 0
                                  # $reg1(C) <= MEM[ptr=3]
line031
             incdec 0, 0, 0
                                  # ptr++
line032
             seed 0, 1, 1
                                  # Seed $reg1(C) into $CR
line033
                                  # REG FRAME 1
             otype rframe, 1
line034
             otype clear, 0
                                  \# \text{ $reg0(i) = 0}
line035
             otype rframe, 0
                                  # REG FRAME 0
             !-- Set jump(to) addresses
line036
             focus 3, 2
                                 # $J2 store &LOOP2 (line042)
line037
             upper 2
line038
             lower 10
             focus 3, 3
line039
                                  # $J3 store &END2 (line052)
line040
             upper 3
line041
             lower 4
L00P2($J2):
                                  # jump to $J3(END2) if NOT i < A</pre>
line042
             jumpif 3, 2
line043
                                  # we can actually do without this, but it's clearer with it
             otype nop
line044
             otype rframe, 1
                                  # REG FRAME 1
line045
             add
                    3, 2
                                  # prodhi += ABhi (overflow into the abyss)
line046
             otype rframe, 0
                                  # REG FRAME 0
line047
             focus 1, 3
                                  # focus on prodhi
                    3, 2
line048
             add
                                  # prodlo += ABlo (overflow into prodhi)
line049
             otype ovrflw, 0
                                  # prodhi++ if overflow
line050
             jumpif 2, 3
                                  # reloop
line051
             incdec 1, 0, 0
                                  # i++ (nop slot)
END2($J3):
line052
             otype rframe, 1
                                  # REG FRAME 1
line053
             focus 1, 0
                                  # ptr = 4
```

```
line054
             lower 4
line055
             upper 0
line056
             store 0, 3
                                  # MEM[ptr=4] <= $reg1(prodhi)</pre>
line057
                                  # REG FRAME 0
             otype rframe, 0
line058
             focus 0, 0
                                  # ptr = 5
line059
             lower 5
line060
             upper 0
line061
                                  # MEM[ptr=5] <= $reg1(prodlo)</pre>
             store 0, 3
line062
             otype halt
                                  # party's over, everyone go home
```

What is the dynamic instruction count of this program if the value in location 1 is 53 and location 2 is 17 and location 3 is 42?

Dynamic Instruction Count for 53 * 17 * 42:

static23 loop6 static12 loop10 static11

<u>Dynamic Instruction Count:</u> 788 = 23 + (53*6 + 2) + 12 + (42*10 + 2) + 11

Static Instruction Count: 62

This count is very dependent on the parameters, and what order the parameters appear in. If we were terribly worried about making this value as small as possible, we would have a preliminary sorter to place the smallest number third, the largest number second, and the remaining number first. For 42 * 53 * 17, the count would be 23 + (42*6 + 2) + 12 + (17*10 + 2) + 11 = 472

18. PROGRAM: STRING MATCH

```
Example:
array: 1111 1010 1111
try to find: 1010
find:
                    0000 1010
loop# arr extract shifted
    # arr extract snitted
1111 1010 0000 1111
1111 0101 0000 1111
1110 1011 0000 1110
1101 0111 0000 1101
1010 1111 0000 1010 MATCH
0101 111X 0000 0101
1011 11XX 0000 1011
0111 1XXX 0000 0111
1111 XXXX 0000 0111
1111 XXXX 0000 1111
1
2
3
4
5
6
7
8
Register Assigments:
______
                                      0
                           0
                    0
                   1
                                 2
                                 i
                                                      length
                                                                   hits
                   pattern byte
______
Pseudo Code:
ptr = 0
$CR = 0000 1010
loop (i = arr.size - 3) {
       $reg0 <= mem[ptr]</pre>
       $CR <= $reg0>>4
       compare $CL and $CR
             matches++ if equal
       ptr++
}
FMAT Assembly:
     INIT:
           otype rframe, 0 # $F= 0
otype clear 0 # $reg0 = 0 (ptr)
            otype rframe, 0
line001
line002
                               # $reg1 = 0 (pattern)
line003
           move 1, 0
           move 2, 0
line004
                                # $reg2 = 0 (byte)
line005
           move 3, 0
                                 # $reg3 = 0 (i)
           otype rframe, 1 # $F=1
line006
line007
           otype clear, 0 # $reg4 = 0 (length)
             mov 1, 0
line008
                             # $reg5 = 0 (hits)
                    !-- Store length of bit stream into $reg4
             focus 1, 0
line009
line010
             upper 3
                                  \# $reg4 = 64 - 3 ....can we just hardcode this ? pls
line011
             lower 13
                    !-- Load pattern string from memory into $CL, located in M[6] (lower 4 bits)
line012
             focus 0, 0
                                 \# points = 6
line013
             lower 6
             load 1, 0
line014
                                 # $reg1 = M[ptr=6]
             focus 1, 0
line015
line016
             upper 0
                                  # $reg1 = 0000 xxxx, get 4 lower bits of M[6]
                    !-- Initialize ptr = M[32], increment onwards
             otype clear 0 # Reset $reg0 (ptr)
line017
```

```
line018
              focus 0, 0
line019
                                   \# points = 32
              upper 2
                     !-- Set jump(to) addresses (LABELS)
line020
              focus 3, 0
                                   # Set $F[0] = &WHILE (line 029)
line021
              upper 1
line022
              lower 13
             focus 3, 1
line023
                                   # Set $F[1] = &END_WHILE (line 43)
line024
              upper 2
line025
              lower 13
                                   # Set $F[1] = &SKIP_IF (line 38)
line026
             focus 3, 2
              upper 2
line027
line028
              lower 6
line029
              seed
                     1, 0, 0# $CL = $reg4
       WHILE:
line030
              jumpif 1, 0
                                   # Break if i =(>) (bit_string_length-3), go to END_WHILE
line031
              seed
                     1, 0, 0# $CL <= $reg1(pattern), nop place
                     !-- Now, get 4 bits from bit string starting from M[ptr]
line032
                                   # $reg2 <= M[ptr], $reg2 now holds first byte of bit_string</pre>
              load
line033
              focus 0, 2
              seed
line034
                     0, 2, 1 # $CR = $reg2
              shift 4, 1
line035
                                   # $reg <= $reg2>>4
                     !-- Compare $CL, $CR, increment num_hits if a match
line036
              otype nset, 1# Negate comparison
line037
              jumpif 2, 0
                                # if $CL (!)= $CR, goto SKIP_IF
                                   # Else, we have a match! num_hit++, nop place
line038
              incdec 1, 1, 0
       SKIP_IF:
                     !-- Increment i, ptr
line039
              otype rframe, 0
                                # $F = 0
              incdec 0, 0, 0 # $reg4(i)i++
line040
line041
              incdec 0, 3, 0 # $reg0(ptr)++
                     !-- Reset i as the left comparison value
line042
              jumpif 0, 3
                                   # Reloop
line043
                     1, 0, 0 # $CL = $reg4, nop place
              seed
       END_WHILE:
line044
              otype rframe, 1
line045
              focus 1, 2
line046
              lower 7
                            # Store $reg5(hits) into M[7]
line047
              store 2, 1
                                   # M[7] <= $reg5(hits)
line048
              halt
                                   # EOP, exit
```

What is the dynamic instruction count of this program. If it varies according to the values, assume 10 of the entries have the value 00011001, 20 entries have the value 10111101, 9 entries have the value 11100111, and the rest have 00000000. Assume the string is 0011.

34 Non-LoopInstructions, 14 Loop Instructions if successful case, 11 Loop Instructions if successful case, ; 19 Match Cases, 44 No-Match Cases; (64 - 3) Total Loop Iterations

<u>Dynamic Instruction Count</u>: 784 = 34 + 19*14 + 44*11

Static Instruction Count: 48

19. PROGRAM: CLOSEST PAIR

```
Register Assignment:
              0
1
                    1
reg 0
                                                    3
var size, iA
                            B, diffmin
Psuedo Code:
       i = 128
       $CL = &i
       $CR = 147
START
       otype nset 1
       goto END if i !< $CR
       nop
       load $regA <= mem[i]</pre>
       i++
       load $regB <= mem[i]</pre>
       otype nset 0
       goto SWAP if $regA > $regB
       goto START
       nop
END
       i = 128
       min = 255
START2
       load $regA <= mem[i]</pre>
       load $regB <= mem[i]</pre>
       $diff <= $regB - $regA</pre>
       otype nset 0
       goto SETMIN if $diff < min</pre>
       nop
       goto START2
       nop
END2
       return min
       halt
SWAP
       store mem[i] <= $regA</pre>
       store mem[i] <= $regB</pre>
       goto START
       nop
SETMIN
       $diff = $regB - $regA
       min = $diff
       goto START2
       nop
FMAT Assembly:
     INIT:
                                # REG FRAME 0
# $reg0 = 0 (i)
# $reg1 = 0 (A)
             otype rframe, 0
line001
line002
            otype clear, 0
line003
            move 1, 0
                                    \# \text{ $reg2 = 0 (B)}
line004
            move 2, 0
line005
            move 3, 0
                                     # $reg3 = 0 (min)
```

```
!-- Seed $CR
line006
             focus 0, 0
                                   # size = 147
line007
             lower 3
line008
             upper 9
line009
              seed 0, 0, 1 \# CR = 147
                     !-- Seed $CL, i = 128
line010
              focus 0, 0
                                  # i = 128
line011
             lower 0
line012
             upper 8
line013
              seed 0, 0, 0# $CL = &i
                     !-- Seed $J0(START), $J1(END), $J2(SWAP)
line014
              focus 3, 0
                                  # $J0(START) line023
line015
             lower 7
line016
             upper
                    1
             focus 3, 0
line017
                                   # $J1(END) line034
             lower 2
line018
line019
             upper 2
line020
             focus 3, 0
                                   # $J2(SWAP) line065
             lower 1
line021
             upper 4
line022
START($J0):
line023
             otype nset, 1
line024
             jumpif 1, 2
                                   # goto END if $CL !< $CR
line025
             otype nop
                                   # $reg1(A) <= mem[i]
line026
             load
                     1, 0
             incdec 0, 0, 0# i++
line027
line028
             load
                     2, 0
                                   # $reg2(B) <= mem[i]
line029
             otype nset, 0
             jumpif 2, 1
                                   # goto SWAP if $CL > $CR
line030
             otype nop
line031
line032
             jumpif 0, 3
                                   # goto START
line033
             otype nop
END($J1):
line034
             focus 0, 0
                                   # i = 128
line035
             lower 0
             upper 8
line036
             focus 0, 3
line037
                                   # min = 255
             lower 15
line038
line039
             upper 15
                     !-- Seed $J0(START2), $J1(END2), $J2(SETMIN)
line040
              focus 3, 0
                                  # $J0(START2) line049
line041
             lower
                    1
line042
             upper 3
line043
             focus 3, 0
                                   # $J1(END2) line060
line044
             lower 12
             upper 3
line045
line046
              focus 3, 0
                                   # $J2(SETMIN) line071
              lower 7
line047
line048
              upper 4
START2($J0):
line049
             load
                                   # load $regA <= mem[i]</pre>
                     1, 0
line050
             indec 0, 0, 0# i++
                                   # load $regB <= mem[i]</pre>
line051
             load
                     2, 0
line052
              sub
                     2, 1
                                   # $diff <= $regB - $regA, $reg2 = diff
line053
              otype nset, 0
line054
              seed
                     0, 2, 0 # $CL = diff
```

```
0, 3, 1 # $CR = min
line055
              seed
line056
              jumpif 2, 1
                                   # goto $J2(SETMIN) if $diff < min
              otype nop
line057
line058
              jumpif 0, 3
                                   # goto $J0(START2)
line059
             otype nop
END2($J1):
                                    # i = 127
line060
             focus 0, 0
line061
              lower 15
line062
              upper
line063
              store 0, 3
                                    # M[127] <= min
line064
                                    # Exit
              otype halt
SWAP($J2):
line065
             store 0, 1
                                    # store mem[i] <= $regA</pre>
line066
             incdec 0, 2, 1# i--
line067
             store 0, 2
                                    # store mem[i] <= $regB</pre>
line068
             incdec 0, 0, 0# i++
line069
            jumpif 0, 3
                                    # goto START
line070
             otype nop
SETMIN:
                     2, 1
line071
              sub
                                   # $diff = $regB - $regA
line072
              move
                     3, 2
                                    # min <= $diff
line073
              jumpif 0, 3
                                    # goto START2
line074
              otype nop
```

What is the dynamic instruction count of this program? Assume the array contains the sequence: 34, -12, 18, 61, 0, 100, 49, -51, -22, 3, 41, 88, -100,14, 39, 10, 90, -90, -80, 75. (The correct answer should be 2)

Static Instruction Count: 74

Dynamic Instruction Count: 1006

static22 loop11 static15 loop11 static5, swap6, setmin4

```
22 + (11*19 + 2) + 15 + (11*19 + 2) + 5 + 6*(89swaps) + 4*(2setmins) = 1006
0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000 \ 0000
                                 3 41 88 -100 14 39 10 90 -90 -80
-12 18 61 0 100 49 -51 -22
-12
     18
          Θ
             61 100
                     49 -51 -22
                                  3
                                     41
                                          88 -100
                                                 14
                                                     39
                                                         10
                                                              90 -90 -80
                                                                          75
-12 18
          Θ
             61
                49 100 -51 -22
                                  3
                                     41
                                          88 -100
                                                 14
                                                     39
                                                         10
                                                              90 -90 -80
                                                                          75
                                                      39
-12 18
          0
             61
                 49 -51 100 -22
                                  3
                                     41
                                          88 -100
                                                 14
                                                         10
                                                              90 -90 -80
                                                                          75
                 49 -51 -22 100
                                  3
-12 18
          0
                                     41
                                          88 -100
                                                  14
                                                      39
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                                                              90
                                                                 -90
                                                                     -80
             61 49 -51 -22
                            3 100
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                                          88 -100
                                                                 -90 -80
-12
     18
          0
                 49 -51 -22
                                 41 100
                                          88 -100
                                                      39
                                                         10
                                                              90
                                                                 -90 -80
             61
                              3
                                                 14
                                                                          75
          0 61 49 -51 -22 3 41 88 100 -100
-12 18
                                                              90 -90 -80
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                                                     39
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                                                                          75
-12 18
                                     88 -100 100
          0
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                              3 41
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                                                              90 -90 -80
                                                                          75
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                              3 41 88 -100
          0
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                 49 -51 -22
          0
-12 18
             61
                              3 41
                                     88 -100
                                             14
                                                 39 100
                                                         10
                                                              90 -90 -80
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                                 41
                                     88 -100
                                             14
                                                 39
                                                     10 100
                                                              90
                                                                 -90 -80
                                                                          75
             61 49 -51 -22 3
-12 18
                                 41
                                     88 -100
                                                         90 100
                                                                 -90 -80
-12
          0
                 49 -51 -22
                              3
                                     88 -100
                                                      10
                                                          90
                                                             -90
          0 61 49 -51 -22
                                     88 -100
                                                          90 -90
-12 18
                              3 41
                                             14
                                                                 -80 100
                                                 39
                                                     10
-12
     18
          0
                 49 -51 -22
                              3
                                 41
                                     88 -100
                                                 39
                                                          90 -90
                                                                         100
             61
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                                                                 -80
                                                                      75
-12 18
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                                                          90 -90 -80
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          0 49 -51 61 -22
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                                                          90 -90
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                                                          90
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                                 61 -100 88
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                                                                         100
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-12
     18
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                                         14
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                                                                      75
                                                                         100
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                                         14
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                                                      88 -90 -80
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                                                                  75
                                                                         100
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                                             39
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                                                            -80
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                                                  10
                                                      88
          0 -51 -22 3 49 41
                                 61 -100
                                                      88 -90 -80
-12 18
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0 -51 -22 3 41 49 -100 61
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                                                      88 -90
                                                            -80
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-12 18
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                                                                      90 100
-12
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3 41 49 -100
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                                                                  75
                                                                      90 100
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                                     14
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                                                      88 -90 -80
                                                                  75
                                                                      90
                                                                        100
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                                             10 61
                                                                 75
                                                                      90 100
```

```
-12
     18
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                      3 41 49 -100
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                                               10
                                                    61 -90 88 -80
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-12
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                       3 41
                               49 -100
                                            39
                                                     61 -90 -80
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                                                                  88
                                                                      75
                                                                              100
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          0 -51 -22
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                                                     61 -90 -80
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-10, 2: total of 2 guesses, the second guess was correct