

CSE12 - Lecture 20 - B00

Wednesday, November 9, 2022 9:00 AM

PA7 released today

PA6 hard deadline → tonight 6pm

PA7 late / resubmit → Tuesday

Friday - holiday → no class

Exam 2 → Friday of Week 8 → 11/18

↳ counting, steps, run-time, sorting, hash tables

Max Heap → largest values comes out first

Assume the key and value are identical for this example

Draw the picture of the tree and the array for the following:

ArrayList<Integer> heap = new ArrayList<>(2); //initial capacity of 2

Add the following elements to the max heap (in this order):

5, 10, 15, 20, 25, 30, 35, 40

Call poll() twice

What elements were returned?

add(5)

5

add(10)

5	10
10	5

add(15)

10	5	15
15	5	10

add(20)

10	5	15	20
20	15	10	5

add(25)

20	15	10	5	25
25	20	10	5	15

add(30)

25	20	10	5	15	30
30	20	25	5	15	10

add(35)

30	20	25	5	15	10	35
35	20	30	5	15	10	25

add(40)

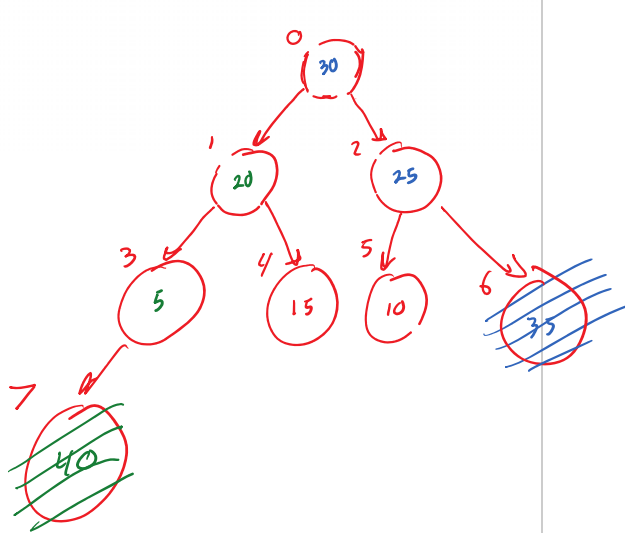
35	20	30	5	15	10	25	40
40	35	30	20	15	10	25	5

poll()

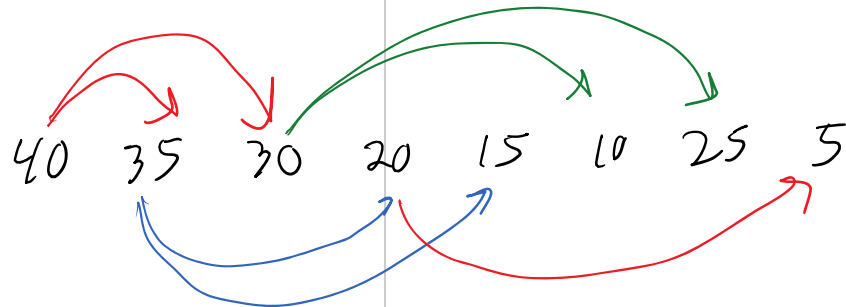
35	20	30	5	15	10	25
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poll()

30	20	25	5	15	10
----	----	----	---	----	----



height
↳ $\log_2(n)$



```

void bubbleDown(int index) {
    if(index >= this.entries.size()) { return; }
    int leftIndex = left(index);
    if(leftIndex >= this.entries.size()) { return; }
    int largerChildIndex = leftIndex;
    int rightIndex = right(index);
    if(existsAndGreater(rightIndex, leftIndex)) {
        largerChildIndex = rightIndex;
    }
    if(existsAndGreater(largerChildIndex, index)) {
        swap(index, largerChildIndex);
        bubbleDown(largerChildIndex);
    }
}

void bubbleUp(int index) {
    if(index <= 0) { return; }
    Entry<K,V> e = this.entries.get(index);
    Entry<K,V> parent = this.entries.get(parent(index));
    int comp = this.comparator.compare(e.key, parent.key);
    if(comp > 0) {
        swap(index, parent(index));
        bubbleUp(parent(index));
    }
    else {
        return;
    }
}

```

What is the run-time for a Max Heap

add()

Worst Case $\Theta(\log_2(n))$

What conditions make up the worst case for add()?

sorted for max heap

Best Case: $\Theta(1)$

What conditions make up the best case for add()?

added key already
in heap order

max heap \rightarrow reverse sorted list
min heap \rightarrow sorted

poll()

Worst Case $\Theta(\log_2(n))$

What conditions make up the worst case for poll()?

smallest k was last added

Best Case: $\Theta(1)$

What conditions make up the best case for poll()?

duplicate k 's