Homework 10

Jing Leng (GSI: Jiahe)
December 12, 2014

 $\mathbf{2}$

```
library(scatterplot3d)
mix <- read.table("mixgauss.dat")</pre>
c1 \leftarrow c(-2, -2, -4) # observed centers
c2 \leftarrow c(-4, -2, 2)
c3 \leftarrow c(4, 6, 2)
centroids <- rbind(c1, c2, c3)</pre>
classify <- function(x) {</pre>
  dis <- apply(centroids, 1, function(y) sqrt(sum((x - y)^2)));</pre>
  which(dis == min(dis))
}
label <- apply(mix, 1, classify )</pre>
label_old <- rep(1, 300)
obj = c()
while (1) {
  label <- apply(mix, 1, classify)</pre>
  if (sum(label != label_old) == 0) break
  centroids[1,] <- apply(mix[label==1,], 2, mean)</pre>
  centroids[2,] <- apply(mix[label==2,], 2, mean)</pre>
  centroids[3,] <- apply(mix[label==3,], 2, mean)</pre>
  label_old <- label</pre>
  obj = c(obj, sum(sapply(1:3,
                             function(i) sum(apply(mix[label == i, ], 1,
                                                      function(y) sqrt(sum((centroids[i,] - y)^2))))))
}
centroids \leftarrow rbind(rep(0, 3), rep(1, 3), rep(2, 3))
label <- apply(mix, 1, classify )</pre>
label_old <- rep(1, 300)
obj = c()
while (1) {
  label <- apply(mix, 1, classify)</pre>
  if (sum(label != label_old) == 0) break
  centroids[1,] <- apply(mix[label==1,], 2, mean)</pre>
  centroids[2,] <- apply(mix[label==2,], 2, mean)</pre>
  centroids[3,] <- apply(mix[label==3,], 2, mean)</pre>
  label_old <- label</pre>
  obj = c(obj, sum(sapply(1:3,
                             function(i) sum(apply(mix[label == i, ], 1,
                                                      function(y) sqrt(sum((centroids[i,] - y)^2))))))
```

```
plot(obj, type = 'l')
```

```
1.0 1.5 2.0 2.5 3.0 3.5 4.0 Index
```

```
centroids <- rbind(rep(0,3), rep(1, 3), rep(2, 3))

pi <- rep(1/3, 3)
mu <- centroids
Sig <- array(rep(diag(3), 3), c(3, 3, 3))

library(MASS)
library(mvtnorm)</pre>
```

Warning: package 'mvtnorm' was built under R version 3.1.2

```
tao = matrix(0, 300, 3)
for (l in 1: 30) { # converge criterion to be added, for now just using number of iteration, works well
  for (n in 1:300) {
    fenmu <- sum(sapply(1:3, function(k) pi[k]*dmvnorm(as.numeric(mix[n,]), as.numeric(mu[k,]), Sig[,,k])
    for (k in 1:3)
        tao[n,k] = pi[k]*dmvnorm(mix[n,], mu[k,], Sig[,,k])/fenmu
}

for (k in 1:3) {
    fenmu = sum(tao[,k])
    mu[k,] = rowSums(sapply(1:300, function(i) tao[i, k] * as.numeric(mix[i,]))) / fenmu
    Sig[,,k] = rowSums(sapply(1:300, function(i) tao[i,k] * as.numeric(mix[i,] - mu[k,]) %*% t(as.numeric[k]) = 1/300*fenmu
}
}</pre>
```

```
centroids <- mu
label <- apply(mix, 1, classify )
scatterplot3d(mix[,1:3], color = label + 1, pch = ifelse(label < 3, label -1, label + 2))</pre>
```

