Homework 8

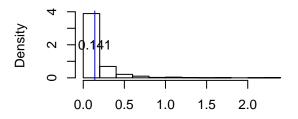
Jing Leng (GSI: Jiahe) November 17, 2014

1

n = 20; mu = 0;

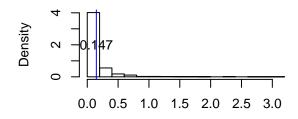
```
kseq = c(1,3,5,7)
nMC = 1000 #Monte Carlo sample size, i.e. number of trimmed means;
tmean = matrix(0, nMC, length(kseq))
\# each\ column\ corresponds\ to\ a\ k,\ with\ 1000\ Monte-Carlo\ trimmed\ means.
for (k in 1:length(kseq)){
 for (i in 1:nMC){
    sym = rcauchy(n)
    OStat = sort(sym)
    tmean[i,k] = median(OStat[((kseq[k]+1):(n-kseq[k]))])
 }
}
MSE_MC = apply(tmean, 2, function(v) mean((v - mu)^2))
MSE_MC
## [1] 0.1407 0.1474 0.1398 0.1374
squerr_MC = (tmean - mu)^2
par(mfrow = c(2,2))
for (k in 1:length(kseq)){
 hist(squerr_MC[,k], prob = TRUE, main = paste('MC squarred errors for k=',kseq[k]),xlab ="MC estimate
  abline(v = MSE_MC[k], col = 'blue')
  text(MSE_MC[k], 2, labels = round(MSE_MC[k],3))
}
```

MC squarred errors for k= 1



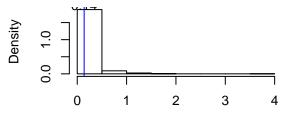
MC estimated squared errors

MC squarred errors for k= 3



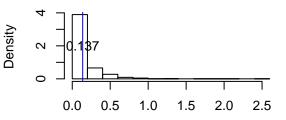
MC estimated squared errors

MC squarred errors for k= 5



MC estimated squared errors

MC squarred errors for k= 7



MC estimated squared errors

```
X = rcauchy(n)
B = 200
Vec = matrix(0, B, length(kseq))
OneSym = rcauchy(n)
TrueMu = median(OneSym)
for (k in 1:length(kseq)){
  for (i in 1:B){
    bsample = sample(OneSym, n, replace = TRUE)
    OStat = sort(bsample)
    Vec[i,k] = median(OStat[((kseq[k]+1):(n-kseq[k]))])
  }
}
MSE_Bt = sapply(1:length(kseq), function(k) mean((Vec[,k] - TrueMu)^2))
MSE_Bt
```

```
## [1] 0.1419 0.1565 0.1657 0.1541
```

```
squerr_Bt = sapply(1:length(kseq), function(k) (Vec[,k] - TrueMu)^2)

par(mfrow = c(2,2))
for (k in 1:length(kseq)){
   hist(squerr_Bt[,k], prob = TRUE, main = paste('Bootstrap squarred errors for k=',kseq[k]),xlab ="Boot abline(v = MSE_Bt[k], col = 'blue')
   text(MSE_Bt[k], 2, labels = round(MSE_Bt[k],3))
}
```

Bootstrap squarred errors for k= 1

0.142

0.5

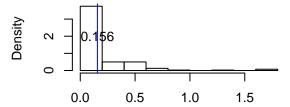
0.0

Bootstrap estimated squared errors

1.0

1.5

Bootstrap squarred errors for k= 3



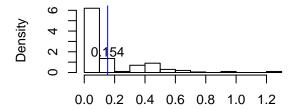
Bootstrap estimated squared errors

Bootstrap squarred errors for k= 5

0.166

Bootstrap estimated squared errors

Bootstrap squarred errors for k= 7



Bootstrap estimated squared errors

 $\mathbf{2}$

estimate for mu is: $\hat{\mu} = \frac{\sum_{k} \ln x_k}{n}$

```
n = 20; mu = 0;
kseq = c(1,3,5,7)
nMC = 1000 #Monte Carlo sample size, i.e. number of trimmed means;
tmean = matrix(0, nMC, length(kseq))
#each column corresponds to a k, with 1000 Monte-Carlo trimmed means.
for (k in 1:length(kseq)){
   for (i in 1:nMC){
      sym = rlnorm(n)
      OStat = sort(sym)
      tmean[i,k] = mean(log(OStat[((kseq[k]+1):(n-kseq[k]))]))
   }
}
MSE_MC = apply(tmean, 2, function(v) mean((v - mu)^2))
MSE_MC
```

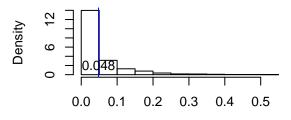
[1] 0.04824 0.05693 0.06079 0.07257

```
squerr_MC = (tmean - mu)^2

par(mfrow = c(2,2))
for (k in 1:length(kseq)){
  hist(squerr_MC[,k], prob = TRUE, main = paste('MC squarred errors for k=',kseq[k]),xlab ="MC estimate"
```

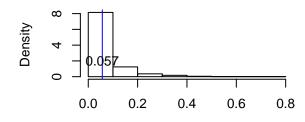
```
abline(v = MSE_MC[k], col = 'blue')
  text(MSE_MC[k], 2, labels = round(MSE_MC[k],3))
}
```

MC squarred errors for k= 1



MC estimated squared errors

MC squarred errors for k= 3



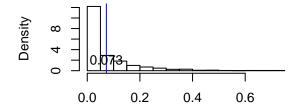
MC estimated squared errors

MC squarred errors for k= 5

Density 0.1 0.2 0.3 0.4 0.5 0.6

MC estimated squared errors

MC squarred errors for k= 7



MC estimated squared errors

```
B = 200
Vec = matrix(0, B, length(kseq))
OneSym = rlnorm(n)
TrueMu = mean(log(OneSym))
for (k in 1:length(kseq)){
  for (i in 1:B){
    bsample = sample(OneSym, n, replace = TRUE)
    OStat = sort(bsample)
    Vec[i,k] = mean(log(OStat[((kseq[k]+1):(n-kseq[k]))]))
  }
}
MSE_Bt = sapply(1:length(kseq), function(k) mean((Vec[,k] - TrueMu)^2))
MSE_Bt
```

[1] 0.07659 0.07700 0.08517 0.09830

```
squerr_Bt = sapply(1:length(kseq), function(k) (Vec[,k] - TrueMu)^2)
par(mfrow = c(2,2))
for (k in 1:length(kseq)){
 hist(squerr_Bt[,k], prob = TRUE, main = paste('Bootstrap squarred errors for k=',kseq[k]),xlab ="Boot
 abline(v = MSE_Bt[k], col = 'blue')
```

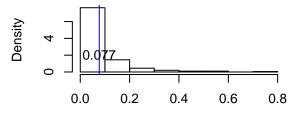
```
text(MSE_Bt[k], 2, labels = round(MSE_Bt[k],3))
}
```

Bootstrap squarred errors for k= 1

0.0 0.1 0.2 0.3 0.4 0.5

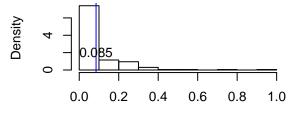
Bootstrap estimated squared errors

Bootstrap squarred errors for k= 3



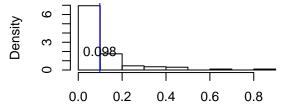
Bootstrap estimated squared errors

Bootstrap squarred errors for k= 5



Bootstrap estimated squared errors

Bootstrap squarred errors for k= 7



Bootstrap estimated squared errors