Recommendation Systems

Data Science Immersive



By the end of the lesson students will be able to

- Explain the advantages/disadvantages of each type of recommendation system
- Implement code to calculate similarity metrics and determine predicted ratings in a collaborative filtering context
- Explain latent factor recommendation models and how they are created

Outline

- Why Recommendation Systems?
- Content-Based
- Collaborative Filtering
 - Memory-based techniques (Neighborhood Based)
 - Similarity Metrics
 - Making Recommendations
 - Model-Based techniques
- Evaluating Recommendation Engines
- Issues with Recommendation Engines

Why Recommendation Systems??





Why Recommendation Systems??



Benoit Mandelbrot: "Father of the Long Tail"

Types of Recommendation Engines

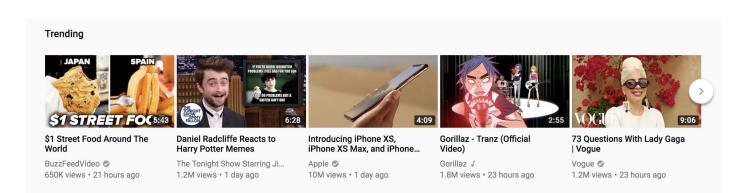
Non-personalized

- Suggest the most popular items to users
- Make the same suggestion to users regardless of characteristics
- Content-Based
 - Recommend based on the properties of the items
 - Other user behavior is not considered

- Collaborative Filtering
 - Make use of user data to make recommendations
 - User User
 - Item Item
 - Memory Based
 - Model Based

Non-Personalized Recommendation Engines

- Non-personalized
 - Suggest the most popular items to users
 - Top 10, Top 5% etc...
 - Make the same suggestion to users regardless of characteristics



Non-Personalized Recommendation Summary

Advantages

- Super Easy (computationally and for the user to understand)
- Items are usually popular for a reason

Disadvantages

- Not personalized
- New items won't gain traction

Types of Recommendation Engines

Non-personalized

- Suggest the most popular items to users
- Make the same suggestion to users regardless of characteristics

Content-Based

- Recommend based on the properties of the items
- Other user behavior is not considered

- Collaborative Filtering
 - Make use of user data to make recommendations
 - User User
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 - Memory Based
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Types of Recommendation Engines

Content-Based

- Recommend based on the properties of items
- User Profile and Item Profile
- Every item has the same set of attributes
- User profile is based off of an average of the item profiles that they've rated positively
- Similarity metrics are frequently based off of cosine similarity (angle)
- Often used when recommending similar articles (take the cosine similarity of TF-IDF vectors for each article)

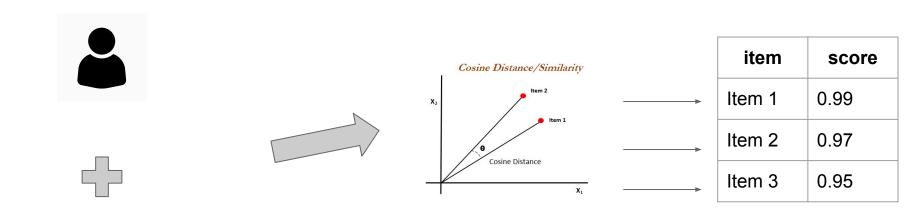
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Content-Based Recommendation

	Items							
		Α	В	С	D			
Features	Genre	2	3	5	1			
	Actor	5	4	2	1			
	Director	1	1	1	3			
	Year	3	4	5	2			
	IMDB Ratings	5	4	1	2			

Content-Based Recommendation Engines



Genre	Actor	Director	Year	IMDB rating

Content-Based Recommendation Summary

Advantages:

- More transparent
- No cold start issue (new items can be recommended immediately)
- Easy to do!
- Recommend items to user with unique tastes

Disadvantages:

- Requires some type of tagging of items
- Overspecialization to certain types of items

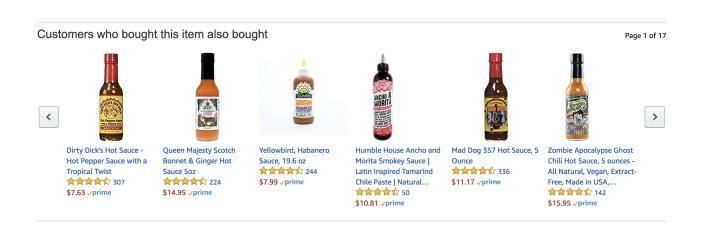
Types of Recommendation Engines

- Non-personalized
 - Suggest the most popular items to users
 - Make the same suggestion to users regardless of characteristics
- Content-Based
 - Recommend based on the properties of the items
 - Other user behavior is not considered

- Collaborative Filtering
 - Make use of user data to make recommendations
 - User User
 - Item Item
 - Memory Based (Neighborhood Techniques)
 - Model Based

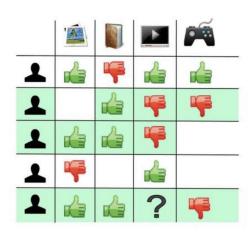
Types of Recommendation Engines

- Collaborative Filtering
 - Make use of other user data to make recommendations
 - User User
 - Item Item



Utility Matrix: A matrix that contains users' ratings of different items

	King Kong	LOTR	Matrix	National Treasure
Alice	1		0.2	
Bob		0.5		0.3
Carol	0.2		1	
David				0.4



Our goal is to make predictions about all of the blank values and then return the new items that have the highest predicted rating

User 2 BLANK 5 BLANK 3 User 3 BLANK BLANK 1 BLANK User 4 2 3 BLANK BLANK User 5 BLANK BLANK 1 BLANK User 6 4 BLANK 5 BLANK		Movie 1	Movie 2	Movie	Movie N			Movie 1	Movie 2	Movie	Movie N
User 3 BLANK BLANK 1 BLANK User 4 2 3 BLANK BLANK User 5 BLANK BLANK 1 BLANK User 6 4 BLANK 5 BLANK	User 1	1	BLANK	BLANK	3		User 1	1	4	2	3
User 4 2 3 BLANK BLANK User 5 BLANK 1 BLANK User 6 4 BLANK 5 BLANK	User 2	BLANK	5	BLANK	3		User 2	1	5	3	3
User 5 BLANK BLANK 1 BLANK User 5 2.5 2.8 1 User 6 4 BLANK 5 BLANK 1 User 6 4 1.2 5	User 3	BLANK	BLANK	1	BLANK		User 3	2.5	2.8	1	3.5
User 6 4 BLANK 5 BLANK 1 User 6 4 1.2 5	User 4	2	3	BLANK	BLANK		User 4	2	3	2	3.5
4 DEATH 3 DEATH	User 5	BLANK	BLANK	1	BLANK	ALS	User 5	2.5	2.8	1	3.1
User 7 BLANK 4 BLANK BLANK User 7 1 4 2.	User 6	4	BLANK	5	BLANK		User 6	4	1.2	5	1.4
	User 7	BLANK	4	BLANK	BLANK		User 7	1	4	2.5	3
User BLANK 3 BLANK BLANK User 2 3 2	User	BLANK	3	BLANK	BLANK		User	2	3	2	3
User m BLANK BLANK BLANK 4 User m 1 4 2	User m	BLANK	BLANK	BLANK	4		User m	1	4	2	4

	ltems							
		sw	HP	LTR	Avengers			
	Cersei	2	?	5	1			
	Daenerys	5	4	?	1			
Users	Joffrey	?	1	1	3			
	Jon	3	?	5	2			
	Tyrion	?	4	?	2			

Explicit Ratings

Typically matrices will be extremely sparse!

	ltems							
		sw	HP	LTR	Avengers			
Users	Cersei	1	0	1	1			
	Daenerys	1	1	0	1			
	Joffrey	0	1	1	1			
	Jon	1	0	1	1			
	Tyrion	1	1	0	1			

Implicit Ratings

If we don't have numerical ratings, we can make assumptions based on users' behavior.

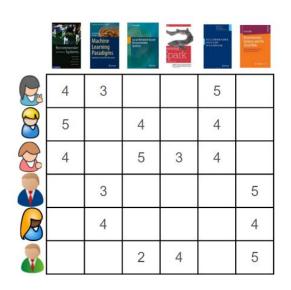
What are some examples?

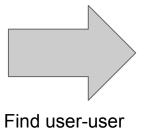
User-User Similarity

	Items							
		sw	HP	LTR	Avengers			
Users	Cersei	2	?	5	1			
	Daenerys	5	4	?	1			
	Joffrey	?	1	1	3			
	Jon	3	?	5	2			
	Tyrion	?	4	?	2			

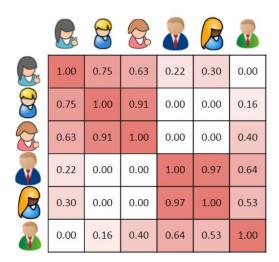
- 1. Choose similarity metric
- 2. Compare similarity of one user to other users
- 3. Take a weighted average of N similiar users' rating of the movies

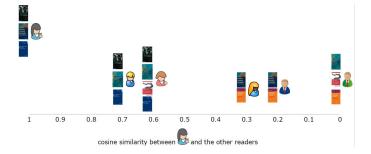
Collaborative Filtering (User-User)



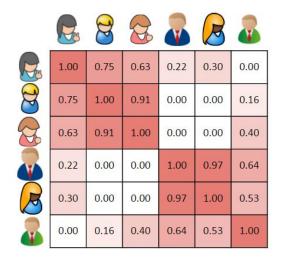


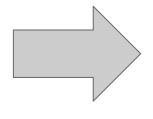
Find user-user similarity

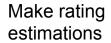


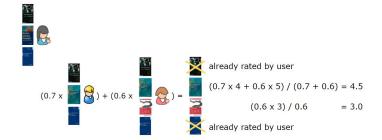


Collaborative Filtering (User-User)







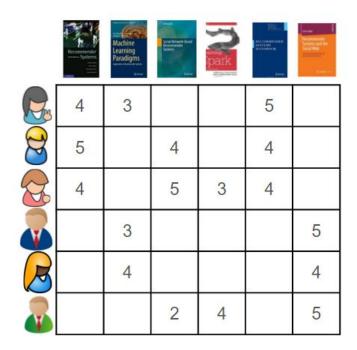


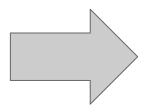
Item-Item Similarity

	ltems						
		sw			HP	LTR	Avengers
	Cersei		2		?	5	1
	Daenerys		5		4	?	1
Users	Joffrey		?		1	1	3
	Jon		3		?	5	2
	Tyrion		?		4	?	2

- 1. Choose similarity metric
- 2. Compare similarity of items to the item that you are trying to determine the rating of
- 3. Multiply the similarity of each item by the rating of other items a given user has rated

Collaborative Filtering (Item-Item)





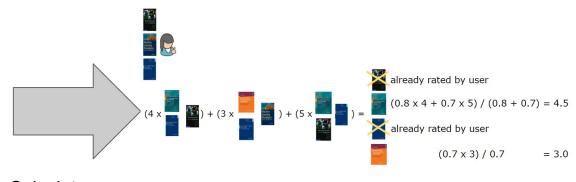
Find item-item similarity



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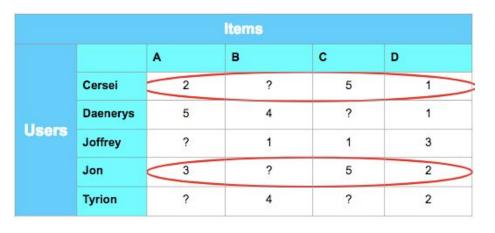
Collaborative Filtering (Item-Item)

		Machine Learning Paradigms	Com-	Spark	SOCIONAMO PERM WHITE SHO HE COMMON IN	Section 1 to 1
Reconstruction and the second	1.00	0.27	0.79	0.32	0.98	0.00
Machine Learning Paradigms	0.27	1.00	0.00	0.00	0.34	0.65
	0.79	0.00	1.00	0.69	0.71	0.18
Spark	0.32	0.00	0.69	1.00	0.32	0.49
The state of the s	0.98	0.34	0.71	0.32	1.00	0.00
Transport of the Control of the Cont	0.00	0.65	0.18	0.49	0.00	1.00



Calculate Predicted Utility for each person

User-User or Item-Item?



			Items		
		A	В	С	D
	Cersei	2	?	5	1
	Daenerys	5	4	?	1
Users	Joffrey	?	1	1	3
	Jon	3	?	5	2
	Tyrion	?	4	?	2

Which one do you think will perform better?

User-User or Item-Item, which wins??

- Item-Item or User-User Collaborative Filtering????
 - In general, item-item has proven to be more effective than user-user
 - Users have unique tastes that are difficult to predict
- Depends on whether you have a higher number of items or users

Given *m* : users, *n* : items

Time Complexity

```
User-user ≈ O(m^2n)
Item-Item ≈ O(mn^2)
```

Time make a recommendation!

	ltems						
		sw	НР	LTR	Avengers		
	Cersei	2	?	5	1		
	Daenerys	5	4	?	1		
Users	Joffrey	?	1	1	3		
	Jon	3	?	5	2		
	Tyrion	?	4	?	2		

Let's calculate how much Jon will like HP with user-user and item-item collaborative filtering. Assume a neighborhood of N = 2



$$r_{xi} = \frac{\sum_{y \in N} s_{xy} r_{yi}}{\sum_{y \in N} s_{xy}}$$

$$s_{xy} = sim(x, y)$$

Memory Based Collaborative Filtering

Also known as **neighborhood-based**:

These are models that are based off of how similar users/items are for items that have already been rated

We want users with more similar tastes to have higher similarity than those with different tastes. We have multiple ways of achieving this:

- 1) Jaccard Similarity
- 2) Euclidean Distance
- 3) Cosine Similarity
- 4) Pearson Correlation

- Jaccard Index
 - Typically used for implicit data
 - The intersection of items rated by users divided by the union of items rated by both users
 - Ignores rating values!

$$sim(A, B) = \frac{|r_A \cap r_B|}{|r_A \cup r_B|}$$

- Euclidean Distance
 - A simple measure of distance between the vectors

$$r_2(\mathbf{x}_1,\mathbf{x}_2) = \sqrt{(x_{11}-x_{21})^2 + (x_{12}-x_{22})^2 + \dots + (x_{1d}-x_{2d})^2} = \sqrt{\sum_{j=1}^d (x_{1j}-x_{2j})^2}$$

Manhattan Distance

$$r_1(\mathbf{x}_1,\mathbf{x}_2) = |x_{11}-x_{21}| + |x_{12}-x_{22}| + \dots + |x_{1d}-x_{2d}| = \sum_{j=1}^d |x_{1j}-x_{2j}|.$$

To make this measurement more useful, we can normalize this measurement between 0 and 1.

$$sim(\mathbf{x}, \mathbf{y}) = \frac{1}{1 + r_2(\mathbf{x}, \mathbf{y})}.$$

- Cosine Similarity
 - We assume that the unrated values are 0
 - Scale between [-1,1]
 - Issue: It treats the missing ratings as if the person has rated them poorly
 - This can lead to misleading information for someone who has not rated many movies

$$sim(A, B) = \frac{r_A \cdot r_B}{\|r_A\| \|r_B\|}$$

- Adjusted Cosine Similarity
 - Insensitive to the magnitude of users' ratings and trends of users
 - For example, if one critic rated everything as 5 and another rated everything as 1
 - Positive Ratings mean that a user liked an item more than average, negative ratings means they liked a movie less than average

$$AC(i,j) = \frac{\sum_{U \in u_{ij}} (r_{ui} - \bar{r}_u)(r_{uj} - \bar{r}_u)}{\sqrt{\sum_{U \in u_{ij}} (r_{ui} - \bar{r}_u)^2 \sum_{U \in u_{ij}} (r_{uj} - \bar{r}_u)^2}}$$

- Pearson Correlation/
 - Find the correlation between users' ratings
 - Scaled from -1 to +1
 - Only includes set I of items that both users have rated

$$PCC_{-}Sim(u,v) = \frac{\sum_{i \in I} (r_{u,i} - \overline{r}_{u,I})(r_{v,i} - \overline{r}_{v,I})}{\sqrt{\sum_{i \in I} (r_{u,i} - \overline{r}_{u,I})^{2} + \sum_{i \in I} (r_{v,i} - \overline{r}_{v,I})^{2}}}$$

Where $\overline{r}_{u,I}$ and $\overline{r}_{v,I}$ represents Average rating of user u and user v, respectively, for co-rated items represented by set I

Which metric is best???

It Depends



although pearson correlation has been demonstrated experimentally to be the best

User-User Similarity Recommendation

Items								
		sw	HP	LOTR	Avengers			
Users	Cersei	2	?	5	1			
	Daenerys	5	4	?	1			
	Joffrey	?	1	1	3 _			
	Jon	3	?	5	2			
	Tyrion	?	4	?	2			

Avg rating for each user

2.66
3.33
1.66
3.33 **3**

Find Similarity (Using adjusted cosine similarity)

First we are going to mean normalize to account for individuals' average rating

User-User Similarity Rec. Part 2

ltems									
		sw	HP	LOTR	Avengers				
	Cersei	-0.66	0	2.33	-1.66				
	Daenerys	1.66	0.66	0	-2.33				
Users	Joffrey	0	-0.66	-0.66	1.33				
	Jon	-0.33	?	1.66	-1.33				
	Tyrion	0	1	0	-1				

How similar Jon is to other users (using cosine similarity)

0.995	
0.414	
-0.896	
1	
0.6178	

Compare similarity of one user to other users using adjusted cosine similarity

$$r = \frac{\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^{n} (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^{n} (Y_i - \bar{Y})^2}}$$

User-User Similarity Rec. Part 3

Take a weighted average of the users' rating of the movies

	Items						
		sw	HP				
	Cersei	2	?				
11	Daenerys	5	4				
Users	Joffrey	?	1				
	Jon	3	?				
	Tyrion	?	4				

 \mathbf{r}

0.995	
0.414	
-0.896	
1	
0.6178	

$$r_{xi} = \frac{\sum_{y \in N} s_{xy} r_{yi}}{\sum_{y \in N} s_{xy}}$$

Local v. Global Effects (Advanced)

Local "Naive" Approach

$$r_{xi} = \frac{\sum_{j \in N(i;x)} S_{ij} \cdot r_{xj}}{\sum_{j \in N(i;x)} S_{ij}}$$

s_{ij}... similarity of items *i* and *j*r_{xj}...rating of user *x* on item *j*N(i;x)... set items rated by *x* similar to *i*

$$r_{xi} = b_{xi} + \frac{\sum_{j \in N(i;x)} S_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i;x)} S_{ij}}$$

$$\mathbf{baseline \ estimate \ for \ } r_{xi}$$

$$\mathbf{b}_{xi} = \mu + \mathbf{b}_{x} + \mathbf{b}_{i}$$

$$\mathbf{b}_{x} = \text{rating deviation of user } x$$

$$= (avg. \ rating \ of \ user \ x) - \mu$$

$$\mathbf{b}_{i} = \text{rating deviation of movie } i$$

Collaborative Filtering (Memory Based) Summary

Advantages:

Personalized. You're special!

Disadvantages:

- Can require a lot of computation (most often the computation is done offline and the points are calculated easily)
- Cold start: need to have a lot of ratings to be worthwhile
- Popularity Bias: biased towards items that are popular. May not capture people's unique tastes.

Model Based Collaborative Filtering



Types of Recommendation Engines

Non-personalized

- Suggest the most popular items to users
- Make the same suggestion to users regardless of characteristics

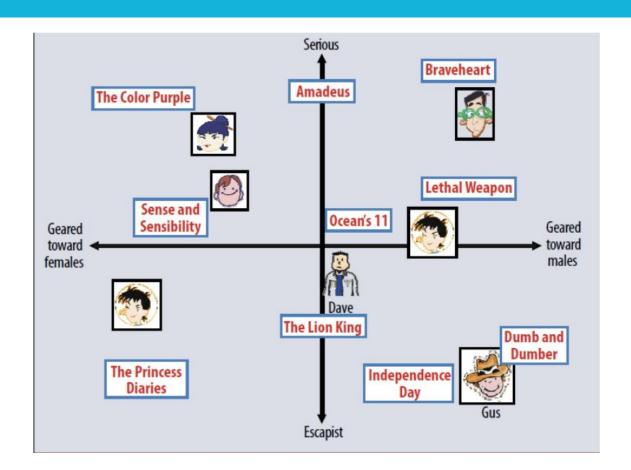
Content-Based

- Recommend based on the properties of the items
- Other user behavior is not considered

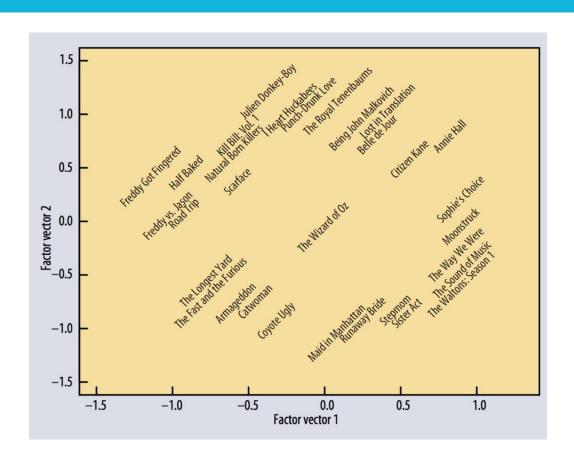
Collaborative Filtering

- Make use of user data to make recommendations
- User User
- Item Item
- Memory Based
- Model Based (Matrix Factorization)

Latent Features

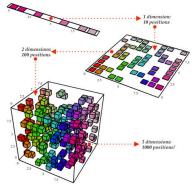


Latent Features



Dimensionality Reduction

What is a more compact way for us to represent our data?



Through matrix factorization, we can discover "latent features" that are present in our data.

Also known as "topic-modelling"

We choose the value for *d*, the number of features

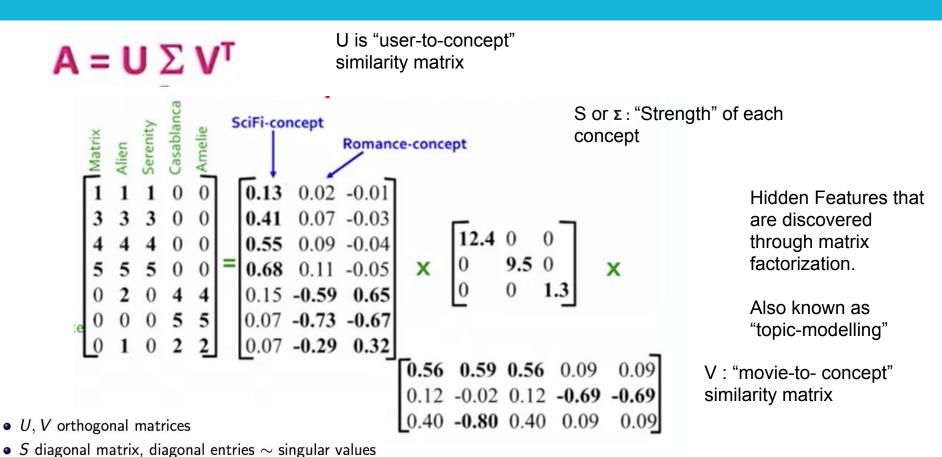
$$\begin{bmatrix} A \\ n \times d \end{bmatrix} = \begin{bmatrix} \hat{U} \\ n \times r \end{bmatrix} \begin{bmatrix} \hat{\Sigma} \\ r \times r \end{bmatrix} \begin{bmatrix} \hat{V}^T \\ r \times d \end{bmatrix}$$

$$U \qquad \Sigma \qquad V^T$$

$$n \times d \qquad n \times d \qquad d \times d$$

- *U*, *V* orthogonal matrices
- ullet S diagonal matrix, diagonal entries \sim singular values

SVD Example



Modified SVD

- The issue with SVD:
 - SVD only works with non-sparse matrices
- There is a way to factor our matrices into two components
 - Each item is modeled by a vector

$$q_i \in \mathbb{R}^k$$

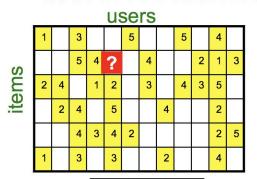
$$Q = U, P^{T} = \sum V^{T}$$

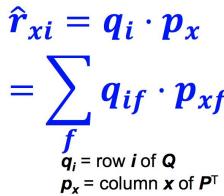
- o Each user is modeled by a vector
- $p_u \in \mathbb{R}^k$
- Such that a value close to the actual rating r_{ui} can be computed by the dot product

$$r_{ui} pprox \hat{r}_{ui} = q_i^T p_u$$

Calculating Rating in Model Based Approach

■ How to estimate the missing rating of user x for item i?





items	.1	4	.2			
	5	.6	.5			
	2	.3	.5			
	1.1	2.1	.3			
	7	2.1	-2			
	-1	.7	.3			
factors						

92	uscis											
S	1.1	2	.3	.5	-2	5	.8	4	.3	1.4	2.4	9
• ctc	8	.7	.5	1.4	.3	-1	1.4	2.9	7	1.2	1	1.3
Ę,	2.1	4	.6	1.7	2.4	.9	3	.4	.8	.7	6	.1

LICORC

PT

Alternating Least Squares

- Matrices are determined by minimizing the regular square error on only known ratings. Usually done through Alternating Least Squares:
 - Usually slower to calculate than Stochastic Gradient Descent, but it is more parallelizable
- Its training routine is different: ALS minimizes two loss functions alternatively; It first
 holds user matrix fixed and runs gradient descent with item matrix; then it holds item
 matrix fixed and runs gradient descent with user matrix

$$\min_{q,p} \sum_{(u,i)\in R_o} (r_{ui} - \langle p_u, q_i \rangle)^2 + \lambda(||q_i||^2 + ||p_u||^2)$$

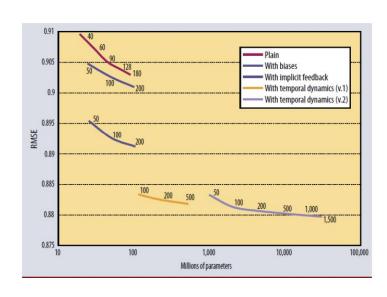
Collaborative Filtering (Model Based) Summary

Advantages:

The best in class models use latent features

Disadvantages:

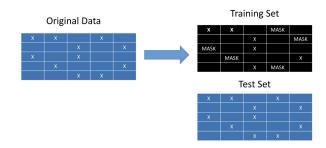
- Not interpretable to users
- Cold start problem
- Computational Complexity



Evaluating Recommenders

- We can quantify goodness of fit for recommendation engines using RMSE if we are estimating explicit ratings
- If we are estimating implicit ratings, we would use classification metrics such as ROC curve, AUC, Accuracy, Precision

$$RMSE = \sqrt{\frac{1}{|R_o|} \sum_{(u,i) \in R_o} (r_{ui} - \hat{r}_{ui})^2}$$



Problems with Evaluating Systems

- Accurate models tend to predict items that are extremely similar
 - Not great for displaying a wide diversity of items
- Prediction Context
- Order of Predictions
- "Offline Evaluation": Based on historic data
- "Online Evaluation": A/B Testing with users

Best way to evaluate.....



What makes you the most money! (Or keeps your customers satisfied)

Often done with "online evaluation"

Problems with Evaluating Systems

- Sometimes the best performing systems are not optimized for reality!
- Netflix Starting RMSE: 0.9525
- BellKor's Pragmatic Chaos RMSE: 0.8567



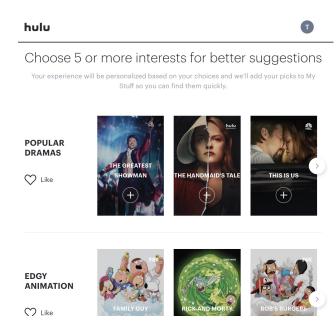


Issues with Recommendation Engines

- The "Cold Start" Problem
 - When a new user signs up, we don't know anything about their preferences. What can we do?

- Force users to rate a certain number of items when they join
- Force users to integrate their social media information
- Show users the most popular items





More Models!!

- Hybrid Methods
 - Models using a combination of content-based similarity and collaborative filtering. Some also include demographic information, previous behavior, etc.
 - Survey of Hybrid Recommender Systems
 - Recommendation systems based on previous behavior
- Deep Learning: Some of the best performing models
 - Survey of Deep Learning Recommendation Systems
 - Git Repo with a ton of resources on deep learning recommendation systems
- It's not all about the accuracy
 - http://ir.ii.uam.es/rim3/publications/ddr11.pdf

Python Libraries

- http://surpriselib.com/
- https://spark.apache.org/docs/2.2.0/mllib-collaborative-filtering.html



recommender systems.



Smaller Scale

Large Scale

THANK YOU!



User-User or Item-Item, which wins??

Item-Item Based Algorithm

- for every item i that u has no preference for yet
 - o for every item j that u has a preference for
 - compute a similarity s between i and j
 - add u's preference for j, weighted by s, to a running average
- return the top items, ranked by weighted average

User-User Based Algorithm

- for every item i that u has no preference for yet
 - for every other user v that has a preference for i
 - compute a similarity s between u and v
 - add v's preference for i, weighted by s, to a running average
- return the top items, ranked by weighted average

Item-Item Similarity Breakout

Items									
		sw	HP	LOTR	Avengers				
	Cersei	2	?	5	1				
	Daenerys	5	4	?	1				
Users	Joffrey	?	1	1	3				
	Jon	3	?	5	2				
	Tyrion	?	4	?	2				



Using Item-Item similarity, how much would Joffrey like Star Wars?
Assume N = 2 Try different similarity metrics!

$$r_{xi} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{xj}}{\sum_{j \in N(i;x)} s_{ij}}$$

Item-Item Similarity Breakout

ltems								
		sw	HP	LOTR	Avengers			
	Cersei	2	?	5	1			
	Daenerys	5	4	?	1			
Users	Joffrey	1	1	1	3			
	Jon	3	?	5	2			
	Tyrion	?	4	?	2			