

Statistical inference Project

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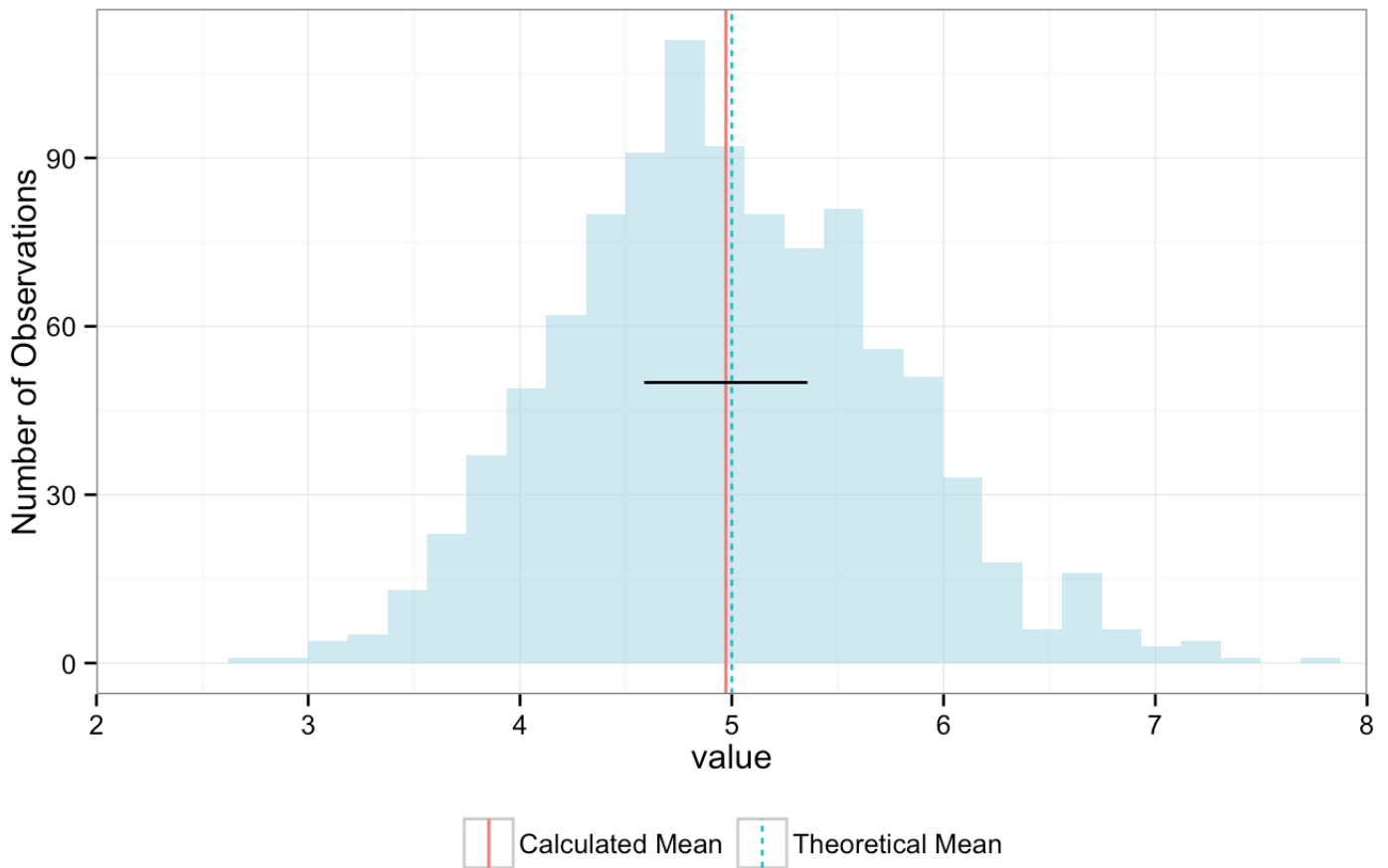
This is my Class Project for the Coursera Class of Statistical Inference, August 2014

Question A: Explore Exponential Distribution with Lambda = 0.2

1. Repeatedly sample 40 exponential random numbers and plot their averages

```
require(plyr)
require(ggplot2)
require(scales)
set.seed(12345)
n = 40
lambda = 0.2
samples = 1000
data <- data.frame(Measure = "Sample Means", value = sapply(1:1000, function(x) mean(rexp(n,
  lambda))), stringsAsFactors = F)
# data <- ddply(data, .(), mutate, calc=mean(value), theory=1/lambda)
means <- data.frame(Type = c("Calculated Mean", "Theoretical Mean"), mean = c(mean(data$value),
  1/lambda))
sd_calc <- sd(data$value)
title <- expression(paste("Sample Means for Exp. Dist. (", lambda, "=", "0.2",
  ")", sep = ""))
ggplot(data, aes(x = value)) + geom_histogram(alpha = 0.6, fill = "lightblue") +
  theme_bw() + theme(legend.position = "bottom") + ggtitle(title) + coord_cartesian(xlim = c(
2,
  8)) + geom_vline(data = means, aes(xintercept = mean, color = Type, linetype = Type),
  show_guide = TRUE) + guides(color = guide_legend(title = NULL), linetype = guide_legend(tit
le = NULL)) +
  scale_y_continuous("Number of Observations", labels = comma) + geom_line(data = NULL,
  aes(x = c(mean(data$value) - sd_calc/2, mean(data$value) + sd_calc/2), y = c(50,
  50)), color = "black")
```

Sample Means for Exp. Dist. ($\lambda=0.2$)



The figure above shows the distribution of means from 1,000 repeated samples of 40 exponential random numbers with $\lambda=0.2$. The red line is the calculated average of the 1,000 sample means, while the blue line denotes the theoretical mean of an exponential distribution which is $\frac{1}{\lambda} = 5$. The Calculated Mean is 4.972 with a 95% confidence interval of 4.9241 to 5.0198. The Calculated standard deviation of the sample means centered around the calculated sample mean which is equal to 0.77. According to the central limit theorem the standard deviation of the sample means (the standard error) is equal to the standard deviation of the actual distribution divided by \sqrt{n} , where n is the sample size (40 in this case), given that with some basic algebra we calculate the estimated population standard deviation to be 4.88 which is close to the theoretical value of $\frac{1}{\lambda} = 5$. As expected the distribution of sample means appears to be normal and centered around the distribution mean.