

Chapter 3 - Functions

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Chapter 3 - Functions

Outline

- 3.16 Inline Functions**
- 3.17 References and Reference Parameters**
- 3.18 Default Arguments**
- 3.19 Unary Scope Resolution Operator**
- 3.20 Function Overloading**
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3.1 Introduction

- Divide and conquer
 - Construct a program from smaller pieces or components
 - Each piece more manageable than the original program



3.2 Program Components in C++

- Modules: functions and classes
- Programs use new and “prepackaged” modules
 - New: programmer-defined functions, classes
 - Prepackaged: from the standard library
- Functions invoked by function call
 - Function name and information (arguments) it needs
- Function definitions
 - Only written once
 - Hidden from other functions



3.2 Program Components in C++

- Boss to worker analogy
 - A boss (the calling function or caller) asks a worker (the called function) to perform a task and return (i.e., report back) the results when the task is done.



3.3 Math Library Functions

- Perform common mathematical calculations
 - Include the header file **<cmath>**
- Functions called by writing
 - `functionName (argument);`
 - or
 - `functionName(argument1, argument2, ...);`
- Example
 - `cout << sqrt(900.0);`
 - `sqrt` (square root) function The preceding statement would print 30
 - All functions in math library return a **double**



3.3 Math Library Functions

- Function arguments can be
 - Constants
 - `sqrt(4);`
 - Variables
 - `sqrt(x);`
 - Expressions
 - `sqrt(sqrt(x)) ;`
 - `sqrt(3 - 6x);`



Method	Description	Example
ceil(x)	rounds x to the smallest integer not less than x	ceil(9.2) is 10.0 ceil(-9.8) is -9.0
cos(x)	trigonometric cosine of x (x in radians)	cos(0.0) is 1.0
exp(x)	exponential function ex	exp(1.0) is 2.71828 exp(2.0) is 7.38906
fabs(x)	absolute value of x	fabs(5.1) is 5.1 fabs(0.0) is 0.0 fabs(-8.76) is 8.76
floor(x)	rounds x to the largest integer not greater than x	floor(9.2) is 9.0 floor(-9.8) is -10.0
fmod(x, y)	remainder of x/y as a floating-point number	fmod(13.657, 2.333) is 1.992
log(x)	natural logarithm of x (base e)	log(2.718282) is 1.0 log(7.389056) is 2.0
log10(x)	logarithm of x (base 10)	log10(10.0) is 1.0 log10(100.0) is 2.0
pow(x, y)	x raised to power y (xy)	pow(2, 7) is 128 pow(9, .5) is 3
sin(x)	trigonometric sine of x (x in radians)	sin(0.0) is 0
sqrt(x)	square root of x	sqrt(900.0) is 30.0 sqrt(9.0) is 3.0
tan(x)	trigonometric tangent of x (x in radians)	tan(0.0) is 0

Fig. 3.2 Math library functions.



3.4 Functions

- Functions
 - Modularize a program
 - Software reusability
 - Call function multiple times
- Local variables
 - Known only in the function in which they are defined
 - All variables declared in function definitions are local variables
- Parameters
 - Local variables passed to function when called
 - Provide outside information



3.5 Function Definitions

- Function prototype
 - Tells compiler argument type and return type of function
 - **int square(int);**
 - Function takes an **int** and returns an **int**
 - Explained in more detail later
- Calling/invoking a function
 - **square(x);**
 - Parentheses an operator used to call function
 - Pass argument x
 - Function gets its own copy of arguments
 - After finished, passes back result



3.5 Function Definitions

- Format for function definition

```
return-value-type function-name( parameter-list )  
{  
    declarations and statements  
}
```

- Parameter list

- Comma separated list of arguments
 - Data type needed for each argument
- If no arguments, use **void** or leave blank

- Return-value-type

- Data type of result returned (use **void** if nothing returned)



3.5 Function Definitions

- Example function

```
int square( int y )  
{  
    return y * y;  
}
```

- **return** keyword
 - Returns data, and control goes to function's caller
 - If no data to return, use **return;**
 - Function ends when reaches right brace
 - Control goes to caller
- Functions cannot be defined inside other functions
- Next: program examples



fig03_03.cpp
(1 of 2)

```
1  // Fig. 3.3: fig03_03.cpp
2  // Creating and using a programmer-defined function.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  int square( int );    // function prototype
9
10 int main()
11 {
12     // loop 10 times and calculate and output the square of x each time
13     // square of x each time
14     for ( int x = 1; x <= 10; x++ )
15         cout << square( x ) << " ";    // function call
16
17     cout << endl;
18
19     return 0;    // indicates successful termination
20
21 } // end main
22
```

Function prototype: specifies data types of arguments and return values. **square** expects and **int**, and returns an **int**.

Parentheses () cause function to be called. When done, it returns the result.



Outline



fig03_03.cpp
(2 of 2)

fig03_03.cpp
output (1 of 1)


```
23 // square function definition returns square of an integer
24 int square( int y ) // y is a copy of argument to function
25 {
26     return y * y; // returns square of y as an int
27
28 } // end function square
```

```
1  4  9 16 25 36 49 64 81 100
```

Definition of **square**. **y** is a copy of the argument passed. Returns **y * y**, or **y** squared.

**fig03_04.cpp**
(1 of 2)

```
1  // Fig. 3.4: fig03_04.cpp
2  // Finding the maximum of three floating-point numbers.
3  #include <iostream>
4
5  using std::cout;
6  using std::cin;
7  using std::endl;
8
9  double maximum( double, double, double ); // function prototype
10
11 int main()
12 {
13     double number1;
14     double number2;
15     double number3;
16
17     cout << "Enter three floating-point numbers: ";
18     cin >> number1 >> number2 >> number3;
19
20     // number1, number2 and number3 are arguments to
21     // the maximum function call
22     cout << "Maximum is: "
23         << maximum( number1, number2, number3 ) << endl;
24
25     return 0; // indicates successful termination
```



Function **maximum** takes 3 arguments (all **double**) and returns a **double**.



fig03_04.cpp
(2 of 2)

fig03_04.cpp
output (1 of 1)

Comma separated list for
multiple parameters.

```
26
27 } // end main
28
29 // function maximum definition;
30 // x, y and z are parameters
31 double maximum( double x, double y, double z )
32 {
33     double max = x;    // assume x is largest
34
35     if ( y > max )      // if y is larger,
36         max = y;        // assign y to max
37
38     if ( z > max )      // if z is larger,
39         max = z;        // assign z to max
40
41     return max;        // max is largest value
42
43 } // end function maximum
```

Enter three floating-point numbers: 99.32 37.3 27.1928

Maximum is: 99.32

Enter three floating-point numbers: 1.1 3.333 2.22

Maximum is: 3.333

Enter three floating-point numbers: 27.9 14.31 88.99

Maximum is: 88.99

3.6 Function Prototypes

- Function prototype contains
 - Function name
 - Parameters (number and data type)
 - Return type (**void** if returns nothing)
 - Only needed if function definition after function call
- Prototype must match function definition
 - Function prototype
`double maximum(double, double, double);`
 - Definition

```
double maximum( double x, double y, double z )
{
    ...
}
```



3.6 Function Prototypes

- Function signature

- Part of prototype with name and parameters

- `double maximum(double, double, double);`

Function signature

- Argument Coercion

- Force arguments to be of proper type

- Converting **int** (4) to **double** (4.0)

- `cout << sqrt(4)`

- Conversion rules

- Arguments usually converted automatically

- Changing from **double** to **int** can truncate data

- 3.4 to 3

- Mixed type goes to highest type (promotion)

- **Int * double**



3.6 Function Prototypes

Data types	
long double	
double	
float	
unsigned long int	(synonymous with unsigned long)
long int	(synonymous with long)
unsigned int	(synonymous with unsigned)
int	
unsigned short int	(synonymous with unsigned short)
short int	(synonymous with short)
unsigned char	
char	
bool	(false becomes 0, true becomes 1)
Fig. 3.5 Promotion hierarchy for built-in data types.	



3.7 Header Files

- Header files contain
 - Function prototypes
 - Definitions of data types and constants
- Header files ending with .h
 - Programmer-defined header files
`#include "myheader.h"`
- Library header files
`#include <cmath>`



3.8 Random Number Generation

- **rand** function (**<cstdlib>**)
 - **i = rand();**
 - Generates unsigned integer between 0 and RAND_MAX (usually 32767)
- Scaling and shifting
 - Modulus (remainder) operator: %
 - **10 % 3** is **1**
 - **x % y** is between **0** and **y - 1**
 - Example
 - i = rand() % 6 + 1;**
 - **"Rand() % 6"** generates a number between **0** and **5** (scaling)
 - **" + 1"** makes the range **1** to **6** (shift)
 - Next: program to roll dice



fig03_07.cpp
(1 of 2)

```
1  // Fig. 3.7: fig03_07.cpp
2  // Shifted, scaled integers produced by 1 + rand() % 6.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  #include <iomanip>
9
10 using std::setw;
11
12 #include <cstdlib>    // contains function prototype for rand
13
14 int main()
15 {
16     // loop 20 times
17     for ( int counter = 1; counter <= 20; counter++ )
18
19         // pick random number from 1 to 6 and output it
20         cout << setw( 10 ) << ( 1 + rand() % 6 );
21
22         // if counter divisible by 5, begin new line of output
23         if ( counter % 5 == 0 )
24             cout << endl;
25
26     } // end for structure
```

Output of **rand()** scaled and shifted to be a number between 1 and 6.



```
27
28     return 0; // indicates successful termination
29
30 }
```

6	6	5	5	6
5	1	1	5	3
6	6	2	4	2
6	2	3	4	1

fig03_07.cpp**(2 of 2)****fig03_07.cpp****output (1 of 1)**

3.8 Random Number Generation

- Next
 - Program to show distribution of **rand()**
 - Simulate 6000 rolls of a die
 - Print number of 1's, 2's, 3's, etc. rolled
 - Should be roughly 1000 of each



**fig03_08.cpp**
(1 of 3)

```
1  // Fig. 3.8: fig03_08.cpp
2  // Roll a six-sided die 6000 times.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  #include <iomanip>
9
10 using std::setw;
11
12 #include <cstdlib>    // contains function prototype for rand
13
14 int main()
15 {
16     int frequency1 = 0;
17     int frequency2 = 0;
18     int frequency3 = 0;
19     int frequency4 = 0;
20     int frequency5 = 0;
21     int frequency6 = 0;
22     int face;  // represents one roll of the die
23
```

**fig03_08.cpp**
(2 of 3)

```
24 // loop 6000 times and summarize results
25 for ( int roll = 1; roll <= 6000; roll++ ) {
26     face = 1 + rand() % 6; // random number from 1 to 6
27
28     // determine face value and increment appropriate counter
29     switch ( face ) {
30
31         case 1:           // rolled 1
32             ++frequency1;
33             break;
34
35         case 2:           // rolled 2
36             ++frequency2;
37             break;
38
39         case 3:           // rolled 3
40             ++frequency3;
41             break;
42
43         case 4:           // rolled 4
44             ++frequency4;
45             break;
46
47         case 5:           // rolled 5
48             ++frequency5;
49             break;
```



fig03_08.cpp (3 of 3)

```

50
51     case 6:           // rolled 6
52         ++frequency6;
53         break;
54
55     default:          // invalid value
56         cout << "Program should never get here!";
57
58 } // end switch
59
60 } // end for
61
62 // display results in tabular form
63 cout << "Face" << setw( 13 ) << "Frequency"
64      << "\n  1" << setw( 13 ) << frequency1
65      << "\n  2" << setw( 13 ) << frequency2
66      << "\n  3" << setw( 13 ) << frequency3
67      << "\n  4" << setw( 13 ) << frequency4
68      << "\n  5" << setw( 13 ) << frequency5
69      << "\n  6" << setw( 13 ) << frequency6 << endl;
70
71 return 0; // indicates successful termination
72
73 } // end main

```

Default case included even though it should never be reached. This is a matter of good coding style

Face	Frequency
1	1003
2	1017
3	983
4	994
5	1004
6	999



Outline

fig03_08.cpp
output (1 of 1)

3.8 Random Number Generation

- Calling `rand()` repeatedly
 - Gives the same sequence of numbers
- Pseudorandom numbers
 - Preset sequence of "random" numbers
 - Same sequence generated whenever program run
- To get different random sequences
 - Provide a seed value
 - Like a random starting point in the sequence
 - The same seed will give the same sequence
 - **`srand(seed);`**
 - **`<cstdlib>`**
 - Used before **`rand()`** to set the seed



**fig03_09.cpp**
(1 of 2)

```
1  // Fig. 3.9: fig03_09.cpp
2  // Randomizing die-rolling program.
3  #include <iostream>
4
5  using std::cout;
6  using std::cin;
7  using std::endl;
8
9  #include <iomanip>
10
11 using std::setw;
12
13 // contains prototypes for functions srand and rand
14 #include <cstdlib>
15
16 // main function begins program execution
17 int main()
18 {
19     unsigned seed;
20
21     cout << "Enter seed: ";
22     cin >> seed;
23     srand( seed ); // seed random number generator
24
```

Setting the seed with
srand().



fig03_09.cpp
(2 of 2)

fig03_09.cpp
output (1 of 1)

```

25 // loop 10 times
26 for ( int counter = 1; counter <= 10; counter++ ) {
27
28     // pick random number from 1 to 6 and output it
29     cout << setw( 10 ) << ( 1 + rand() % 6 );
30
31     // if counter divisible by 5, begin new line of output
32     if ( counter % 5 == 0 )
33         cout << endl;
34
35 } // end for
36
37 return 0; // indicates s
38
39 } // end main

```

rand() gives the same sequence if it has the same initial seed.

Enter seed: 67

6	1	4	6	2
1	6	1	6	4

Enter seed: 432

4	6	3	1	6
3	1	5	4	2

Enter seed: 67

6	1	4	6	2
1	6	1	6	4

3.8 Random Number Generation

- Can use the current time to set the seed
 - No need to explicitly set seed every time
 - `srand(time(0));`
 - `time(0);`
 - `<ctime>`
 - Returns current time in seconds
- General shifting and scaling
 - $Number = shiftingValue + \mathbf{rand}() \% scalingFactor$
 - `shiftingValue` = first number in desired range
 - `scalingFactor` = width of desired range



3.9 Example: Game of Chance and Introducing enum

- Enumeration

- Set of integers with identifiers

enum *typeName* { *constant1*, *constant2*... } ;

- Constants start at 0 (default), incremented by 1
- Constants need unique names
- Cannot assign integer to enumeration variable
 - Must use a previously defined enumeration type

- Example

```
enum Status {CONTINUE, WON, LOST};
```

```
Status enumVar;
```

```
enumVar = WON; // cannot do enumVar = 1
```



3.9 Example: Game of Chance and Introducing enum

- Enumeration constants can have preset values

```
enum Months { JAN = 1, FEB, MAR, APR, MAY,  
             JUN, JUL, AUG, SEP, OCT, NOV, DEC};
```

- Starts at 1, increments by 1

- Next: craps simulator

- Roll two dice
- 7 or 11 on first throw: player wins
- 2, 3, or 12 on first throw: player loses
- 4, 5, 6, 8, 9, 10
 - Value becomes player's "point"
 - Player must roll his point before rolling 7 to win



**fig03_10.cpp**
(1 of 5)

```
1  // Fig. 3.10: fig03_10.cpp
2  // Craps.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  // contains function prototypes for functions srand and rand
9  #include <cstdlib>
10
11 #include <ctime> // contains prototypes for functions time and
12                  // srand
13 int rollDice( void ); // function prototype
14
15 int main()
16 {
17     // enumeration constants represent game status
18     enum Status { CONTINUE, WON, LOST };
19
20     int sum;
21     int myPoint;
22
23     Status gameStatus; // can contain CONTINUE, WON or LOST
24
```

Function to roll 2 dice and
return the result as an **int**.

Enumeration to keep track of
the current game.

**fig03_10.cpp**
(2 of 5)

```
25 // randomize random number generator using current time
26 srand( time( 0 ) );
27
28 sum = rollDice(); // first
29
30 // determine game status and
31 switch ( sum ) {
32
33     // win on first roll
34     case 7:
35     case 11:
36         gameStatus = WON;
37         break;
38
39     // lose on first roll
40     case 2:
41     case 3:
42     case 12:
43         gameStatus = LOST;
44         break;
45
```

switch statement
determines outcome based on
die roll.

**fig03_10.cpp**
(3 of 5)

```
46     // remember point
47     default:
48         gameStatus = CONTINUE;
49         myPoint = sum;
50         cout << "Point is " << myPoint << endl;
51         break;                // optional
52
53 } // end switch
54
55 // while game not complete ...
56 while ( gameStatus == CONTINUE ) {
57     sum = rollDice();          // roll dice again
58
59     // determine game status
60     if ( sum == myPoint )      // win by making point
61         gameStatus = WON;
62     else
63         if ( sum == 7 )        // lose by rolling 7
64             gameStatus = LOST;
65
66 } // end while
67
```

**fig03_10.cpp**
(4 of 5)

```
68 // display won or lost message
69 if ( gameStatus == WON )
70     cout << "Player wins" << endl;
71 else
72     cout << "Player loses" << endl;
73
74 return 0; // indicates successful termination
75
76 } // end main
77
78 // roll dice, calculate sum and d
79 int rollDice( void )
80 {
81     int die1;
82     int die2;
83     int workSum;
84
85     die1 = 1 + rand() % 6; // pick random die1 value
86     die2 = 1 + rand() % 6; // pick random die2 value
87     workSum = die1 + die2; // sum die1 and die2
88
```

Function **rollDice** takes no arguments, so has **void** in the parameter list.



fig03_10.cpp
(5 of 5)

fig03_10.cpp
output (1 of 2)

```
89 // display results of this roll
90 cout << "Player rolled " << die1 << " + " << die2
91     << " = " << workSum << endl;
92
93 return workSum;           // return sum of dice
94
95 } // end function rollDice
```

```
Player rolled 2 + 5 = 7
Player wins
```

```
Player rolled 6 + 6 = 12
Player loses
```

```
Player rolled 3 + 3 = 6
Point is 6
```

```
Player rolled 5 + 3 = 8
Player rolled 4 + 5 = 9
Player rolled 2 + 1 = 3
Player rolled 1 + 5 = 6
Player wins
```



fig03_10.cpp
output (2 of 2)

```
Player rolled 1 + 3 = 4
Point is 4
Player rolled 4 + 6 = 10
Player rolled 2 + 4 = 6
Player rolled 6 + 4 = 10
Player rolled 2 + 3 = 5
Player rolled 2 + 4 = 6
Player rolled 1 + 1 = 2
Player rolled 4 + 4 = 8
Player rolled 4 + 3 = 7
Player loses
```


3.10 Storage Classes

- Variables have attributes
 - Have seen name, type, size, value
 - Storage class
 - How long variable exists in memory
 - Scope
 - Where variable can be referenced in program
 - Linkage
 - For multiple-file program (see Ch. 6), which files can use it



3.10 Storage Classes

- Automatic storage class
 - Variable created when program enters its block
 - Variable destroyed when program leaves block
 - Only local variables of functions can be automatic
 - Automatic by default
 - keyword **auto** explicitly declares automatic
 - **register** keyword
 - Hint to place variable in high-speed register
 - Good for often-used items (loop counters)
 - Often unnecessary, compiler optimizes
 - Specify either **register** or **auto**, not both
 - **register int counter = 1;**



3.10 Storage Classes

- Static storage class
 - Variables exist for entire program
 - For functions, name exists for entire program
 - May not be accessible, scope rules still apply (more later)
- **static** keyword
 - Local variables in function
 - Keeps value between function calls
 - Only known in own function
- **extern** keyword
 - Default for global variables/functions
 - Globals: defined outside of a function block
 - Known in any function that comes after it



3.11 Scope Rules

- Scope
 - Portion of program where identifier can be used
- File scope
 - Defined outside a function, known in all functions
 - Global variables, function definitions and prototypes
- Function scope
 - Can only be referenced inside defining function
 - Only labels, e.g., identifiers with a colon (**case:**)



3.11 Scope Rules

- Block scope
 - Begins at declaration, ends at right brace }
 - Can only be referenced in this range
 - Local variables, function parameters
 - **static** variables still have block scope
 - Storage class separate from scope
- Function-prototype scope
 - Parameter list of prototype
 - Names in prototype optional
 - Compiler ignores
 - In a single prototype, name can be used once



**fig03_12.cpp**
(1 of 5)

```
1  // Fig. 3.12: fig03_12.cpp
2  // A scoping example.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  void useLocal( void );
9  void useStaticLocal( void );
10 void useGlobal( void );
11
12 int x = 1;           // global variable
13
14 int main()
15 {
16     int x = 5;       // local variable to main
17
18     cout << "local x in main's outer scope is " << x << endl;
19     { // start new scope
20
21         int x = 7;
22
23         cout << "local x in main's inner scope is " << x << endl;
24     } // end new scope
25
26 }
```

Declared outside of function;
global variable with file
scope.

Local variable with function
scope.

Create a new block, giving **x**
block scope. When the block
ends, this **x** is destroyed.

**fig03_12.cpp**
(2 of 5)

```
27
28     cout << "local x in main's outer scope is " << x << endl;
29
30     useLocal();           // useLocal has local x
31     useStaticLocal();    // useStaticLocal has static local x
32     useGlobal();         // useGlobal uses global x
33     useLocal();           // useLocal reinitializes its local x
34     useStaticLocal();    // static local x retains its prior value
35     useGlobal();         // global x also retains its value
36
37     cout << "\nlocal x in main is " << x << endl;
38
39     return 0;           // indicates successful termination
40
41 } // end main
42
```

**fig03_12.cpp**
(3 of 5)

```
43 // useLocal reinitializes local variable x during each call
44 void useLocal( void )
45 {
46     int x = 25; // initialized each time useLocal is called
47
48     cout << endl << "local x is " << x << endl;
49     << " on entering useLocal\n";
50     ++x;
51     cout << "local x is " << x << endl;
52     << " on exiting useLocal\n";
53
54 } // end function useLocal
55
```

Automatic variable (local variable of function). This is destroyed when the function exits, and reinitialized when the function begins.

**fig03_12.cpp**
(4 of 5)

```
56 // useStaticLocal initializes static local variable x only the
57 // first time the function is called; value of x is saved
58 // between calls to this function
59 void useStaticLocal( void )
60 {
61     // initialized only first time useStaticLocal is called
62     static int x = 50;
63
64     cout << endl << "local static x is " << x
65         << " on entering useStaticLocal" << endl;
66     ++x;
67     cout << "local static x is " <<
68         << " on exiting useStaticLocal" << endl;
69
70 } // end function useStaticLocal
71
```

Static local variable of function; it is initialized only once, and retains its value between function calls.



03_12.cpp
of 5)

03_12.cpp
output (1 of 2)

This function does not declare any variables. It uses the global **x** declared in the beginning of the program.

```
72 // useGlobal modifies global variable x during each call
73 void useGlobal( void )
74 {
75     cout << endl << "global x is " << x
76         << " on entering useGlobal" << endl;
77     x *= 10;
78     cout << "global x is " << x
79         << " on exiting useGlobal" << endl;
80
81 } // end function useGlobal
```

```
local x in main's outer scope is 5
local x in main's inner scope is 7
local x in main's outer scope is 5
```

```
local x is 25 on entering useLocal
local x is 26 on exiting useLocal
```

```
local static x is 50 on entering useStaticLocal
local static x is 51 on exiting useStaticLocal
```

```
global x is 1 on entering useGlobal
global x is 10 on exiting useGlobal
```



fig03_12.cpp
output (2 of 2)

```
local x is 25 on entering useLocal
```

```
local x is 26 on exiting useLocal
```

```
local static x is 51 on entering useStaticLocal
```

```
local static x is 52 on exiting useStaticLocal
```

```
global x is 10 on entering useGlobal
```

```
global x is 100 on exiting useGlobal
```

```
local x in main is 5
```

3.12 Recursion

- Recursive functions
 - Functions that call themselves
 - Can only solve a base case
- If not base case
 - Break problem into smaller problem(s)
 - Launch new copy of function to work on the smaller problem (recursive call/recursive step)
 - Slowly converges towards base case
 - Function makes call to itself inside the return statement
 - Eventually base case gets solved
 - Answer works way back up, solves entire problem



3.12 Recursion

- Example: factorial

$$n! = n * (n - 1) * (n - 2) * \dots * 1$$

- Recursive relationship ($n! = n * (n - 1)!$)

$$5! = 5 * 4!$$

$$4! = 4 * 3! \dots$$

- Base case ($1! = 0! = 1$)



**fig03_14.cpp**
(1 of 2)

```
1  // Fig. 3.14: fig03_14.cpp
2  // Recursive factorial function.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  #include <iomanip>
9
10 using std::setw;
11
12 unsigned long factorial( unsigned long ); // function prototype
13
14 int main()
15 {
16     // Loop 10 times. During each iteration, calculate
17     // factorial( i ) and display result.
18     for ( int i = 0; i <= 10; i++ )
19         cout << setw( 2 ) << i << "! = "
20             << factorial( i ) << endl;
21
22     return 0; // indicates successful termination
23
24 } // end main
```

Data type **unsigned long**
can hold an integer from 0 to
4 billion.



fig03_14.cpp
(2 of 2)

fig03_14.cpp
output (1 of 1)

The base case occurs when we have **0!** or **1!**. All other cases must be split up (recursive step).

```
25
26 // recursive definition of function factorial
27 unsigned long factorial( unsigned long
28 {
29     // base case
30     if ( number <= 1 )
31         return 1;
32
33     // recursive step
34     else
35         return number * factorial( number - 1 );
36
37 } // end function factorial
```

```
0! = 1
1! = 1
2! = 2
3! = 6
4! = 24
5! = 120
6! = 720
7! = 5040
8! = 40320
9! = 362880
10! = 3628800
```

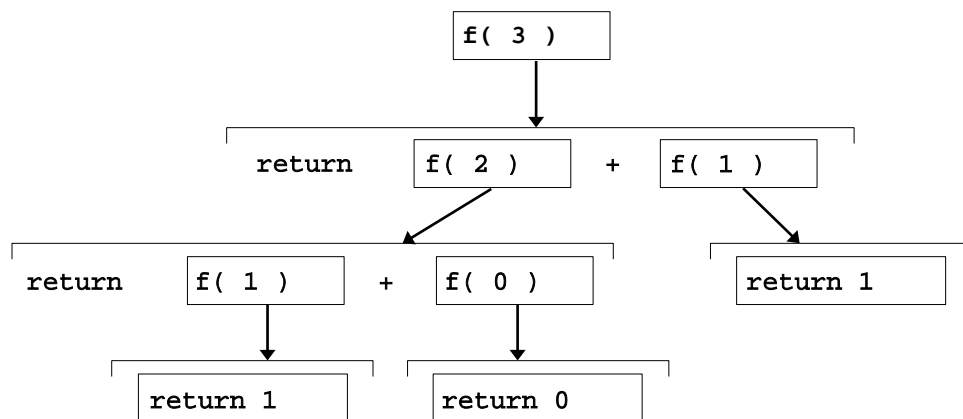
3.13 Example Using Recursion: Fibonacci Series

- Fibonacci series: 0, 1, 1, 2, 3, 5, 8...
 - Each number sum of two previous ones
 - Example of a recursive formula:
 - $fib(n) = fib(n-1) + fib(n-2)$
- C++ code for Fibonacci function

```
long fibonacci( long n )
{
    if ( n == 0 || n == 1 )    // base case
        return n;
    else
        return fibonacci( n - 1 ) +
               fibonacci( n - 2 );
}
```



3.13 Example Using Recursion: Fibonacci Series



3.13 Example Using Recursion: Fibonacci Series

- Order of operations
 - `return fibonacci(n - 1) + fibonacci(n - 2);`
- Do not know which one executed first
 - C++ does not specify
 - Only `&&`, `||` and `?:` guaranteed left-to-right evaluation
- Recursive function calls
 - Each level of recursion doubles the number of function calls
 - 30th number = $2^{30} \sim 4$ billion function calls
 - Exponential complexity





fig03_15.cpp

of 2)

The Fibonacci numbers get large very quickly, and are all non-negative integers. Thus, we use the **unsigned long** data type.

```
1  // Fig. 3.15: fig03_15.cpp
2  // Recursive fibonacci function.
3  #include <iostream>
4
5  using std::cout;
6  using std::cin;
7  using std::endl;
8
9  unsigned long fibonacci( unsigned long ); // fu
10
11 int main()
12 {
13     unsigned long result, number;
14
15     // obtain integer from user
16     cout << "Enter an integer: ";
17     cin >> number;
18
19     // calculate fibonacci value for number input by user
20     result = fibonacci( number );
21
22     // display result
23     cout << "Fibonacci(" << number << ") = " << result << endl;
24
25     return 0; // indicates successful termination
```

**fig03_15.cpp****(2 of 2)****fig03_15.cpp****output (1 of 2)**

```
26
27 } // end main
28
29 // recursive definition of function fibonacci
30 unsigned long fibonacci( unsigned long n )
31 {
32     // base case
33     if ( n == 0 || n == 1 )
34         return n;
35
36     // recursive step
37     else
38         return fibonacci( n - 1 ) + fibonacci( n - 2 );
39
40 } // end function fibonacci
```

Enter an integer: 0

Fibonacci(0) = 0

Enter an integer: 1

Fibonacci(1) = 1

Enter an integer: 2

Fibonacci(2) = 1

Enter an integer: 3

Fibonacci(3) = 2

**fig03_15.cpp**
output (2 of 2)

Enter an integer: 4

Fibonacci(4) = 3

Enter an integer: 5

Fibonacci(5) = 5

Enter an integer: 6

Fibonacci(6) = 8

Enter an integer: 10

Fibonacci(10) = 55

Enter an integer: 20

Fibonacci(20) = 6765

Enter an integer: 30

Fibonacci(30) = 832040

Enter an integer: 35

Fibonacci(35) = 9227465

3.14 Recursion vs. Iteration

- Repetition
 - Iteration: explicit loop
 - Recursion: repeated function calls
- Termination
 - Iteration: loop condition fails
 - Recursion: base case recognized
- Both can have infinite loops
- Balance between performance (iteration) and good software engineering (recursion)



3.15 Functions with Empty Parameter Lists

- Empty parameter lists
 - **void** or leave parameter list empty
 - Indicates function takes no arguments
 - Function **print** takes no arguments and returns no value
 - `void print();`
 - `void print(void);`



**fig03_18.cpp**
(1 of 2)

```
1  // Fig. 3.18: fig03_18.cpp
2  // Functions that take no arguments.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  void function1();          // function prototype
9  void function2( void );   // function prototype
10
11 int main()
12 {
13     function1();           // call function1 with no arguments
14     function2();           // call function2 with no arguments
15
16     return 0;              // indicates successful termination
17
18 } // end main
19
```




fig03_18.cpp
(2 of 2)

fig03_18.cpp
output (1 of 1)

```
20 // function1 uses an empty parameter list to specify that
21 // the function receives no arguments
22 void function1()
23 {
24     cout << "function1 takes no arguments" << endl;
25
26 } // end function1
27
28 // function2 uses a void parameter list to specify that
29 // the function receives no arguments
30 void function2( void )
31 {
32     cout << "function2 also takes no arguments" << endl;
33
34 } // end function2
```

```
function1 takes no arguments
function2 also takes no arguments
```

3.16 Inline Functions

- Inline functions
 - Keyword **inline** before function
 - Asks the compiler to copy code into program instead of making function call
 - Reduce function-call overhead
 - Compiler can ignore **inline**
 - Good for small, often-used functions

- Example

```
inline double cube( const double s )  
    { return s * s * s; }
```

- **const** tells compiler that function does not modify **s**
 - Discussed in chapters 6-7



**fig03_19.cpp**
(1 of 2)

```
1  // Fig. 3.19: fig03_19.cpp
2  // Using an inline function to calculate.
3  // the volume of a cube.
4  #include <iostream>
5
6  using std::cout;
7  using std::cin;
8  using std::endl;
9
10 // Definition of inline function cube. Definition of function
11 // appears before function is called, so a function prototype
12 // is not required. First line of function definition acts as
13 // the prototype.
14 inline double cube( const double side )
15 {
16     return side * side * side; // calculate cube
17
18 } // end function cube
19
```

**fig03_19.cpp****(2 of 2)****fig03_19.cpp****output (1 of 1)**

```
20  int main()
21  {
22      cout << "Enter the side length of your cube: ";
23
24      double sideValue;
25
26      cin >> sideValue;
27
28      // calculate cube of sideValue and display result
29      cout << "Volume of cube with side "
30           << sideValue << " is " << cube( sideValue ) << endl;
31
32      return 0; // indicates successful termination
33
34  } // end main
```

```
Enter the side length of your cube: 3.5
Volume of cube with side 3.5 is 42.875
```

3.17 References and Reference Parameters

- Call by value
 - Copy of data passed to function
 - Changes to copy do not change original
 - Prevent unwanted side effects
- Call by reference
 - Function can directly access data
 - Changes affect original



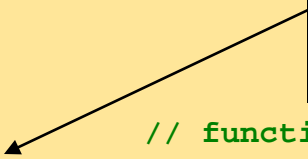
3.17 References and Reference Parameters

- Reference parameter
 - Alias for argument in function call
 - Passes parameter by reference
 - Use **&** after data type in prototype
 - **void myFunction(int &data)**
 - Read “**data** is a reference to an **int**”
 - Function call format the same
 - However, original can now be changed



fig03_20.cpp
(1 of 2)

```
1  // Fig. 3.20: fig03_20.cpp
2  // Comparing pass-by-value and pass-by-reference
3  // with references.
4  #include <iostream>
5
6  using std::cout;
7  using std::endl;
8
9  int squareByValue( int );           // function prototype
10 void squareByReference( int & );    // function prototype
11
12 int main()
13 {
14     int x = 2;
15     int z = 4;
16
17     // demonstrate squareByValue
18     cout << "x = " << x << " before squareByValue\n";
19     cout << "Value returned by squareByValue: "
20          << squareByValue( x ) << endl;
21     cout << "x = " << x << " after squareByValue\n" << endl;
22
```



Notice the & operator,
indicating pass-by-reference.

fig03_20.cpp
(2 of 2)

```
23 // demonstrate squareByReference
24 cout << "z = " << z << " before squareByReference" << endl;
25 squareByReference( z );
26 cout << "z = " << z << " after squareByReference" << endl;
27
28 return 0; // indicates successful termination
29 } // end main
30
31 // squareByValue multiplies number by itself
32 // result in number and returns the new value
33 int squareByValue( int number )
34 {
35     return number *= number; // caller's argument not modified
36
37 } // end function squareByValue
38
39 // squareByReference multiplies numberRef by itself
40 // stores the result in the variable to which numberRef
41 // refers in function main
42 void squareByReference( int &numberRef )
43 {
44     numberRef *= numberRef; // caller's argument modified
45
46 } // end function squareByReference
```

Changes **number**, but original parameter (**x**) is not modified.

Changes **numberRef**, an alias for the original parameter. Thus, **z** is changed.



fig03_20.cpp
output (1 of 1)

```
x = 2 before squareByValue  
Value returned by squareByValue: 4  
x = 2 after squareByValue
```

```
z = 4 before squareByReference  
z = 16 after squareByReference
```

3.17 References and Reference Parameters

- Pointers (chapter 5)
 - Another way to pass-by-reference
- References as aliases to other variables
 - Refer to same variable
 - Can be used within a function

```
int count = 1; // declare integer variable count
Int &cRef = count; // create cRef as an alias for count
++cRef; // increment count (using its alias)
```

- References must be initialized when declared
 - Otherwise, compiler error
 - Dangling reference
 - Reference to undefined variable



**fig03_21.cpp**

(1 of 1)

fig03_21.cpp

output (1 of 1)

```
1  // Fig. 3.21: fig03_21.cpp
2  // References must be initialized.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  int main()
9  {
10     int x = 3;
11
12     // y refers to (is an alias for) x
13     int &y = x;
14
15     cout << "x = " << x << endl << "y = " << y << endl;
16     y = 7;
17     cout << "x = " << x << endl << "y = " << y << endl;
18
19     return 0; // indicates successful termination
20
21 } // end main
```

y declared as a reference to x.

```
x = 3
y = 3
x = 7
y = 7
```



fig03_22.cpp
(1 of 1)

fig03_22.cpp
output (1 of 1)

```

1  // Fig. 3.22: fig03_22.cpp
2  // References must be initialized.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  int main()
9  {
10     int x = 3;
11     int &y;           // Error: y must be initialized
12
13     cout << "x = " << x << endl << "y = " << y << endl;
14     y = 7;
15     cout << "x = " << x << endl << "y = " << y << endl;
16
17     return 0;  // indicates successful termination
18
19 } // end main

```

Uninitialized reference –
compiler error.

Borland C++ command-line compiler error message:

Error E2304 Fig03_22.cpp 11: Reference variable 'y' must be
initialized- in function main()

Microsoft Visual C++ compiler error message:

D:\cpphttp4_examples\ch03\Fig03_22.cpp(11) : error C2530: 'y' :
references must be initialized

3.18 Default Arguments

- Function call with omitted parameters
 - If not enough parameters, rightmost go to their defaults
 - Default values
 - Can be constants, global variables, or function calls

- Set defaults in function prototype

```
int myFunction( int x = 1, int y = 2, int z = 3 );
```

- **myFunction(3)**
 - **x = 3**, **y** and **z** get defaults (rightmost)
- **myFunction(3, 5)**
 - **x = 3**, **y = 5** and **z** gets default



fig03_23.cpp
(1 of 2)

Set defaults in function prototype.

Function calls with some parameters missing – the rightmost parameters get their defaults.

```
1  // Fig. 3.23: fig03_23.cpp
2  // Using default arguments.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  // function prototype that specifies default arguments
9  int boxVolume( int length = 1, int width = 1, int height = 1 );
10
11 int main()
12 {
13     // no arguments--use default values for all dimensions
14     cout << "The default box volume is: " << boxVolume();
15
16     // specify length; default width and height
17     cout << "\n\nThe volume of a box with length 10,\n"
18          << "width 1 and height 1 is: " << boxVolume( 10 );
19
20     // specify length and width; default height
21     cout << "\n\nThe volume of a box with length 10,\n"
22          << "width 5 and height 1 is: " << boxVolume( 10, 5 );
23 }
```



fig03_23.cpp
(2 of 2)

fig03_23.cpp
output (1 of 1)

```
24 // specify all arguments
25 cout << "\n\nThe volume of a box with length 10,\n"
26     << "width 5 and height 2 is: " << boxVolume( 10, 5, 2 )
27     << endl;
28
29 return 0; // indicates successful termination
30
31 } // end main
32
33 // function boxVolume calculates the volume of a box
34 int boxVolume( int length, int width, int height )
35 {
36     return length * width * height;
37
38 } // end function boxVolume
```

The default box volume is: 1

The volume of a box with length 10,
width 1 and height 1 is: 10

The volume of a box with length 10,
width 5 and height 1 is: 50

The volume of a box with length 10,
width 5 and height 2 is: 100

3.19 Unitary Scope Resolution Operator

- Unary scope resolution operator (`::`)
 - Access global variable if local variable has same name
 - Not needed if names are different
 - Use `::variable`
 - `y = ::x + 3;`
 - Good to avoid using same names for locals and globals



**fig03_24.cpp**
(1 of 2)

```
1  // Fig. 3.24: fig03_24.cpp
2  // Using the unary scope resolution operator.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  #include <iomanip>
9
10 using std::setprecision;
11
12 // define global constant PI
13 const double PI = 3.14159265358979;
14
15 int main()
16 {
17     // define local constant PI
18     const float PI = static_cast< float >( ::PI );
19
20     // display values of local and global PI constants
21     cout << setprecision( 20 )
22         << "   Local float value of PI = " << PI
23         << "\nGlobal double value of PI = " << ::PI << endl;
24
25     return 0; // indicates successful termination
```

Access the global **PI** with
::PI.

Cast the global **PI** to a
float for the local **PI**. This
example will show the
difference between **float**
and **double**.



```
26  
27 } // end main
```

Borland C++ command-line compiler output:

Local float value of PI = 3.141592741012573242

Global double value of PI = 3.141592653589790007

Microsoft Visual C++ compiler output:

Local float value of PI = 3.1415927410125732

Global double value of PI = 3.14159265358979

fig03_24.cpp

(2 of 2)

fig03_24.cpp

output (1 of 1)

3.20 Function Overloading

- Function overloading
 - Functions with same name and different parameters
 - Should perform similar tasks
 - I.e., function to square **ints** and function to square **floats**

```
int square( int x) {return x * x;}  
float square(float x) { return x * x; }
```
- Overloaded functions distinguished by signature
 - Based on name and parameter types (order matters)
 - Name mangling
 - Encodes function identifier with parameters
 - Type-safe linkage
 - Ensures proper overloaded function called



**fig03_25.cpp**
(1 of 2)

Overloaded functions have the same name, but the different parameters distinguish them.

```
1  // Fig. 3.25: fig03_25.cpp
2  // Using overloaded functions.
3  #include <iostream>
4
5  using std::cout;
6  using std::endl;
7
8  // function square for int values
9  int square( int x )
10 {
11     cout << "Called square with int argument: " << x << endl;
12     return x * x;
13 }
14 // end int version of function square
15
16 // function square for double values
17 double square( double y )
18 {
19     cout << "Called square with double argument: " << y << endl;
20     return y * y;
21 }
22 // end double version of function square
23
```



fig03_25.cpp
(2 of 2)

fig03_25.cpp
output (1 of 1)

```
24 int main()
25 {
26     int intResult = square( 7 );           // calls int version
27     double doubleResult = square( 7.5 ); // calls double version
28
29     cout << "\nThe square of integer 7 is 49\n";
30         << "\nThe square of double 7.5 is 56.25\n";
31         << endl;
32
33     return 0; // indicates successful termination
34
35 }
```

The proper function is called
based upon the argument
(**int** or **double**).

Called square with int argument: 7
Called square with double argument: 7.5

The square of integer 7 is 49
The square of double 7.5 is 56.25

**fig03_26.cpp**
(1 of 2)

```
1  // Fig. 3.26: fig03_26.cpp
2  // Name mangling.
3
4  // function square for int values
5  int square( int x )
6  {
7      return x * x;
8  }
9
10 // function square for double values
11 double square( double y )
12 {
13     return y * y;
14 }
15
16 // function that receives arguments of types
17 // int, float, char and int *
18 void nothing1( int a, float b, char c, int *d )
19 {
20     // empty function body
21 }
22
```



fig03_26.cpp
(2 of 2)

fig03_26.cpp
output (1 of 1)

```
23 // function that receives arguments of types
24 // char, int, float * and double *
25 char *nothing2( char a, int b, float *c, double *d )
26 {
27     return 0;
28 }
29
30 int main()
31 {
32     return 0; // indicates successful termination
33
34 } // end main
```

Mangled names produced in
assembly language.

\$q separates the function
name from its parameters. **c**
is **char**, **d** is **double**, **i** is
int, **pf** is a pointer to a
float, etc.

```
_main
@nothing2$qcipfpd
@nothing1$qifcpi
@square$qd
@square$qi
```

3.21 Function Templates

- Compact way to make overloaded functions
 - Generate separate function for different data types
- Format
 - Begin with keyword **template**
 - Formal type parameters in brackets **<>**
 - Every type parameter preceded by **typename** or **class** (synonyms)
 - Placeholders for built-in types (i.e., **int**) or user-defined types
 - Specify arguments types, return types, declare variables
 - Function definition like normal, except formal types used



3.21 Function Templates

- Example

```
template < class T > // or template< typename T >
T square( T value1 )
{
    return value1 * value1;
}
```

- **T** is a formal type, used as parameter type
 - Above function returns variable of same type as parameter
- In function call, **T** replaced by real type
 - If **int**, all **T**'s become **ints**

```
int x;
int y = square(x);
```



fig03_27.cpp
(1 of 3)

```
1  // Fig. 3.27: fig03_27.cpp
2  // Using a function template.
3  #include <iostream>
4
5  using std::cout;
6  using std::cin;
7  using std::endl;
8
9  // definition of function template
10 template < class T > // or template < typename T >
11 T maximum( T value1, T value2, T value3 )
12 {
13     T max = value1;
14
15     if ( value2 > max )
16         max = value2;
17
18     if ( value3 > max )
19         max = value3;
20
21     return max;
22
23 } // end function template maximum
24
```

Formal type parameter **T**
placeholder for type of data to
be tested by **maximum**.

maximum expects all
parameters to be of the same
type.

fig03_27.cpp
(2 of 3)

maximum called with various data types.

```
25 int main()
26 {
27     // demonstrate maximum with int values
28     int int1, int2, int3;
29
30     cout << "Input three integer values: ";
31     cin >> int1 >> int2 >> int3;
32
33     // invoke int version of maximum
34     cout << "The maximum integer value is: "
35           << maximum( int1, int2, int3 );
36
37     // demonstrate maximum with double values
38     double double1, double2, double3;
39
40     cout << "\n\nInput three double values: ";
41     cin >> double1 >> double2 >> double3;
42
43     // invoke double version of maximum
44     cout << "The maximum double value is: "
45           << maximum( double1, double2, double3 );
46
```



fig03_27.cpp
(3 of 3)

fig03_27.cpp
output (1 of 1)

```
47 // demonstrate maximum with char values
48 char char1, char2, char3;
49
50 cout << "\n\nInput three characters: ";
51 cin >> char1 >> char2 >> char3;
52
53 // invoke char version of maximum
54 cout << "The maximum character value is: "
55      << maximum( char1, char2, char3 )
56      << endl;
57
58 return 0; // indicates successful termination
59
60 } // end main
```

Input three integer values: 1 2 3

The maximum integer value is: 3

Input three double values: 3.3 2.2 1.1

The maximum double value is: 3.3

Input three characters: A C B

The maximum character value is: C