# Garment Industry: Predicting Productivity

Using Regression and Classification Models

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#### 1 Introduction

This project aims to determine productivity given multiple characteristics such as idle time, incentive, number of workers. The main response variable, "actual productivity", is an element within the unit interval leading us to mutate it into a binary variable named "productivity".

Name	Description
Date	Date
Day	Day of the week
quarter	A month was divided into four quarters
department	Associated department: finishing
team	Associated team number 1-12
no of worker	Number of workers in each team
no of style_change	Number of changes in the style of a particular product
targeted productivity	set by the Authority for each team for each day
smv : Standard Minute Value	it is the allocated time for a task
wip: Work in progress	Includes the number of unfinished items for products
over time	Represents the amount of overtime by each team in minutes
incentive	Represents the amount of financial incentive
idle time	Time production was interrupted due to several reasons
idle men	Number of workers in idle due to production interruption
actual productivity	the actual productivity by percent
productivity	"Yes", if 80% completion is reached

**Table 1** – Attributes of the Dataset.

# 2 Research Questions

Both Regression and Classification models were applied using 14 predictors to find productivity continuously or as a binary. Our research questions:

- Can we find a model which most accurately predicts productivity given the 14 predictors?
- How do incentives correlate with productivity?
- Does the idle time affect productivity?
- What is the predicted productivity for large idle time and idle men?

# 3 Analysis

#### 3.1 Data Preparation

The data set includes nearly 1200 observations along with 16 variables. The data set was opened through Google Sheets to observe the data set. It was noticed that variable wip has empty elements. Dropping NAs gives us a subset with about 700 observations with 15 variables where we lose department variable. Note, that variable, day, was dropped as it is already covered by variable "quarter".

It was mentioned that targeted productivity is correlated with response variable "actual productivity". Due to this correlation, targeted variable will be dropped. See the following figure for a corelation matrix.

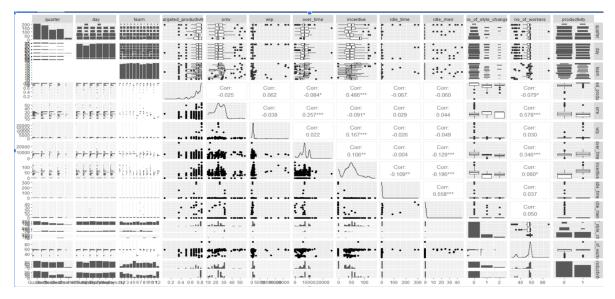


Figure 1 – Correlation Scatterplot for all values in subset



Figure 2 – Google Sheets with depicting NA's.

# 3.2 Logistic Regression

We know that actual productivity is an element of the unit interval. Our goal is to run classification models by mutating actual productivity into new variable. Here the threshold for new variable, productivity, to be successful was if actual productivity is greater than .80.

Run the logistic model. Then, rerun Logit model on variables that meet 95% threshold.

```
glm(formula = productivity ~ ., family = "binomial", data = train_set2)
Deviance Residuals:
             1Q Median
   Min
-2.1625 -0.4182 -0.0363
                           0.4001
                                     3.5824
Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
(Intercept)
                    -7.768e+00 2.393e+00
                                          -3.246
                                                   0.00117
                    4.256e-01
                               4.009e-01
                                           1.062
quarterQuarter2
                                                   0.28838
                    -3.503e-01
                               4.228e-01
                                           -0.829
                                                   0.40737
auarterOuarter3
auarterOuarter4
                    -6.727e-01
                               4.332e-01
                                           -1.553
                                                   0.12048
quarterQuarter5
                    -1.451e+00
                               1.029e+00
                                           -1.410
                                                   0.15857
                                4.975e-01
daySaturday
                    4.859e-02
                                            0.098
                                                   0.92220
daySunday
                    -3.295e-01
                                4.994e-01
                                           -0.660
                                                   0.50937
dayThursday
                    5.118e-02
                                5.081e-01
                                            0.101
                                                   0.91976
dayTuesday
                    -2.488e-01
                                4.582e-01
                                           -0.543
                                                   0.58711
dayWednesday
                     3.270e-02
                                4.573e-01
                                                   0.94300
                                            0.071
team2
                     7.160e-01
                                8.703e-01
                                            0.823
                                                   0.41062
team3
                    -1.250e-02
                                7.445e-01
                                           -0.017
                                                   0.98661
                     1.462e-01
                                7.303e-01
                                                   0.84134
team4
                                            0.200
                    -1.179e+00
                                8.947e-01
                                           -1.318
                                                   0.18766
team5
                     1.703e+00
                                1.208e+00
                                            1.409
                                                   0.15873
team6
                     1 866e+00
                                8.222e-01
                                            2 269
                                                   0 02324
team7
                     8.135e-01
                                7.973e-01
                                            1.020
                                                   0.30755
team8
                    -7.400e-01
                                7.281e-01
                                           -1.016
                                                   0.30943
team9
                    -6.008e-01
                                8.003e-01
                                           -0.751
                                                   0.45277
team10
team11
                    -1.401e+00
                                8.427e-01
                                           -1.662
                                                   0.09649
team12
                     2.273e+00
                                1.215e+00
                                            1.871
                                                   0.06137
                                                   0.00656 **
                    -9.496e-02
                                3.493e-02
                                           -2.718
smv
                    -3.613e-05
                                8.062e-05
                                           -0.448
                                                   0.65403
wip
over_time
                    -1.769e-04
                                6.452e-05
                                           -2.742
                                                   0.00611
                                                   < 2e-16 **
incentive
                    1.267e-01
                                1.365e-02
                                            9.280
idle_time
                    3.159e-02
                                1.680e+01
                                            0.002
                                                   0.99850
idle_men
                    -1.228e+00
                                6.511e+01
                                           -0.019
                                                   0.98495
no_of_style_change1 -1.374e+00
                                5.633e-01
                                           -2.439
                                                   0.01472
no_of_style_change2 -1.126e+00
                               8.647e-01
                                           -1.302
                                                   0.19280
no_of_workers
                     9.757e-02 4.322e-02
                                            2.258
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 754.74 on 551
                                   degrees of freedom
Residual deviance: 334.69 on 522 degrees of freedom
AIC: 394.69
Number of Fisher Scoring iterations: 17
```

Figure 3

# 3.3 Linear Discriminate Analysis: A Different Approach to Classification

The binary variable, prediction, is successful when 80% of actual productivity is reached. This partitions the data set somewhat evenly where productivity = 44.44% of the time. In other words, out of 693 observations, productivity = 1,304 times. We know that LDA is more stable when the classifiers are evenly (linearly) split. So the goal of using LDA is to see if LDA can successfully predict productivity knowing that it is more stable than Logistic Regression

The following code is meant to apply LDA model onto the data set and verify if LDA performances better by demonstrating higher stability when predicting.

This code this mean to output a confusion matrix and determine model accuracy using ROC curve and AUC.

Recall:

Sensitivity (True Positive Rate) = 
$$\frac{\text{True Positive}}{\text{True Positive} + \text{False Negative}} = \frac{142}{15 + 142} = 0.9044586 = 90.44\%$$

Hence, the our positive rate of our model is very high in predicting productivity.

```
Call:
glm(formula = productivity ~ team + over_time + smv + incentive +
    no_of_style_change + no_of_workers, family = "binomial",
    data = train_set2)
Deviance Residuals:
   Min
              1Q
                   Median
                                        Max
-2.1601
        -0.4304
                 -0.0488
                            0.4638
                                     3.6452
Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
(Intercept)
                    -7.045e+00 2.237e+00
                                          -3.150
                                                  0.00163 **
                     6.977e-01 8.424e-01
team2
                                            0.828
                                                   0.40759
team3
                     3.006e-02
                                7.241e-01
                                            0.042
                                                   0.96688
                     3.629e-02
                                7.133e-01
                                            0.051
                                                   0.95943
team4
team5
                    -1.602e+00
                                8.912e-01
                                           -1.797
                                                   0.07232
team6
                     1.260e+00 1.147e+00
                                            1.098
                                                   0.27206
                     1.606e+00
                               7.847e-01
                                            2.047
                                                   0.04067
team7
team8
                     6.193e-01
                                7.562e-01
                                            0.819
                                                   0.41283
                    -7.912e-01
                                7.098e-01
team9
                                           -1.115
                                                   0.26500
team10
                    -7.664e-01
                                8.052e-01
                                           -0.952
                                                   0.34122
                    -1.505e+00
team11
                                8.084e-01
                                           -1.861
                                                   0.06271
team12
                    1.741e+00
                                1.146e+00
                                            1.519
                                                   0.12868
                                                   0.00903 **
over_time
                    -1.482e-04
                                5.676e-05
                                           -2.611
                    -9.352e-02 3.333e-02
                                           -2.806
                                                   0.00502 **
smv
incentive
                    1.221e-01 1.295e-02
                                            9.428
                                                   < 2e-16 ***
no_of_style_change1 -1.329e+00 5.004e-01
                                           -2.655
                                                   0.00793 **
no_of_style_change2 -1.490e+00
                               7.700e-01
                                           -1.935
                                                   0.05294
                     8.168e-02 4.071e-02
                                            2.006
                                                  0.04480 *
no_of_workers
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 754.74 on 551 degrees of freedom
Residual deviance: 351.76 on 534 degrees of freedom
AIC: 387.76
Number of Fisher Scoring iterations: 6
[1] 0.8705036
```

#### Figure 4

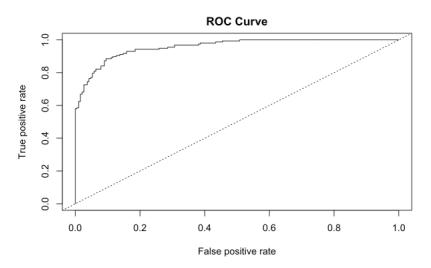


Figure 5 – ROC Curve. The desired result is for the curve to close to the upper left corner as much as possible.

Figure 6 – It shows that it was found that productivity was successful 43% of the time.

Figure 7 – Confusion matrix for LDA + Accuracy. AUC = 94%

$$\text{Specificity (True Negative Rate) } = \frac{\text{True Negative}}{\text{True Negative} + \text{False Positive}} = \frac{66}{66 + 27} = 0.70967770.96\%$$

Specificity at 71% level shows that this model is also accurate enough to predict productivity incorrectly. In other words, False negative rate is at 29%

Accuracy (Prediction Correctly Identified) = 
$$\frac{\text{True Negative} + \text{True Positive}}{\text{True Negative} + \text{False Positive} + \text{ True Positive} + \text{ False Negative}}$$
$$= \frac{66 + 55}{66 + 55 + 7 + 11} = 0.87050 = 87.70\%$$

#### 3.4 Shrinkage Method: Lasso Model

Shrinkage method is a method to improve regression and logistic models. Here, the method will take 14 predictors and shrink them by using  $\lambda$  parameter. Our sample size is more than 600, this helps minimize model variance but minimally increase bias. Note: since variables within the data set are not related with the response variable, Ridge regression will not be used. Instead, this section aims to seek results that come from the Lasso Model.

Our first step is to standardize our variables which means that each observation of each column will be divided by its respective standard deviation. This is presented in the following:

After applying cross validation methods, our  $\lambda$  is found to be 0.0037. With out MSE = 0.5. Here, we can see that variables are sent to 0 as they were found to be insignificant in predicting response variable production. With out MSE being near 0, we can use the coefficients from each variable and report our new classification model.

```
[1] 0.01041201
30 x 1 sparse Matrix of class "dgCMatrix"
                    -3.568742888
(Intercept)
quarterQuarter2
                    0.160149355
quarterQuarter3
                    -0.054777551
quarterQuarter4
                    -0.154317169
quarterQuarter5
                    -0.038246060
daySaturday
daySunday
dayThursday
dayTuesday
dayWednesday
team2
team3
team4
                    -0.269801122
team5
team6
                     0.266593225
team7
                     0.007085545
team8
                    -0.121031380
team9
team10
                    -0.073313077
team11
                    -0.263239897
team12
                     0.159081094
\mathsf{smv}
                    -0.846678348
wip
over_time
                    -0.337453633
incentive
                     5.136383071
idle_time
                    -0.015199253
idle_men
no_of_style_change1 -0.268963310
no_of_style_change2 -0.063617866
no_of_workers
[1] 0.8920863
```

Figure 8 – AUC = .95 while Accuracy is at 88%

# 3.5 Tree Model: A Search For Minimum requirements for Maximum Out for Prediction

The aim of this model is to understand what variables, at a specific level, yields a success in productivity for the day. A classification tree model was used to answer the following questions: what variables are the most significant, and at what value of these variables yields successful productivity

# 3.5.1 Classification Tree: What combination of features yields 80% level of productivity?

First comes data preparation. Here, productivity is converted to class productivity as classification tree model does not accept binary numeric values. The following tree is without pruning.

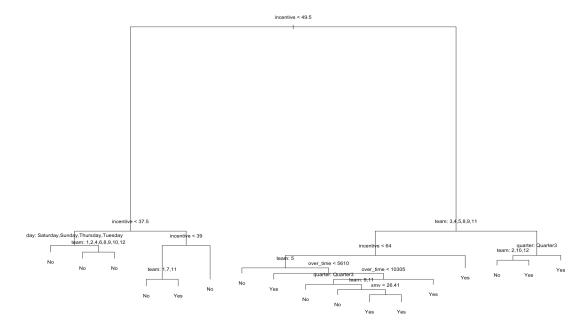
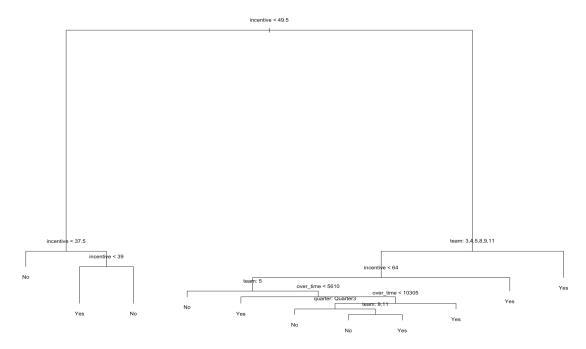


Figure 9 – Incentive dominated the decision tree of the data set.

For the best results, we prune tree model.



 $\mathbf{Figure}\ \mathbf{10}-\mathbf{Target}\ \mathbf{Productivity}\ \mathbf{and}\ \mathbf{Incentive}\ \mathbf{are}\ \mathbf{the}\ \mathbf{most}\ \mathbf{important}\ \mathbf{predictors}\ \mathbf{of}\ \mathbf{the}\ \mathbf{data}\ \mathbf{set}.$ 

The confusion matrix:

true\_status

predict\_status No Yes

No 67 6

Yes 6 60

[1] 0.9136691

true\_status

predict\_status No Yes

No 67 4

Yes 6 62

[1] 0.9280576

Figure 11 – Accuracy of full tree vs. Accuracy of pruned tree, respectively.

The output shows that given high target productivity and incentive lowered at 36 BDT (local currency) is the threshold that determines whether 80% of the daily quota will be met. If incentive is higher, then it will increase chances that the quota will be met, but it may not need as much of an incentive. On the other hand, if there is a lower amount of target productivity, then it is shown that it is required much more of an incentive for workers in order to reach a 80% of the daily quota.

- 3.6 Extension of Tree Models: Random Forest, Bagging, and Gradient Boosting
- 3.6.1 Random Forest:

Figure 12 – Variation Explained is at 84.27%.

true pred 0 1 0 69 3 1 4 63 [1] 0.9496403

Figure 13 – Variation Explained: 94.96%.

## Variable Importance

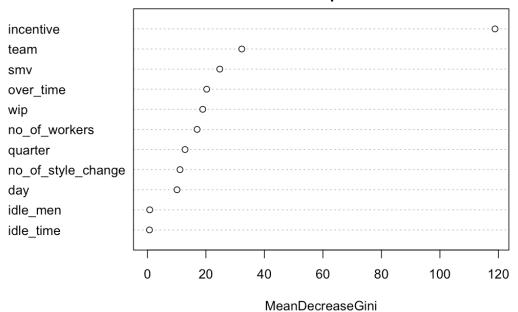


Figure 14 – Incentive is proven to be the most significant out of the bunch.

# 3.6.2 Bagging Model

The output of the model shows that number of tree used is 500. Mean squared residual is 0.004

Figure 15 – 11 nodes used along with Out of Bag Estimation.

Figure 16 – Accuracy = 92%.

#### 3.6.3 Gradient Boosting

The following output is the confusion matrix from the pre-tuned gradient boosting model.

Figure 17 – Variation Explained: 82.94%.

Tune parameters for boosting model.

```
true
pred 0 1
0 180 5
1 9 152
[1] 0.9595376
```

Figure 18 – Variation Explained: 82.94%.

#### 3.7 Support Vector Machine

CV-10 validation was applied to all 3 variations of SVM.

#### 3.7.1 Linear

Cost was found to be 0.1. Our support vectors are 164. Where 83 are for output being 0 and 81 are for outputs being 1.

```
truth
pred 0 1
0 67 12
1 6 54
[1] 0.8705036
```

Figure 19 – Variation Explained: 82.94%.

#### 3.7.2 Polynomial

```
truth
pred 0 1
0 73 57
1 0 9
[1] 0.5899281
```

Figure 20 - Variation Explained: 82.94%.

Here our cost was found to be 10. The fit model showed that our support vector total is 105 where 46 is for outputs being 0. Our polynomial was of degree 3.

#### 3.7.3 Radial

Here the cost was also 10. The fit moel was set to 552 vectors where 238 vectors were set to for outputs being 0.

```
truth
pred 0 1
0 31 13
1 42 53
[1] 0.6043165
```

Figure 21 – Variation Explained: 82.94%.

# 4 Prediction: Random Forest

We concluded that random forest and gradient boosting are our best models for accuracy. Since we care more about predicting accuracy levels of determining fails and success, we decided to predict using random forest and as our main model for this task. In the interest of time, we will only using random forest as our main model. The following are predictions regarding variables incentive, over time, idle men, and idle time. We created a new data frame that considered a values of the average, minimum, maximum, and average - standard deviation, and average + standard deviation. Each are of simulation that ranges from 1-5 respectively.

#### 4.1 Incentives

1 2 3 4 5 0 0 1 0 1

Figure 22 – Simulation 3 yielded a success along with Simulation 5.

Incentives prove to be significant when it come to predicting productivity. At our maximum value and a standard deviation above the average, yields a successful day. This shows that there is an interval between these two values (that does not include the mean) has an affect on productivity.

#### 4.2 Over Time

1 2 3 4 5 0 0 0 0 0 Levels: 0 1

 ${\bf Figure} \ {\bf 23} - {\rm Simulations} \ {\rm were} \ {\rm unsuccessful} \ .$ 

In addition, over time shows a similar characteristic with idle time and idle men. It shows, even at a maximum amount of over time, does not yield a successful day.

#### 4.3 Idle Time

Analysis is shown in Idle Time and Idle Men.

1 2 3 4 5 0 0 0 0 0 Levels: 0 1

 ${\bf Figure} \ {\bf 24} - {\bf Simulations} \ {\bf were} \ {\bf unsuccessful} \ .$ 

#### 4.4 Idle Men

Analysis is shown in Idle Time and Idle Men.

1 2 3 4 5 0 0 0 0 0 Levels: 0 1

Figure 25 – Simulations were unsuccessful.

#### 4.5 Idle Men and Idle Time

1 2 3 4 5 0 0 0 0 0 Levels: 0 1

Figure 26 – Simulations were unsuccessful .

Idle time and Idle men, which is time wasted due to interruptions in productivity, even at minimum values (0), does not change the outcome of having a successful day. This shows that idle time and idle men, even when the warehouse is having the worst day or best day, will always yield an unproductive day. This shows that the idle time and men are not important enough to sway the probability.

#### 4.6 Over Time and Incentives

1 2 3 4 5 0 0 1 0 1 Levels: 0 1

Figure 27 – Simulations were successful for simulation 3 and 5.

Combining Incentives with Over time yields a successful day. Here, it is not surprising that simulation 3 and 5 are successful as we just saw that incentives alone makes simulation 3 and 5 successful.

#### 4.7 Conclusion

These prediction tables directly answers our research questions. Ultimately, we have found that incentives is the most important predictor in our data set and random forest is our best model behind gradient boosting. If we have more time, we would have predicted using gradient boosting. We decided away from gradient boosting as it took longer to run as our trees increased.

## 4.8 Appendix

```
2
  title: "Final Project"
4 author: "Angel Silvar, Matthew Michael Rublee, Safwat Abdul Rahman"
5 date: "4/21/2022"
6 output: html_document
  '''{r include=FALSE ,message=FALSE, warning=FALSE}
10 Packages <- c( 'MASS', 'dplyr' ,'tidyverse', 'GGally', 'ISLR', 'caret'
11 'class','ROCR', 'boot', 'glmnet', 'pROC' ,'tree','randomForest', 'e1071 ',
12 'skimr')
 lapply ( Packages , library, character.only = TRUE)
13
  ( ( (
14
15
  '''{r include=FALSE ,message=FALSE, warning=FALSE}
 df=read_csv('/Users/angelsilvar/Desktop/STATS 473/Final Project/
17
              SweatShop.csv')
19 df = as_tibble(df)
  ""
20
21
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
23
factors = c( "date", "quarter", "day", "department",
          "no_of_style_change", "team")
25
_{27} df1 = df %>%
    mutate_at( factors , factor) %>%
28
    dplyr::select(-c(department, date, targeted_productivity))%>% drop_na()
29
30
31
32 <!-- '''{r include=TRUE ,message=FALSE, warning=FALSE} -->
| < ! -- n = nrow(df1) -->
```

```
_{34} <!-- prop = .8 -->
35 <!-- set.seed(123) -->
36 <!-- train_id = sample(1:n, size = n*prop, replace = FALSE) -->
37 <!-- test_id = (1:n)[-which(1:n %in% train_id)] -->
38 <!-- train_set = df[train_id,] -->
39 <!-- test_set = df[ test_id,] -->
40 <!-- ((( -->
41
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
42
43 # Set a threshold of 80% for productivity to create binary
      #response variable
45 logit_df = df1 %>%
   mutate (productivity = ifelse ( actual_productivity >=.8 ,1,0))%>%
46
   dplyr::select(-c(actual_productivity))%>% drop_na() %>%
47
   mutate_at('productivity', factor)
49 logit_df
  ( ( (
51
52
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
54 # Check for unique values of each predictor
55 #lapply(df1[,], unique)
56 k = nrow(logit_df)
_{57} prop = .8
58 set.seed (123)
59 train_id = sample(1:k, size = k*prop, replace = FALSE)
|_{60}| test_id = (1:k)[-which(1:k \%in\% train_id)]
61 train_set = logit_df[train_id,]
62 test_set = logit_df[ test_id,]
63 ( ( (
64
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
67 logit = glm( formula = productivity ~. ,data = train_set,family = "binomial")
68 summary (logit)
  ""
70
71
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
73 logit_best = glm( formula = productivity ~ team + over_time
                     + smv + incentive + no_of_style_change + no_of_worker|s ,
74
                     family = 'binomial', data = train_set)
75
76
577 summary(logit_best)
78 logit_pred = predict( logit_best , test_set , type = "response" )
79 tb_log = table(predict_status = logit_pred > 0.5 , true_status =
              test_set$productivity == 1
  (tb_{log}[1,1] + tb_{log}[2,2])/sum(tb_{log})
81
82
  ( ( (
83
85
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
87 glm_pred2 = predict( logit_best ,test_set )
ss glm.pred2 = prediction(glm_pred2, test_set$productivity)
89 glm.perf = performance(glm.pred2, "tpr", "fpr")
```

```
90 plot(glm.perf, main = "ROC Curve")
  abline(0, 1, lty=3)
92
  auc = as.numeric(performance(glm.pred2, "auc")@y.values)
93
94 auc
96
97
  ### LDA Model
99
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
  lda_fit = lda(formula = productivity ~. , data = train_set )
102 | lda_fit
103
104
105
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
107
  lda_pred_class = predict(lda_fit, test_set)$class
  tb_lda = table(predict_status = lda_pred_class,
               true_status=test_set$productivity)
  tb_lda
111
112
  (tb_lda[1,1] + tb_lda[2,2])/sum(tb_lda)
113
114
115
116
117 | lda_pred = predict(lda_fit, test_set)
118 | lda_pred_post = lda_pred$posterior[,2]
pred = prediction(lda_pred_post, test_set$productivity)
perf = performance(pred, "tpr", "fpr")
plot(perf, main = "ROC Curve")
122 abline (0, 1, lty=3)
auc1 = as.numeric(performance(pred, "auc")@y.values)
  auc1
126
  "
128
129
130 ### Lasso Model
131
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
133 set.seed (123)
| xmat = model.matrix(productivity ~., data = train_set )[,-1]
  xmat = apply(xmat, 2, function (x) scale(x, center=FALSE))
135
  mod.lasso = glmnet(xmat, train_set$productivity ,family = "binomial"
137
                    ,alpha=1)
  plot(mod.lasso, xvar = "lambda", label = TRUE)
139
141
  cv.out = cv.glmnet(xmat, train_set$productivity,
                   family = "binomial", alpha = 1 , nfolds=10)
143
best.lambda = cv.out$lambda.min
```

```
146 best.lambda
pcoefs = predict(mod.lasso, s = best.lambda, type = "coefficients")
  pcoefs
  xmat2 = model.matrix(productivity ~., data = test_set )[,-1]
  xmat2 = apply(xmat2, 2, function (x) scale(x, center=FALSE))
  lasso_pred = predict(mod.lasso,newx = xmat2, s=best.lambda ,
                   type = "class" )
153
  ######
154
  tb_lasso = table(predict_status = lasso_pred == '1' , true_status =
155
               test_set$productivity == 1 )
  (tb_lasso[1,1] + tb_lasso[2,2])/sum(tb_lasso)
157
158
159
  ,,,
160
161
  ### Tree Models: Classification Tree
163
164
         include=TRUE ,message=FALSE, warning=FALSE}
165
  train_set_tree = train_set %>%
166
    mutate(class_productivity = ifelse(
167
                            productivity == 1 , "Yes", "No"))%>%
168
    dplyr::select(-productivity)
169
170
  train_set_tree = train_set_tree %>%
171
    mutate_at('class_productivity', factor)
172
173
174
175
  test_set_tree = test_set %>%
176
    mutate(class_productivity = ifelse(productivity == 1 , "Yes", "No"))%>%
177
    dplyr::select(-productivity)
178
  test_set_tree = test_set_tree %>%
180
181
    mutate_at('class_productivity', factor)
182
  skim(train_set_tree)
184
mod.tree2 = tree( class_productivity ~. , data = train_set_tree )
186
  summary(mod.tree2)
187
mod.tree2
189 plot (mod.tree2)
text(mod.tree2, pretty = 0)
191
192
193
  '''{r
          include=TRUE ,message=FALSE, warning=FALSE}
195
196 set.seed (123)
197 cv.out = cv.tree(mod.tree2)
  prune.mod = prune.misclass(mod.tree2, best =
                        cv.out$size[which.min(cv.out$dev)])
199
200 summary (prune.mod)
201 prune.mod
```

```
202 plot (prune.mod)
  text(prune.mod, pretty = 0)
204
  '''{r,message=FALSE,warning=FALSE}
206
207 #Confusion matrix - Full Tree
tree_pred_class = predict(mod.tree2, newdata = test_set_tree, type = "class")
  tb_full = table(predict_status =
209
                        tree_pred_class, true_status=test_set_tree $class_productivity)
211 tb_full
  (tb_full[1,1] + tb_full[2,2])/sum(tb_full)
212
213
_{214}| #Confusion matrix - Pruned Tree
tree_pred_class = predict(prune.mod,newdata= test_set_tree, type = "class")
216 tb_prune = table(predict_status =
               tree_pred_class,true_status=test_set_tree$class_productivity)
217
218 tb_prune
  (tb_prune[1,1] + tb_prune[2,2])/sum(tb_prune)
219
221
222
223
224
  ### Tree Based Model: Bagging, Random Forest, Gradient Boosting
225
226
227
  ### Random Forest
228
         include=TRUE ,message=FALSE, warning=FALSE}
230
231 set.seed (123)
  p = ncol(train_set) - 1
232
234 rf_fit = randomForest(productivity ~ ., data = train_set,
                          mtry = round(sqrt(p)), importance = TRUE)
236 rf_fit
237 summary (rf_fit)
238 varImpPlot(rf_fit, main = "Variable Importance", type = 2 )
yhat.test_rf = predict(rf_fit, test_set, type = "class")
tb_rf = table(pred = yhat.test_rf,
242 true = test_set$productivity)
243 tb_rf
244
  (tb_rf[1,1] + tb_rf[2,2])/sum(tb_rf)
245
246
  ""
247
248 # Incentive
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
249
250 avg = data.frame( day = train_set$day[1] ,
                       quarter = train_set$quarter[1],
251
                       no_of_style_change = train_set$no_of_style_change[1],
                       team = train_set$team[1]
253
                        , smv = 24.23, wip = 1190
                       incentive = c(44,0,138,17,71)
255
                   over_time = 6508, idle_time = 1.2 ,
                       idle_men = 0.63 , no_of_workers = 52.44 )
257
```

```
_{258} # 17 = AVG - ST.D
  #71 = AVG + ST.D
260
261
262 as.tibble(avg)
263 yhat.test.rf = predict(rf_fit, avg, type = "class")
264 yhat.test.rf
266 yhat.test_rf = predict(rf_fit, test_set, type = "class")
267 tb_rf = table(pred = yhat.test_rf, true = test_set$productivity)
268 tb_rf
269
270
   ,,,
271
272 #Over time
  '''{r
         include=TRUE ,message=FALSE, warning=FALSE}
  avg = data.frame( day = train_set$day[1] ,
275
                       quarter = train_set$quarter[1],
                       no_of_style_change = train_set$no_of_style_change[1]|,
277
                       team = train_set$team[1]
278
279
                       smv = 24.23, wip = 1190,
280
                       incentive = 44
281
                       over_time = c(4567, 0, 25920, 4567 + 2864, 4567 - 2864)
282
                       idle_time = 1.2 ,
                       idle_men = 0.63 , no_of_workers = 52.44 )
284
285
286
287
288
290 as.tibble(avg)
  yhat.test.rf = predict(rf_fit, avg, type = "class")
  yhat.test.rf
294 yhat.test_rf = predict(rf_fit, test_set, type = "class")
295 tb_rf = table(pred = yhat.test_rf,
296 true = test_set$productivity)
297 tb_rf
  ""
298
  # idle_time
   '''{r include=TRUE ,message=FALSE, warning=FALSE}
        = data.frame( day = train_set$day[1] ,
301
                       quarter = train_set$quarter[1],
302
                       no_of_style_change = train_set$no_of_style_change[1],
303
                       team = train_set$team[1]
304
                       , smv = 24.23, wip = 1190,
305
                       incentive = 44 , over_time = 6508,
                       idle_{time} = c(1.2, 0, 300, 0, 1.2+16),
307
                       idle_men = 0.63
                       ,no\_of\_workers = 52.44 )
309
311
312
313
```

```
314
315 as.tibble(avg)
yhat.test.rf = predict(rf_fit, avg, type = "class")
  yhat.test.rf
318
yhat.test_rf = predict(rf_fit, test_set, type = "class")
320 tb_rf = table(pred = yhat.test_rf,
321 true = test_set$productivity)
322 tb_rf
323
324
325
326 # idle_men
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
327
  avg = data.frame( day = train_set$day[1] ,
                       quarter = train_set$quarter[1],
329
                       no_of_style_change = train_set$no_of_style_change[1],
                       team = train_set$team[1],
331
                       smv = 24.23, wip = 1190,
332
                       incentive = 44 , over_time = 6508,
333
                       idle_time = 1.2
334
                       idle_men = c(0.63, 0, 45, 0, 0.63 + 4.28)
335
                       ,no_of_workers = 52.44)
336
337
338
339
340
341
342 as.tibble(avg)
yhat.test.rf = predict(rf_fit, avg, type = "class")
  yhat.test.rf
344
346 yhat.test_rf = predict(rf_fit, test_set, type = "class")
347 tb_rf = table(pred = yhat.test_rf,
348 true = test_set$productivity)
349 tb_rf
  ""
350
351
352
353
354 # idle_men & Idle_time
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
  avg = data.frame( day = train_set$day[1] , quarter = train_set$quarter[1] ,
                   no_of_style_change =
357
                       train_set$no_of_style_change[1],
358
                       team = train_set$team[1],
359
                        smv = 24.23, wip = 1190,
360
                       incentive = 44 , over_time = 6508,
361
                       idle_{time} = c(1.2, 0, 300, 0, 1.2+16),
                       idle_men = c(0.63, 0, 45, 0, 0.63 + 4.28)
363
                       ,no\_of\_workers = 52.44)
365
366
367
368
369
```

```
370 as.tibble(avg)
yhat.test.rf = predict(rf_fit, avg, type = "class")
372 yhat.test.rf
374 yhat.test_rf = predict(rf_fit, test_set, type = "class")
375 tb_rf = table(pred = yhat.test_rf,
376 true = test_set$productivity)
  tb_rf
  ""
378
379
380
381
  #Over time + Incentives
         include=TRUE ,message=FALSE, warning=FALSE}
383
  avg = data.frame( day = train_set$day[1] ,
385
                       quarter = train_set$quarter[1],
                       no_of_style_change = train_set$no_of_style_change[1],
387
                       team = train_set$team[1]
388
                       , smv = 24.23, wip = 1190,
389
                       incentive = c (44,0 ,138, 17 , 71 )
390
                       , over_time = c( 4567 ,0, 25920, 4567+ 2864, 4567 - 2864)
391
                       , idle_{time} = 1.2 ,
392
                       idle_men = 0.63 , no_of_workers = 52.44 )
393
394
395
396
397
398
399 as.tibble(avg)
  yhat.test.rf = predict(rf_fit, avg, type = "class")
  yhat.test.rf
402
  yhat.test_rf = predict(rf_fit, test_set, type = "class")
404 tb_rf = table(pred = yhat.test_rf,
405 true = test_set$productivity)
406 tb_rf
407
   . . .
408
409
410
411
412 # Bagging Model
413
         include=TRUE ,message=FALSE, warning=FALSE}
414
415
416 set.seed (123)
_{417} p = ncol(train_set) - 1
419 bag_fit = randomForest(productivity ~ ., data = train_set,
                          mtry = p, importance = TRUE)
421 bag_fit
422 varImpPlot(bag_fit, main = "Variable Importance", type = 2)
423 #plot(bag_fit)
425
```

```
426
427
          include=TRUE ,message=FALSE, warning=FALSE}
428
  yhat.test_bag = predict(bag_fit, test_set, type = "class")
  tb_bag = table(predicted_status = yhat.test_bag,
                   true_status = test_set$productivity)
431
  tb_bag
432
433
   (tb_bag[1,1] + tb_bag[2,2])/sum(tb_bag)
435
436
437
          include=TRUE ,message=FALSE, warning=FALSE}
438
439
  fhat_rf = predict(rf_fit, newdata = test_set, type = 'class')
  tb_rf = table(predict_status= fhat_rf,
441
                  true_status = test_set$productivity)
443 tb rf
   (tb_rf[1,1] + tb_rf[2,2])/sum(tb_rf)
445
446
  #Gradient Boosting
447
448
   '''{r
         include=TRUE ,message=FALSE, warning=FALSE}
449
  library (gbm)
450
451
  set.seed (123)
452
  boost_fit = gbm( productivity ~ ., train_set, n.trees = 100, shrinkage = 0.1,
                    interaction.depth = 1,
454
                    distribution = "bernoulli")
455
456
  phat.test_boost = predict(boost_fit, test_set, type = "response")
458
  yhat.test_boost = ifelse(phat.test_boost > 0.5, 1, 0)
460
  tb_boost = table(pred = yhat.test_boost, true = test_set$productivity)
461
462
  tb_boost
463
464
  (tb\_boost[1, 1] + tb\_boost[2, 2])/sum(tb\_boost)
465
466
467
  '''{r
          include=TRUE ,message=FALSE, warning=FALSE}
468
469
470 set.seed (123)
  grid = expand.grid(
n.trees_vec = c(100, 200),
|473| shrinkage_vec = c(0.2, 0.1, 0.06, 0.05, 0.04, 0.02, 0.01),
| \text{interaction.depth\_vec} = c(1, 2, 3),
miss_classification_rate = NA,
_{476} time = NA
477 )
  ""
478
479
          include=TRUE ,message=FALSE, warning=FALSE}
481 for(i in 1:nrow(grid)){ time = system.time({
```

```
boost_fit = gbm(productivity ~ ., train_set2, n.trees = grid$n.trees_vec[i],
               shrinkage = grid$shrinkage_vec[i],
483
               interaction.depth = grid$interaction.depth_vec[i], distribution =
484
               "bernoulli", cv.folds = 5)} )
485
               grid$miss_classification_rate[i]
486
               =boost_fit$cv.error[which.min(boost_fit$cv.error)]
487
               grid$time[i] = time[["elapsed"]]
488
489
490
  grid %>% arrange(miss_classification_rate)
491
  boost_fit_best = gbm(productivity ~ ., train_set2, n.trees = 200, shrinkage = 0.05,
493
                         = 3, distribution = "bernoulli")
494
phat.test_boost_best = predict(boost_fit_best, test_set2 , type = "response")
  yhat.test_boost_best = ifelse(phat.test_boost_best > 0.5, 1, 0)
  tb_boost_best = table(pred = yhat.test_boost_best,
  true = test_set2$productivity)
499 tb boost best
  sum(diag(tb_boost_best))/sum(tb_boost_best)
501
502
503
504
505
506
507
  #### Support Vector Machine #####
508
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
510
  set.seed (123)
511
  tune_svm_linear = tune(svm, productivity ~., data = train_set, kernel =
512
                        ranges = list(cost = 10^ seq(-3, 2, length.out=6)))
  summary(tune_svm_linear)
514
  tune_svm_radial = tune(svm, productivity ~., data = train_set, kernel = "radial",
516
517
               gamma = 1, ranges = list(cost = 10^ seq(-3, 2, length.out=6)))
  summary(tune_svm_radial)
518
519
  tune_svm_poly = tune(svm, productivity ~., data = train_set,
520
                        kernel = "radial", degree = 3,
521
  ranges = list(cost = 10^ seq(-3, 2, length.out=6)))
522
  summary(tune_svm_poly)
523
  ""
524
  "'{r
         include=TRUE ,message=FALSE, warning=FALSE}
525
526
  svm_fit = svm(productivity ~., data = train_set, kernel = "linear",
527
                   cost = .1, scale = FALSE)
528
  svm_fit_radia = svm(productivity ~., data = train_set,
529
                   kernel = "radial", cost = 10, scale = FALSE)
                = svm(productivity ~., data = train_set,
  svm fit polv
531
                   kernel = "polynomial", cost = 10, scale = FALSE)
533
  summary(svm_fit)
  summary(svm_fit_poly)
  summary(svm_fit_radia)
537
```

```
"
538
539
_{540} ### Confusion Matrix for Maximal Machine Classifier,
      ####Support Vector Classifier, Support Vector Machine
541
  '''{r include=TRUE ,message=FALSE, warning=FALSE}
542
543
yhat_test = predict(svm_fit, test_set)
545 tb_svm = table(pred = yhat_test, truth = test_set$productivity)
546 tb_svm
_{547} (tb_svm[1,1] + tb_svm[2,2])/sum(tb_svm)
549 | yhat_test = predict(svm_fit_radia, test_set)
tb_svm2 = table(pred = yhat_test, truth = test_set$productivity)
551 tb_svm2
552 (tb_svm2[1,1] + tb_svm2[2,2])/sum(tb_svm2)
553
| yhat_test = predict(svm_fit_poly, test_set)
tb_svm3 = table(pred = yhat_test, truth = test_set$productivity)
556 tb_svm3
  (tb_svm3[1,1] + tb_svm3[2,2])/sum(tb_svm3)
558
559
560
561
  ""
562
```