NLP - Fall 2019 - Sample Midterm Exam

(1) **Language Models**

Ms. Malaprop would like to build a spelling corrector focused on the particular problem of *there* vs *their*. The idea is to build a model that takes a sentence as input, for example:

1. He saw their football in the park
2. He saw their was a football in the park

For each instance of *their* or *there* Ms. Malaprop wants to predict whether the true spelling should be *their* or *there*. So for sentence (1) the model should predict *their*, and for sentence (2) the model should predict *there*. Note that for the second example the model would correct the spelling mistake in the sentence. Ms. Malaprop recently took some NLP classes so she wants to use a language model for this task. Given a language model $p(w_1, \ldots, w_n)$, return the spelling that gives the highest probability under the language model. So for example for the second sentence we would implement the rule: replace *there* with *their* and vice versa and compare the language model scores:

If	p(*He saw there was a football in the park*) >
	p(*He saw their was a football in the park*)
Then	return(*there*)
Else	return(*their*)

Ms. Malaprop decides to use an unigram model: $p(w_1, \ldots, w_n) = \prod_{i=1}^{n} q(w_i)$ where $q(w_i) = \frac{\text{Count}(w_i)}{N}$ and $N = \sum_w \text{Count}(w)$. Count$(\cdot)$ returns the number of times a word was seen in the corpus and N is the sum of counts for all words in the corpus. Assume $N = 10,000$ and Count(*there*) = 110 and Count(*their*) = 50. Also assume that for every word w in the vocabulary Count$(w) > 0$.

a. What does the Ms. Malaprop rule return for *He saw their was a football in the park*?

b. Is the Ms. Malaprop rule a good solution to the *their* versus *there* problem? Say yes or no and give a short and precise one sentence justification for your answer.

(2) **Smoothing**:

Let c_{i+k}^{i} represent a sequence of characters $c_i, c_{i+1}, \ldots, c_{i+k}$. You are given a 4-gram character model: $P(c_i \mid c_{i-1}^{i-3})$. Assume that all the characters have been observed at least once in the training data such that $P(c_i)$ is never zero in unseen data.

a. Consider a backoff smoothing model $\hat{P}$ which deals with events that have been observed zero times in the training data:

$$\hat{P}(c_i \mid c_{i-1}^{i-3}) = \begin{cases} P(c_i \mid c_{i-1}^{i-3}) & \text{if } f(c_i^{i-3}) > 0 \\ P(c_i \mid c_{i-1}^{i-2}) & \text{if } f(c_i^{i-3}) = 0 \text{ and } f(c_i^{i-2}) > 0 \\ P(c_i \mid c_{i-1}) & \text{if } f(c_i^{i-2}) = 0 \text{ and } f(c_i^{i-1}) > 0 \\ P(c_i) & \text{otherwise} \end{cases}$$

where $f(c_{i+k}^{i})$ is the number of times the n-gram c_{i+k}^{i} was observed in the training data. What condition that holds in the original model $P(c_i \mid c_{i-1}^{i-3})$ is violated by $\hat{P}(c_i \mid c_{i-1}^{i-3})$?

b. The recursive definition of Jelinek-Mercer style interpolation smoothing is:

$$\hat{P}_4(c_i \mid c_{i-1}^{i-3}) = \lambda_3 \cdot P(c_i \mid c_{i-1}^{i-3}) + (1 - \lambda_3) \cdot \hat{P}_3(c_i \mid c_{i-1}^{i-2})$$

Note the difference between $P(\cdot)$ and $\hat{P}(\cdot)$ where $P(\cdot)$ is computed using the character frequencies in the training corpus. Based on the definition of $\hat{P}_4(\cdot)$ provide the definitions for $\hat{P}_3(\cdot)$, $\hat{P}_2(\cdot)$, and $\hat{P}_1(\cdot)$ using the interpolation parameters λ_2, λ_1.

c. State the condition on values assigned to $\lambda_3, \lambda_2, \lambda_1$ in Question 2b in order to ensure that $\hat{P}_4(c_i \mid c_{i-1}^{i-3})$ is a well-defined probability model.

d. Consider the bigram character model $P(c_i \mid c_{i-1})$ where

$$P(c_0, \ldots, c_n) = P(c_0) \times \prod_{i=1,2,\ldots,n} P(c_i \mid c_{i-1}) \tag{1}$$

Based on this model, for the English word *booking* the probability would be computed as:

$$P(booking) = P(b) \times P(o \mid b) \times P(o \mid o) \times P(k \mid o) \times P(i \mid k) \times P(n \mid i) \times P(g \mid n)$$

Let us assume we want to generate the suffix *ing* after the stem *book* using a separate probability:

$$P(ing) = P(i) \times P(n \mid i) \times P(g \mid n)$$

In Semitic languages, like Arabic and Hebrew, the process of inflection works a bit differently. In Arabic, for a word like *kitab* the stem would be *k-t-b* where the place-holders '-' for inflection characters have been added for convenience. We will assume that each word is made up of a sequence of consonant-vowel sequences CVCVCV… and the vowels always form the inflection.
Provide the definition of an *n*-gram model that will compute the probability for the word *kitab* and *k-t-b* as follows:

$$P(kitab) = P(k) \times P(t \mid k) \times P(b \mid t) \times P(i) \times P(a \mid i)$$

$$P(k\text{-}t\text{-}b) = P(k) \times P(t \mid k) \times P(b \mid t) \times P(\text{-}) \times P(\text{-} \mid \text{-})$$

Write down the equation for this *n*-gram model in the same mathematical notation as equation (1). You can assume that the input will be longer than some minimum length.