



**PYCON**  
INDONESIA 2018

# **Better Science Understanding With Sympy**

**(Introduction to Sympy)**

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## Overview

- **Introduction**
- Sympy Fundamentals
  - Numbers and Symbols
  - Math Expression and Evaluations
  - Lambdify, Solver, and Matrix
  - Plotting
  - Calculus
- What's next?

## Introduction

- **SymPy** is an open source Python library for symbolic mathematics
- **SymPy** was started in August 2006 by Ondrej Certik
- Why **Sympy**?
  - Standalone
  - Full featured
  - BSD licensed
  - Embraces Python
  - Usable as a library

# Introduction : Features

## ■ Core Capabilities

- ☐ Basic arithmetic: Support for operators such as  $+$ ,  $-$ ,  $*$ ,  $/$ ,  $**$  (power)
- ☐ Simplification
- ☐ Expansion
- ☐ Functions: trigonometric, hyperbolic, exponential, roots, logarithms, absolute value, spherical harmonics, factorials and gamma functions, zeta functions, polynomials, special functions, ...
- ☐ Substitution
- ☐ Numbers: arbitrary precision integers, rationals, and floats
- ☐ Noncommutative symbols
- ☐ Pattern matching

## ■ Polynomials

- ☐ Basic arithmetic: division, gcd, ...
- ☐ Factorization
- ☐ Square-free decomposition
- ☐ Gröbner bases
- ☐ Partial fraction decomposition
- ☐ Resultants

## ■ Calculus

- ☐ Limits:  $\lim_{x \rightarrow 0} x \log(x) = 0$
- ☐ Differentiation
- ☐ Integration: It uses extended Risch-Norman heuristic
- ☐ Taylor (Laurent) series

## ■ Solving equations

- ☐ Polynomial equations
- ☐ Algebraic equations
- ☐ Differential equations
- ☐ Difference equations
- ☐ Systems of equations

## ■ Combinatorics

- ☐ Permutations
- ☐ Combinations
- ☐ Partitions
- ☐ Subsets
- ☐ Permutation Groups: Polyhedral, Rubik, Symmetric, ...
- ☐ Prufer and Gray Codes

# Introduction : Features (contd.)

## ■ Discrete math

- ☐ Binomial coefficients
- ☐ Summations
- ☐ Products
- ☐ Number theory: generating prime numbers, primality testing, integer factorization, ...
- ☐ Logic expressions

## ■ Matrices

- ☐ Basic arithmetic
- ☐ Eigenvalues/eigenvectors
- ☐ Determinants
- ☐ Inversion
- ☐ Solving
- ☐ Abstract expressions

## ■ Geometric Algebra

## ■ Geometry

- ☐ points, lines, rays, segments, ellipses, circles, polygons, ...
- ☐ Intersection
- ☐ Tangency
- ☐ Similarity

## ■ Plotting

- ☐ Coordinate modes
- ☐ Plotting Geometric Entities
- ☐ 2D and 3D
- ☐ Interactive interface
- ☐ Colors

## ■ Physics

- ☐ Units
- ☐ Mechanics
- ☐ Quantum
- ☐ Gaussian Optics
- ☐ Pauli Algebra

## ■ Statistics

- ☐ Normal distributions
- ☐ Uniform distributions
- ☐ Probability

## ■ Printing

- ☐ Pretty printing: ASCII/Unicode pretty printing, LaTeX
- ☐ Code generation: C, Fortran, Python

## Introduction : Setup

The rest of the slides will be run on the virtual environment, so it won't ruin our existing python environment.

```
virtualenv --python=python3 --no-site-packages venv  
source venv/bin/activate  
pip install jupyter sympy numpy matplotlib
```

Please wait for the library installation. Once finished, start the **jupyter**.

```
jupyter notebook
```

## Introduction : Setup (contd.)

The rest of code demonstration in this workshop will use library and setup as follows :

```
from sympy import *  
import matplotlib.pyplot as plt  
import numpy as np  
  
%matplotlib notebook  
init_printing()
```

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## Sympy Fundamentals : Numbers and Symbols

Symbolic computation deals with the computation of mathematical objects symbolically. In other words, a mathematical number is represented exactly, not by approximation. If the number or expression is not evaluated, it will remain in symbolic form.

```
# Irrational number by approximation
import math
print(144/12)           # rational number
print(121/33)           # irrational number
print(math.sqrt(4))     # rational number
print(math.sqrt(12))    # irrational number
print(math.pi)          # irrational number
```

```
# Irrational number in symbolic form
display(S('144/12'))    # rational number
display(S('121/33'))    # irrational number
display(sqrt(4))         # rational number
display(sqrt(12))        # irrational number
display(pi)              # irrational number
```

## Sympy Fundamentals : Numbers and Symbols (contd.)

SymPy also allows us to define variables and compute them symbolically. Variables in SymPy must be declared beforehand. This can be done either using `symbols`, `var`, `sympify`, or `S` function.

```
x = symbols('x')
var('y')
z = S('z')
sigma = sympify('sigma')
rho = S('rho')
display(x, y, z, sigma, rho)
```

 $x$  $y$  $z$  $\sigma$  $\rho$

## Sympy Fundamentals : Numbers and Symbols (contd.)

Sympy has reserved common symbols name as defined in `sympy.abc`, so instead of declaring variables name by ourself, we can import them. Here are some of usable common

symbols : `A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z, a, alpha, b, beta, c, chi, d, delta, e, epsilon, eta, f, g, gamma, h, i, iota, j, k, kappa, l, m, mu, n, nu, o, omega, omicron, p, phi, pi, psi, q, r, rho, s, sigma, t, tau, theta, u, upsilon, v, w, x, xi, y, z, zeta`

```
from sympy.abc import delta, psi, m, i
Eq((i*delta-m)*psi, 0)
```

$$\psi(\delta i - m) = 0$$

## Sympy Fundamentals : Numbers and Symbols (contd.)

Once variables are declared, we can do further calculation and manipulation upon these variables.

```
display(x + 1)
display(x + y**2)
display(sqrt(z))
display(factor(x**3 + 2*x**2*y))
display(Eq(x + y, z))
```

$$x + 1$$

$$x + y^2$$

$$\sqrt{z}$$

$$x^2(x + 2y)$$

$$x + y = z$$

## Sympy Fundamentals : Numbers and Symbols (contd.)

Besides variables, SymPy also support mathematical and physical constants. Here are some of the common constant : `pi` , `oo` , `I` , `E`

```
display(pi) # pi  
display(oo) # infinity  
display(I)  # imaginary / complex number  
display(E)  # euler's number
```

$\pi$

$\infty$

$i$

$e$

## Sympy Fundamentals : Numbers and Symbols (contd.)

### Challenges

- Expand  $(x + 1)^2$
- Expand  $(\alpha + 4) \cdot (\beta - 4)$
- Compute  $\sqrt{-1}$
- Compute  $e^{i\pi} + 1$

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## Sympy Fundamentals : Math Expression and Evaluations

Mathematical operation in SymPy is no different with math operation in python. Sympy can both do numerical and symbolic computation. The basic mathematic equation can be expressed using following operator :

| Operator | Operation      | Example             |
|----------|----------------|---------------------|
| +        | addition       | <code>x + 1</code>  |
| -        | subtraction    | <code>x - 1</code>  |
| *        | multiplication | <code>x * 2</code>  |
| **       | exponent       | <code>x ** 3</code> |
| /        | division       | <code>x / 2</code>  |
| //       | floor division | <code>x // 2</code> |
| %        | modulo         | <code>x % 2</code>  |



## Sympy Fundamentals : Math Expression and Evaluations (contd.)

```
x, y = symbols('x, y')  
expr = x + 2  
expr + 2 * y
```

$$x + 2$$

```
expr * y
```

$$x + y + 2$$

```
expr % y
```

$$(x + 2) \bmod y$$

```
expr**2
```

$$(x + 2)^2$$

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

Mathematical expression can be assigned in to other variable and evaluated or manipulated afterward. There are dozen of function to perform various operations. Here are some of handy function :

| Function              | Operation  |
|-----------------------|--|
| <code>expand</code>   | expand mathematical expression                                   |
| <code>factor</code>   | find factor of an expression into irreducible factors            |
| <code>simplify</code> | find the intelligent simplest representation                     |
| <code>collect</code>  | collects common powers of a term in an expression                |
| <code>cancel</code>   | put expression into the standard canonical form                  |
| <code>apart</code>    | performs a partial fraction decomposition on a rational function |

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

```
#Expansion example  
expr = (x + 2)**2  
display(expr)  
display(expand(expr))
```

$$(x + 2)^2$$

$$x^2 + 4x + 4$$

```
# Factorization example  
expr = x**3 - x**2 + x - 1  
display(expr)  
display(factor(expr))
```

$$x^3 - x^2 + x - 1$$

$$(x - 1)(x^2 - 1)$$

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

```
# Simplification example
expr = (x**3 + x**2 - x - 1)/(x**2 + 2*x + 1)
display(expr)
display(factor(expr))
```

$$\frac{x^3 + x^2 - x - 1}{x^2 + 2x + 1}$$

$$x - 1$$

```
# Collect example
expr = x*y + x - 3 + 2*x**2 - y*x**2 + x**3
display(expr)
display(collect(expr, x))
```

$$x^3 - x^2y + 2x^2 + xy + x - 3$$

$$x^3 + x^2(2 - y) + x(y + 1) - 3$$

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

```
# Cancel example
expr = (x**2 + 2*x + 1)/(x**2 + x)
display(expr)
display(cancel(expr))
```

$$\frac{x^2 + 2x + 1}{x^2 + x}$$

$$\frac{x + 1}{x}$$

```
# Apart example
expr = (8*x + 7)/(x**2 + x - 2)
display(expr)
display(apart(expr))
```

$$\frac{8x + 7}{x^2 + x - 2}$$

$$\frac{3}{x + 2} + \frac{5}{x - 1}$$

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

After manipulating the mathematical expression, one of the most common things we might want to do is substitution. There are at least two way to do substitution; `subs` for substituting symbolic expression and `evalf` for evaluating numerically.

```
# Substitute variable with other variable  
expr = x**2  
expr.subs(x, y + 2)
```

```
# Substitute variable with number  
expr = x ** 3  
expr.subs(x, -1)
```

```
# Substitute multivariate expression  
expr = x ** 3 + y ** 2 + 2*x*y + 4  
expr.subs({x:1, y:2})
```

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

To evaluate a numerical expression into a floating point number, use `evalf`. SymPy can evaluate floating point expressions to arbitrary precision. By default, 15 digits of precision are used, but you can pass any number as the argument to `evalf`. Let's compute the first 50 digits of  $\pi$ .

```
print(pi.evalf())  
print(pi.evalf(20))  
print(pi.evalf(50))
```

```
3.14159265358979
```

```
3.1415926535897932385
```

```
3.1415926535897932384626433832795028841971693993751
```

## Sympy Fundamentals : Math Expression and Evaluations (contd.)

To evaluate an symbolic expression numerically, we need to combine `subs` and `evalf`.

```
expr = sin(x * pi / 180)
print(expr.subs(x, 45).evalf())
print(expr.evalf(subs={x:45})) # preferred
```

0.707106781186548

0.707106781186548



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## Sympy Fundamentals : Lambdify, Solver, and Matrix

Function `evalf` are good for evaluating a mathematical function at a single point, but it is typically more convenient to turn the symbolic expression to reusable numerical function. Let me show you the inconvenience as follows,

```
var('x')
inputs = np.linspace(1, 10, 10)

f = x**2
f(1) # error, not callable
f(inputs) # even not possible
```

Error object is not callable

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

To overcome this, `lambdify` takes in a symbolic variable (or list of variables) and an expression, then returns a callable function that corresponds to the expression.

```
var('x, y')
g = lambdify(x, x**2)
h = lambdify((x, y), x+y)
print(g(0), g(10), g(100)) # become callable
print(h(2, 3), h(0.1, 3.14)) # much more convenient
```

```
0 100 10000
```

```
5 3.24
```

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

`lambdify` has `module` input argument to define how the computation behaves. It maps the symbolic function in to numerical implementation. We can use either `sympy` , `numpy` , `math` , `numexpr` , or `mpmath` . If not specified differently by the user, SymPy functions are replaced as far as possible by either `python-math` , `numpy` (if available) or `mpmath` functions - exactly in this order. The choice also determine computational speed.

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

```
points = np.random.random(20000)
expr = sinh(x)

# Time using evalf() on each of the random points.
%time _ = [expr.subs(x, pt).evalf() for pt in points]

# Lambdify the expression and time using the resulting function.
f = lambdify(x, expr)
%time _ = [f(pt) for pt in points]

# Lambdify the expression and time using the default module order.
f = lambdify(x, expr)
%time _ = f(points)

# Lambdify the expression and time using only numpy module.
f = lambdify(x, expr, "numpy")
%time _ = f(points)
```

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

CPU times: user 9.3 s, sys: 518  $\mu$ s, total: 9.3 s

Wall time: 9.31 s

CPU times: user 24.5 ms, sys: 0 ns, total: 24.5 ms

Wall time: 24.5 ms

CPU times: user 855  $\mu$ s, sys: 0 ns, total: 855  $\mu$ s

Wall time: 582  $\mu$ s

CPU times: user 738  $\mu$ s, sys: 0 ns, total: 738  $\mu$ s

Wall time: 465  $\mu$ s

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

A SymPy expression by itself is not an equation. However, `solve` equates an expression with zero and solves for a specified variable.

```
expr = x**2 - 4
display(expr) # right-hand side is equated as zero
solve(expr, x)
```

$$x^2 - 4$$
$$[-2, 2]$$

We can also define both sides using `Eq` instead of assuming the right hand-side to be zero.

```
expr = Eq(x**2, 4)
display(expr) # two sides equation
solve(expr, x)
```

$$x^2 - 4$$
$$[-2, 2]$$

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

Sometimes we also calculate systems of equation. For example a system of linear equation as following

$$\begin{array}{rcrcrcrcrcrl} x & + & y & + & z & = & 5 \\ 2x & + & 3y & + & 2z & = & 2 \\ 7x & + & y & + & 6z & = & 12 \end{array}$$

We can rewrite in sympy and find the solutions.

```
var('x, y, z')
M = Matrix([
    [1, 1, 1, 5],
    [2, 3, 2, 2],
    [7, 1, 6, 12]
])
solve_linear_system(M, x, y, z)
```

$$\{x : -58, \quad y : -8, \quad z : 71\}$$



## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

SymPy matrices support the standard matrix operations of addition `+`, subtraction `-`, and multiplication `*`. Additionally, SymPy matrices are equipped with many useful methods, some of which are listed below. See <http://docs.sympy.org/latest/modules/matrices/matrices.html> for more methods and examples.

| Method                    | Return  |
|---------------------------|---|
| <code>det()</code>        | The determinant.                                      |
| <code>eigenvals()</code>  | The eigenvalues and their multiplicities.             |
| <code>eigenvects()</code> | The eigenvectors and their corresponding eigenvalues. |
| <code>inv()</code>        | The matrix inverse.                                   |
| <code>norm()</code>       | The Frobenius, $\infty$ , 1, or 2 norm.               |
| <code>T</code>            | The transpose.  |

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

```
# Example of matrix
A = Matrix([[1, 2],[3, 4]])

display(A, T)
display(A.T)
display(A.norm())
display(A * A.inv())
```

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$$

$$\sqrt{30}$$

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

```
# Example of symbolic matrix
var('a, b, c, d')
B = Matrix([[a, b],[c, d]])

display(B)
display(B.inv())
```

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$\begin{bmatrix} \frac{d}{ad-bc} & -\frac{b}{ad-bc} \\ -\frac{c}{ad-bc} & \frac{a}{ad-bc} \end{bmatrix}$$

## Sympy Fundamentals : Lambdify, Solver, and Matrix (contd.)

### Challenges

- Solve  $x$  for  $\sqrt{x - 8} = 3$
- Solve  $x$  for  $|2x - 1| = 5$
- Solve  $x$  for  $e^x = 72$

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## Sympy Fundamentals : Plotting

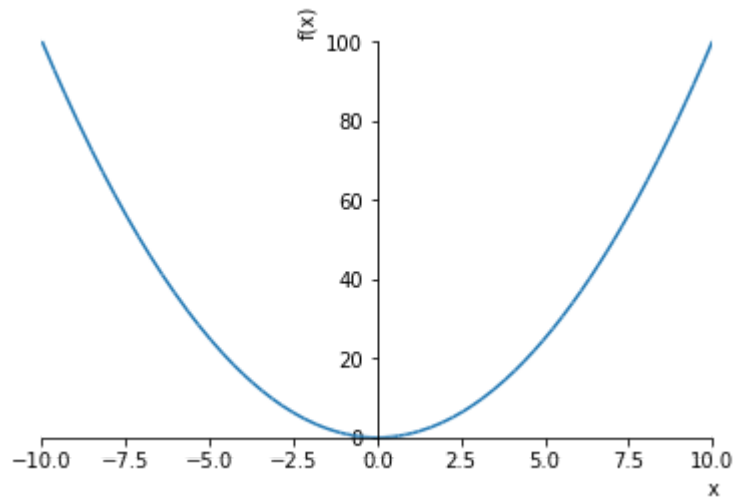
The plotting module allows you to make 2-dimensional and 3-dimensional plots. Presently the plots are rendered using matplotlib as a backend. It is also possible to plot 2-dimensional plots using a TextBackend if you don't have matplotlib.

The plotting module has the following functions:

- `plot` : Plots line plots.
- `plot_parametric` : Plots 2D parametric plots.
- `plot3d` : Plots 3D plots of functions in two variables.
- `plot_implicit` : Plots 2D implicit and region plots.
- `plot3d_parametric_line` : Plots 3D line plots, defined by a parameter.
- `plot3d_parametric_surface` : Plots 3D parametric surface plots.

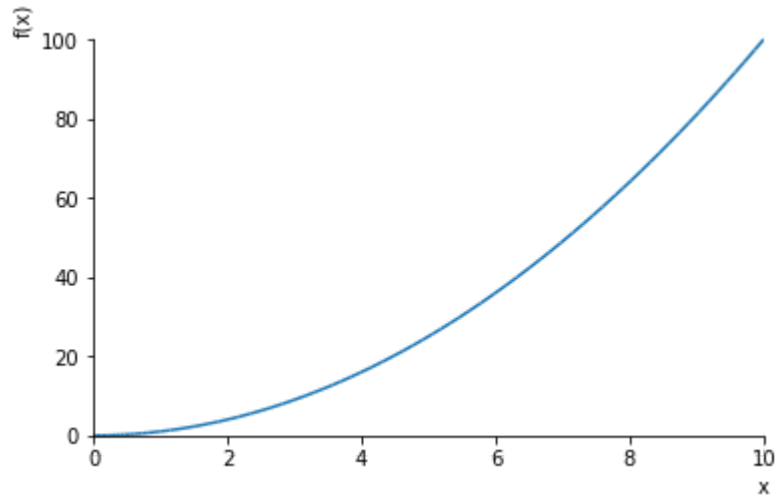
## Sympy Fundamentals : Plotting (contd.)

```
# Plot  
var('x')  
plot(x**2)
```



## Sympy Fundamentals : Plotting (contd.)

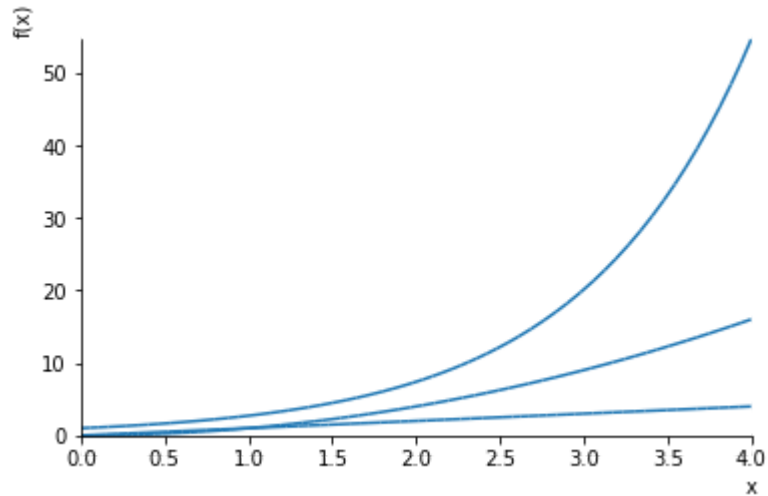
```
# Plot with range  
plot(x**2, (x, 0, 10))
```





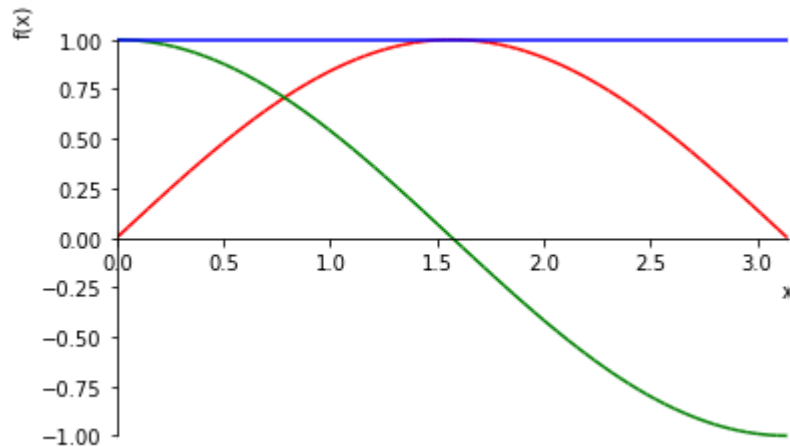
## Sympy Fundamentals : Plotting (contd.)

```
# Multiple plot  
p = plot(E**x, x**2, x, (x, 0, 4))
```



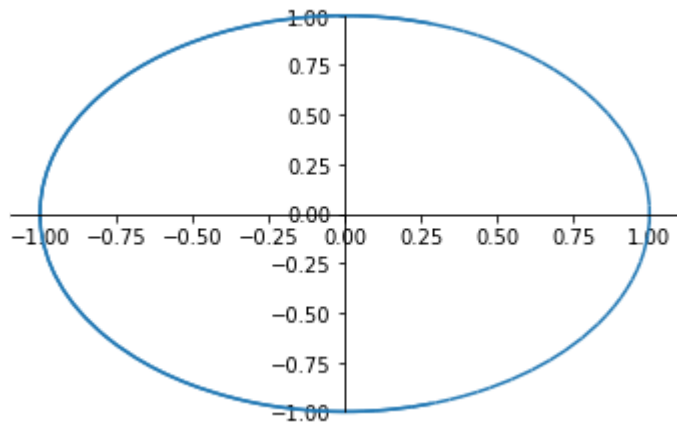
## Sympy Fundamentals : Plotting (contd.)

```
# Multiple plot with color  
p = plot(sin(x), cos(x), cos(x)**2 + sin(x)**2, (x, 0, pi), show=false)  
  
p[0].line_color = 'r'  
p[1].line_color = 'g'  
p[2].line_color = 'b'  
  
p.show()
```



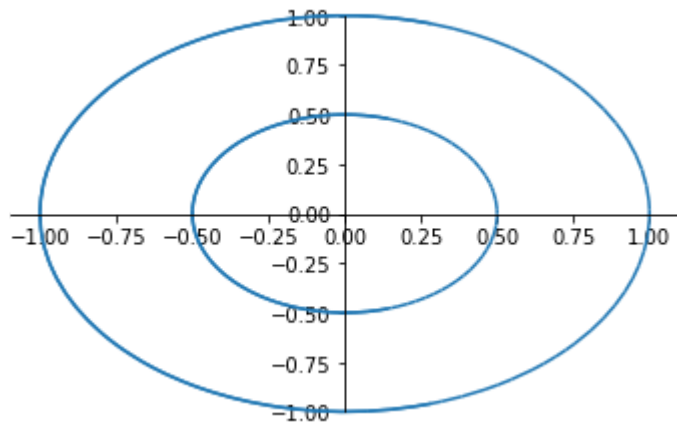
## Sympy Fundamentals : Plotting (contd.)

```
# Single parametric plot  
plotting.plot_parametric(cos(x), sin(x), (x, -5, 5))
```



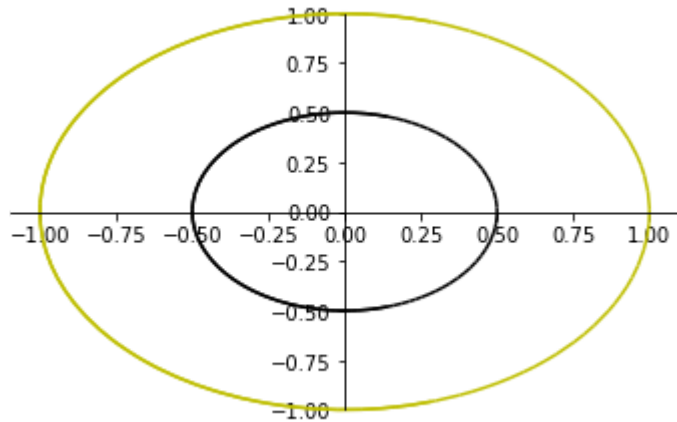
## Sympy Fundamentals : Plotting (contd.)

```
# Multiple plot  
plotting.plot_parametric((cos(x), sin(x)), (0.5*cos(x), 0.5*sin(x)), (x, -5, 5))
```



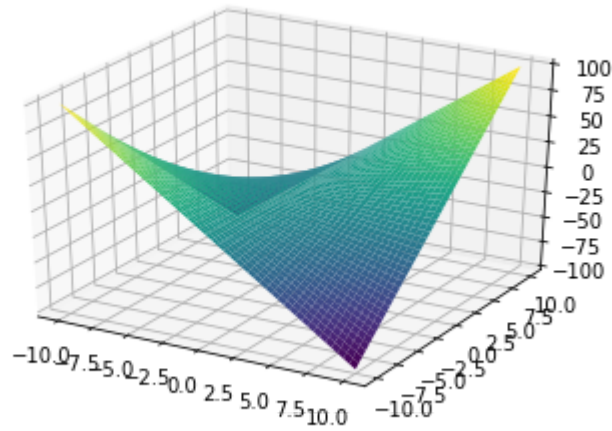
## Sympy Fundamentals : Plotting (contd.)

```
# Multiple plot with different color  
p = plotting.plot_parametric((cos(x), sin(x)), (0.5*cos(x), 0.5*sin(x)), (x, -5, 5)  
  
p[0].line_color = 'y'  
p[1].line_color = 'k'  
  
p.show()
```



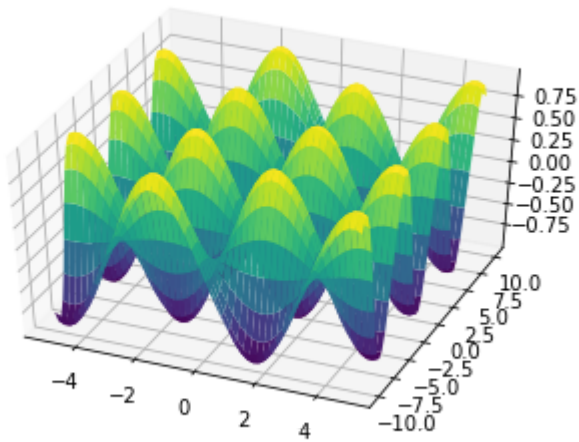
## Sympy Fundamentals : Plotting (contd.)

```
var('x,y')  
plotting.plot3d(x*y)
```



## Sympy Fundamentals : Plotting (contd.)

```
plotting.plot3d(sin(x)*cos(y), (x, -5, 5), (y, -10, 10))
```



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## **Sympy Fundamentals : Calculus**

In SymPy we are allowed to perform standard calculus operations, including derivatives, integrals, and limits. Like other elements of SymPy, calculus operations can be temporally expensive, but they give exact solutions whenever solutions exist.

## Sympy Fundamentals : Calculus (contd.)

### Differentiation

We can do differentiation in two ways in Sympy, first the unevaluated form using `Derivative` function and immediate evaluation using `diff` function. While using `Derivative`, we need to execute `doit` function to evaluate the derivation.

# Sympy Fundamentals : Calculus (contd.)

## Differentiation

```
# Unevaluated derivation  
  
var('alpha')  
f = cos(alpha)**2  
  
df = Derivative(f, alpha)  
display(df)  
  
display(df.doit())
```

$$\frac{d}{d\alpha} \cos^2(\alpha)$$

$$-2 \sin(\alpha) \cos(\alpha)$$

## Sympy Fundamentals : Calculus (contd.)

### Differentiation

```
# Immediate derivation

df = diff(f, alpha)
display(df)

df = f.diff(alpha) # alternative
display(df)
```

$$-2 \sin(\alpha) \cos(\alpha)$$

$$-2 \sin(\alpha) \cos(\alpha)$$

## Sympy Fundamentals : Calculus (contd.)

### Integrals

With the same fashion with differentiation, integration also poses two way of computation, `Integral` and `integrate` ; the unevaluated and immediate evaluation respectively. Note that in Sympy indefinite integrals will not preceeded by constants :D

## Sympy Fundamentals : Calculus (contd.)

### Integrals

```
# Unvealed integration  
  
var('beta')  
f = tanh(beta)  
  
F = Integral(f, beta)  
display(F)  
  
display(F.doit())
```

$$\int \tanh(\beta) d\beta$$

$$\beta - \log(\tanh(\beta) + 1)$$

## Sympy Fundamentals : Calculus (contd.)

### Integrals

```
# Immediate integration

F = integrate(f, beta)
display(F)

F = f.integrate(beta) # alternative
display(F)
```

$$\beta - \log(\tanh(\beta) + 1)$$

$$\beta - \log(\tanh(\beta) + 1)$$

# Sympy Fundamentals : Calculus (contd.)

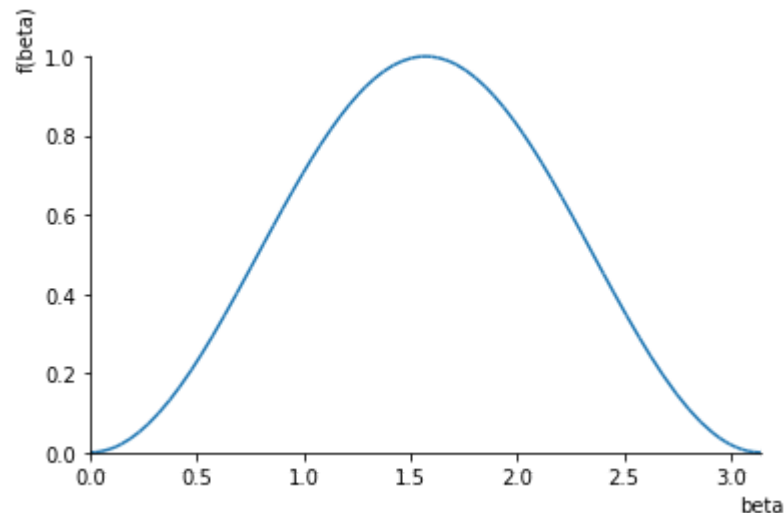
## Integrals

We can do finite integration by giving bounds to the integral expression

```
f = sin(beta)**2  
integrate(f, (beta, 0, pi))
```

$$\frac{\pi}{2}$$

```
plot(f, (beta, 0, pi))
```





## Limits

Limits can be expressed, similar to derivatives or integrals, with `Limit`. Alternatively, `limit` evaluates a limit directly.

```
# Unevaluated limits
var('x')

f = 1/x

lf = Limit(f, x, 0)
display(lf)

display(lf.doit())

# Immediate evaluation of limits
limit(f, x, 0)
```

$$\lim_{x \rightarrow 0^+} \frac{1}{x}$$

$\infty$

$\infty$

## Sympy Fundamentals : Calculus (contd.)

### Challenges

- Find the differential of  $\frac{x^2}{\sin(x)}$  over  $x$
- Find maximum and minimum values of  $f(x) = 2x^3 - 3x^2 - 6$
- Calculate  $\int \frac{s^2 + 1}{s^2 - 1} ds$
- Evaluate  $\lim_{z \rightarrow 4} \frac{\sqrt{z} - 2}{z - 4}$

## Overview

- Introduction
- Sympy Fundamentals
  - Numbers and Symbols
  - Math Expression and Evaluations
  - Lambdify, Solver, and Matrix
  - Plotting
  - Calculus
- **What's next?**

## What's next?

Here we have demonstrated the SymPy fundamentals. There are still a lot of things to explore in SymPy including physics, statistics, units, geometry, and so forth. Yet the most important thing is to start making use of SymPy to work smarter and understand better.

**This slideshow and all the materials can be accessed via**

**`https://github.com/linerocks/pyconid18`**

## References\*

- [www.sympy.org](http://www.sympy.org)
- [docs.sympy.org](http://docs.sympy.org)
- [mattpap.github.io/scipy-2011-tutorial/html/](http://mattpap.github.io/scipy-2011-tutorial/html/)
- [www.sympy.org/scipy-2016-tutorial/](http://www.sympy.org/scipy-2016-tutorial/)
- and many more...

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