

Assignment 2 8/31/2022

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1] (a) $(\pi < 0) \wedge (\pi < 10)$

$\hookrightarrow \boxed{0 < \pi < 10}$

(b) $(p \geq 7) \wedge (p < 12)$

$\boxed{7 \leq p < 12}$

(c) $(x > 5) \wedge (x < 7) \rightarrow \boxed{5 < x < 7}$

(d) $(x < 4) \wedge (x < 6) \rightarrow \boxed{x < 4}$

(e) $(y < 4) \wedge (y^2 < 9)$

$\hookrightarrow (y < 4) \wedge (y > -3) \wedge (y < 3)$

$\boxed{-3 < y < 3}$

(f) $(x \geq 0) \wedge (x \leq 0) \rightarrow \boxed{x = 0}$

2] (a) 0 is less than π and π is less than 10

(b) 7 is less than or equal to p and p is less than 12

(c) 5 is less than x and x is less than 7

(d) x is less than 4

(e) 3 is less than y and y is less than 5

(f) x is 0

3] To prove that $\phi_1 \wedge \phi_2 \wedge \dots \wedge \phi_n$ is true, prove ϕ_p is true $\forall p \in [1, n]$

4] To prove that $\phi_1 \wedge \phi_2 \wedge \dots \wedge \phi_n$ is false, prove $\exists p \in [1, n]$ such that ϕ_p is false.

5] $(\pi > 3) \vee (\pi > 10) \rightarrow \boxed{\pi > 3}$

(b) $(x < 0) \vee (x > 0) \rightarrow \boxed{\{x \in \mathbb{R} \mid x \neq 0\}}$

(c) $\boxed{x \geq 0}$

(d) $\boxed{x \geq 0}$

(e) $(x > 3) \vee [(x > 3) \wedge (x < -3)]$
 $x > 3 \vee x < -3$

~~$\boxed{x > 3 \wedge x < -3}$~~

6] (a) π is greater than 3

(b) x is not equal to 0

(c) x is greater than or equal to 0

(d) " " (e) x is greater than 3 or x is less than -3

7] $\phi_1 \vee \phi_2 \vee \dots \vee \phi_n$ is true if $\exists p \in [1, n]$ such that ϕ_p is true.

8] $\phi_1 \vee \phi_2 \vee \dots \vee \phi_n$ is false if ϕ_p is false $\forall p \in [1, n]$

9] (a) $\pi \leq 3.2$ (b) $x \geq 0$ (c) ~~$\boxed{x = 0}$~~

(d) $x \neq 1$ (e) ψ

10] (a) π is less than or equal to ~~3~~ 2.

(b) x is greater than or equal to 0

(c) x is zero

(d) x is not 1

(e) ψ

III) $D = \text{"The dollar is strong"}$

$Y = \text{"The Yuan is strong"}$

$T = \text{"New US-China trade agreement signed"}$

(a) $\boxed{D \wedge Y}$ (b) $\boxed{T \wedge \neg Y \wedge D}$

(c) $\boxed{\neg(D \wedge Y)}$

(d) $\boxed{T \wedge D \wedge Y}$

(e) $\boxed{\neg T \wedge D \wedge Y}$