



Bhartiya Vidya Bhavan's  
**Sardar Patel Institute of Technology**  
 (Autonomous Institute Affiliated to University of Mumbai)  
Department of Master of Computer Application

**MSE Oct 2022**

Max. Marks: 20

Class: FYMCA

Course Code: MA503

Subject: Probability and Statistics

Duration: 1 hr

Semester: II

Date: 18 / 10 /2022

Time: –

Instructions: (1) Attempt any FOUR questions.  
 (2) Use of non-programmable scientific calculator is allowed.  
 (3) Assume any necessary data but justify the same.

Q.N		Marks	CO																
1.	<p>A binary communication channel carries data as one of two types of signals denoted by 0 and 1. Owing to noise, a transmitted 0 is sometimes received as 1 and a transmitted 1 is sometimes received as 0. For a given channel, assume a probability of 0.94 that a transmitted 0 is correctly received as a 0 and a probability of 0.91 that a transmitted 1 is correctly received as a 1. Further assume a probability of 0.45 of transferring a 0. If a signal is sent, determine probability of an error.</p>	[5]	3																
2.	<p>Two discrete random variables X and Y have joint pmf given by the following table.</p> <table border="1" style="margin: 10px auto;"> <tr> <td style="text-align: center;">Y X \</td><td style="text-align: center;">1</td><td style="text-align: center;">2</td><td style="text-align: center;">3</td></tr> <tr> <td style="text-align: center;">1</td><td style="text-align: center;">2/16</td><td style="text-align: center;">2/16</td><td style="text-align: center;">1/16</td></tr> <tr> <td style="text-align: center;">2</td><td style="text-align: center;">3/16</td><td style="text-align: center;">2/16</td><td style="text-align: center;">1/16</td></tr> <tr> <td style="text-align: center;">3</td><td style="text-align: center;">2/16</td><td style="text-align: center;">1/16</td><td style="text-align: center;">2/16</td></tr> </table> <p>Compute the probability that: (i) <math>X \leq 1\frac{1}{2}</math> (ii) XY is even</p>	Y X \	1	2	3	1	2/16	2/16	1/16	2	3/16	2/16	1/16	3	2/16	1/16	2/16	[5]	3
Y X \	1	2	3																
1	2/16	2/16	1/16																
2	3/16	2/16	1/16																
3	2/16	1/16	2/16																
3.	<p>The number of hardware failure system in a week of operation has the following probability mass function.</p> <table border="1" style="margin: 10px auto;"> <tr> <td style="text-align: center;">No. of failures</td><td style="text-align: center;">0</td><td style="text-align: center;">1</td><td style="text-align: center;">2</td><td style="text-align: center;">3</td><td style="text-align: center;">4</td><td style="text-align: center;">5</td><td style="text-align: center;">6</td></tr> <tr> <td style="text-align: center;">Probability</td><td style="text-align: center;">0.18</td><td style="text-align: center;">0.28</td><td style="text-align: center;">0.25</td><td style="text-align: center;">0.18</td><td style="text-align: center;">0.06</td><td style="text-align: center;">0.04</td><td style="text-align: center;">0.01</td></tr> </table> <p>Find the expectation and variance of the number of failure.</p> <p><b>OR</b></p> <p>Let X be a random variable for which <math>E(X)=10</math> and <math>V(X)=25</math>. Find the values of a and b such that <math>Y=aX-b</math> has expectation zero and variance 1.</p>	No. of failures	0	1	2	3	4	5	6	Probability	0.18	0.28	0.25	0.18	0.06	0.04	0.01	[5]	3
No. of failures	0	1	2	3	4	5	6												
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4	<p>It is given that 2% of the electric bulbs manufactured by a company are defective. Using Poisson distribution, find the probability that a sample of 200 bulbs will contain (i) no defective bulbs (ii) 2 defective bulbs.</p> <p><b>OR</b></p> <p>The mean and variance of binomial distribution are 4 and <math>\frac{4}{3}</math> respectively. Find <math>P(x \geq 1)</math>.</p>	[5]	4																