Dependency preservation Example

Decomposition $D = \{R_1, R_2, R_3,..., R_m\}$ of R is said to be dependency-preserving with respect to F if the union of the projections of F on each R_i , in D is equivalent to F. In other words, $R \subset \text{join of } R_1$, $R_1 \text{over } X$.

Example 1: Let a relation R(A,B,C,D) and set a FDs $F = \{ A \rightarrow B , A \rightarrow C , C \rightarrow D \}$ are given.

A relation R is decomposed into -

$$R_1 = (A, B, C)$$
 with FDs $F_1 = \{A -> B, A -> C\}$, and

$$R_2 = (C, D)$$
 with FDs $F_2 = \{C \rightarrow D\}$.

$$F' = F_1 \cup F_2 = \{A -> B, A -> C, C -> D\}$$

so,
$$F' = F$$
.

And so,
$$F'_+ = F_+$$
.

Example 2: R(A,B,C) is decomposed into R1(A,B) and R2(B,C)
The relation R contains following data.

| A | В | С |
|---|---|---|
| 1 | 1 | 1 |
| 2 | 1 | 2 |
| 3 | 2 | 1 |
| 4 | 2 | 2 |

Answer:

Here the FD's for R, $F = \{ A \rightarrow B, A \rightarrow C, BC \rightarrow A \}$

Now for R1(A,B) the relation would be

| Α | В |
|---|---|
| 1 | 1 |
| 2 | 1 |
| 3 | 2 |
| 4 | 2 |

Hence, $F1 = \{ A \rightarrow B \}$

Now for R2(B,C) the relation would be

| В | С |
|---|---|
| 1 | 1 |
| 1 | 2 |
| 2 | 1 |
| 2 | 2 |

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Here, F != F1 U F2
Hence the relation is not dependency preserved.
Example 3: R(A,B,C,D,E) and F = \{A -> B, B -> C, C -> D, D -> A\}
            and R1(A,B,C) and R2(C,D,E)
Answer:
            For R1(A,B,C) we will find F1
             We need to find closure of A,B,C
             A+=\{A, B, C, -D\} hence FD will be A->BC
             B+ = \{ B,C,D,A \} hence FD will be B -> CA
             C + = \{C, D, A, B\} hence FD will be C \rightarrow AB
             AB+ = \{A,B,C,D\} hence FD will be AB -> C duplicate FD as A -> C and definitely
AB-> C. Hence we will discard it.
             AC+ = \{A, C, B, D\} hence FD will b AC -> B hence duplicated
             BC + = \{B,C,D,A\} hence FD will be BC -> A hence duplicated.
             ABC+ no need to calculate as it is trivial dependency,
            Hence F1 = \{ A -> BC, B -> CA, C -> AB \}
             For R2(C,D,E) we will find F2
             C + = \{C, D, A, B\} hence FD will be C \rightarrow D
             D+ = \{D,A,B,C\} hence FD will be D -> C
             E + = \{E\}
             CD + = \{ C, D, A, B \}
             DE + = \{D, E, A, B, C\} hence FD will be DE -> C which is duplicated as D -> C.
             CE + = \{C, E, D, A, B\} hence FD will be CE \rightarrow D duplicated as C \rightarrow D
             Hence F2 = \{ C \rightarrow D, D \rightarrow C \}
            For dependency preservation, F = F1 U F2
                F1 U F2 = \{ A \rightarrow BC, B \rightarrow CA, C \rightarrow AB, C \rightarrow D, D \rightarrow C \}
                Simplified F1 U F2 after applying Armstrong's axiom:
                F1 U F2 = \{ A \rightarrow B, A \rightarrow C, B \rightarrow C, B \rightarrow A, C \rightarrow A, C \rightarrow B, C \rightarrow D, D \rightarrow C \}
                F = \{ A -> B, B -> C, C -> D, D -> A \}
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Hence $F2 = \{ \}$

For, A -> B, B -> C, C-> D they are part of F1 U F2 but D-> A is not a part of F1 U F2, Hence find D+ from F1 U F2

 $D+ = \{D,C,A,B\}$ here A is in closure of D hence D -> A is already preserved.

Hence This relation R is dependency preserved.