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## **Basic Psychrometry**

**Relative Humidity:** RH = 
$$\frac{P_W}{P_{WS}} \times 100\%$$

- Saturation Vapor Pressure: P<sub>WS</sub>
- Vapor Pressure: P<sub>W</sub>

Absolute Humidity: 
$$\rho_v = \frac{m_{H_2O}}{V_{net}}$$

$$\rho_v = \frac{P_w \times M_W}{R \times T_K}$$

- Universal Gas Constant: R
- Molar mass of water: M<sub>w</sub>
- Temperature in Kelvin: T<sub>K</sub>

**Dew Point:** 
$$T_d = \frac{c \times ln(\frac{P_W}{a})}{b - ln(\frac{P_W}{a})}$$

• Constants: a, b, c

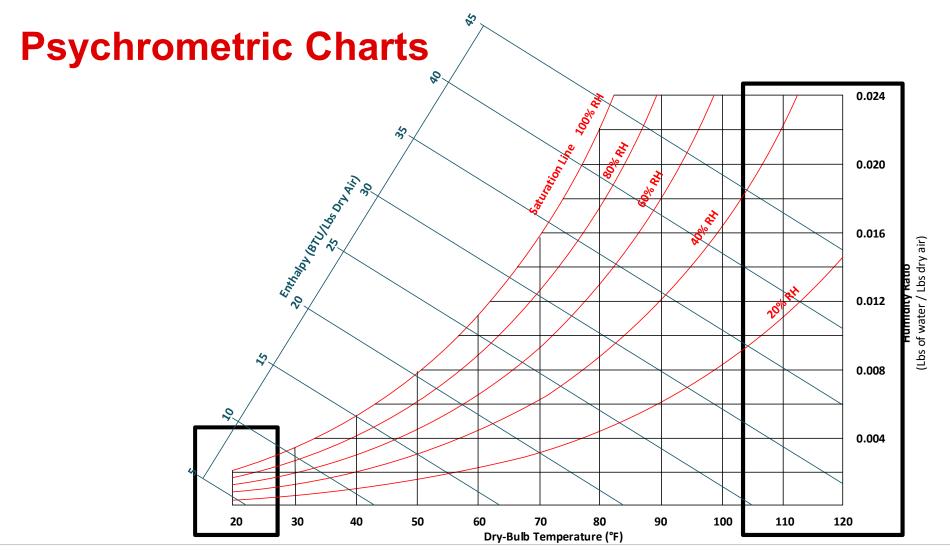
Mixing Ratio: 
$$X = \frac{M_{H20}}{M_{air}} \times \frac{P_W}{P_{amb} - P_W}$$

- Molecular Weight of water: M<sub>H20</sub>
- Molecular Weight of air: Mair
- Total Ambient Pressure: P<sub>amb</sub>

Enthalpy:  $h = T \times (1.01 + 0.00189X) + 2.5X$ 

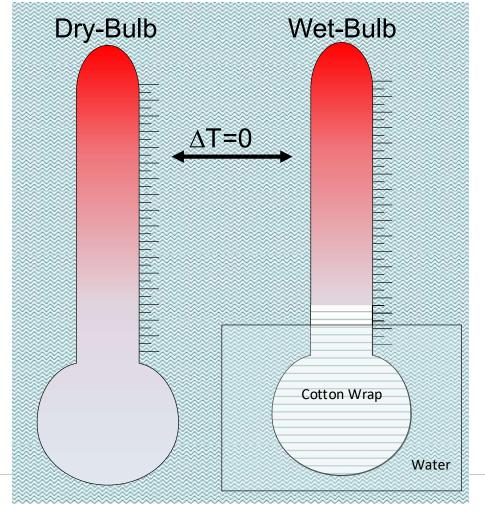
Temperature in Celsius: T

**Dry Bulb Temperature Wet Bulb Temperature** 





## **Psychrometers**



## Psychrometric Formulas Ferrel Equation:

$$P_{W} = P'_{WS} - A * P * (T - T_{W})$$

$$A = (f + gT_{W}), f & g \text{ are Constants}$$

$$P'_{WS} = P_{WS}(T_{W})$$
[1]

#### **Apjohn Equation:**

$$P_W = P'_{WS} - P * B/755 * (T - T_W)$$
  
B = 0.5 or 0.44 for frozen °C<sup>-1</sup> [2]

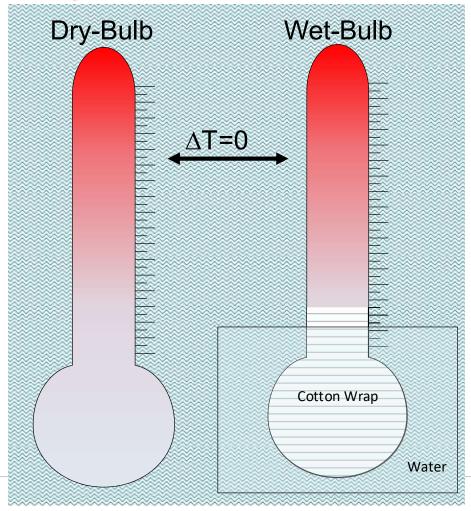
#### **Carrier Equation:**

$$P_W = P'_{WS} - \frac{(P - P'_{WS})(T - T_W)}{1527.4 - 1.3T_W}$$
 [2]

#### In General:

$$P_W = P'_{WS} - C * f(P, T, T_W)$$
  
 $f(P, T, T_W) = 0 \text{ when } (T - T_W) = 0$ 

## **Psychrometers**



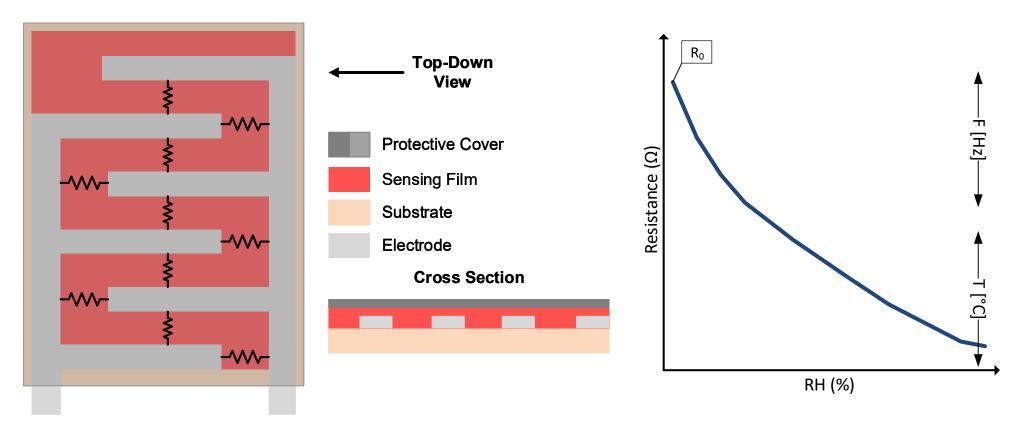
#### **Advantages:**

- No power required
- Wide Temperature and humidity range
- No drift
- Very low Hysteresis

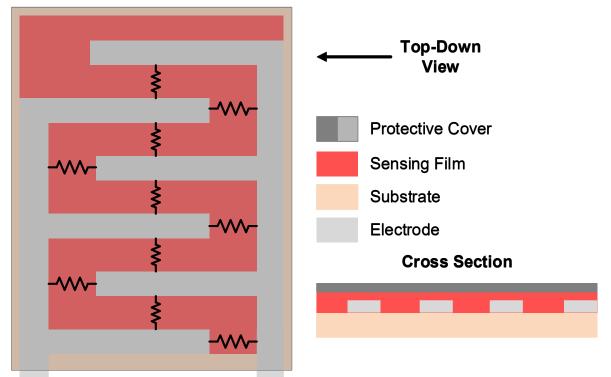
#### **Disadvantages:**

- Complex and expensive
- Requires regular maintenance

## **Resistive Humidity Sensors**



## **Resistive Humidity Sensors**

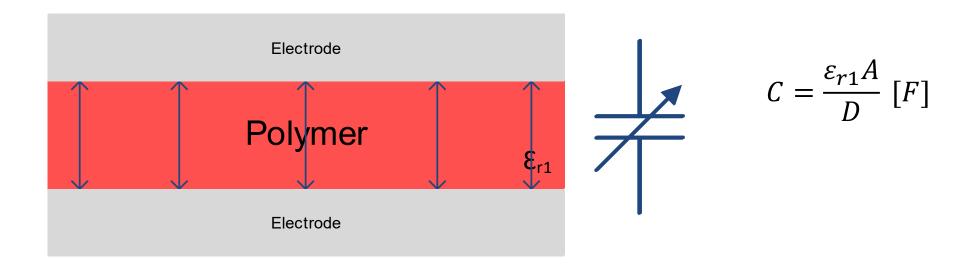


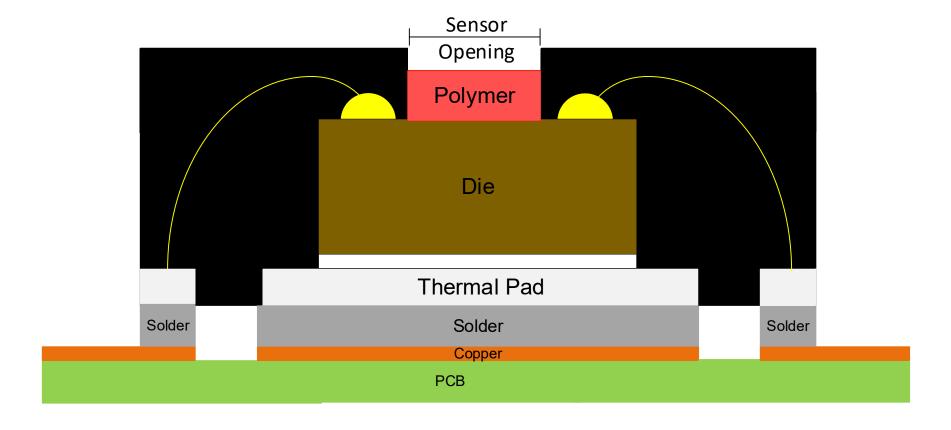
#### **Advantages:**

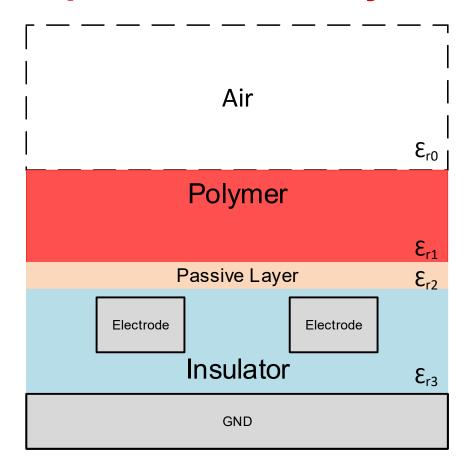
- Low Cost
- Easily interchangeable

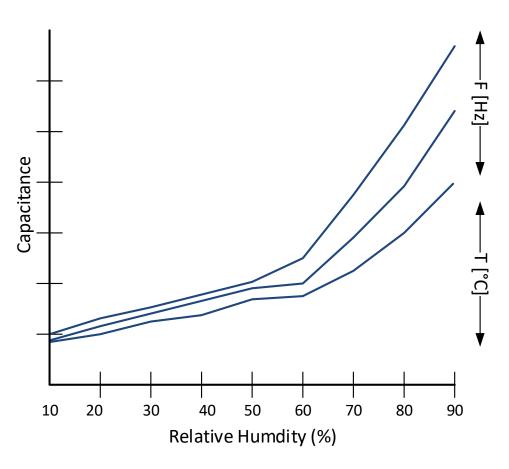
#### **Disadvantages:**

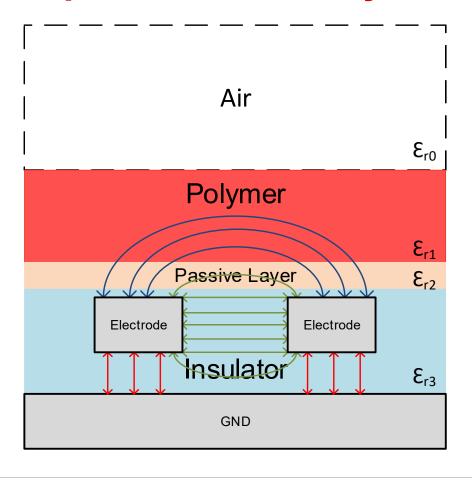
- Limited RH Range (above 15%)
- Strong temperature & Frequency dependence
- Sensitive to contamination
- Poor stability











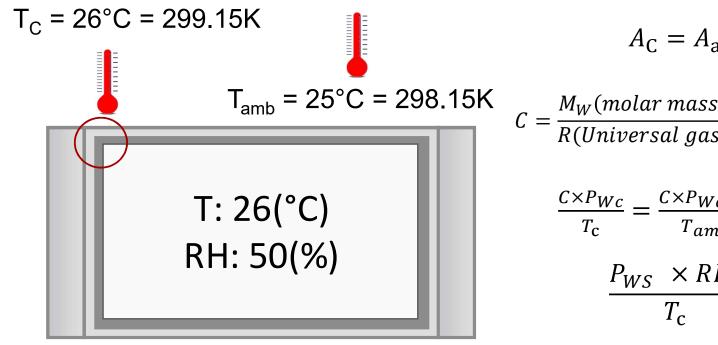
#### **Advantages:**

- Low Cost
- Good Humidity Range
- Small Hysteresis (typ. 1% or less)
- Fast Response Time
- Ease of manufacturing and integration

#### **Disadvantages:**

- Low accuracy below 5% RH
- Additional circuitry required to sample capacitance and convert to RH
- Exposed sensing polymer is sensitive to chemical contamination

## **Application: Compensating for Case Temperature**



$$A_{C} = A_{amb} \qquad A_{X} = \frac{C \times P_{Wx}}{T_{X}}$$

$$C = \frac{M_{W}(molar\ mass\ of\ water)}{R(Universal\ gas\ constant)} = \frac{18.01528 \frac{g}{mol}}{8.3145 \frac{J}{mol * K}}$$

$$\frac{C \times P_{Wc}}{T_{C}} = \frac{C \times P_{Wam}}{T_{amb}} \quad RH_{X} = \frac{P_{WX}}{P_{Wsx}} \times 100\%$$

$$\frac{P_{WS}}{T_{C}} \times RH_{C}}{T_{C}} = \frac{P_{WSamb}}{T_{amb}} \times RH_{amb}$$

$$RH_{amb} = \frac{P_{WSc}}{P_{WSamb}} \times \frac{T_{amb}}{T_{C}} \times H_{C}$$

Note: Temperature ratio should calculated in Kelvin, if used.

# To find more humidity sensor resources and products, visit ti.com/humidity

#### References

[1] National Aeronautics and Space Administration, 1977. *Equations For The Determination Of Humidity From Dewpoint And Psychrometric Data*. Edwards: N.A.S.A., pp.2-15.

[2] Ramgopal, Lesson 27 Psychrometry, 1st ed. Kharagpur: IIT, 2006, pp. 1-16.