

## 数据库系统原理

## Database System Principle

#### 邵蓥侠

Email: shaoyx@bupt.edu.cn

北京邮电大学计算机学院

计算机应用技术中心



## PART 2

## RELATIONAL DATABASES



## Chapter 7

# Relational-Database Design schema normalization



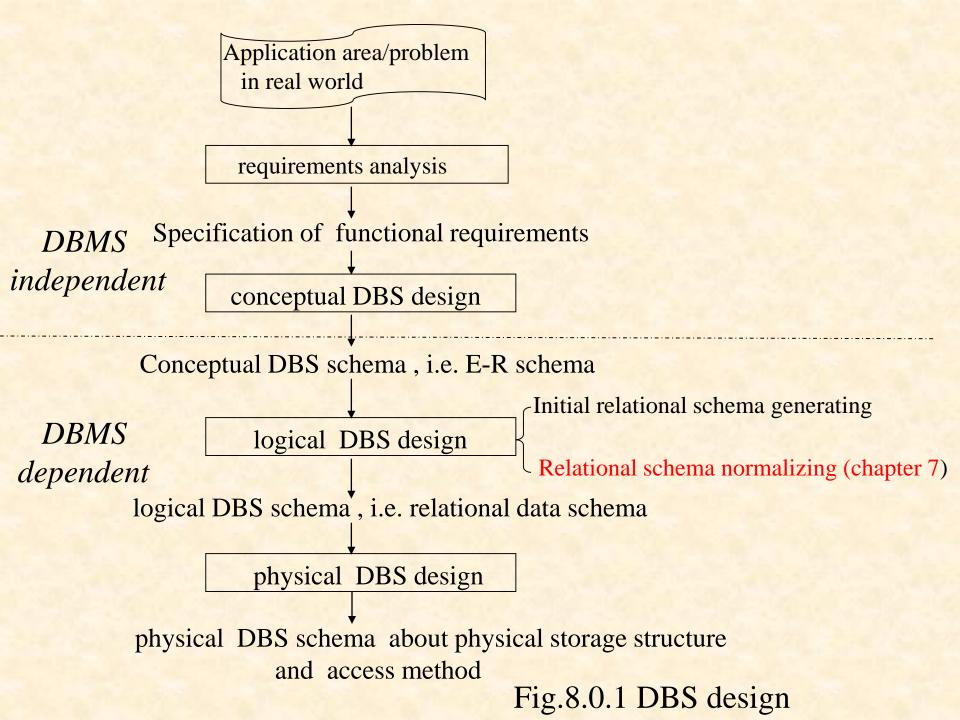
- Features of Good Relational Design
- Atomic Domains and First Normal Form
- Decomposition Using Functional Dependencies
- Functional Dependency Theory
- Algorithms for Functional Dependencies
- (Decomposition Using Multivalued Dependencies) 略
- (More Normal Form) 略
- Database-Design Process
- (Modeling Temporal Data) 略





-Why Normalization Needed?

- As shown in Fig. 8.0.1, logical DBS design consists of
  - initial relational schema generating (§ 7.6)
  - relational schema normalizing
- A bad DB design, i.e. schema not being normalized well, may result in
  - repetition of information
  - inability to represent certain information





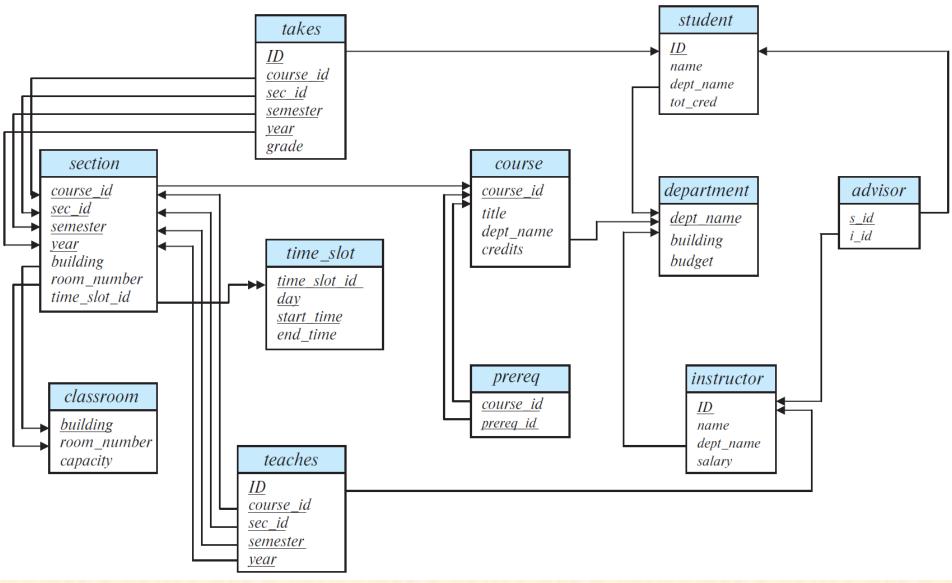


Fig. 8.0.2 Schema Diagram



## 7.1.1 Combine Schemas

- Suppose we combine instructor(ID, name, salary, dept\_name) and department(dept\_name, building, budget) into inst\_dept
  - (No connection to relationship set inst\_dept)
- Result is possible repetition of information on department
  - many-to-one mapping cardinality from instructor to department
- Pitfalls due to information repetition, when
  - inserting
  - deleting
  - updating

1					[iii	北海海山
	ID	name	salary	dept_name	building	budget
	22222	Einstein	95000	Physics	Watson	70000
	12121	Wu	90000	Finance	Painter	120000
	32343	El Said	60000	History	Painter	50000
	45565	Katz	75000	Comp. Sci.	Taylor	100000
	98345	Kim	80000	Elec. Eng.	Taylor	85000
	76766	Crick	72000	Biology	Watson	90000
	10101	Srinivasan	65000	Comp. Sci.	Taylor	100000
Miss	58583	Califieri	62000	History	Painter	50000
	83821	Brandt	92000	Comp. Sci.	Taylor	100000
	15151	Mozart	40000	Music	Packard	80000
	33456	Gold	87000	Physics	Watson	70000
	76543	Singh	80000	Finance	Painter	120000
$t_1$	201081,	, Zhang,	60000,	Comp.Sci,	Taylor,	100000
$t_2$	null,	null,	null,	Soft.Eng.,	Taylor,	100000

Fig. 7.2





- Inserting problem and information redundancy
  - adding a new instructor
    - tuple  $t_1 = (201081, Zhang, 60000, Comp.Sci, Taylor, 10000)$  is inserted into *inst\_dept*
  - data for the attributes dept\_name, building and budget are repeated for the instructors in the 4rd, the 7th, the 9th, and the last row that the department "Comp.Sci" makes, space is wasted





- Deleting problem
  - e.g. if the department *Comp.Sci* is canceled, all *instructor* in it should then be removed
  - in Fig 7.1, every tuples containing the *Comp.Sci* department should be deleted ▶
    - the 4rd, the 7th, and the 9th row





- Updating problem and information redundancy
  - information redundancy complicates updating, introducing possibility of inconsistency of the *budget* values
  - e.g. change *budget* of the *Comp.Sci* department from 100000 to 120000,





- Information Representation Problem
  - to represent directly information about a *new-opened* department in which there no exists *instructor*, a tuple containing *null* values, such as

```
t_2 = (\text{null, null, Noft.Eng.}, Taylor, 100000), is inserted
```

• null values in DB complicate data handling in DBS

- An improved design
  - decompose inst\_dept-schema into inst and department





### A Combined Schema Without Repetition

- Consider combining relations
  - sec\_class(sec\_id, building, room\_number) and
  - section(course\_id, sec\_id, semester, year)into one relation
  - section(course\_id, sec\_id, semester, year, building, room\_number)
- No repetition in this case, why?
  - one to one mapping from section to sec\_class cardinality



#### 7.1.2 Smaller Schemas

- Suppose we had started with *inst\_dept*. How would we know to split up (**decompose**) it into *instructor* and *department*?
- Write a rule "if there were a schema (dept\_name, building, budget), then dept\_name would be a candidate key"
- Denote as a functional dependency:

dept\_name → building, budget

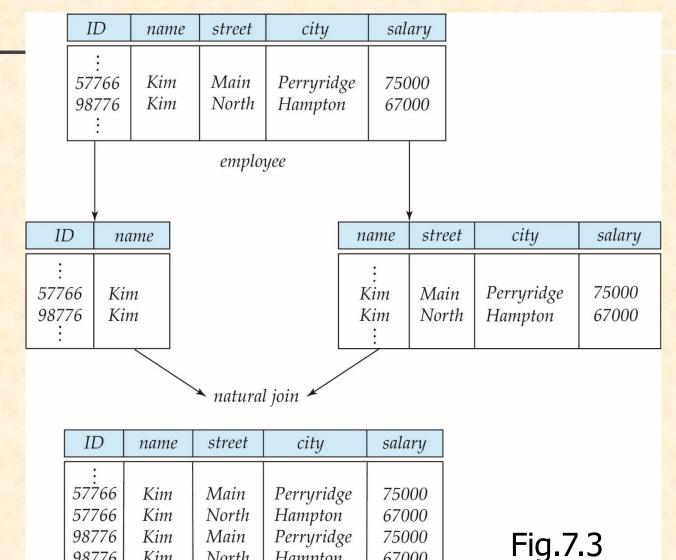
- In *inst\_dept*, because *dept\_name* is not a candidate key, the building and budget of a department may have to be repeated.
  - This indicates the need to decompose *inst\_dept*



#### **Smaller Schemas**

- Not all decompositions are good. Suppose we decompose employee(ID, name, street, city, salary) into employee1 (ID, name) employee2 (name, street, city, salary)
- The next slide shows how we lose information -- we cannot reconstruct the original *employee* relation -- and so, this is a **lossy decomposition**.

## A Lossy Decomposition 对京都電大學



98776

Kim

North

Hampton

67000

## Example:





## Lossless-Join Decomposition

#### **Lossless join decomposition**

■ Decomposition of R = (A, B, C)

$$R_1 = (A, B) R_2 = (B, C)$$

A	В	C
$\alpha$	1	A B
p	r	D

$$\begin{array}{c|c}
A & B \\
\hline
\alpha & 1 \\
\beta & 2 \\
\hline
\Pi_{A,B}(r)
\end{array}$$

В	С
1 2	A B
П	B,C(r)

$$\prod_{A} (r) \bowtie \prod_{B} (r)$$

А	В	С
$\alpha \beta$	1 2	A B

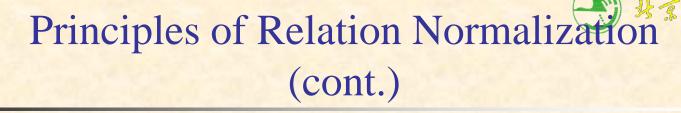


## Normalization Principles

- 一在逻辑DBS设计过程中,将E—R图进行转换,得到面向特定应用领域的初始关系模式集
- 这些初始关系模式集中可能存在多种(作为完整性约束的) 关系模式属性间的数据依赖 (Data Dependencies) 关系
  - 函数依赖 (functional dependencies, FD, § 7.4)
  - 多值依赖 (Mutivalued Dependencies, MVD, § 7.6)
  - 连接依赖 (Join Dependencies, JD) 略

## Principles of Relation Normalization (cont.)

- 如果直接根据初始关系模式构造DBS,由于初始关系模式中数据依赖关系的存在,可能会违反DB的完整性约束,导致DBS使用过程中出现如下问题,影响DBS的正确性、性能、效率
  - 数据冗余问题、插入问题、更新问题、删除问题 (pitfalls, § 7.1)



- 因此,对初始关系模式集,需要根据关系规范化理论,在保证关系模式的
  - 函数无损连接性 (lossless join),和/或
  - 函数依赖保持性 (dependency preservation)

约束前提下,对关系模式集进行规范化处理——等价变换/模式分解

- 关系模式规范化主要步骤为
  - 根据函数依赖的Armstrong's 公理系统(§7.4.1)和多值 依赖的公理系统,从初始关系模式集中已知的函数依赖 和多值依赖出发,推导出初始关系模式集中所有的函数 依赖(§8.4)和多值依赖



# Principles of Relation Normalization (cont.)

- 对具有函数依赖和多值依赖的初始关系模式集,采用
  - 模式分解算法,对其进行(等价)分解和变换,将其转换为各种范式形式,包括:
  - 1NF(§ 7.2) 、 2NF (Exercise 7.16) 、 BCNF(§ 7.3.2) 、 3NF (§ 7.3.4) 、 4NF(§ 7.6.2)
- ,以消除模式集中的函数依赖和多值依赖带来的负面影响,保证数据库系统的完整性
- 关系模式规范化处理的基本要求为:
  - 静态关系具有第一范式形式
  - (理论上)动态关系最好具有3NF或BCNF形式

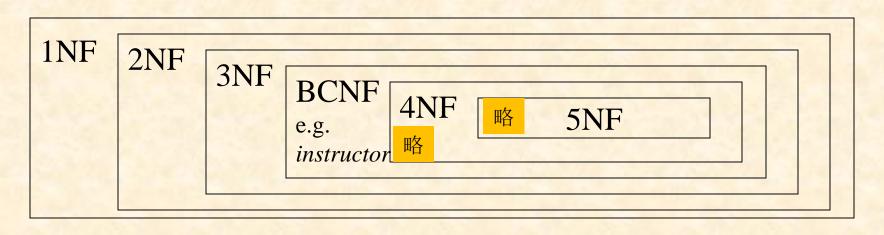


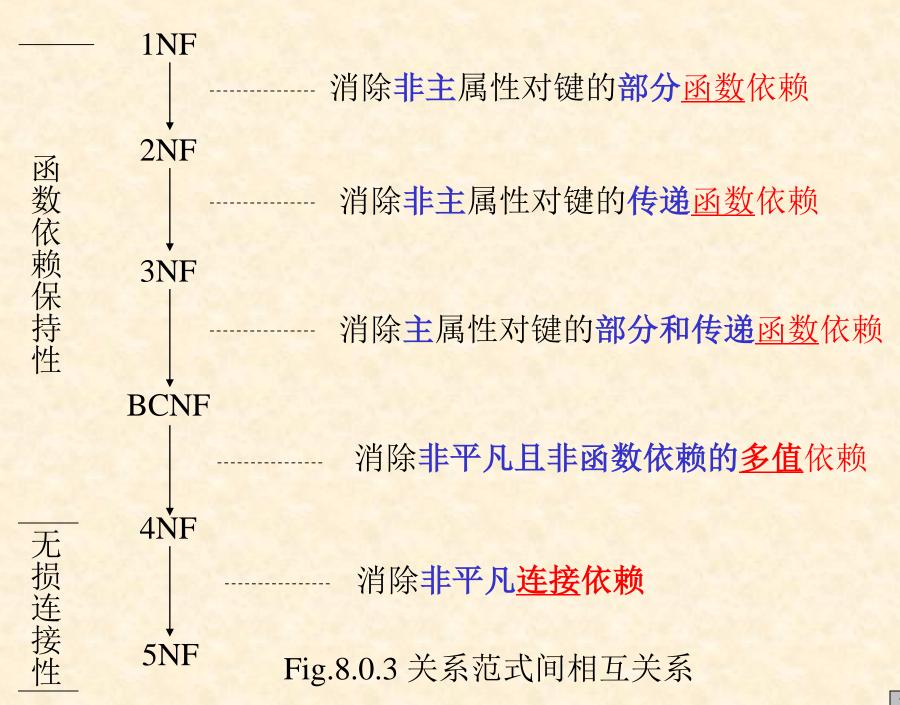
## Principles of Relation Normalization (cont.)

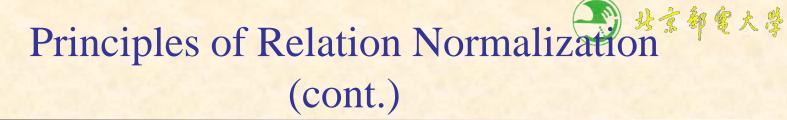
- 3种数据依赖间的关系
  - 函数依赖是特殊的多值依赖
  - 多值依赖又是连接依赖的特例
- 范式1NF、2NF、3NF、BCNF可以看作由符合范式要求的各种关系模式组成的关系模式的集合

e.g.  $1NF = \{R \mid R满足第一范式的定义\}$ 

■ 各种范式间的关系,参见Fig.8.0.3







- 给定一个关系模式,可以采用规范化算法将其转换为1NF、 2NF、3NF、BCNF
- 对连接依赖和第五范式, 无相应的模式规范化算法



## Goal — Devise a Theory for the Following

- Decide whether a particular relation *R* is in "good" form.
- In the case that a relation R is not in "good" form, decompose it into a set of relations  $\{R_1, R_2, ..., R_n\}$  such that
  - each relation is in good form
  - the decomposition is a lossless-join decomposition
- Our theory is based on:
  - functional dependencies
  - multivalued dependencies



#### 7.2 Atomic Domains and First Normal Form

- Domain is atomic if its elements are considered to be indivisible units
  - Examples of non-atomic domains:
    - Set of names, composite attributes
    - Identification numbers like CS101 that can be broken up into parts
- A relational schema R is in **first normal form** if the domains of all attributes of R are atomic
- Non-atomic values complicate storage and encourage redundant (repeated) storage of data
  - Example: Set of *accounts* stored with each *customer*, and set of owners stored with each *account*
  - We assume all relations are in first normal form





- Atomicity is actually a property of how the elements of the domain are used.
  - Example: Strings would normally be considered indivisible
  - Suppose that students are given roll numbers which are strings of the form CS0012 or EE1127
  - If the first two characters are extracted to find the department, the domain of roll numbers is not atomic.
  - Doing so is a bad idea: leads to encoding of information in application program rather than in the database.



# 7.3 Decomposition Using Functional Dependencies

## Goal — Devise a Theory for the Following

- Decide whether a particular relation *R* is in "good" form.
- In the case that a relation R is not in "good" form, decompose it into a set of relations  $\{R_1, R_2, ..., R_n\}$  such that
  - each relation is in good form
  - the decomposition is a lossless-join decomposition
- Our theory is based on:
  - functional dependencies
  - multivalued dependencies



## 7.3.1 Functional Dependencies

- Constraints on the set of legal relations.
- Require that the value for a certain set of attributes determines uniquely the value for another set of attributes.
- A functional dependency is a generalization of the notion of a *key*.
- Function:  $f: X \rightarrow Y$ ,  $x \in X, y \in Y, y = f(x)$ e.g. y = 2x
  - for  $x_1, x_2 \in X$ , if  $x_1 = x_2$ , then  $f(x_1) = f(x_2)$



Let R be a relation schema

$$\alpha \subseteq R$$
 and  $\beta \subseteq R$ 

**■** The functional dependency

$$\alpha \rightarrow \beta$$

**holds on** R if and only if for any legal relations r(R), whenever any two tuples  $t_1$  and  $t_2$  of r agree on the attributes  $\alpha$ , they also agree on the attributes  $\beta$ . That is,

$$t_1[\alpha] = t_2[\alpha] \implies t_1[\beta] = t_2[\beta]$$

**Example:** Consider r(A,B) with the following instance of r.

• On this instance,  $A \rightarrow B$  does **NOT** hold, but  $B \rightarrow A$  does hold.



**Definition 1.** Functional dependency (FD) holds on R

/\*函数依赖FD在关系模式R上成立/保持\*/

Let R be a relation schema, and

$$\alpha \subseteq R$$
,  $\beta \subseteq R$ 

, the functional dependency  $\alpha \to \beta$  holds on schema R

if and only if

for *any* legal relation (or *relation instance*) r(R), whenever any two tuples  $t_i$  and  $t_j$  in r agree on the attributes  $\alpha$ , they also agree on the attributes  $\beta$ , that is,

$$t_{i}[\alpha] = t_{j}[\alpha] \implies t_{i}[\beta] = t_{j}[\beta]$$



- Keys in relational schema can be defined in terms of FD
  - K is a superkey for relation schema R, if and only if  $K \rightarrow R$
  - K is a candidate key for R, if and only if
    - $K \rightarrow R$ , and
    - for no  $\alpha \subset K$ ,  $\alpha \to R$



- Functional dependencies allow us to express constraints that cannot be expressed using superkeys.
- Consider the schema:

inst\_dept (ID, name, salary, dept\_name, building, budget).

We expect these functional dependencies to hold:

$$dept\_name \rightarrow building$$
and 
$$ID \rightarrow building$$

but would not expect the following to hold:

 $dept_name \rightarrow salary$ 



■ **Definition2.** (A particular relation instance) r(R) satisfy FD, or FD is satisfied by r(R)

/\*关系 r(R) 满足函数依赖集FD, FD 被r满足\*/

Given  $FD = {\alpha \rightarrow \beta}$  holding on R, and a relation (instance) r(R) on R,

- r is said to satisfy FD, if r is legal under functional dependency set FD
- note:
  - *r* is legal under FD= $\{\alpha \rightarrow \beta\}$  means
  - for  $t_i$ ,  $t_j \in r(R)$ , if  $t_i[\alpha] = t_j[\alpha]$ , then  $t_i[\beta] = t_j[\beta]$
- FD requires that the values for a certain set of attributes determines uniquely the value for another set of attributes





- Given relation r(R) shown below, which FD is satisfied by r
- A. A  $\rightarrow$ B B. AC  $\rightarrow$  B C. BC  $\rightarrow$ A D. B  $\rightarrow$  C

	A	В	C
t1	1	4	2
t2	3	5	6
t3	3	4	6
t4	7	3	8
t5	9	1	0

Fig. 7.0.4





#### Example One (cont.)

- t2[A]=t3[A]=3,  $t2[B]=5 \neq t3[B]=4$ , A  $\rightarrow$ B is not satisfied
- t2[AC]=t3[AC]=36,  $t2[B]=5 \neq t3[B]=4$ , AC  $\rightarrow$ B is not satisfied
- $\blacksquare$  BC  $\rightarrow$ A is satisfied
- t1[B]=t3[B]=4,  $t1[C]=2 \neq t3[C]=6$ , B  $\rightarrow$ C is not satisfied





#### Example Two

Consider the schema  $R=(employee\_ID, date, turnover per-day, department_name, manager)$  that describes the information about the turnover per-day (日营业额) for each employee everyday, the department that each employee works at, and the manager of the department the employee works at.

it is assumed that

- at every day, each employee has only one turnover per-day
- each employee works at only one department
- each department is managed by only one manager
- According to the descriptions mentioned above, list all the functional dependencies that hold on R
- Q&A: How about the E-R diagram for this example?





#### Example Two (cont.)

Answer

```
    F = { employee_ID, date → turnover per-day, employee_ID → department_name, department_name → manager }
```





- While E-R diagrams describe the objects in practice and the associations among them, functional dependencies (FDs) illustrate the relationships among the features/attributes of the objects (i.e. entities or relationships in E-R diagrams)
- How to guarantee the FD in DBS?
  integrity mechanisms in DBMS, i.e. keys, assertions, triggers



#### Use of Functional Dependencies

- We use functional dependencies to:
  - test relations to see if they are legal under a given set of functional dependencies.
    - If a relation r is legal under a set F of functional dependencies, we say that r satisfies F.
  - specify constraints on the set of legal relations
    - We say that F holds on R if all legal relations on R satisfy the set of functional dependencies F.
- Note: A specific instance of a relation schema may satisfy a functional dependency even if the functional dependency does not hold on all legal instances.
  - For example, a specific instance of *instructor* may, by chance, satisfy

 $name \rightarrow ID$ .



# 4

#### FD holds on R vs FD is satisfied by r(R)

- FD holds on R
  - 定义在R的属性间的语义约束,或R的属性间体现出的语义约束
  - ■从设计角度, R应满足的约束
- FD is satisfied by r(R)
  - 根据 R构造的实际数据r(R)是否满足语义约束FD



## FD holds on R vs FD is satisfied by r(R)

- For a schema R, there may be more than one relation instance r(R), i.e.  $r_1(R)$ ,  $r_2(R)$ ,  $r_3(R)$ ,...,  $r_m(R)$ , defined on R
  - e.g. consider R = (A, B, C, D), and with respect to the instances  $r_1(R)$  and  $r_2(R)$  in Fig. 8.0.5
- Relation r(R) satisfies  $\alpha \rightarrow \beta$  vs.  $\alpha \rightarrow \beta$  holds on schema R
  - if  $\alpha \rightarrow \beta$  holds on R, then every legal r(R) satisfies this R
  - but for schema R and  $\alpha \rightarrow \beta$ , if only some  $r_i(R)$  satisfies R,  $\alpha \rightarrow \beta$  may not hold on R.
  - e.g. in Fig.8.0.5,  $A \to C$  and  $AB \to D$  are satisfied by  $r_1(R)$ , but  $A \to C$  is not satisfied by  $r_2(R)$ , so  $A \to C$  does not holds on R



$$FD_1 = \{A \rightarrow C, AB \rightarrow D\}$$
, satisfied by  $r_1$ 

$$FD_2 = \{AB \rightarrow D\}$$
, satisfied by  $r_2$ 

	$\mathbf{r}_1$					$r_2$			
	A	В	C	D		lacksquare	B	C	D
	$a_1$	$b_1$	$c_1$	$d_1$		$a_1$	$b_1$	$c_1$	$d_1$
t2_	$a_1$	$b_2$	$(c_1)$	$d_2$	t2_	$a_1$	$b_2$	$(c_1)$	$d_2$
	$a_2$	$b_2$	<u>C</u> 2+	$d_2$		$a_2$	$b_2$	$c_2$	$d_2$
	$a_2$	$b_3$	$c_2$	$d_3$		$a_2$	$b_3$	$c_2$	$d_3$
	$a_3$	$b_3$	<i>c</i> 2←	$d_4$		$a_3$	$b_3$	<i>c</i> <sub>2</sub>	$d_4$
					t6 –	$\mathbf{a}_1$	$b_4$	c <sub>2</sub> ←	$d_5$

 $A \rightarrow C$  does not hold on R, because of t6 Fig. 8.0.5 instance  $r_1$  and  $r_2$  defined on schema R





- E.g. True or false?
  - for a relation r(R) defined on schema R, if r satisfies functional dependency FD =  $\{\alpha \rightarrow \beta\}$ , then FD holds on schema R
  - false



#### Functional Dependencies (Cont.)

- A functional dependency is **trivial** if it is satisfied by all instances of a relation
  - Example:
    - ID, name  $\rightarrow ID$
    - $name \rightarrow name$
  - In general,  $\alpha \rightarrow \beta$  is trivial if  $\beta \subseteq \alpha$





- Def. Transitive dependency (传递函数依赖)
  - a functional dependency  $\alpha \rightarrow \gamma$  is *transitive* if:

$$\alpha \rightarrow \beta$$
, ( $\beta \leq \alpha$ ),  $\beta \leftrightarrow \alpha$ ,  $\beta \rightarrow \gamma$ 

; and  $\gamma$  is called transitive dependent on  $\alpha$ 

- E.g. Student(sno, sname, address, depart)
  - for transitive dependency

$$sno \rightarrow address$$

, there are

 $sno \rightarrow sname$ ,  $sname \rightarrow address$ 





#### VII-2-1 Basic Concepts (cont.)

- Def. Partial dependency (部分函数依赖)
  - a functional dependency  $\alpha \to \beta$  is *partial* if there is a proper subset  $\gamma$  of  $\alpha$ , i.e.  $\gamma \subset \alpha$ , such that

$$\gamma \rightarrow \beta$$

- ; and  $\beta$  is partially dependent on  $\alpha$
- ■/\*α非最小化/冗余
- E.g. Student(sno, sname, address, depart)
  - for partial dependency

$$(sno, sname) \rightarrow address$$

, there are  $sname \rightarrow address$ ,  $sno \rightarrow address$ 



## Closure of a Set of Functional Dependencies

- Given a set F of functional dependencies, there are certain other functional dependencies that are logically implied by F.
  - For example: If  $A \to B$  and  $B \to C$ , then we can infer that  $A \to C$
- The set of all functional dependencies logically implied by F is the closure of F, denoted as  $F^+$ .





A relation schema R is in BCNF with respect to a set F of functional dependencies if for all functional dependencies in  $F^+$  of the form

$$\alpha \to \beta$$

where  $\alpha \subseteq R$  and  $\beta \subseteq R$ , at least one of the following holds:

- $\bullet \alpha \to \beta$  is trivial (i.e.,  $\beta \subseteq \alpha$ )
- $\bullet$  a is a superkey for R

Example schema *not* in BCNF:

instr\_dept (ID, name, salary, dept\_name, building, budget)

because *dept\_name*→ *building*, *budget*holds on *instr\_dept*, but *dept\_name* is not a superkey

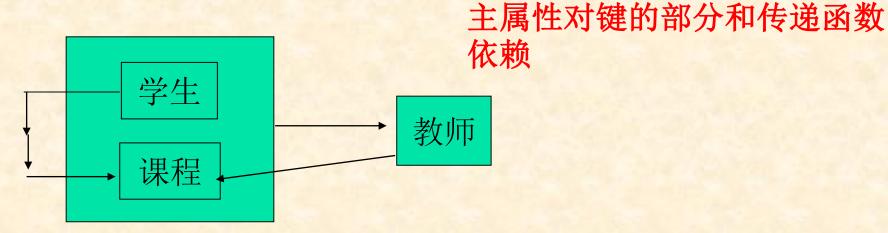


3NF: (学生, 教师, 课程)

教师只教一门课,每门课有若干教师,某一学生选定某门课,

就对应一个固定的教师

主键(学生,课程)或(学生,教师)



主属性对键的传递依赖: 课程依赖学生





#### BCNF (cont.)

#### 消除主属性对键的部分和传递函数依赖

3NF

BCNF

- BCNF性质
  - 不存在属性(主属性,非主属性)对候选键的传递和部分依赖
- If *R* is in BCNF, *R* is also in 3NF
- 以FD作为模式规范化程度度量,BCNF达到了最高规范化程度。
- 如果DBS中所有模式都属于BCNF,则消除了<u>插入</u>和<u>删除</u>异常





■ Suppose we have a schema R and a non-trivial dependency  $\alpha \rightarrow \beta$  causes a violation of BCNF.

We decompose *R* into:

- $-(\alpha U\beta)$
- $R (\beta \alpha)$
- In our example,
  - $\alpha = dept_name$
  - $\beta$  = building, budget and inst\_dept is replaced by
  - $(\alpha \cup \beta) = (dept\_name, building, budget)$
  - $(R (\beta \alpha)) = (ID, name, salary, dept\_name)$



#### 7.3.3 BCNF and Dependency Preservation

- Constraints, including functional dependencies, are costly to check in practice unless they pertain to only one relation
- If it is sufficient to test only those dependencies on each individual relation of a decomposition in order to ensure that *all* functional dependencies hold, then that decomposition is *dependency preserving*.
- Because it is not always possible to achieve both BCNF and dependency preservation, we consider a weaker normal form, known as third normal form (3NF).



#### 7.3.4 Third Normal Form

■ **Def 1:** A relation schema *R* is in **third normal form (3NF)** if for all:

 $\alpha \rightarrow \beta \text{ in } F^+$  at least one of the following holds:

- $\alpha \rightarrow \beta$  is trivial (i.e.,  $\beta \in \alpha$ )
- $\bullet$  a is a superkey for R

- E.g. B  $\rightarrow$ ABC, (ABC) - (B) =AC
- Each attribute A in  $\beta \alpha$  is contained in a candidate key for R.

(NOTE: each attribute may be in a different candidate key)

- If a relation is in BCNF it is in 3NF (since in BCNF one of the first two conditions above must hold).
- Third condition is a minimal relaxation of BCNF to ensure dependency preservation (will see why later).



#### VII-3-3 Third Normal Form (cont.)

Def.2. 如果关系模式R是2NF,而且每一个非主属性都不传递依赖于R的任何候选键,则R是3NF

消除非主属性对键的传递函数依赖

 $2NF \longrightarrow 3NF$ 

- If *R* is in 3NF,
- ■3NF性质
  - R is also in 2NF
  - ■不存在非主属性对候选键的*部分和传递*依赖,i.e.每一个 非主属性都不传递依赖于R的任何候选键





#### Example 1 about 3NF

- Scheme SSS ( $\underline{S\#}$ , SD, SL)  $F_{SSS} = \{S\# \to SD, SD \to SL, S\# \to SL\} \quad \exists \mathbb{R}$
- On basis of 3NF definition1, SSS is not in 3NF, because
  - for  $SD \rightarrow SL$ , RHS SL in  $\{SL\}$ - $\{SD\}$ =  $\{SL\}$  is not in candidate key  $\{S\#\}$

(/\*each attribute A in  $\beta$  –  $\alpha$  is contained in a candidate key for R)

- On basis of 3NF definition2, SSS is not in 3NF, because
  - for  $S\# \to SL$ , RHS SL is non-primacy attribute, and is transitive dependent on candidate key  $\{S\#\}$

(非主属性对键的传递函数依赖)



# Practice Exe. 7.19 Second Normal Form

- **Def.** A schema R is in second normal form (2NF) if
  - R is in 1NF, and
  - $\blacksquare$  each attribute A in R meets one of the following criteria
    - it appears in a candidate key, *that is* A is a *prime* attribute
    - it is not *partially* dependent on a candidate key

      /\* A is completely dependent on a candidate key \*/





#### VII-3-2 Second Normal Form (cont.)

消除非主属性对候选键的部分函数依赖

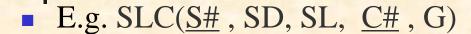
1NF

2NF

- ■2NF性质
  - ■不存在非主属性对候选键的部分依赖
  - ■每一个非主属性都完全依赖于R的候选键







• 
$$(S\#, C\#) \rightarrow G$$
,  $SD \rightarrow SL$ ,  
 $S\# \rightarrow SD$ ,  $(S\#, C\#) \rightarrow SD$ ,  
 $S\# \rightarrow SL$ ,  $(S\#, C\#) \rightarrow SL$ }

- SLC is not in 2NF, because
  - for non-primary attribute SD, there exits  $S\# \to SD$ , so SD is partially dependent on the key (S#, C#)
  - for non-primary attribute SL, there exits  $S\# \to SL$ , so SL is partially dependent on the key (S#, C#)





#### 2NF Example (cont.)

- Decompose  $SLC(\underline{S\#}, SD, SL, \underline{C\#}, G)$  into  $SC(\underline{S\#}, \underline{C\#}, G)$ ,  $SSS(\underline{S\#}, SD, SL)$ 
  - $F_{SC} = \{ (S\#, C\#) \rightarrow G \}$  $F_{SSS} = \{ S\# \rightarrow SD, SD \rightarrow SL, S\# \rightarrow SL \}$
  - schema SC and SSS are in 2NF





- Let *R* be a relation scheme with a set *F* of functional dependencies.
- Decide whether a relation scheme *R* is in "good" form.
- In the case that a relation scheme R is not in "good" form, decompose it into a set of relation scheme  $\{R_1, R_2, ..., R_n\}$  such that
  - each relation scheme is in good form
  - the decomposition is a lossless-join decomposition
  - Preferably, the decomposition should be dependency preserving.



#### How good is BCNF?

- There are database schemas in BCNF that do not seem to be sufficiently normalized
- Consider a relation

inst\_info (ID, child\_name, phone)

 where an instructor may have more than one phone and can have multiple children

ID	child_name	phone
99999 99999 99999	David David William Willian	512-555-1234 512-555-4321 512-555-1234 512-555-4321



#### How good is BCNF? (Cont.)

- There are no non-trivial functional dependencies and therefore the relation is in BCNF
- Insertion anomalies i.e., if we add a phone 981-992-3443 to 99999, we need to add two tuples

(99999, David, 981-992-3443)

(99999, William, 981-992-3443)



#### How good is BCNF? (Cont.)

Therefore, it is better to decompose *inst\_info* into:

inst\_child

ID	child_name
99999 99999 99999	David David William Willian

inst\_phone

ID	phone
99999 99999 99999	512-555-1234 512-555-4321 512-555-1234 512-555-4321

This suggests the need for higher normal forms, such as Fourth Normal Form (4NF), which we shall see later.