

MODULE 2:

#PROPOSITIONAL LOGIC:

If any statement is a declarative statement with outcome true or false, then declarative sentence called a proposition.

• Logical connectives or logical operators:

(i) Conjunction (AND)

(ii) Disjunction (OR)

(iii) Negation (NOT)

The truth value of any proposition are the logical outcomes of the statements which can be denoted by true or false [OR] 1 or 0. \therefore Combining 2 or more propositions we may generate truth table.

TRUTH TABLES:

(i) Conjunction (AND)

p	q	$p \wedge q$
T	T	T
T	F	F
F	T	F
F	F	F

(ii) Disjunction (OR)

p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F

(iii) Negation (NOT)

p	$\neg p$
T	F
F	T

• Conditional Operator:

(i) Implication:

The implication of a statement p into a statement q is defined as $p \rightarrow q$, means if p then q. The truth table is given by,

p	q	$p \rightarrow q$
T	T	T
T	F	F
F	T	T
F	F	T

(ii) Contrapositive :

If any implication is of the form $p \rightarrow q$, then its contrapositive will be given as $\neg q \rightarrow \neg p$. The implication statement is [if the 2nd year students are very naughty then I would love to take this class]

The contrapositive version is -

If I would not love to take this class then the 2nd year students are not naughty.

Truth table of is given by -

p	q	$p \rightarrow q$	$\neg q \rightarrow \neg p$
T	T	T	T
T	F	F	F
F	T	T	T
F	F	T	T

(iii) Converse :

If an implication is given in the form ~~$p \rightarrow q$~~ $p \rightarrow q$, then the converse will be of the form $q \rightarrow p$.

(iv) Inverse :

If an implication is of the form $p \rightarrow q$, then the inverse will be of the form $\neg p \rightarrow \neg q$.

The truth table is given by -

p	q	$\neg p \rightarrow \neg q$
T	T	T
T	F	T
F	T	F
F	F	T

TAUTOLOGY :

In a compound statement of 2 or more propositions with the application of 1 or more logical and conditional connectives if all the outcomes of a truth table comes true (T), then this compound proposition is called a tautology and if all outcomes will come False (F), then it is called a contradiction.

p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F