



WARSAW UNIVERSITY OF TECHNOLOGY  
FACULTY OF MATHEMATICS  
AND INFORMATION SCIENCE



# Neural Networks

Lecture 1

# Course objectives

Relay students a knowledge of artificial neural networks using information from biological structures. After completing the course (lecture and project) students should:

- have theoretical knowledge about principles of construction and operation of basic models,
- be able to select proper structure to execute the assumed functions,
- be able to select proper programming tools (languages, packages etc.) to carry out tasks,
- being the part of a team be able to carry out the tasks for team members,
- prepare and test computer program,
- prepare the final report.

# Learning outcomes

## knowledge

- a student knows theoretical background of operation and modelling of neuronlike elements and the rules of construction of neuronal multi layer structures

## skills

- is able to analyse given net, prepare its functional description, carry out the proof of its correct work
- is able to analyse given net, prepare its functional description, carry out the proof of its correct work

# Learning outcomes

## skills (cont)

- can evaluate the usefulness of programming tools to model the network based on given parameters
- can obtain information from literature, databases and other selected sources appropriate for problems solved

## soft competences

- can cooperate individually and in a work team, accepting various role in it



# Learning outcomes realisation and verification

Assumed learning outcomes – student	course form	verification criteria	verification methods
knows theoretical background of operation and modelling of neuronlike elements and the rules of construction of neuronal multi layer structures	lecture (examples) exercises before-exam	discussion of various structures and modela	exam – written and/or oral part
is able to analyse given net, prepare its functional description, carry out the proof of its correct work	lecture (examples) project (exercises) project	completion of proper analysis and description	exam written part, project
can design a complex device related to solve a practical problem (i.e from the area of finances or data classification)	lecture (examples) project (exercises)	design of a project of device, analysis of correctness	exam written part, project
can evaluate the usefulness of programming tools to model the network based on given parameters	exercises before-exam project exercises + consultations	selecdfthn of a proper programming language with justification	project's course and pass
can obtain information from literature, databases and other selected sources appropriate for problems solved	project	bibliography selectios, justification	project's course and pass
can cooperate individually and in a work team, accepting various role in it	project	split of work within a team members, completion of entrusted tasks	teachers' observation

# ECTS credits

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- contact hours 75h:
  - lectures – 30h,
  - laboratory work – 30h
- preparation for laboratory work – 20h
- familiarize with basic literature – 15h
- computer program preparation, debugging, verification (out of lab) – 30h
- final report preparation – 10h
- preparation for the exam and written exam – 20h

**Total students' workload 155h = 5 ECTS credits**

# **Course Contents**

## ***Introduction***

***What cybernetics and biocybernetics are***

***Modeling***

***Neurocomputers and Neurocomputing***

***Comparison of humans and computers***

***Methods of learning***

***The nervous system***

# **Course Contents**

***The brief overview of the brain***

***Biological neuron***

***Signal processing in the biological nervous system***

***The Artificial Neuron***

***McCulloch & Pitts Model***

***Single-layer Artificial Neural Network***



# **Course Contents**

***Multi-layer Artificial Neural Network***

***Mathematical Model of a Single Neuron and a Network***

***The Rosenblatt's Perceptron***

***Method of Learning***

***Perceptron Representation***

***Perceptron limitations (XOR Problem)***

***Linear Separability***

# **Course Contents**

***The Rosenblatt's Perceptron cont.***

***Overcoming the limitations***

***Existence Theorem***

***The Delta Rule***

***ADALINE model***

***The Backpropagation Algorithm***

# **Course Contents**

***Associative Memories***

***3 - Layer Model***

***Kohonen Self-Organizing Model***

***Learning Method***

***Winner Takes All Rule***

***Neighborhood definition***

# **Course Contents**

***Adaptive Resonance Theorem***

***ART Architecture***

***Learning Method***

***Hamming Model***

***Network for Logic Operations***

***Neural Networks for Compression***

***Optimization Problems***

***Neural Networks for Matrix Algebra Problems***



# Bibliography

- **T. Kohonen** *Associative Memory*, Springer, 1978
- **P. D. Wasserman** *Neural Computing, theory and practice*, Van Nostrand Reinhold 1989
- **R. Beale, T. Jackson** *Neural Computing, An Introduction*, A.Hilger IOP Publ. Co. Bristol 1990.
- **A. Cichocki, R. Unbehauen**, *Neural Networks for Optimization and Signal Processing*, J.Wiley 1993.

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- **J. J. Hopfield** *Neural Networks and physical systems with emergent collective computational abilities*, Proc. Natl. Acad., Sci. USA, 79, 1982
- **J. J. Hopfield** *Neurons with Graded Response have collective computational properties like those of two-state neurons*, Proc. Natl. Acad., Sci. USA, 81, 1982

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- **J. J. Hopfield, D. W. Tank** „*Neural*” *Computation and Decisions in Optimization Problems*, Biol. Cyber. 52, 141-152, 1985.
- **R. P. Lippman** *An introduction to Computing with Neural Networks*, IEEE ASSP Mag. April 1987
- **J. Kinoshita, N. G. Palevsky** *Computing with Neural Networks*, High Technology, May 1987
- **R. Hecht-Nielsen** *Neurocomputing, Picking the Human Brain*, IEEE Spectrum, March 1988

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- **D. L. Alkon** *Memory Storage and Neural Systems*, Sci.Amer. July 1989
- **D. R. Hush, B. H. Horne** *Progress in Supervised Neural Networks*, IEEE Sign Proc.Mag. Jan. 1993
- **L.Rutkowski** *New Soft Computing Techniques for System Modelling, Pattern Classification and Image Processing*, Springer-Verlag, 2004



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- **L.Rutkowski** *Computational Intelligence*, Springer Verlag, 2008
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*Neural Networks and Soft Computing*  
2000-2015

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- **J. Korbicz, A. Obuchowicz, D. Uciński**, *Sztuczne sieci neuronowe, podstawy i zastosowania*, Akademicka Oficyna Wydawnicza PLJ, Warszawa 1994.
- **T. Kacprzak, K. Ślot**, *Sieci neuronowe komórkowe*, PWN 1995

## Bibliography - Polish

- **T. Masters**, *Sieci neuronowe w praktyce*, WNT 1996
- **J. Zurada, M. Barski, W. Jędruch** *Sztuczne sieci neuronowe*, PWN 1996
- **S. Osowski** *Sieci neuronowe w ujęciu algorytmicznym*, WNT 1996.
- **L. Rutkowski** (ed) *Sieci neuronowe i neurokomputery* Wyd. Pol.Czest. 1996

## Bibliography - Polish

- **D. Rutkowska, M. Piliński, L. Rutkowski** *Sieci neuronowe, algorytmy genetyczne i systemy rozmyte*, PWN 1997
- **R. Tadeusiewicz** *Elementarne wprowadzenie do technik sieci neuronowych z przykł. progr.*, Akad. Ofic.Wyd. PLJ 1998
- **S. Osowski** *Sieci neuronowe do przetwarzania informacji*, Ofic. Wyd. PW, 2000



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- **J. Mańdziuk** *Sieci neuronowe typu Hopfielda*, Akad. Ofic. Wyd. EXIT 2000
- **L. Rutkowski** *Biocybernetyka i inżynieria biomedyczna, t.6 Sieci Neuronowe*, EXIT, 2000
- **B. Borowik** *Pamięci asocjacyjne*, Mikom 2002
- **R. A. Kosiński** *Sztuczne sieci neuronowe*, WNT 2002
- **L. Rutkowski** *Metody i techniki sztucznej inteligencji*, PWN 2005

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Neural Networks

IEEE Transaction on Neural Networks

Proceedings of the IEEE

IEEE Transaction on System, Man and  
Cybernetics

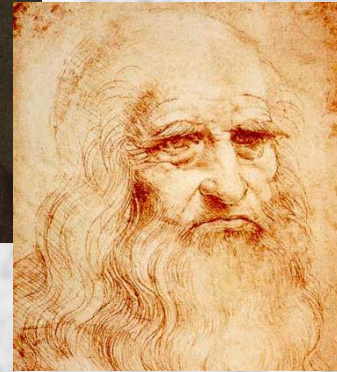
Artificial Intelligence

Computer IEEE

Neurocomputing

Network, Computation in Neural Systems

# Introduction



## ***History***

Born on April 15, 1452, in Vinci, Italy, Leonardo da Vinci was the epitome of a “Renaissance man.” Man of a curious mind and keen intellect, da Vinci studied the laws of science and nature, which greatly informed his work as a painter, sculptor, architect, inventor, military engineer and draftsman.

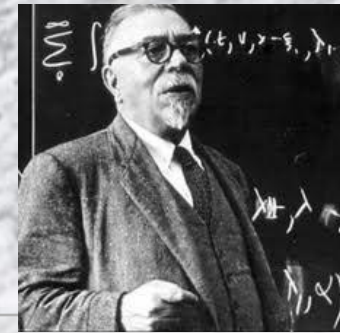
***Specialization*** means to focus on a specific aspect of a larger topic.

is necessary, but ...

***Synthesis*** is the act of combining elements to form something new.



# Introduction



## *Cybernetics*

Norbert Wiener, with Artur Rosenbluth,  
1940th, analogy between humans and technical  
systems

Book:

***Cybernetics or Control and Communication  
in the Animal and the Machine – 1948***  
*(Cybernetyka – czyli sterowanie i komunikacja w  
zwierzęciu i maszynie – 1971)*  
word from greek – **κύβερνέτεσ** - helmsman



# Introduction

## *Cybernetics*

data transmission, on the base of  
mathematical logic, electronics, theory  
of probability, computer sciences

*and*

on the analogy between machines and  
living organisms

# Introduction

## *Modeling*

mathematical  
physical  
simulation

## *Model*

formal description of a system or  
process allowing precise and logical  
analysis; background for technical  
realization, can be a prototype

# Introduction

***Modeling can be controversial because***

object description is impossible

description is extremely complicated

description is general.

Some simplifications and limitations  
have to be used, next verified by the  
results

# Introduction

We will model the nervous system, or precisely – the elements of the nervous system.

We do not intend to build the copy of any real nervous system.



# Introduction

We are not attempting to build computer brains, not to mimic parts of real brains – we are aiming rather to discover the properties of models that take their behavior from extremely simplified versions of neural systems, usually on massively reduced scale.

# Introduction

## Stages of modeling

1. collection, analysis and evaluation of existing biological data, defining the useful properties
2. defining the possibilities for exact mathematical description

# Introduction

## Stages of modeling (cont.)

3. model of a process or structure
4. comparison of the results biological experiments
5. computer model
6. technical device

# Introduction

## Why neural modeling ???

1. Realization of important functions
2. The vast amount of information received from the environment and appropriate selection of this information,
3. Adaptability to varying conditions
4. The great reliability of a system - comprised of a huge number of elements –  
minor or major damage, do not lead to an interruption in the work of the system



# Introduction

## System reliability:

assuming

$10^{10}$  elements

probability of correct functioning =  
0,9999999999

theoretical probability of correctness of the  
system

**< 0,367**

**but, it works !!!**

# Introduction

## Nervous system

- system of data transmission, multilayer, hierarchical, and optimal
- mostly parallel processing
- perfect selection of important information

# History

## **XVIII - XIX century**

tissue excitation together with electrical processes

## **XX century**

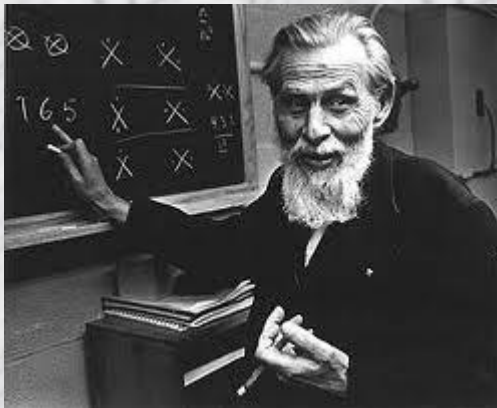
nervous system is composed from many cells  
electrochemical processes inside cells

# History

## 1943 McCulloch & Pitts model

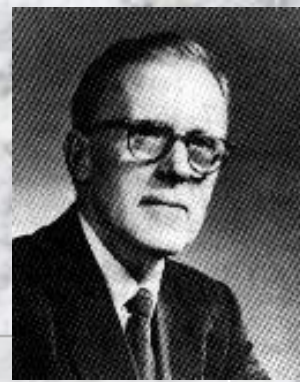
*The logical calculus of the ideas immanent in nervous activity*

**Formal neuron**, on – off switch and can be combined to compute logical functions





# History



## 1949 r. Hebb's theory

### *The organization of Behavior*

Concept of cell assemblies, behavior is coded by collections of neurons,

**Hebb's (or Hebbian) learning rule :** „When an axon of cell A is near enough to excite cell B and repeatedly or persistently takes part in firing it, some growth process or metabolic change takes place in one or both cells such that A's efficiency, as one of the cells firing B, is increased.”

The use of existing or active pathway strengthens the connections between the neurons

*The Organization  
of Behavior*  
A NEUROPSYCHOLOGICAL THEORY

D. O. HEBB  
McGill University

1949  
New York · JOHN WILEY & SONS, Inc.  
London · CHAPMAN & HALL, Limited

# History



**1962 Frank Rosenblatt's** (an American sychologist)  
book

***The Principles of Neurodynamics***

model of the perceptron

**1969 Marvin Minsky & Seymour Papert** book

***Perceptrons: An introduction to Computational Geometry***

Perceptron are impractical  
and/or inadequate to solve  
problems - **death of the perceptron**



# History

Quote from Minsky and Papert's book, *Perceptrons*  
*"[The perceptron] has many features to attract attention: its linearity; its intriguing learning theorem; its clear paradigmatic simplicity as a kind of parallel computation.*

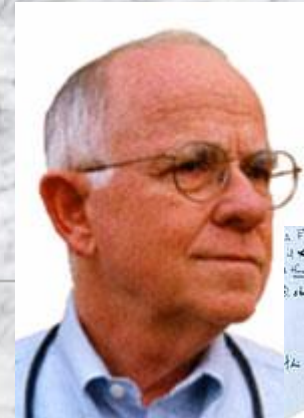
*There is no reason to suppose that any of these virtues carry over to the many-layered version. Nevertheless, we consider it to be an important research problem to elucidate (or reject) our intuitive judgment that the extension is sterile."*



# History

**1960 Widrow & Hoff**

*Adaptive switching circuits*



**AD**Aptive **L**inear **NE**uron = **ADALINE**

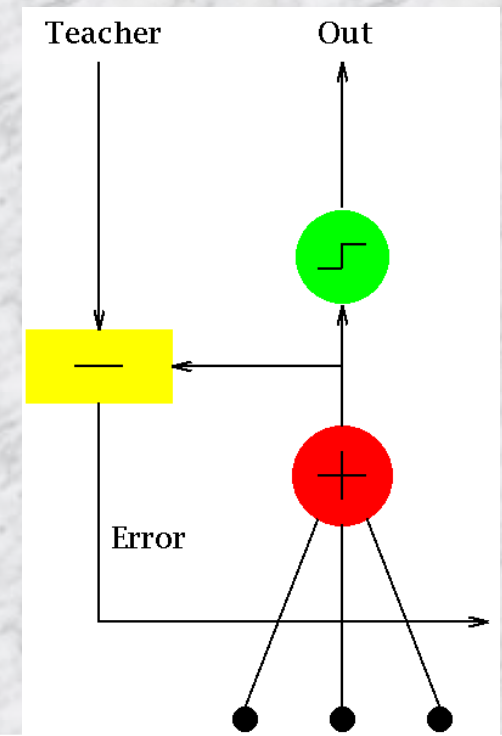
**rule:**

difference between actual output and  
desired output is the background for  
error correction



# History

- **ADALINE** is a single-layer artificial neural network and the name of the physical device that implemented this network. It is based on the McCulloch-Pitts neuron. It consists of a weight, a bias and a summation function.
- The difference between Adaline and the standard perceptron is that in the learning phase the weights are adjusted according to the weighted sum of the inputs (the net). In the standard perceptron, the net is passed to the activation (transfer) function and the function's output is used for adjusting the weights. There also exists an extension known as Madaline.
- 8 cells, 128 connections,  $10^4$ /sec.



# History



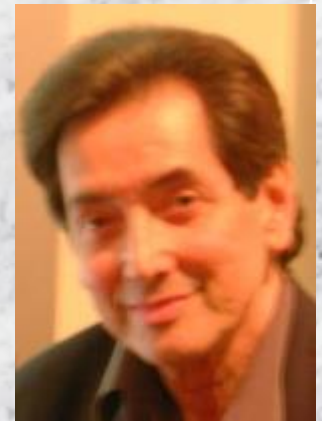
**Teuvo Kohonen** from Helsinki University of Technology has made many contributions to the field of artificial neuron networks, including the Learning Vector Quantization algorithm, fundamental theories of distributed associative memory and optimal associative mappings. His most famous contribution is the Self-Organizing Map (also known as the *Kohonen map* or *Kohonen artificial neural networks*, although Kohonen himself prefers *SOM*).

# History

**James Anderson** from Brown University studied how brains and computers are different in the way they compute



**Stephen Grossberg** introduced in 1976 Adaptive Resonance Theory and Self-Organizing Maps for the learning. Outstar and Instar learning were combined by Grossberg in 1976 in a three-layer network for the learning of multi-dimensional maps.





# History



**In 1985-1990 Adaptive resonance theory (ART)** was a theory developed by **Stephen Grossberg** and **Gail Carpenter** on aspects of how the brain processes information. It describes a number of neural network models which use supervised and unsupervised learning methods, and address problems such as pattern recognition and prediction



# History



**Kunihiro Fukushima** from NHK Science and Technical Research Laboratories invented an artificial neural network, "Neocognitron", which has a hierarchical multi-layered architecture and acquires the ability to recognize visual patterns through learning. He described a "Neocognitron: a self-organizing neural network model for a mechanism of pattern recognition unaffected by shift in position"

# History



**1982 John Joseph Hopfield**

*Neural Networks and Physical Systems with  
Emergent Collective Computational Abilities*

**New impulse for research !!!**



# Hopfield's Model

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Hopfield found similarities between the neural networks and some physical, magnetic systems – the spin glass. Hopfield exploited an analogy to energy states in physics and introduced the *computational energy function*. Like a physical system, the network seeks its lowest energy state and with the iteration procedure converges to the stable state.





# Hopfield's Model

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System matches unknown input signal to one of previously stored signals.

**Why Hopfield's works are so important ??**

*„stimulated“ the interest in neural networks, gave the new way in the development in computers, united together the theory of neural networks with physics (particularly – optics, or optical information processing).*







# History



**Backpropagation**, an abbreviation for "backward propagation of errors", a method of training artificial neural networks used in conjunction with an optimisation method such as gradient descent. The method calculates the gradient of a loss function with respects to all the weights in the network. The gradient is fed to the optimization method which in turn uses it to update the weights, in an attempt to minimize the loss function.

The backpropagation algorithm was originally introduced in the 1970s, by Paul Werbos, wasn't fully appreciated until a famous 1986 book by David Rumelhart and James McClelland „*Parallel Distributed Processing*” .

# History



**Boltzmann machine** is a type of stochastic recurrent neural network invented by Geoffrey Hinton and Terry Sejnowski in 1983. Boltzmann machines can be seen as the stochastic generative counterpart of Hopfield nets. The networks use well known ideas like simulated annealing.

# Hardware implementation

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From middle 80th the competition between laboratories and business from the electronic elements. The important parameters are:

- ◆ number of neuronlike element in the network ,
- ◆ number of connections,
- ◆ the speed,



# Hardware implementation of neural networks in 1985-1988

Neurocomputer's name	Year	Number of elements	Number of connections	Speed	Creator
Mark III	1985	$8 \cdot 10^3$	$4 \cdot 10^5$	$3 \cdot 10^5$	R. Hecht-Nielsen, TRW
Neural Emulator Processor	1985	$4 \cdot 10^3$	$1.6 \cdot 10^4$	$4.9 \cdot 10^5$	C. Cruz, IBM
Mark IV	1986	$2.5 \cdot 10^5$	$5 \cdot 10^6$	$5 \cdot 10^6$	R. Hecht-Nielsen, TRW
Odyssey	1986	$8 \cdot 10^3$	$2.5 \cdot 10^5$	$2 \cdot 10^6$	A. Penz, Tex. Inst. CRL
Crossbar Chip	1986	256	$6.4 \cdot 10^4$	$6 \cdot 10^9$	L. Jackel, AT&T Bell Labs
Anza	1987	$3 \cdot 10^4$	$5 \cdot 10^5$	$1.4 \cdot 10^5$	R. Hecht-Nielsen, Neurocomp. Corp.
Parallon	1987	$9.1 \cdot 10^4$	$3 \cdot 10^5$	$3 \cdot 10^4$	S. Bogoch, Human Dev.
Anza plus	1988	$10^6$	$1.5 \cdot 10^6$	$6 \cdot 10^6$	R. Hecht-Nielsen, Neurocomp. Corp.



# Neurocomputers

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## Neurocomputers

are computers, computer programs, or both, whose computational structure is very similar to the biological structure of the human brain.



# Neurocomputers

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Neurocomputers have been described as:

- neural computers
- neural networks machines
- artificial neural systems
- electronics neural systems
- parallel associative networks,
- parallel distributed processors
- sixth generation computers.



# Neurocomputing

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The field of **neurocomputing**, especially in the area of psychology, is often called connectionism.



# Neurocomputers vs conventional computers

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*different tasks, different structure, so ... why  
expect similarities ???*

Neurocomputers „exist“ in the traditional  
computers, are simulated.

Neurocomputers should solve problems at  
which the brain seems very good and at  
which conventional computers and artificial  
intelligence seem poor.





# Neurocomputers

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Neurocomputers are both fast and excellent at recognizing patterns and thus they can also operate as expert systems. Like the brain they are self-organizing and essentially self-programming.



# Comparison

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Different structure and different rules, difficult to find the area of comparison.

## Speed:

neuron sends approximately 1000 imp/sec  
electronic chip – billion or more

## Structure:

neural networks – parallel, many connections,  
(10 000)  
electronic chip – serial ( $< 100$ )



# Comparison

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Computers are designed to carry out one instruction after another, extremely rapidly, whereas our brain works with many more slow units. Whereas computer can carry out a millions of operations every second - the brain respond about ten times per second. The computer is a high-speed, serial machine, and is used as such, compared to a slow, highly parallel nature of the brain.



# Comparison

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Computer usually has a long and complicated program, which gives it specific instructions as to what to do at every stage in its operation.

In such a computer its processing power is located, is concentrated in a single processing unit - central processing unit (CPU). The information on which computations or operations have to be performed are stored in the computer memory.





# Comparison

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As a result of a single processor - only one processing step can be executed in time. Moreover, when executing a processing step, the CPU has access only to a very small fraction of the memory. It means that in practice, only an insignificant portion of a system and systems' knowledge participates in the processing.



# Comparison

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It seem appropriate to distribute the processing capability across the computer's memory - each memory cell become an active processing element interacting with other such elements. This results in a massively parallel computer made up of an extremely large number of simple processing units - as many as these are memory cells.



# Comparison



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Using such a massively parallel architecture would increase the computational power of a computer. This computer would be capable to execute many billions of operations per second.

The understanding of a neural architecture is very important for the development of massively parallel models of computation.



# Comparison

	processing elements	element size	energy use	processing speed	style of computation	fault tolerant	learns	intelligent, conscious
	$10^{14}$ synapses	$10^{-6}$ m	30 W	100 Hz	parallel, distributed	yes	yes	usually
	$10^8$ transistors	$10^{-6}$ m	30 W (CPU)	$10^9$ Hz	serial, centralized	no	a little	not (yet)

- • Volume:  $1400 \text{ cm}^3$
- • Surface:  $2000 \text{ cm}^2$
- • Weight: 1,5 kg
- • Cerebral cortex covering hemispheres contains  $10^{10}$  nerve cells
- • Number of connections between cells:  $10^{15}$
- • Speed of sending/receiving information's =  $10^{15}$  operations/sec





# Software and Functional Comparisons

	Neurocomputers	Conventional Computers
Feedback Sensitivity	Excellent	None
Memory	High density Distributed, Associative	Low Density Localized, Specific
Database Search	Fast Close Match	Slow Exact Match
Mathematical and Algorithmic Ability	Poor	Excellent
Heuristic Ability	Excellent	Poor
Pattern Recognition Ability	Fast	Slow
Incomplete Pattern Recognition	Excellent	Poor



# Hardware and Structural Comparisons

	<b>Neurocomputers</b>	<b>Conventional Computers</b>
Data Signal	Quasi-analog	Digital
Connectivity of Processing Elements	About 10 dynamically Changeable by Self-Programming	About 3 Not Changeable
Processing Sequence	Parallel, Simultaneous	Serial Independent
Site of Memory, Logic and Control	Nonlocal, Distributed in Connections	Localized to Processing Elements
Processing elements	Nonlinear. May be Nonthreshold. Arranged in Parallel	Linear, Threshold. Arranged in Series



# Comparison of Fifth- and Sixth Generation Computers

	5th Generation	6th Generation
Main Usage	Artificial Intelligence	Pattern Recognition
Processing elements	VLSI	Artificial Neural Networks
Technologies	Silicon	Silicon, Optics, Molecular electronics
Architecture	Parallel Modules	Parallel Processing Elements
Connections	Externally Programmable	Dynamically Self-Programmable
Self-Learning	Limited	Good
Software Development	Major Role in Success	Minor Role in Success
Use of Neurobiology in Design	None	Moderate



# Summary

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**Neurocomputer** – it is information processing machine, composed from elements mimicking neural elements (neurons). These elements are of very simple construction:

- *many inputs but one output only*
- *incoming signals are summarized*
- *the magnitude of the output signal depends from the input and so called threshold*





# Summary

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To distinguish the importance of the inputs signals are multiplied by *weights*.

So, the signal from out input can be different than identical signal from the another input.



# Summary

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Elements are connected forming the *net*. Part of a net receive the input signals, the other part is connected to the net input, but the majority are interconnected to each other

**structure of connections + weights**

decides what neurocomputer will do



# Summary

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Main advantage:

**ability for parallel processing**

„Normal” computer perform operations in serial, while a neurocomputer perform many operations in parallel.

*Even computer specially design for parallel processing – thousands processors – but neural networks – billions of processing elements.*



# Summary

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**Computer usually has a long and complicated program, which gives it specific instructions as to what to do at every stage in its operation.**



# Summary

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**The program for neurokomputer is in the structure of connections and the values of weights are its parameters. Moreover it has the learning capability.**

# Learning

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Learning system is simple. The system has to solve the task with known answer and we correct parameters in such a way – the system answer to be consistent with this answer.

Because about the elements' operation depends from its structure and weights

**Learning =  
change of weights**



# Learning

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Two main rules:

- **only neurons with wrong output signal are subject of the weights change**
- **the value of correction is proportional to the signal at the element input**



# Learning

For the simple nets (1-2 layers) learning is simple. For the multilayer nets the special learning methods are used, more popular to ***the backpropagation method***



*(Parallel distributed processing.,  
1986, D.E.Rumelhart & J.L.McClelland,  
MIT)*

