Quiz 2, STATS 401 F18

In lab on 11/16

PRELIMINARY VERSION. QUESTIONS NEED TO BE REWRITTEN AND/OR REAR-RANGED. This document produces different random quizzes each time the source code generating it is run. The actual quiz will be a realization generated by this random process, or something similar.

This version lists all the questions currently in the quiz generator. The quiz will have one question drawn at random from each of the five categories. No new questions will be added after Wednesday 11/14. Small changes may be made.

Instructions. You have a time allowance of 40 minutes, though the quiz may take you less time and you can leave lab once you are done. The quiz is closed book, and you are not allowed access to any notes. Any electronic devices in your possession must be turned off and remain in a bag on the floor.

Formulas

The following formulas are provided. To use these formulas properly, you need to make appropriate definitions of the necessary quantities.

- (1) $\mathbf{b} = (\mathbb{X}^{\mathrm{T}}\mathbb{X})^{-1}\mathbb{X}^{\mathrm{T}}\mathbf{y}$
- (2) $\operatorname{Var}(X) = \operatorname{E}[(X \operatorname{E}[X])^{2}] = \operatorname{E}[X^{2}] (\operatorname{E}[X])^{2}$
- (3) The probability density function of the standard normal distribution is $\frac{1}{\sqrt{2\pi}}e^{-x^2/2}$
- (4) Syntax from ?pnorm:

```
pnorm(q, mean = 0, sd = 1)
qnorm(p, mean = 0, sd = 1)
q: vector of quantiles.
p: vector of probabilities.
```

(5) If a random variable is normally distributed, the probability it falls within one standard deviation of the mean is 68%, within two standard deviations of the mean is 95%, and within three standard deviations of the mean is 99.7%.

Q1. Normal approximations, mean and variance

Q1-1. Recall the following analysis where the director of admissions at a large state university wants to assess how well academic success can be predicted based on information available at admission. She fits a linear model to predict freshman GPA using ACT exam scores and percentile ranking of each student within their high school, as follows.

```
gpa <- read.table("gpa.txt",header=T)
gpa_lm <- lm(GPA~ACT+High_School,data=gpa)
summary(gpa_lm)</pre>
```

```
##
## Call:
## lm(formula = GPA ~ ACT + High_School, data = gpa)
```

```
##
## Residuals:
##
        Min
                  1Q
                       Median
                      0.07311
##
   -2.10265 -0.29862
                               0.40355
                                         1.31336
##
##
  Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
   (Intercept) 1.292793
                          0.136725
                                      9.455
                                            < 2e-16
##
  ACT
               0.037210
                          0.005939
                                      6.266 6.48e-10 ***
  High_School 0.010022
                          0.001279
                                      7.835 1.74e-14 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  Signif. codes:
##
## Residual standard error: 0.5672 on 702 degrees of freedom
## Multiple R-squared: 0.2033, Adjusted R-squared: 0.2011
## F-statistic: 89.59 on 2 and 702 DF, p-value: < 2.2e-16
```

Suppose that an analysis of a large dataset from another comparable university gave a coefficient of 0.03528 for the ACT variable when fitting a linear model using ACT score and high school rank. The admissions director is interested whether the difference could reasonably be chance variation due to having only a sample of 705 students, or whether the universities have differences beyond what can be explained by sample variation. Suppose that population value for this school is also 0.03528. Supposing the usual probability model for a linear model (which you don't have to write out here) and using a normal approximation, find an expression for the probability that the difference between the coefficient estimate for the data (0.03721) and the hypothetical true value (0.03528) is larger in magnitude than the observed value (0.03721-0.03528). Write your answer as a call to pnorm(). Your call to pnorm may involve specifying any necessary numerical calculations that you can't work out without access to a computer or calculator.

Q1-2. Let X_1, X_2, \ldots, X_n be independent random variables each of which take the value 0 with probability 0.5, 1 with probability 0.25 and -1 with probability 0.25. Find the mean and variance of X_1 . Use this to find the mean and variance of $\bar{X} = \frac{1}{n} \sum_{i=1}^{n} X_i$. Now suppose n = 100 and suppose that \bar{X} is well approximated by a normal distribution. Find a number c such that $P(-c < \bar{X} < c)$ is approximately 0.9. Write your answer as a call to qnorm(). Your call to qnorm may involve specifying any necessary numerical calculations that you can't work out without access to a computer or calculator.

Q1-3. Let X_1, X_2, \ldots, X_n be independent random variables each of which take value 0 with probability 1/3 and 1 with probability 2/3.

- (a) Use the definitions and basic properties of expectation and variance to find the expected value and variance of X_1 .
- (b) Use these results to find the mean and variance of $\bar{X} = \frac{1}{n} \sum_{i=1}^{n} X_i$. (You might notice that this calculation is related to the binomial distribution. You can use that to check your work, if you like, but you are asked to find the solution directly.)
- (c) Now suppose n=50 and suppose that \bar{X} is well approximated by a normal distribution. Find $P(0.45 < \bar{X} < 0.55)$. Write your answer as a call to pnorm(). Your call to pnorm may involve specifying any necessary numerical calculations that you can't work out without access to a computer or calculator.

Q1-4. Let X_1, X_2, \ldots, X_n be independent random variables each of which take the value 0 with probability 0.25, and 4 with probability 0.75. Find the mean and variance of X_1 . Use this to find the mean and variance of $X = \sum_{i=1}^{n} X_i$. Now suppose n = 200 and suppose that X is well approximated by a normal distribution. Find a number c such that P[X < c] is approximately 0.9. Write your answer as a call to qnorm(). Your call

to quorm may involve specifying any necessary numerical calculations that you can't work out without access to a computer or calculator.

Q1-5. Let X_1, X_2, \ldots, X_n be independent random variables each of which has possible values 0, 1 and -1. The probability of taking 0 is 0.2 and the probability of 1 is 0.4. Find the mean and variance of $X = \frac{1}{n} \sum_{i=1}^{n} X_i$. Now suppose n = 100 and suppose that X is well approximated by a normal distribution. Find a number c such that P[X > c] is approximately 0.8. Write your answer as a call to qnorm(). Your call to qnorm may involve specifying any necessary numerical calculations that you can't work out without access to a computer or calculator.

Q2. Covariance and the multivariate normal distribution

To do

Q3. Prediction

Q3-1. To investigate the consequences of metal poisoning, 25 beakers of minnow larvae were exposed to varying levels of copper and zinc. The data were

```
toxicity <- read.table("toxicity.txt")
head(toxicity)</pre>
```

```
##
     Copper Zinc Protein
## 1
                0
                        201
           0
## 2
              375
                        186
              750
## 3
           0
                        173
                        110
## 4
           0 1125
## 5
           0 1500
                        115
## 6
          38
                        202
```

```
lm_toxicity <- lm(Protein~Copper+Zinc,data=toxicity)
round(coef(summary(lm_toxicity),3))</pre>
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 196 9 23 0
## Copper 0 0 -2 0
## Zinc 0 0 -6 0
```

The sample linear model is $\mathbf{y} = \mathbb{X}\mathbf{b} + \mathbf{e}$. Here, y_i is a measurement of total larva protein at the end of the experiment (in microgram, μg). $\mathbb{X} = [x_{ij}]$ is a 25×3 matrix where $x_{i1} = 1$, x_{i2} is copper concentration (in parts per million, ppm) in beaker i, and x_{i3} is zinc concentration (in parts per million, ppm) in beaker i.

Suppose we're interested in predicting the protein in a new observation at 100ppm copper and 1000ppm zinc.

- (a) Specify the values in a row matrix \mathbf{x}^* so that $\mathbf{y}^* = \mathbf{x}^* \mathbf{b}$ gives a least squares prediction of the new observation.
- (b) Explain how to use the data vector \mathbf{y} , the design matrix \mathbb{X} , and your row vector \mathbf{x}^* to construct a prediction interval that will cover the new measurement in approximately 95% of replications. Your answer should include formulas to construct this interval.
- (c) Explain briefly some things you would look for to check whether your prediction interval is reasonable.

Q3-2. Consider the birth weight data set we have seen in lab. For this question, we will look at columns bwt (birth weight), lwt (mother's weight), age (mother's age) and race (mother's race, 1 for white, 2 for black and 3 for other).

```
library(MASS)
data(birthwt)
head(birthwt,3)
      low age lwt race smoke ptl ht ui ftv
##
##
  85
                                0
           19 182
                      2
                            0
                                   0
                                      0
                                           3 2551
## 86
        0
           33 155
                      3
                            0
                                0
## 87
           20 105
                                   0
                      1
                                           1 2557
lm_bw <- lm(bwt ~ lwt + age +factor(race), data = birthwt)</pre>
summary(lm bw)$coef
##
                     Estimate Std. Error
                                             t value
                                                          Pr(>|t|)
## (Intercept)
                 2461.147482 314.722327
                                           7.8200600 3.968682e-13
                                          2.5840294 1.054066e-02
## lwt
                     4.619545
                                1.787729
## age
                     1.298831
                              10.107701 0.1284991 8.978943e-01
## factor(race)2 -447.614691 161.369310 -2.7738527 6.110757e-03
## factor(race)3 -239.356515 115.188920 -2.0779474 3.910220e-02
```

Now suppose we are interested in predicting the birthweight of a baby who has a 30-year-old white mother with weight 130.

- (a) Specify a row matrix \mathbf{x}^* so that $\hat{y}^* = \mathbf{x}^* \mathbf{b}$ gives the least square predictor.
- (b) Write a matrix expression for the variance of $\hat{Y}^* = \mathbf{x}^* \hat{\boldsymbol{\beta}}$ where $\hat{\boldsymbol{\beta}}$ is the least squares fit on model-generated data, i.e., $\hat{\boldsymbol{\beta}} = (\mathbb{X}^T \mathbb{X})^{-1} \mathbb{X}^T \mathbf{Y}$.

Q3-3. We analyze the following data on video game sales in North America. This dataset records sales (in millions of dollars) for 580 games within three genres (shooter, sports and action) from two publishers (Electronic Arts and Activision) with years of release from 2006 to 2010 inclusive, on ten different platforms.

```
vg <- read.table("vg_sales.txt") ; head(vg)</pre>
```

```
##
                           Name Platform Year
                                                 Genre
                                                             Publisher Sales
        Call of Duty: Black Ops
## 1
                                     X360 2010 Shooter
                                                            Activision
                                                                         9.70
## 2
        Call of Duty: Black Ops
                                      PS3 2010 Shooter
                                                            Activision
                                                                         5.99
## 3 Call of Duty: World at War
                                     X360 2008 Shooter
                                                            Activision
                                                                         4.81
## 4 Call of Duty: World at War
                                      PS3 2008 Shooter
                                                            Activision
                                                                         2.73
## 5
                 FIFA Soccer 11
                                      PS3 2010
                                                Sports Electronic Arts
                                                                         0.61
## 6
                  Madden NFL 07
                                     PS2 2006
                                                Sports Electronic Arts
```

Consider the probability model $Y_{ijk} = \alpha + \beta_j + \gamma_k + \epsilon_{ijk}$ where j = 1, 2, 3 specifies the genre (shooter, sports and action, respectively), k = 1, 2 gives the publisher (Electronic Arts and Activision, respectively), and i ranges over all the games in each (j, k) category. In order to code these factors, we set $\beta_1 = \gamma_1 = 0$. As usual, ϵ_{ijk} gives an independent $N[0, \sigma]$ error for game (i, j, k). Parameters in this probability model are estimated by least squares as follows:

```
lm_vg1 <- lm(Sales ~ Publisher + Genre, data = vg)
summary(lm_vg1)</pre>
```

```
##
## Call:
## lm(formula = Sales ~ Publisher + Genre, data = vg)
##
```

```
## Residuals:
##
       Min
                1Q Median
                                30
                                        Max
                            0.0858
                                    8.8556
##
  -0.8444 -0.2662 -0.1352
##
##
  Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                             0.271127
                                         0.061346
                                                    4.420 1.18e-05 ***
## PublisherElectronic Arts -0.004955
                                         0.071076
                                                   -0.070
                                                              0.944
  GenreShooter
                              0.573315
                                         0.095061
                                                    6.031 2.91e-09 ***
## GenreSports
                              0.118062
                                         0.077585
                                                    1.522
                                                              0.129
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.7818 on 576 degrees of freedom
## Multiple R-squared: 0.06154,
                                     Adjusted R-squared:
## F-statistic: 12.59 on 3 and 576 DF, p-value: 5.546e-08
```

Note that the output of summary(lm_vg1) tells you that R is using $\beta = (\alpha, \beta_2, \beta_3, \gamma_2)$ as the parameter vector.

- (a) Write the first six lines of the design matrix \mathbb{X} in the matrix version of the linear model $\mathbf{Y} = \mathbb{X}\boldsymbol{\beta} + \boldsymbol{\epsilon}$. Hint: the output from head(vg) tells you what the values of j and k are for each of the first six observations.
- (b) Suppose we're interested in the predicting the North American Sales of a shooting game released by Activision. Specify a row matrix \mathbf{x}^* such that $y^* = \mathbf{x}^* \mathbf{b}$ gives the least square predictor of this quantity.

Q3-4. We consider a subset of the National Education Longitudinal Study of 1988 which examined schoolchildren's performance on a math test score in 8th grade. ses is the socioeconomic status of parents and paredu is the parents highest level of education achieved (less than high school, high school, college, BA, MA, PhD). The dataset called nels88 starts as follows:

head(nels88)

```
##
                     ses paredu math
        sex race
## 1 Female White -0.13
                                   48
                              hs
       Male White -0.39
                              hs
                                   48
## 3
       Male White -0.80
                                   53
                              hs
## 4
       Male White -0.72
                                   42
## 5 Female White -0.74
                                   43
                              hs
## 6 Female White -0.58
                                   57
```

We fit a regression model to the data. The rounded co-efficients for the model are provided below:

```
fit <- lm(math ~ ses + paredu, data = nels88)
round(summary(fit)$coef)</pre>
```

```
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          59
                                       2
                                               33
                                                          0
                           3
                                       1
                                                2
                                                          0
## ses
                          -8
                                       2
                                               -4
## pareducollege
                                                          0
## pareduhs
                        -12
                                       3
                                               -5
                                                          0
## paredulesshs
                                       3
                                               -4
                         -13
                                                          0
## pareduma
                          -1
                                       2
                                                0
                                                          1
## pareduphd
                          -2
                                       3
                                               -1
                                                          0
```

- (a) Describe a suitable probability model, in matrix form, to give a sample version of the linear model that has been fit above.
- (b) Find the predicted math score for a student whose family has an ses value of -0.5 and whose parents' highest education level is high school (hs).
- (c) How is the residual standard error calculated for this model? (Give a formula).

Q4. Linear models with factors

Q4-1. We consider a dataset of measurements on crabs. The start of the dataset **crabs** is shown below. Here, BD refers to the body depth of the crabs. The species **sp** corresponds to the color of the crabs, which is a factor with two levels, Blue (B) and Orange (0). We want to study the difference of frontal lobe size (FL) of two species.

head(crabs)

```
##
     sp sex index
                     FL
                        RW
                              CL
                                    CW
                                        BD
## 1
          М
                 1
                    8.1 6.7 16.1 19.0 7.0
## 2
                 2
                    8.8 7.7 18.1 20.8 7.4
      В
          Μ
                 3
## 3
      В
          Μ
                    9.2 7.8 19.0 22.4 7.7
## 4
      В
                 4
                    9.6 7.9 20.1 23.1 8.2
          M
                   9.8 8.0 20.3 23.0 8.2
## 5
      В
          М
## 6
                 6 10.8 9.0 23.0 26.5 9.8
      В
```

Consider the probability model $Y_i = \mu_1 x_{Bi} + \mu_2 x_{Oi} + \epsilon_i$ for i = 1, ..., 200. Y_i is the frontal lobe size of crab i. x_{Bi} is 1 if crab i is of species Blue and 0 otherwise. Similarly, x_{Oi} is 1 if crab i is of species Orange and 0 otherwise. ϵ_i are i.i.d with mean 0 and variance σ^2 . This model can be fitted to the **crabs** dataset in R using the lm() function. The resulting summary is provided below.

```
lm_crab <- lm(FL~sp-1, data=crabs)
summary(lm_crab)</pre>
```

```
##
## Call:
## lm(formula = FL ~ sp - 1, data = crabs)
##
## Residuals:
##
     Min
              1Q Median
                            3Q
                                  Max
  -8.010 -2.410 0.390
                        2.169
                               7.244
##
##
##
  Coefficients:
##
       Estimate Std. Error t value Pr(>|t|)
         14.056
                     0.315
                             44.62
                                     <2e-16 ***
## spB
                                     <2e-16 ***
         17.110
                     0.315
                             54.31
## sp0
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.15 on 198 degrees of freedom
## Multiple R-squared: 0.9615, Adjusted R-squared: 0.9611
## F-statistic: 2470 on 2 and 198 DF, p-value: < 2.2e-16
```

- (a) Interpret the meaning of μ_1 and μ_2 in the above probability model?
- (b) Build a 95% confidence interval for μ_1 using normal approximation

(c) Recall in homework we know that the full estimated covariance matrix of $\hat{\boldsymbol{\mu}} = (\hat{\mu}_1, \hat{\mu}_2)$ can be found by

Use V and information provided in summary(lm_crab) to write down an expression that constructs a 95% confidence interval for $\mu_1 - \mu_2$.

Q4-2. Consider the following linear model for the mouse diet data that we have studied repeatedly

```
mice <- read.table("femaleMiceWeights.csv",sep=",",header=TRUE)
head(mice)</pre>
```

```
##
       (Intercept) Diethf
## 1
                  1
                          0
## 2
                  1
                          0
## 3
                  1
                          0
                          0
## 4
                  1
## 5
                  1
                          0
## 6
                  1
                          0
## 7
                          0
                  1
                          0
## 8
                  1
                          0
## 9
                  1
## 10
                  1
                          0
## 11
                  1
                          0
## 12
                          0
                  1
## 13
                  1
                          1
                          1
## 14
                  1
## 15
                          1
                  1
## 16
                  1
                          1
## 17
                  1
                          1
## 18
## 19
                  1
                          1
## 20
                          1
## 21
                  1
                          1
## 22
                  1
                          1
## 23
                  1
                          1
## 24
                          1
                  1
## attr(,"assign")
## [1] 0 1
## attr(,"contrasts")
```

sp0 0.00000000 0.09923719

```
## attr(,"contrasts")$Diet
## [1] "contr.treatment"
```

- (a) Write down the sample linear model fitted in lm_mice using the subscript format.
- (b) Explain how to obtain estimates of the means of both treatment groups, and the difference between these means, from the coefficients of this sample linear model.

Q4-3. We analyze the following data on video game sales in North America. This dataset records sales (in millions of dollars) for 580 games within three genres (shooter, sports and action) from two publishers (Electronic Arts and Activision) with years of release from 2006 to 2010 inclusive, on ten different platforms. We consider the following analysis

```
vg <- read.table("vg sales.txt") ; head(vg)</pre>
##
                            Name Platform Year
                                                  Genre
                                                              Publisher Sales
## 1
        Call of Duty: Black Ops
                                     X360 2010 Shooter
                                                             Activision
## 2
        Call of Duty: Black Ops
                                      PS3 2010 Shooter
                                                             Activision
                                                                          5.99
## 3 Call of Duty: World at War
                                     X360 2008 Shooter
                                                             Activision
                                                                          4.81
## 4 Call of Duty: World at War
                                      PS3 2008 Shooter
                                                             Activision
                                                                          2.73
## 5
                 FIFA Soccer 11
                                      PS3 2010
                                                 Sports Electronic Arts
                                                                          0.61
## 6
                  Madden NFL 07
                                      PS2 2006
                                                 Sports Electronic Arts
lm_vg2 <- lm(Sales ~ Publisher-1, data = vg)</pre>
summary(lm_vg2)
##
## Call:
## lm(formula = Sales ~ Publisher - 1, data = vg)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
##
   -0.4412 -0.3212 -0.2136
                             0.0464
                                     9.2588
##
## Coefficients:
##
                             Estimate Std. Error t value Pr(>|t|)
## PublisherActivision
                              0.44124
                                          0.05095
                                                    8.661
                                                            <2e-16 ***
## PublisherElectronic Arts
                              0.41361
                                          0.04434
                                                    9.327
                                                            <2e-16 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.8055 on 578 degrees of freedom
## Multiple R-squared: 0.2189, Adjusted R-squared: 0.2162
## F-statistic:
                   81 on 2 and 578 DF, p-value: < 2.2e-16
```

The fitted probability model is $Y_{ij} = \pi_j + \epsilon_{ij}$ where j = 1, 2 specifies the publisher (Electronic Arts and Activision, respectively), and i ranges over all the games for each publisher. As usual, ϵ_{ij} gives an independent $N[0, \sigma]$ error for game (i, j). Parameters in this probability model are estimated by least squares as follows:

- (a) What do the coefficients in the summary above measure?
- (b) Explain how to build a 95% confidence interval for Activision sales using a normal approximation. You can use the property that P[Z < 1.96] = 0.975 when Z has a N[0, 1] distribution.

Q4-4. We consider a dataset of measurements on crabs. The start of the dataset crabs is shown below. Here, BD refers to the body depth of the crabs, and sp denotes the colour of the crabs, which is one of blue or

orange.

```
head(crabs)
```

```
##
     sp sex index
                    FL RW
                              CL
                                   CW BD
## 1
     В
          Μ
                1
                   8.1 6.7 16.1 19.0 7.0
                   8.8 7.7 18.1 20.8 7.4
                 2
## 2
     B
          М
## 3
      В
          М
                3
                   9.2 7.8 19.0 22.4 7.7
## 4
     В
          М
                 4
                   9.6 7.9 20.1 23.1 8.2
## 5 B
          М
                5 9.8 8.0 20.3 23.0 8.2
                6 10.8 9.0 23.0 26.5 9.8
## 6 B
          М
crabs$mu1 <- (crabs$sp == "B")*1</pre>
crabs$mu2 <- (crabs$sp == "0")*1
crabs$mu3 <- 1
crabs$mu4 <- 1-crabs$mu1
crabs$mu_diff <- crabs$mu2</pre>
fit1 <- lm(BD \sim mu1+mu2-1, data = crabs)
fit2 <- lm(BD ~ mu3 + mu_diff - 1, data = crabs)
fit3 <- lm(BD \sim mu2, data = crabs)
fit4 <- lm(BD \sim 1-mu1, data = crabs)
fit5 <- lm(BD \sim mu4, data = crabs)
fit6 <- lm(BD~ mu1+mu2, data = crabs)
```

(a) Would any of the models (fit1 to fit6) give the same coefficients? If yes, list them.

Now consider the probability model $Y_i = \mu_1 x_{Bi} + \mu_2 x_{Oi} + \epsilon_i$, where i = 1, ..., 200. Y_i models the body weight of observation i. x_{Bi} is 1 if sp=B for observation i and 0 otherwise. Similarly, x_{Oi} is 1 if sp=0 for observation i and 0 otherwise. $\epsilon_1, ..., \epsilon_{200}$ are i.i.d with mean 0 and variance σ^2 . This model can be fitted to the crabs dataset in R using the lm() function. The resulting summary is provided below.

```
summary(fit1)
```

```
##
## Call:
## lm(formula = BD ~ mu1 + mu2 - 1, data = crabs)
## Residuals:
##
                 1Q Median
## -8.0780 -2.1830 0.0695 2.3170 7.4170
##
## Coefficients:
       Estimate Std. Error t value Pr(>|t|)
## mu1
         12.583
                      0.311
                               40.46
                                        <2e-16 ***
## mu2
         15.478
                      0.311
                               49.77
                                        <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.11 on 198 degrees of freedom
## Multiple R-squared: 0.9541, Adjusted R-squared: 0.9536
## F-statistic: 2057 on 2 and 198 DF, p-value: < 2.2e-16
 (b) Interpret \mu_1 and \mu_2 in the above model?
 (c) Recall from homework that the estimated covariance matrix of \hat{\beta} = (\hat{\mu}_1, \hat{\mu}_2) can be found by
```

V <- summary(fit1)\$cov.unscaled * summary(fit1)\$s^2; V

mu1 mu2 ## mu1 0.09671882 0.00000000 ## mu2 0.00000000 0.09671882
Construct a 95% confidence interval for $\mu_1 - \mu_2$ using normal approximation. Based on this, do we have sufficient evidence to conclude that $\mu_1 = \mu_2$ at the 95% level?

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