## Panal Data 1: Framework

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# Section 1

Introduction

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#### Introduction

- ▶ Panel data has observations on n cross-sectional units at T time periods:  $(X_{it}, Y_{it})$
- Examples:
  - 1. Person *i*'s income in year *t*.
  - 2. Vote share in county *i* for the presidential election year *t*.
  - 3. Country i's GDP in year t.
- Panel data is useful because
  - 1. More variation (both cross-sectional and temporal variation)
  - 2. Can deal with time-invariant unobserved factors.
  - 3. (Not focus in this course) Dynamics of individual over time.

#### Overview

Consider the model

$$y_{it} = \beta' x_{it} + \epsilon_{it}, E[\epsilon_{it}|x_{it}] = 0$$

where  $x_{it}$  is a k-dimensional vector

- ▶ If there is no correlation between  $x_{it}$  and  $\epsilon_{it}$ , you can estimate the model by OLS (pooled OLS)
- ▶ A natural concern here is the omitted variable bias.
- ▶ We now consider that  $\epsilon_{it}$  is written as

$$\epsilon_{it} = \alpha_i + u_{it}$$

where  $\alpha_i$  is called **unit fixed effect**, which is the time-invariant unobserved heterogeneity.

▶ With panel data, we can control for the unit fixed effects by incorporating the dummy variable for each unit i!

$$y_{it} = \beta' x_{it} + \gamma_2 D2_i + \cdots + \gamma_n Dn_i + u_{it}$$

where  $Dl_i$  takes 1 if l = i.

- Notice that we cannot do this for the cross-section data!
- ▶ We often write the model with unit FE as

$$y_{it} = \beta' x_{it} + \alpha_i + u_{it}$$

#### Framework

► The fixed effects model

$$y_{it} = \beta' x_{it} + \alpha_i + u_{it}$$

- ► Assumptions:
  - 1.  $u_{it}$  is uncorrelated with  $(x_{i1}, \dots, x_{iT})$ , that is  $E[u_{it}|x_{i1}, \dots, x_{iT}] = 0$
  - 2.  $(Y_{it}, x_{it})$  are independent across individual i.
  - 3. No outliers
  - 4. No Perfect multicollinarity
- Let's discuss Assumptions 1, 2, and 4 in detail.

- Assumption 1 is weaker than the assumption in OLS, because the time-invariant factor  $\alpha_i$  is captured by the fixed effect.
  - **Example:** Unobserved ability is caputured by  $\alpha_i$ .
- Assumption 2 allows for serial correlation (i.e.,  $Cov(x_{it}, x_{it'}) \neq 0$ ) within individual i.
  - ▶ This is related to the cluster-robust standard error.
- Assumption 4 seems as usual, but it has an important role in panel data analysis.
- Consider the following regression with unit FE

$$wage_{it} = \beta_0 + \beta_1 experience_{it} + \beta_2 male_i + \beta_3 white_i + \alpha_i + u_{it}$$

where  $experience_{it}$  measures how many years worker i has worked before at time t.

- ▶ In the regression above, we have multicollinearity issue because of *male<sub>i</sub>* and *white<sub>i</sub>*.
- Intuitively, we cannot estimate the coefficient  $\beta_2$  and  $\beta_3$  because those **time-invariant** variables are completely captured by the unit fixed effect  $\alpha_i$ .

# Estimation (within transformation)

- You can estimate the model by adding dummy variables for each individual. This is called least square dummy variables (LSDV) estimator.
- ► This is computationary demanding if we have many cross-sectional observations.
- ▶ We often use the following within transformation.
- ▶ Define the new variable  $\tilde{Y}_{it}$  as

$$\tilde{Y}_{it} = Y_{it} - \bar{Y}_i$$

- where  $\bar{Y}_i = \frac{1}{T} \sum_{t=1}^{T} Y_{it}$ .
- Nhy is this useful? By applying the within transformation to the regression model, we can eliminate the unit fixed effect  $\alpha_i$

$$\tilde{Y}_{it} = \beta' \tilde{X}_{it} + \tilde{u}_{it}$$

Then apply the OLS estimator to the above equation!.

### Importance of within variation

- As I talked before, the variation of the explanatory variable is key for precisely estimating the coefficients (once we control for the endogeneity).
- ▶ Within transformation eliminates the time-invariant unobserved factor, which is a large source of endogeneity in many situations.
- $\triangleright$  But, within transformation also absorbs the variation of  $X_{it}$ .
- Remember that

$$\tilde{X}_{it} = X_{it} - \bar{X}_i$$

- ▶ The transformed variable  $\tilde{X}_{it}$  has the variation over time t within unit i.
- ▶ If  $X_{it}$  is fixed over time within unit i,  $\tilde{X}_{it} = 0$ , so that no variation.

### FE, FE, and FE

▶ In addition to unit FE, you can also add time fixed effects (FE)

$$y_{it} = \beta' x_{it} + \alpha_i + \gamma_t + u_{it}$$

- ► The regression above controls for both time-invariant individual heterogeneity and (unobserved) aggregate year shock.
- ▶ Panel data is useful to capture various unobserved shock by including fixed effects.

## Panel + IV

▶ You can use IV regression with panel data. This is PS5.

#### Standard Errors

- ► In the cross-section data, we need to use the heteroskedasticity robust standard error.
  - Remember: Heteroskedasticity means  $Var(u_i|x_i) = \sigma(x_i)$ .
- ▶ In the panel data setting, we need to consider the **autocorrelation** of the variable, that is the correlation between  $u_{it}$  and  $u_{it'}$  across periods for each individual i.
- ► The current standard is to use so-called **cluster-robust standard error**.
  - ► The cluster is unit *i*. The observations within cluster are allowed to be freely correlated.
  - Cluster-robust standard error takes care for such correlation.
- ▶ I will explain how to deal with this in R.