ETC3250 2018 - Lab 1 and 2 solutions

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Getting up and running with the computer:

- R and RStudio
- RStudio Projects
- RMarkdown
- R syntax and basic functions

What is R?

From Wikipedia: "R is a programming language and software environment for statistical computing and graphics supported by the R Foundation for Statistical Computing. The R language is widely used among statisticians and data miners for developing statistical software and data analysis."

R is free to use and has more than 11,000 user contributed add-on packages on the Comprehensive R Archive Network (CRAN).

What is RStudio?

From Julie Lowndes:

If R were an airplane, RStudio would be the airport, providing many, many supporting services that make it easier for you, the pilot, to take off and go to awesome places. Sure, you can fly an airplane without an airport, but having those runways and supporting infrastructure is a game-changer.

The RStudio integrated development environment (IDE) has multiple components including:

- 1. Source editor (to edit your scripts):
- Docking station for multiple files,
- Useful shortcuts ("Knit"),
- Highlighting/Tab-completion,
- Code-checking (R, HTML, JS),
- Debugging features
- 2. Console window (to run your scripts, to test small pieces of code):
- Highlighting/Tab-completion,
- Search recent commands
- 3. Other tabs/panes:
- Graphics,
- R documentation,
- Environment pane,
- File system navigation/access,
- Tools for package development, git, etc

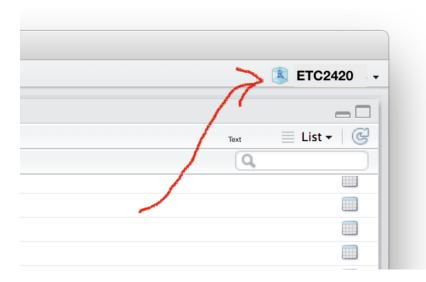


Figure 1: Using projects to organise your work

RStudio Projects

- Project directories keep your work organized since you will keep your data, your code, your results all located in one place.
- For the unit ETC2420, I have created a project on my laptop called ETC2420. Note that the name of the current project can be seen at the top right of the RStudio window.
- Each time you start RStudio for this class, be sure to open the right project.

Exercise 1

Create a project for this unit, in the directory.

• File -> New Project -> Existing Directory -> Empty Project

Exercise 2

Open a new Rmarkdown document. You are going to want to call it Lab1 (it will automatically get the file extension .Rmd when you save it).

- File -> New File -> R Markdown -> OK -> Knit HTML

What is RMarkdown?

- R Markdown is an authoring format that enables easy creation of dynamic documents, presentations, and reports from R.
- It combines the core syntax of **markdown** (an easy-to-write plain text format) **with embedded R code chunks** that are run so their output can be included in the final document.
- R Markdown documents are fully reproducible (they can be automatically regenerated whenever underlying R code or data changes).

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document.

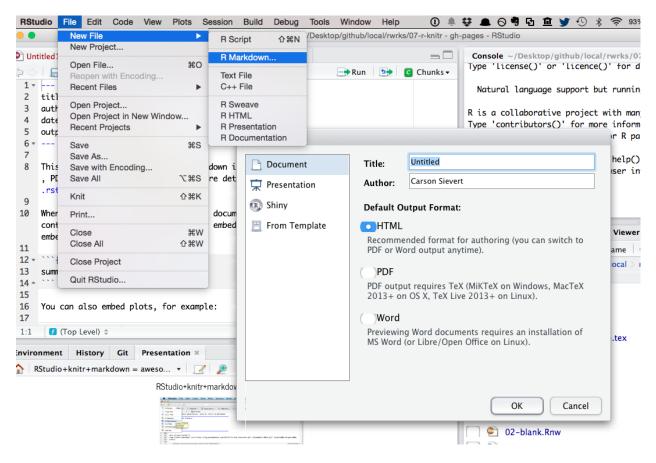


Figure 2: Writing and computing with the one document

Equations can be included using LaTeX (https://latex-project.org/) commands like this:

$$s^2 = \frac{1}{n-1}\sum_{i=1}^n (x_i-\frac{x})^2.$$

$$s^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2}.$$

We can also use inline mathematical symbols such as α and α , which produce α and α , respectively.

For more details on using R Markdown see http://rmarkdown.rstudio.com. Spend a few minutes looking over that website before continuing with this document.

Exercise 3

Look at the text in the lab1.Rmd document.

- What is R code?
- How does knitr know that this is code to be run?
- Using the RStudio IDE, work out how to run a chunk of code. Run this chunk, and then run the next chunk.
- Using the RStudio IDE, how do you run just one line of R code?
- Using the RStudio IDE, how do you highlight and run multiple lines of code?
- What happens if you try to run a line that starts with ""'{r}"? Or try to run a line of regular text from the document?
- Using the RStudio IDE, knit the document into a Word document.

Some R Basics

• Type and Figure out what each of the following command is doing:

```
(100+2)/3

5*10^2

1/0

0/0

(0i-9)^(1/2)

sqrt(2*max(-10,0.2,4.5))+100

x <- sqrt(2*max(-10,0.2,4.5))+100

x

log(100)

log(100,base=10)
```

- Check that these are equivalent: y <- 100, y = 100 and 100 \rightarrow y
- Find the help page for the mean command, either from the help menu, or by typing one of these: help(mean) and ?mean. Most help pages have examples at the bottom.
- The summary command can be applied to almost anything to get a summary of the object. Try summary(c(1, 3, 3, 4, 8, 8, 6, 7))

Data Types

- list's are heterogeneous (elements can have different types)
- data.frame's are heterogeneous but elements have same length (dim reports the dimensions and colnames shows the column names)
- vector's and matrix's are homogeneous (elements have the same type), which would be why c(1, "2") ends up being a character string.
- function's can be written to save repeating code again and again
- Try to understand these commands: class, typeof, is.numeric, is.vector and length
- See Hadley Wickham's online chapters on data structures (http://adv-r.had.co.nz/Data-structures.html) for more

Operations

• Use built-in *vectorized* functions to avoid loops

```
set.seed(1000)
x <- rnorm(6)
x
# [1] -0.44577826 -1.20585657  0.04112631  0.63938841 -0.78655436 -0.38548930
sum(x + 10)
# [1] 57.85684</pre>
```

- R has rich support for documentation, see ?sum
- Use [to extract elements of a vector.

```
x[1]

# [1] -0.4457783

x[c(T, F, T, T, F, F)]

# [1] -0.44577826 0.04112631 0.63938841
```

• Extract named elements with \$, [[, and/or [

```
x <- list(
    a = 10,
    b = c(1, "2")
)
x$a
# [1] 10
x[["a"]]
# [1] 10
x["a"]
# $a
# [1] 10</pre>
```

Examining 'structure'

• str() is a very useful R function. It shows you the "structure" of (almost) any R object (and everything in R is an object!!!)

```
str(x)
# List of 2
# $ a: num 10
# $ b: chr [1:2] "1" "2"
```

Missing Values

- NA is the indicator of a missing value in R
- Most functions have options for handling missings

```
x <- c(50, 12, NA, 20)

mean(x)

# [1] NA

mean(x, na.rm=TRUE)

# [1] 27.33333
```

Counting Categories

• the table function can be used to tabulate numbers

```
table(c(1, 2, 3, 1, 2, 8, 1, 4, 2))
#
# 1 2 3 4 8
# 3 3 1 1 1
```

Functions

One of the powerful aspects of R is to build on the reproducibility. If you are going to do the same analysis over and over again, compile these operations into a function that you can then apply to different data sets.

```
average <- function(x)
{
   return(sum(x)/length(x))
}

y1 <- c(1,2,3,4,5,6)
average(y1)
# [1] 3.5

y2 <- c(1, 9, 4, 4, 0, 1, 15)
average(y2)
# [1] 4.857143</pre>
```

Now write a function to compute the mode of some vector, and confirm that it returns 4 when applied on y < -c(1, 1, 2, 4, 4, 4, 9, 4, 4, 8)

Exercise 4

- What's an R package?
- How do you install a package?
- How does the library() function relates to a package?
- How often do you load a package?
- Install and load the package ISLR

Getting data

Data can be found in R packages

These are not usually kept up to date but are good for practicing your analysis skills on.

Or in their own packages

```
library(gapminder)
glimpse(gapminder)
# Observations: 1,704
# Variables: 6
# $ country <fctr> Afghanistan, Afghanistan, Afghanistan, Afghanistan, ...
# $ continent <fctr> Asia, Asi
```

I primarily use the **readr** package for reading data now. It mimics the base R reading functions but is implemented in C so reads large files quickly, and it also attempts to identify the types of variables.

You can pull data together yourself, or look at data compiled by someone else.

Question 1

- Look at the economics data in the ggplot2 package. Can you think of two questions you could answer using these variables?
- Write these into your .Rmd file.

Solution:

There could be many possible questions that might be answered by this data. Examples include these ones:

- Does the personal savings rate dip when unemployment is high?
- Is there a seasonal effect in unemployment?
- Is population increasing?

Question 2

- Read the documentation for gapminder data. Can you think of two questions you could answer using these variables?
- Write these into your .Rmd file.

Solution:

There could be many possible questions that might be answered by this data. Examples include these ones:

- Is life expectancy positively associated with gdp percapita?
- Is life expectancy increasing over time?
- Is the trend in life expectancy similar across all countries?

Question 3

- Read the documentation for pedestrian sensor data. Can you think of two questions you could answer using these variables?
- Write these into your .Rmd file.

Solution:

There could be many possible questions that might be answered by this data. Examples include these ones:

- What places in the city see the most pedestrians?
- What times would be rush hours on week days?
- Can you see the Wednesday night markets location and time based on pedestrian traffic?
- Is White Night visible in terms of pedestrian traffic?
- Are more people out and about in summer than in winter?

Question 4

- 1. Read in the OECD PISA data (available at https://github.com/bsouhaib/BA2018/raw/master/data/student_sub.rds)
- 2. Tabulate the countries (CNT)
- 3. Extract the values for Australia (AUS) and Shanghai (QCN)
- 4. Compute the average and standard deviation of the reading scores (PV1READ), for each country
- 5. Write a few sentences explaining what you learn about reading in these two countries.

Solution

```
student2012.sub <- readRDS("../../data/student_sub.rds")</pre>
student2012.sub <- readRDS(gzcon(url("https://github.com/bsouhaib/BA2018/raw/master/data/student_sub.rd
table(student2012.sub$CNT)
    ARE
          AUS
                AUT
                                         CAN
                                                CHL
                                                                         DNK
                       BEL
                             BGR
                                   BRA
                                                      COL
                                                            CZE
                                                                  DEU
#
 11500 14481
               4755
                     8597
                            5282
                                  5506 21544
                                               6856
                                                     9073
                                                           5327
                                                                 5001
                                                                        7481
    ESP
          EST
                FIN
                      FRA
                             GBR
                                   HKG
                                         HRV
                                               HUN
                                                      IRL
                                                            ISR
                                                                  ITA
                                                                         JPN
         4779
#
 10175
               8829
                      4613
                            4185
                                  4670
                                        5008
                                               4810
                                                     5016
                                                           5055
                                                                 5495
                                                                        6351
                                         POL
                                                            RUS
    KOR
          MAC
                MNE
                      MYS
                             NLD
                                   NOR
                                                PRT
                                                      QCN
                                                                  SGP
                                                                         SRB
#
   5033 5335
               4744
                     5197
                            4460
                                  4686
                                        4607
                                              5722 5177 5231
                                                                 5546 4684
#
         SVN
    SVK
                SWE
                       TAP
                             TUR
                                   URY
                                         USA
  4678 5911 4736
                     6046 4848 5315 4978
australia <- student2012.sub[student2012.sub$CNT=="AUS",]
shanghai <- student2012.sub[student2012.sub$CNT=="QCN",]</pre>
mean(australia$PV1READ)
# [1] 500.8453
sd(australia$PV1READ)
# [1] 100.7817
mean(shanghai$PV1READ)
# [1] 567.4197
sd(shanghai$PV1READ)
# [1] 79.91869
```

The reading scores are higher in Shanghai than in Australia by about 67 points. The variation in scores in Australia is higher, with a standard deviation of 100 as opposed to 80 for Shanghai.

Alternative code:

```
library(dplyr)
library(knitr)
library(tidyr)
student2012.sub %>% select(CNT) %>% group_by(CNT) %>% tally()
# # A tibble: 43 x 2
       CNT
#
#
     <chr> <int>
#
  1
       ARE 11500
#
   2
       AUS 14481
#
   3
       AUT
            4755
#
   4
       BEL
            8597
#
       BGR 5282
   5
#
   6
       BRA
            5506
   7
       CAN 21544
  8
       CHL 6856
```

```
# 9    COL    9073
# 10    CZE    5327
# # ... with 33 more rows
student2012.sub %>% filter(CNT %in% c("AUS", "QCN")) %>%
group_by(CNT) %>%
summarise(m=mean(PV1READ), s=sd(PV1READ)) %>% kable(digits=1)
```

CNT	m	s
AUS	500.8	100.8
QCN	567.4	79.9

Resources

- RStudio cheat sheet
- Q/A site: http://stackoverflow.com
- Dynamic Documents with R and knitr, Yihui Xie,

More exercises

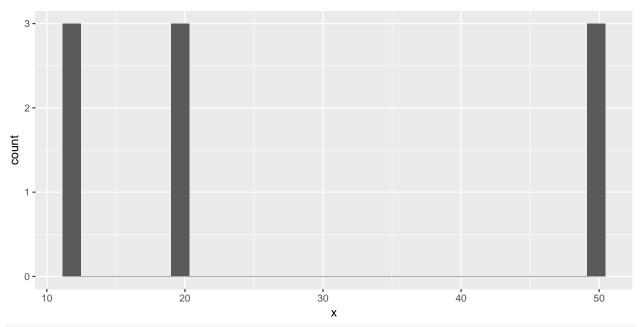
• R is great for matrix calculations:

```
X \leftarrow matrix(c(3,4,5,2), nrow=2, ncol=2)
t(X)
      [,1] [,2]
# [1,] 3 4
# [2,]
      5
Xinv <- solve(X)</pre>
X %*% Xinv
# [,1] [,2]
# [1,] 1 0
# [2,] 0 1
A <- matrix(rnorm(200), nrow=5, ncol=40)
B <- A \ \*\ t(A)
dim(B)
# [1] 5 5
diag(B)
# [1] 32.40283 44.06336 37.12973 33.43034 36.98610
eigen(B)
# $values
# [1] 55.59994 38.03823 34.03742 28.19920 28.13756
# $vectors
            [,1]
                      [,2]
                                [,3]
                                                    [,5]
                                          [,4]
# [1,] 0.07823187 0.4147787 0.6359504 -0.3550793 0.53974460
# [3,] -0.29577628 -0.7898528 0.2640844 0.1557843 0.44117983
# [4,] 0.29027001 -0.1105043 0.6950648 0.3529438 -0.54391882
# [5,] 0.55591392 0.1214021 -0.1791507 0.6529038 0.46673636
svd(A)
```

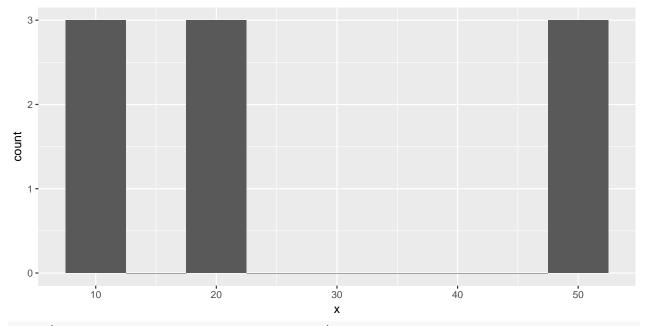
```
# [1] 7.456537 6.167514 5.834160 5.310292 5.304485
#
            [,1]
                      [,2]
                               [,3]
                                         [,4]
# [1,] -0.07823187   0.4147787 -0.6359504   0.3550793 -0.53974460
# [2,] 0.71630943 0.4208819 -0.1030362 -0.5466234 -0.01859059
# [3,] 0.29577628 -0.7898528 -0.2640844 -0.1557843 -0.44117983
# [4,] -0.29027001 -0.1105043 -0.6950648 -0.3529438  0.54391882
# [5,] -0.55591392  0.1214021  0.1791507 -0.6529038 -0.46673636
# $v
              [,1]
                        [,2]
                                   [,3]
                                               [,4]
  [1,] 0.200098106 0.02474797 0.17341971 0.1066878804 -0.006918478
  [2,] 0.052014674 0.01375789 0.22816349 0.0218648906 -0.085911769
  [3,] -0.287775257   0.32296899   0.13189034   -0.2746117793   -0.058730521
  [4,] 0.094352275 -0.07033170 0.19049218 -0.2147126769 -0.041763028
  [5,] 0.041379531 -0.19499058 0.01118734 -0.2253637901 0.277479370
  [6,] -0.039009965 0.09377122 0.17352266 0.2272478976 -0.227766027
  [7,] 0.167078726 0.15649910 0.19956145 0.0416260706 0.002492023
  [9,] -0.027811958   0.22158076   0.15852049   0.0781083047 -0.030552785
# [11,] 0.142994249 -0.40008219 0.19330202 -0.2363837791 -0.167470087
# [12,] 0.211486227 -0.09216712 0.01683007 -0.1193563082 -0.088823094
# [13,] 0.233707080 0.16424741 0.02631102 0.0045267029 0.268331956
# [14,] 0.116145811 -0.12015418 -0.13512613 0.0413285356 -0.159551415
# [15,] 0.060965991 0.03028393 -0.07999491 -0.3197885956 -0.151137319
# [16,] 0.011001116 -0.19474818 -0.13619836 0.0005968125 -0.085966019
# [17,] -0.490987033 -0.02709454 -0.08906072 -0.1138595058 0.139387145
# [18,] 0.027350631 -0.06599522 0.23529252 -0.2218992380 0.155363523
# [19,] 0.083085393 0.07283543 -0.32808370 -0.0100672612 0.311631458
# [20,] 0.002120825 -0.10537633 -0.06409014 -0.0349441748 -0.091483399
# [21,] -0.280149377 -0.26408612 -0.16993959 0.0529700283 -0.059870396
# [22,] -0.057798128 -0.06051053 -0.18989548 -0.0519699464 0.270620215
# [23,] -0.133983109 -0.28353064 -0.08907073 0.0399100396 -0.184805218
# [24,] 0.127239586 -0.14620115 -0.08060288 -0.0389676745 0.034782853
# [25,] -0.046152222 -0.17362359 0.16913197 0.1827168119 0.046604092
# [26,] 0.137260149 0.09121796 -0.12809752 0.0045107477 -0.055126611
# [28,] 0.024661472 -0.12310216 0.05022506 0.2122909568 -0.211978427
# [29,] 0.195397993 0.16271411 -0.27890203 -0.0246315515 0.023520471
# [30,] 0.191241482 -0.14595482 -0.20168331 0.2295189432 -0.035366274
# [31,] 0.073611291 -0.03978370 0.23168329 -0.0536905204 -0.037372871
# [32,] 0.209867159 0.23825555 -0.08056727 -0.0687235080 -0.093530618
# [34,] 0.098599535 0.04065092 0.24180351 0.2247937664 0.118699510
# [35,] -0.011570401 0.21838288 -0.16578060 -0.1999870672 -0.384697844
# [36,] 0.153937887 0.02068612 -0.24701883 -0.1572902824 -0.155070929
# [37,] 0.170385517 -0.12010283 0.02774610 -0.0813152968 -0.049957110
# [38,] -0.182767641 -0.14634955 0.12351262 -0.2473099491 -0.010612227
# [40,] -0.147163035 -0.02549114 0.03688128 0.2820582986 -0.109943400
```

• Visualizing your data is one of the essential elements of data analysis. We are going to primarily use the ggplot2 package for making data plots. The reason is that it provides elegant graphics in a concise conceptual framework. We will learn more about this later in the semester, but let's get started using the quick plot function qplot:

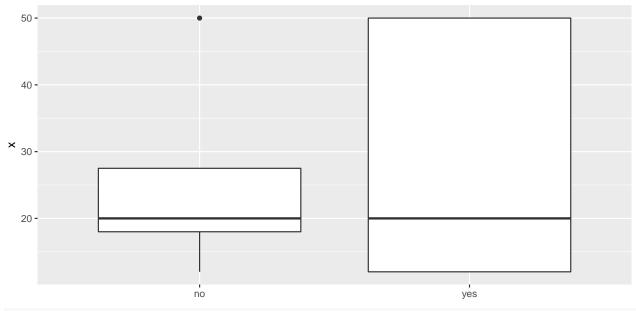
```
library(ggplot2)
df <- data.frame(x=x, y=c(rep("yes", 7), rep("no", 5)))</pre>
df
#
      \boldsymbol{x}
# 1 50 yes
# 2 12 yes
# 3 NA yes
# 4
    20 yes
# 5 50 yes
# 6 12 yes
# 7 NA yes
# 8 20
        no
# 9 50
# 10 12 no
# 11 NA no
# 12 20 no
qplot(x, data=df)
```



qplot(x, data=df, binwidth=5)



qplot(y, x, data=df, geom="boxplot", xlab="")



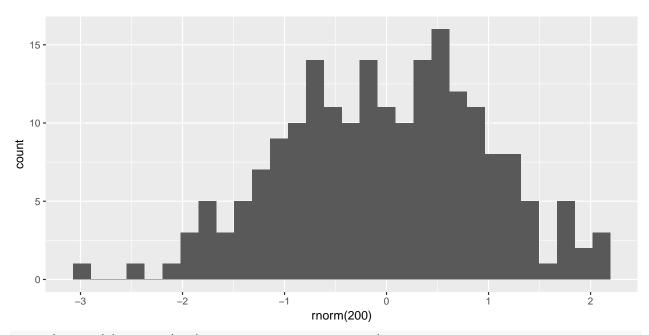
qplot(factor(0), x, data=df, geom="boxplot", xlab="")



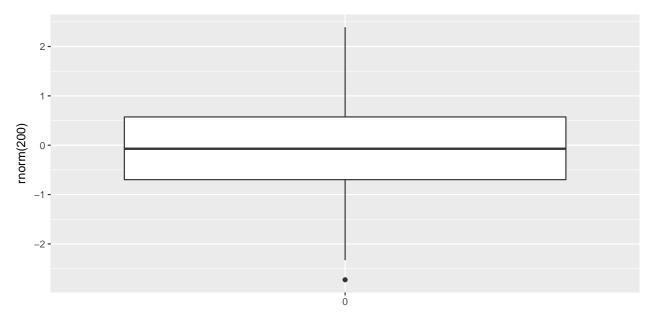
Different R functions can require different data input types. Many of the original functions operate on matrices, but more recently written functions require data frames as input. The package ggplot2 likes to have data frames.

• The function rnorm generates random numbers from a standard normal distribution. Produce a histogram of 200 random numbers from N(0,1)

```
# 200 random numbers from N(0,1)
qplot(rnorm(200))
```



qplot(factor(0), rnorm(200), geom="boxplot", xlab="")



Modify these commands so that the boxplot uses the same numbers as the histogram. (Hint: save the output of rnorm for re-use.) Notice in these commands that the qplot will also take the output of rnorm directly, which is a numeric vector.

• Let's look at some data sets from the ISLR package. First we need to make sure it is installed.

library(ISLR)

If that returns an error, you can use install.packages("ISLR") at the command line.

A package only needs to be installed once, but you have to load it via the *library* command in each session.

Once the package is installed, try again with

library(ISLR)

• Then look at the OJ data set:

```
help(OJ)
head(OJ)
#
    Purchase WeekofPurchase StoreID PriceCH PriceMM DiscCH DiscMM SpecialCH
# 1
           CH
                          237
                                     1
                                          1.75
                                                   1.99
                                                           0.00
                                                                   0.0
                                                                                 0
# 2
           CH
                          239
                                          1.75
                                                   1.99
                                                           0.00
                                                                   0.3
                                                                                 0
                                     1
                                                                                 0
# 3
           CH
                          245
                                     1
                                          1.86
                                                   2.09
                                                           0.17
                                                                   0.0
          MM
                          227
                                     1
                                          1.69
                                                   1.69
                                                           0.00
                                                                   0.0
                                                                                 0
# 4
                                     7
           СН
                          228
                                          1.69
                                                   1.69
                                                                                 0
# 5
                                                           0.00
                                                                    0.0
# 6
           CH
                          230
                                     7
                                          1.69
                                                   1.99
                                                           0.00
                                                                   0.0
                                                                                 0
    SpecialMM LoyalCH SalePriceMM SalePriceCH PriceDiff Store7 PctDiscMM
#
             0 0.500000
# 1
                                              1.75
                                1.99
                                                         0.24
                                                                  No
                                                                       0.000000
# 2
             1 0.600000
                                1.69
                                             1.75
                                                       -0.06
                                                                  No
                                                                       0.150754
# 3
             0 0.680000
                                2.09
                                             1.69
                                                         0.40
                                                                  No
                                                                      0.000000
# 4
             0 0.400000
                                1.69
                                              1.69
                                                         0.00
                                                                  No
                                                                       0.000000
# 5
             0 0.956535
                                1.69
                                              1.69
                                                         0.00
                                                                      0.000000
                                                                 Yes
# 6
             1 0.965228
                                1.99
                                              1.69
                                                         0.30
                                                                 Yes
                                                                       0.000000
    PctDiscCH ListPriceDiff STORE
#
# 1
     0.000000
                         0.24
                                   1
     0.000000
# 2
                         0.24
                                   1
# 3 0.091398
                         0.23
```

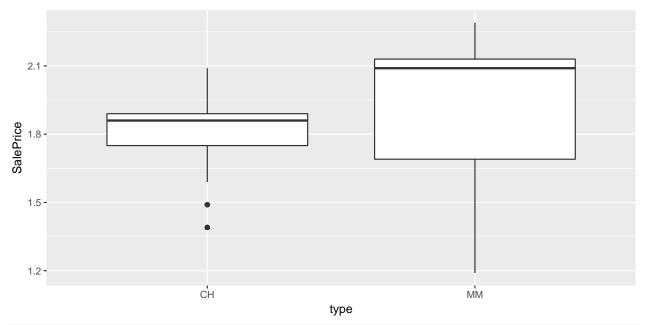
```
# 4 0.000000
                   0.00
# 5 0.000000
                   0.00
                           0
# 6 0.000000
                   0.30
#View(OJ)
summary(OJ)
# Purchase WeekofPurchase
                        StoreID
                                    PriceCH
                                                    PriceMM
# CH:653 Min. :227.0 Min. :1.00
                                   Min. :1.690
                                                 Min. :1.690
 MM:417 1st Qu.:240.0 1st Qu.:2.00
                                   1st Qu.:1.790
                                                 1st Qu.:1.990
         Median :257.0 Median :3.00
                                    Median :1.860
#
                                                 Median :2.090
                      Mean :3.96
                                    Mean :1.867
#
          Mean
               :254.4
                                                  Mean :2.085
#
          3rd Qu.:268.0
                       3rd Qu.:7.00
                                    3rd Qu.:1.990
                                                 3rd Qu.:2.180
#
          Max. :278.0 Max. :7.00 Max. :2.090 Max. :2.290
#
     \mathit{DiscCH}
                    \it DiscMM
                                  SpecialCH
                                               Special MM
#
  Min. :0.00000
                 Min. : 0.0000
                                Min. :0.0000
                                              Min. :0.0000
                                              1st Qu.:0.0000
#
  1st Qu.:0.00000
                 1st Qu.:0.0000 1st Qu.:0.0000
 Median :0.00000 Median :0.0000 Median :0.0000
                                              Median :0.0000
#
 Mean :0.05186 Mean :0.1234
                               Mean :0.1477
                                              Mean :0.1617
  3rd Qu.:0.00000
                 3rd Qu.:0.2300
                               3rd Qu.:0.0000
                                               3rd Qu.:0.0000
#
#
 Max. :0.50000
                 Max. :0.8000 Max. :1.0000 Max. :1.0000
                  SalePriceMM SalePriceCH
   LoyalCH
                                              PriceDiff
# Min. :0.000011 Min. :1.190 Min. :1.390 Min. :-0.6700
#
  1st Qu.:0.325257
                 # Median :0.600000
                 Median :2.090 Median :1.860 Median : 0.2300
# Mean :0.565782
                 Mean :1.962 Mean :1.816
                                             Mean : 0.1465
#
 3rd Qu.:0.850873
                  3rd Qu.:2.130
                               3rd Qu.:1.890
                                              3rd Qu.: 0.3200
# Max. :0.999947
                 Max. :2.290 Max. :2.090
                                             Max. : 0.6400
# Store7
          {\it PctDiscMM}
                         {\it PctDiscCH}
                                       ListPriceDiff
 No :714
          Min. :0.0000 Min. :0.00000 Min.
                                             :0.000
  Yes:356
          1st Qu.:0.0000
                        1st Qu.:0.00000
                                        1st Qu.:0.140
#
          Median :0.0000 Median :0.00000 Median :0.240
#
          Mean :0.0593 Mean :0.02731 Mean :0.218
                                        3rd Qu.:0.300
#
           3rd Qu.:0.1127
                         3rd Qu.:0.00000
#
                        Max. :0.25269
          Max. : 0.4020
                                        Max. : 0.440
#
     STORE
#
 Min. :0.000
#
 1st Qu.:0.000
  Median :2.000
# Mean :1.631
 3rd Qu.:3.000
# Max. :4.000
OJ[, "PriceCH"]
    [1] 1.75 1.75 1.86 1.69 1.69 1.69 1.69 1.75 1.75 1.75 1.86 1.86 1.99
#
   [14] 1.86 2.06 2.06 1.75 1.86 1.86 1.86 1.86 1.76 1.86 1.86 1.86 1.86
   [27] 1.86 1.86 1.86 2.06 1.89 1.86 1.96 1.69 1.99 1.99 1.76 1.99 1.99
#
#
   #
   [53] 1.99 1.99 1.99 1.99 1.99 1.99 1.86 1.99 1.99 1.99 1.99 1.99
   [66] 1.99 1.99 1.99 1.99 1.99 1.99 2.09 2.09 2.09 1.69 1.79 1.79 1.99
#
#
   [79] 1.89 1.99 1.99 1.99 1.99 1.99 2.09 1.99 2.09 1.99 2.09 2.09 1.79
#
   [92] 1.99 1.99 1.86 1.75 1.99 1.99 1.69 1.69 1.69 1.75 1.75 1.75 1.75
  [105] 1.86 1.89 1.86 1.89 1.89 1.89 1.89 1.86 1.99 1.89 1.89 1.89 1.99 1.86
  [131] 1.86 1.86 1.86 1.86 1.86 1.96 1.96 1.99 1.99 1.99 1.75 1.99 1.99
 [144] 1.86 2.09 1.75 1.75 1.86 1.86 1.86 1.86 1.99 1.79 1.79 1.79 1.69
```

```
[157] 1.99 1.99 1.99 1.99 1.99 1.99 1.86 1.99 1.99 1.99 2.09 2.09 2.09
  [170] 1.86 1.69 1.69 1.79 1.79 1.79 1.79 1.86 1.99 1.86 1.99 1.89
 [196] 1.99 1.99 1.99 2.09 1.99 2.09 1.69 1.69 1.69 1.75 1.75 1.86 1.86
  [222] 1.69 1.69 1.86 1.76 1.76 1.99 1.99 1.99 1.86 1.99 1.69 1.75 1.75
 [248] 1.86 1.86 1.86 1.86 1.86 1.86 1.86 1.99 1.69 1.69 1.86 1.99 1.86
#
 [261] 1.86 1.86 1.86 1.86 1.99 1.99 1.86 1.79 1.79 1.86 1.86 2.09 2.09
 [287] 1.99 1.99 1.99 1.99 1.99 1.99 1.86 1.86 1.96 2.09 1.69 1.69 1.69
 [300] 1.69 1.79 1.75 1.75 1.89 1.99 1.89 1.86 1.86 1.99 1.86 1.86 1.86
  [326] 1.69 1.76 1.86 1.99 1.86 1.76 1.86 1.69 1.75 1.75 1.75 1.86 1.86
 [339] 1.86 1.75 1.86 1.86 1.76 1.86 1.86 1.86 1.86 1.86 1.86 1.86 1.99
 [365] 1.86 1.75 1.99 1.86 1.86 1.86 1.86 1.96 1.86 1.69 1.75 1.76 1.69
  [378] 1.69 1.75 1.75 1.89 1.86 1.86 1.69 1.69 1.69 1.69 1.69 1.69 1.75
 [391] 1.75 1.75 1.75 1.79 1.86 1.75 1.86 1.86 1.86 1.86 1.99 1.86 1.86
 [404] 1.96 1.99 1.99 1.69 1.75 1.86 1.86 1.86 1.79 1.75 1.79 1.79
  [417] 1.86 1.99 1.86 1.99 1.99 1.99 1.69 1.69 1.99 2.09 1.99 1.86 1.86
 [430] 1.99 1.99 1.86 1.75 1.86 1.99 1.76 1.76 1.96 1.86 1.76 1.76 1.76
 [443] 1.76 1.76 1.86 1.96 1.75 1.86 1.99 1.86 1.86 1.86 1.86 1.86 1.99
 [456] 1.86 1.86 1.99 1.96 2.09 1.89 1.79 1.69 1.86 1.86 1.86 1.86 1.86
 [469] 1.86 1.86 1.86 1.96 1.99 1.99 1.86 1.86 1.86 1.86 1.86 1.86 1.86
 [482] 1.89 1.89 1.86 1.79 1.79 1.75 1.75 1.79 1.75 1.79 1.75 1.99 1.99
 [495] 1.99 1.69 1.86 1.86 1.96 1.99 1.79 1.79 1.79 1.79 1.99 1.99
 [521] 1.86 1.96 1.86 1.99 1.76 1.76 1.99 1.89 1.89 1.75 1.75 1.75 1.79
 [534] 1.75 1.86 1.86 1.86 1.99 1.86 1.86 1.86 1.86 1.86 1.79 1.69 1.69
 [547] 1.69 1.69 1.75 1.75 1.75 1.75 1.86 1.89 1.89 1.86 1.96 1.99 1.75
 [560] 1.86 1.89 2.06 1.79 1.76 1.86 1.79 1.75 1.99 1.86 1.76 1.79 1.79
 [612] 1.75 1.86 1.86 1.86 1.86 1.86 1.76 1.76 1.86 1.86 1.86 1.86 1.86
  [625] 1.86 1.86 1.86 1.75 1.89 1.86 1.99 1.86 1.86 1.79 1.79 1.99 1.99
 [638] 1.79 1.99 1.86 1.79 1.75 1.75 1.75 1.79 1.75 1.79 1.99 1.99 1.89
  [651] 1.89 1.89 1.86 1.86 1.99 1.86 1.86 1.86 1.86 1.86 1.76 1.86 1.86
  [664] 1.86 1.69 1.86 1.89 1.86 1.86 1.99 1.76 1.86 1.86 1.86 1.86 1.86
 [677] 1.96 1.96 1.99 1.75 1.86 1.99 1.86 1.86 1.86 1.86 2.06 1.79
 [729] 1.86 1.96 1.99 2.09 2.09 1.69 1.86 1.86 1.79 1.99 1.99 1.99 1.99
 [742] 1.99 1.99 1.99 2.09 1.75 1.76 1.79 1.75 1.69 1.69 1.79 1.69 1.86
 [755] 1.86 1.89 1.86 1.89 1.86 1.75 1.99 2.09 1.89 1.89 1.89 1.86 1.86
 [768] 1.86 2.06 1.69 1.69 1.69 1.86 1.89 1.89 1.69 1.86 1.76 1.99 1.99
 [781] 1.69 1.86 1.86 1.79 1.79 1.79 1.79 1.99 1.86 1.96 1.79 1.86 1.75
 [794] 1.76 1.76 1.76 1.76 1.96 1.86 1.99 1.99 1.79 1.79 1.86 1.76 1.86
  [820] 1.86 1.99 1.79 1.79 1.79 1.79 1.79 1.99 1.86 1.99 1.99 1.99 1.69
 [833] 1.79 1.79 1.99 1.79 1.99 1.86 1.86 1.86 1.86 1.86 1.86 1.86 1.96
```

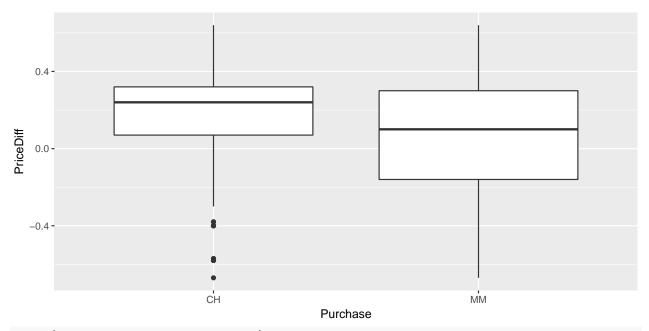
```
[846] 1.96 1.96 1.96 1.75 1.86 1.69 1.69 1.69 1.75 1.86 1.86 1.86 1.86
  [859] 1.86 1.76 1.86 1.75 1.86 1.69 1.69 1.75 1.75 1.99 1.86 1.86 1.86
  [898] 1.86 1.86 1.86 1.86 1.86 1.86 1.99 1.99 1.69 1.75 1.75 1.86 1.86
  [911] 1.96 1.99 1.75 1.86 1.89 1.89 1.89 1.99 1.96 1.86 1.86 1.86
  [937] 1.69 1.69 1.75 1.89 1.89 1.89 1.89 1.99 1.89 1.86 1.86 1.99 1.86
  [950] 1.86 1.86 1.86 1.86 1.99 1.86 1.86 1.99 1.99 1.96 1.99 1.99 1.69
#
  [963] 1.69 1.69 1.69 1.69 1.75 1.75 1.75 1.75 1.75 1.86 1.86 1.86 1.86
 [976] 1.86 1.96 1.99 1.99 1.99 1.75 1.86 1.76 1.86 1.86 1.86 1.86 1.96 1.86
 [989] 1.99 1.99 1.86 1.96 1.69 1.79 1.99 1.86 1.69 1.69 1.86 1.99 1.69
# [1002] 1.86 1.79 1.79 1.79 1.99 1.99 1.99 1.69 1.69 1.69 1.69 1.75 1.75
# [1015] 1.69 1.75 1.75 1.75 1.86 1.86 1.86 1.89 1.99 1.89 1.99 1.86 1.86
# [1028] 1.76 1.86 1.86 1.86 1.99 1.86 1.99 1.99 1.69 1.69 1.69 1.69 1.75
# [1041] 1.75 1.75 1.75 1.75 1.86 1.76 1.76 1.76 1.76 1.69 1.69 1.69 1.75
# [1054] 1.75 1.86 1.69 1.69 1.69 1.75 1.69 1.75 1.86 1.86 1.76 1.86 1.86
# [1067] 1.86 1.86 1.86 1.86
```

Can you figure out what the square brackets mean in the output from the last command?

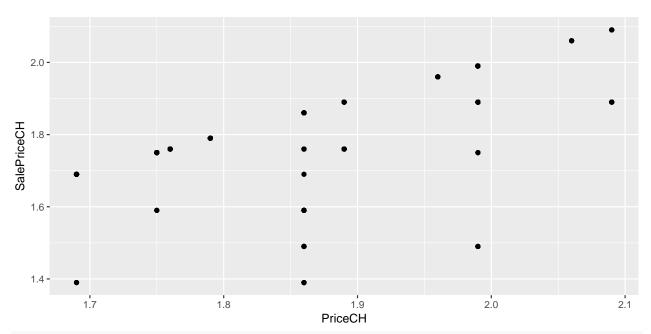
Now lets make some plots of the data



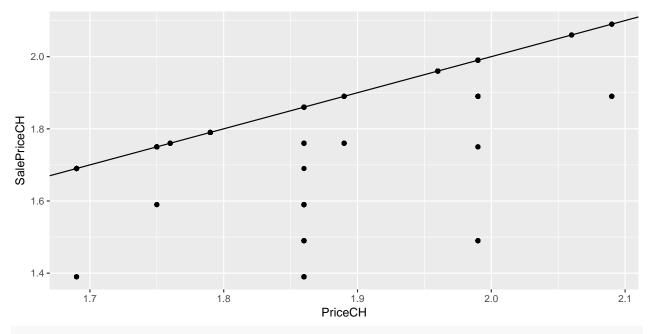
qplot(Purchase, PriceDiff, data=OJ, geom="boxplot")



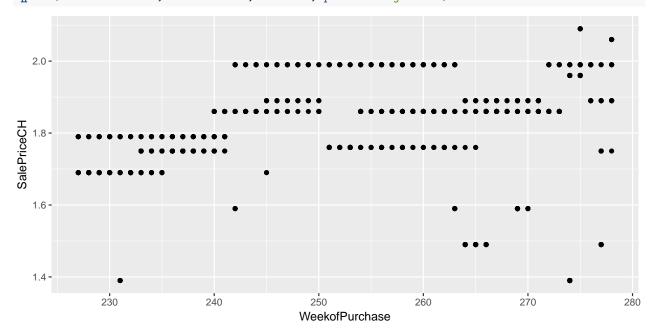
qplot(PriceCH, SalePriceCH, data=OJ)



qplot(PriceCH, SalePriceCH, data=OJ, position="jitter") +
 geom_abline(intercept=0,slope=1)



qplot(WeekofPurchase, SalePriceCH, data=OJ, position="jitter")



Make sure you understand what is being plotted in each case, and what the graphs are telling you about the data.

• Tabulating variables:

```
table(OJ$StoreID)
#
# 1 2 3 4 7
# 157 222 196 139 356
table(OJ$Purchase, OJ$SpecialCH)
#
# 0 1
# CH 532 121
```

```
# MM 380 37
```

What do these tables tell you?

- The *summary* command can be applied to almost anything to get a summary of the object. Try it on some other data sets in the *ISLR* package. Note that the *summary* is just what R thinks should be the summary, and it may not always be the best summary. If someone asks you to "summarise" this data set, you may need to think about what is important and use different functions that are appropriate for the situation.
- Check the PISA data:

```
library(readr)
pisa <- read_csv("https://github.com/bsouhaib/BA2018/raw/master/data/PISA-oz.csv")</pre>
dim(pisa)
# [1] 14481
               80
colnames(pisa)
   [1] "name"
                  "SCHOOLID" "STO3Q01"
                                         "ST03Q02"
                                                    "ST04Q01"
                                                               "ST08Q01"
  [7] "ST09Q01"
                  "ST115Q01"
                             "ST11Q01"
                                         "ST11Q02"
                                                    "ST11Q03"
                                                               "ST11Q04"
                  "ST11Q06"
                                        "ST17Q01"
# [13] "ST11Q05"
                             "ST13Q01"
                                                    "ST27Q01"
                                                               "ST27Q02"
# [19] "ST27Q03"
                  "ST27Q04"
                             "ST27Q05"
                                         "ST28Q01"
                                                    "ST85Q01"
                                                               "ST85Q02"
                  "IC06Q01"
# [25] "ICO5Q01"
                             "IC07Q01"
                                         "IC08Q03"
                                                    "IC08Q04"
                                                               "IC08Q05"
# [31] "PV1MATH"
                  "PV2MATH"
                             "PV3MATH"
                                         "PV4MATH"
                                                    "PV5MATH"
                                                               "PV1MACC"
                                        "PV5MACC"
# [37] "PV2MACC"
                  "PV3MACC"
                             "PV4MACC"
                                                    "PV1MACQ"
                                                               "PV2MACQ"
# [43] "PV3MACQ"
                  "PV4MACQ"
                             "PV5MACQ"
                                         "PV1MACS"
                                                    "PV2MACS"
                                                               "PV3MACS"
                  "PV5MACS"
                                         "PV2MACU"
                                                    "PV3MACU"
                                                               "PV4MACU"
# [49] "PV4MACS"
                             "PV1MACU"
                                         "PV3MAPE"
# [55] "PV5MACU"
                  "PV1MAPE"
                             "PV2MAPE"
                                                    "PV4MAPE"
                                                               "PV5MAPE"
# [61] "PV1MAPF"
                  "PV2MAPF"
                             "PV3MAPF"
                                        "PV4MAPF"
                                                    "PV5MAPF"
                                                               "PV1MAPI"
# [67] "PV2MAPI"
                  "PV3MAPI"
                             "PV4MAPI"
                                         "PV5MAPI"
                                                    "PV1READ"
                                                               "PV2READ"
                  "PV4READ"
                             "PV5READ"
                                                    "PV2SCIE"
                                                               "PV3SCIE"
# [73] "PV3READ"
                                         "PV1SCIE"
# [79] "PV4SCIE"
                  "PV5SCIE"
#View(pisa)
str(pisa)
# Classes 'tbl_df',
                   'tbl' and 'data.frame': 14481 obs. of 80 variables:
                    "Australia" "Australia" "Australia" "Australia" ...
   $ name
             : chr
                    "0000001" "0000001" "0000001" "0000001" ...
   $ SCHOOLID: chr
                    "11" "12" "07" "09" ...
  $ ST03Q01 : chr
  $ ST03Q02 : int
                    #
   $ ST04Q01 : chr
                    "Female" "Female" "Male" ...
                    "One or two times" "None" "One or two times" "One or two times" ...
  $ ST08Q01 : chr
                    "One or two times" "None" "None" "None" ...
#
  $ ST09Q01 : chr
  $ ST115Q01: int
#
                    2 1 1 1 1 1 1 1 1 1 ...
  $ ST11Q01 : chr
                    "Yes" "Yes" "Yes" "Yes" ...
#
   $ ST11Q02 : chr
                    "Yes" "Yes" "Yes" "Yes" ...
                    "Yes" "Yes" "No" "No" ...
#
   $ ST11Q03 : chr
                    "Yes" NA "No" "Yes" ...
#
   $ ST11Q04 : chr
#
   $ ST11Q05 : chr
                    "No" NA "No" "No" ...
#
  $ ST11Q06 : chr
                    "No" NA "No" "No" ...
#
  $ ST13Q01 : chr
                    "<ISCED level 3A>" "<ISCED level 2>" NA "<ISCED level 3A>" ...
  $ ST17Q01 : chr
                    "<ISCED level 2>" "<ISCED level 2>" "<ISCED level 3B, 3C>" "<ISCED level 3A>" ...
                    "Three or more" "Three or more" "Three or more" "Three or more" ...
  $ ST27Q01 : chr
  $ ST27Q02 : chr
                    "Three or more" "Three or more" "Two" "Two" ...
  $ ST27Q03 : chr
                    "Three or more" "Three or more" "Three or more" "Three or more" ...
                    "Three or more" "Two" "Three or more" "Two" ...
  $ ST27Q04 : chr
                    "Three or more" "Two" "One" "Two" ...
   $ ST27Q05 : chr
```

```
# $ ST28Q01 : chr "201-500 books" "26-100 books" "201-500 books" "201-500 books" ...
# $ ST85Q01 : chr "Agree" "Agree" NA NA ...
# $ ST85Q02 : chr "Agree" "Agree" NA NA ...
# $ ICO5Q01 : chr "03" "03" "03" "05" ...
# $ ICO6Q01 : chr "04" "04" "06" "07" ...
# $ ICO7Q01 : chr "04" "04" "06" "07" ...
# $ ICO8Q03 : chr "Once or twice a week" "Once or twice a month" "Almost every day" "Once or twice a
# $ ICO8Q04 : chr "Once or twice a month" "Once or twice a week" "Almost every day" "Every day" ...
# $ ICO8Q05 : chr "Almost every day" "Every day" "Almost every day" "Every day" ...
# $ PV1MATH : num 562 565 507 602 520 ...
# $ PV2MATH : num 569 557 547 594 507 ...
# $ PV3MATH : num 555 553 511 552 501 ...
# $ PV4MATH : num 579 538 454 526 521 ...
# $ PV5MATH : num 548 573 546 619 547 ...
# $ PV1MACC : num 549 588 509 570 485 ...
# $ PV2MACC : num 534 538 501 578 518 ...
# $ PV3MACC : num 502 524 502 564 537 ...
# $ PV4MACC : num 509 589 494 539 533 ...
# $ PV5MACC : num 583 559 453 575 486 ...
# $ PV1MACQ : num 583 595 501 584 530 ...
# $ PV2MACQ : num 593 559 494 581 585 ...
# $ PV3MACQ : num 543 560 496 580 582 ...
# $ PV4MACQ : num 537 594 482 540 571 ...
# $ PV5MACQ : num 622 590 443 562 549 ...
# $ PV1MACS : num 572 556 516 588 469 ...
# $ PV2MACS : num 578 529 493 617 536 ...
# $ PV3MACS : num 537 506 508 602 514 ...
# $ PV4MACS : num 523 555 477 588 518 ...
# $ PV5MACS : num 621 528 444 603 469 ...
# $ PV1MACU : num 598 573 471 601 522 ...
# $ PV2MACU : num 601 545 500 573 550 ...
# $ PV3MACU : num 577 545 471 617 555 ...
# $ PV4MACU : num 558 561 440 560 550 ...
# $ PV5MACU : num 612 573 437 564 554 ...
# $ PV1MAPE : num 566 559 496 578 526 ...
# $ PV2MAPE : num 588 548 503 567 531 ...
# $ PV3MAPE : num 571 573 501 537 522 ...
# $ PV4MAPE : num 553 584 506 631 459 ...
# $ PV5MAPE : num 587 567 484 593 493 ...
# $ PV1MAPF : num 569 585 493 586 487 ...
# $ PV2MAPF : num 595 520 497 589 523 ...
# $ PV3MAPF : num 577 546 536 530 498 ...
# $ PV4MAPF : num 562 569 516 641 455 ...
# $ PV5MAPF : num 595 609 464 601 461 ...
# $ PV1MAPI : num 555 617 471 576 545 ...
# $ PV2MAPI : num 590 619 497 587 571 ...
# $ PV3MAPI : num 589 612 501 574 524 ...
# $ PV4MAPI : num 530 617 502 661 495 ...
# $ PV5MAPI : num 567 603 459 616 488 ...
# $ PV1READ : num 582 617 584 650 554 ...
# $ PV2READ : num 571 572 551 608 560 ...
# $ PV3READ : num 602 560 588 594 517 ...
# $ PV4READ : num 572 564 575 575 564 ...
```

```
# $ PV5READ : num 585 565 624 620 572 ...
# $ PV1SCIE : num 583 627 556 668 574 ...
# $ PV2SCIE : num 579 600 573 665 612 ...
# $ PV3SCIE : num 593 574 584 620 571 ...
# $ PV4SCIE : num 567 582 532 592 598 ...
# $ PV5SCIE : num 587 625 589 656 662 ...
# - attr(*, "spec")=List of 2
  ..$ cols :List of 80
   ....$ name : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ SCHOOLID: list()
#
   .. .. ..- attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ST03Q01 : list()
#
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ST03Q02 : list()
#
   ..... attr(*, "class")= chr "collector_integer" "collector"
#
   ....$ STO4Q01 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ STO8Q01 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ST09Q01 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ST115Q01: list()
#
   ..... attr(*, "class")= chr "collector_integer" "collector"
#
   .. ..$ ST11Q01 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
#
   .. ..$ ST11Q02 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
#
   .. ..$ ST11Q03 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ST11Q04 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ST11Q05 : list()
#
#
   ..... attr(*, "class")= chr "collector_character" "collector"
   .. ..$ ST11Q06 : list()
#
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ST13Q01 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ... ..$ ST17Q01 : list()
   .. .. ..- attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ST27Q01 : list()
#
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ... ..$ ST27Q02 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
#
   .. ..$ ST27Q03 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ST27Q04 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
#
   .. ..$ ST27Q05 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
#
   .. ..$ ST28Q01 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
  .. ..$ ST85Q01 : list()
```

```
..... attr(*, "class")= chr "collector_character" "collector"
   .. ..$ ST85Q02 : list()
#
   .... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ICO5Q01 : list()
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ICO6Q01 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ICO7Q01 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   .. ..$ ICO8Q03 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ....$ ICO8Q04 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
#
   .. ..$ ICO8Q05 : list()
#
   ..... attr(*, "class")= chr "collector_character" "collector"
#
   ....$ PV1MATH : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   \dots $ PV2MATH : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV3MATH : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   .. ..$ PV4MATH : list()
   ..... attr(*, "class") = chr "collector_double" "collector"
#
   ....$ PV5MATH : list()
#
   .... attr(*, "class")= chr "collector_double" "collector"
#
#
   .. ..$ PV1MACC : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   \dots $ PV2MACC : list()
#
   .... attr(*, "class")= chr "collector_double" "collector"
#
#
   \dots $\psi$ PV3MACC : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV4MACC : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   ....$ PV5MACC : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   \dots $\psi PV1MACQ : list()
#
#
   ..... attr(*, "class")= chr "collector_double" "collector"
   \dots $ PV2MACQ : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   \dots $\mathcal{S} PV3MACQ : list()
#
   .... attr(*, "class")= chr "collector_double" "collector"
#
#
   .. ..$ PV4MACQ : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   ....$ PV5MACQ : list()
   ..... attr(*, "class") = chr "collector_double" "collector"
#
#
   ....$ PV1MACS : list()
#
   ..... attr(*, "class") = chr "collector_double" "collector"
#
   ....$ PV2MACS : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV3MACS : list()
#
#
   .... - attr(*, "class")= chr "collector_double" "collector"
#
   .. ..$ PV4MACS : list()
  ..... attr(*, "class")= chr "collector_double" "collector"
```

```
# ....$ PV5MACS : list()
   .... - attr(*, "class")= chr "collector_double" "collector"
#
   .. ..$ PV1MACU : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   .. ..$ PV2MACU : list()
   ..... attr(*, "class") = chr "collector_double" "collector"
#
#
   \dots $\frac{1}{2} PV3MACU : list()
   ..... attr(*, "class")= chr "collector double" "collector"
#
#
   ....$ PV4MACU : list()
#
   ..... attr(*, "class") = chr "collector_double" "collector"
   ....$ PV5MACU : list()
#
#
    ..... attr(*, "class")= chr "collector_double" "collector"
   \dots $\psi$ PV1MAPE : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   \dots $\infty$ PV2MAPE : list()
#
    ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV3MAPE : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV4MAPE : list()
#
   .... attr(*, "class")= chr "collector_double" "collector"
#
   \dots $\(\sigma\) PV5MAPE : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   .. ..$ PV1MAPF : list()
#
    ..... attr(*, "class")= chr "collector_double" "collector"
#
   .... $ PV2MAPF : list()
#
   .. .. ..- attr(*, "class")= chr "collector_double" "collector"
#
#
    .. ..$ PV3MAPF : list()
   ..... attr(*, "class") = chr "collector_double" "collector"
#
#
   .. ..$ PV4MAPF : list()
   ..... attr(*, "class") = chr "collector_double" "collector"
#
#
    ....$ PV5MAPF : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV1MAPI : list()
#
#
   .... attr(*, "class")= chr "collector_double" "collector"
   \dots $\mathcal{PV2MAPI} : list()
#
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   ....$ PV3MAPI : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
    ... ..$ PV4MAPI : list()
   .. .. - attr(*, "class")= chr "collector_double" "collector"
#
   .. ..$ PV5MAPI : list()
#
#
   ..... attr(*, "class")= chr "collector_double" "collector"
   .. ..$ PV1READ : list()
#
   .... attr(*, "class")= chr "collector_double" "collector"
#
#
   .. ..$ PV2READ : list()
#
    ..... attr(*, "class")= chr "collector_double" "collector"
#
   ....$ PV3READ : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   .. ..$ PV4READ : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
#
   .. ..$ PV5READ : list()
   ..... attr(*, "class")= chr "collector_double" "collector"
#
  .. ..$ PV1SCIE : list()
```

```
..... attr(*, "class") = chr "collector_double" "collector"
#
#
    .... $ PV2SCIE : list()
#
    .. .. .. - attr(*, "class")= chr
                                      "collector_double" "collector"
    ... ..$ PV3SCIE : list()
#
    .. .. ..- attr(*, "class")= chr
                                      "collector_double" "collector"
#
    .... $ PV4SCIE : list()
#
    .. .. ..- attr(*, "class")= chr
                                      "collector_double" "collector"
#
    ... ..$ PV5SCIE : list()
#
    \dots \dots - attr(*, "class") = chr
                                     "collector double" "collector"
#
    ..$ default: list()
#
    ....- attr(*, "class")= chr "collector_guess" "collector"
#
    ..- attr(*, "class")= chr "col_spec"
head(pisa)
# # A tibble: 6 x 80
#
         name SCHOOLID ST03Q01 ST03Q02 ST04Q01
                                                         ST08Q01
#
        <chr>
                 <chr>
                         <chr>
                                  \langle int \rangle
                                          <chr>
                                                            <chr>
# 1 Australia
              0000001
                            11
                                   1996 Female One or two times
# 2 Australia 0000001
                            12
                                   1996 Female
# 3 Australia 0000001
                            07
                                  1996
                                       Female One or two times
# 4 Australia 0000001
                            09
                                   1996
                                           Male One or two times
# 5 Australia 0000001
                            06
                                   1996
                                           Male One or two times
# 6 Australia 0000001
                            07
                                   1996 Female
# # ... with 74 more variables: ST09Q01 <chr>, ST115Q01 <int>,
      ST11Q01 <chr>, ST11Q02 <chr>, ST11Q03 <chr>, ST11Q04 <chr>,
# #
      ST11Q05 <chr>, ST11Q06 <chr>, ST13Q01 <chr>, ST17Q01 <chr>,
# #
# #
      ST27Q01 <chr>, ST27Q02 <chr>, ST27Q03 <chr>, ST27Q04 <chr>,
# #
      ST27Q05 <chr>, ST28Q01 <chr>, ST85Q01 <chr>, ST85Q02 <chr>,
# #
      IC05Q01 <chr>, IC06Q01 <chr>, IC07Q01 <chr>, IC08Q03 <chr>,
# #
      ICO8Q04 <chr>, ICO8Q05 <chr>, PV1MATH <dbl>, PV2MATH <dbl>,
# #
      PV3MATH <dbl>, PV4MATH <dbl>, PV5MATH <dbl>, PV1MACC <dbl>,
# #
      PV2MACC <dbl>, PV3MACC <dbl>, PV4MACC <dbl>, PV5MACC <dbl>,
      PV1MACQ <dbl>, PV2MACQ <dbl>, PV3MACQ <dbl>, PV4MACQ <dbl>,
# #
# #
      PV5MACQ <dbl>, PV1MACS <dbl>, PV2MACS <dbl>, PV3MACS <dbl>,
# #
     PV4MACS <dbl>, PV5MACS <dbl>, PV1MACU <dbl>, PV2MACU <dbl>,
# #
      PV3MACU <dbl>, PV4MACU <dbl>, PV5MACU <dbl>, PV1MAPE <dbl>,
# #
      PV2MAPE <dbl>, PV3MAPE <dbl>, PV4MAPE <dbl>, PV5MAPE <dbl>,
# #
      PV1MAPF <dbl>, PV2MAPF <dbl>, PV3MAPF <dbl>, PV4MAPF <dbl>,
      PV5MAPF <dbl>, PV1MAPI <dbl>, PV2MAPI <dbl>, PV3MAPI <dbl>,
# #
      PV4MAPI <dbl>, PV5MAPI <dbl>, PV1READ <dbl>, PV2READ <dbl>,
# #
      PV3READ <dbl>, PV4READ <dbl>, PV5READ <dbl>, PV1SCIE <dbl>,
# #
      PV2SCIE <dbl>, PV3SCIE <dbl>, PV4SCIE <dbl>, PV5SCIE <dbl>
```

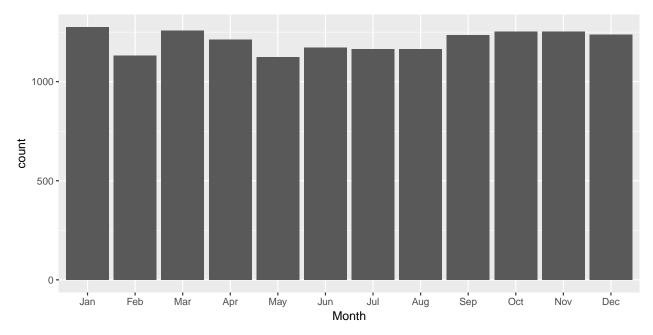
Which columns of pisa are numeric? Which columns are character?

• How many different schools were sampled (according to the variable SCHOOLID)?

There are several ways of answering this question. First use the *table* command. Then try using a combination of *length* and *unique*.

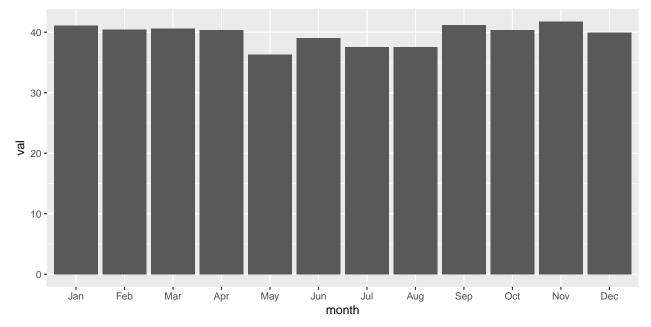
• Look at the distribution of birth months amongst the Australian students:

```
qplot(factor(ST03Q01, labels=month.abb), data=pisa, xlab="Month")
```



Can you explain the variation? Why are February and May the smallest?

• Perhaps we should adjust for month length:



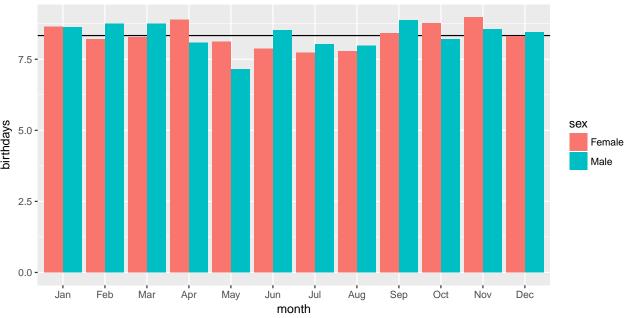
• Check if the differences are statistically significant after adjusting for month length:

```
chisq.test(monthtot, p=monthdays/365)
#
```

```
# Chi-squared test for given probabilities
#
# data: monthtot
# X-squared = 24.723, df = 11, p-value = 0.01001
```

Why is it so?

• What if we split by sex and turn into percentages:



The largest deviation from what you would expect is for males born in May. Why?

• It is easy to create your own data:

```
mynumbers <- 5:12
```

Names can be almost anything, except for special characters ^, !, \$, @, +, -, /, *. It is good practice to name your objects with some meaning for what they contain, be reasonably short (less typing). They should not be the same as common R functions; for example, don't use data because it is also used to load stored data from packages, or c because this is an R function that allows you to collect a bunch of objects together. You won't get errors by using these names but you may get confused when you come back and look at your code later.

• Objects can be of different types. The object mynumbers is a vector of numbers. Numbers can be various types also: integer or double.

```
typeof(mynumbers)
# [1] "integer"
```

```
is.numeric(mynumbers)
# [1] TRUE
is.vector(mynumbers)
# [1] TRUE
length(mynumbers)
# [1] 8
```

• Other common types of objects for data analysis are characters, logicals, factors, dates. Factors store categorical data. Dates have a special format that enables it to be treated similarly to how we use dates in real life.

```
mytext <- c("hello", "class")
length(mytext)
# [1] 2
mylogic <- c(TRUE, FALSE, TRUE, TRUE)
gender <- factor(c("male", "female", "female", "male"))
levels(gender)
# [1] "female" "male"
summary(gender)
# female male
# 3 2</pre>
```

• One of the powerful aspects of R is to build on the reproducibility. If you are going to do the same analysis over and over again, compile these operations into a function that you can then apply to different data sets.

```
y <- c(1,2,3,4,5,6)
average = function(x)
{
   return(sum(x)/length(x))
}
ybar <- average(y)</pre>
```

Try your function on other data.

• Now write a function to compute the mode of some data:

```
mymode <- function(x) {
  ux <- unique(x)
  ux[which.max(tabulate(match(x, ux)))]
}
mymode(c(rep("A", 5), rep("B", 3)))
# [1] "A"</pre>
```

• Write an R function stats to compute the mean, min, max, and the deciles, from a vector of data. You will need to search the R help facilities to find functions to compute each of the statistics. The function should return the statistics as a single vector in numerical order with appropriate names for the elements. Your function should be robust to missing values (i.e., the statistics should be computed on the non-missing values).