Questions on Calculus

Rob Hayward

November 28, 2014

1. What are the drivatives of

•
$$y = 2 + 6x$$

$$\frac{d(y)}{d(x)} = 6$$

•
$$y = 5 - 4x + 2x^3$$

$$\frac{d(y)}{d(x)} = 4 + 6x$$

$$y = 25 + 6x^2 - 3x^3 + 25x^4$$

$$\frac{d(y)}{d(x)} = 12x - 9x^2 + 100x^3$$

•
$$y - 3 = 2x$$

$$\frac{d(y)}{d(x)} = 2$$

•
$$TPP = 24 + 5L + 2L^2 - L^3$$

$$\frac{d(TPP)}{d(L)} = 5 + 4L - 3L^2$$

• What does your answer to the prevous question tell you about the shape of the Total Physical Product Curve?

It goes up initially but starts rise at a slower pace. There are diminishing returns.

Find the second derivative of the following

•
$$TU = 25 + X_1 - X_1^2$$

$$\frac{d^2(U)}{d(X_1)} = -2$$

•
$$TU = 25 + 25X_1 - 2X_1^2$$

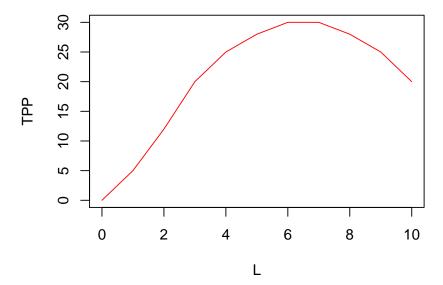
 $\frac{d^2(U)}{d(X_1)} = -4$

•
$$TPP = 15 + 15Q + Q^2 - Q^3$$

$$\frac{d^2(TPP)}{d(L)} = 2 - 6Q$$

- What does your answer to the previous question tell you about the shape of the Total Physical Product Curve?
 It shows that the rate of change is falling.
- Here is the total physical product curve. Show the average physical product? for a particular point on the graph.

Total Physical Product



• How would you calculate the marginal physical product?

- 2. What is the gradient of the TPP at its peak?
- 3. What is the value of the MPP when TPP is at its peak?
- 4. Given the $TPP = 100 + 32Q + 23Q^2 Q^3$,
 - What is the TPP' or MPP? $32 + 46Q 3Q^2$
 - How would you find the maximum TPP?

$$3Q^2 - 46Q - 32 = 0$$
$$(3Q + 2)(Q - 16) = 0$$

Therefore
$$3Q = -2$$
 or $Q = 16$

- 5. Given the $TPP = 500 + 180Q + 15Q^2 2Q^3$,
 - What is the TPP' or MPP? $MPP = 180 + 30Q 6Q^2$
 - How would you find the maximum TPP?

$$6Q^2 - 30Q - 180 = 0$$
$$(6Q + 90)(Q - 20) = 0$$

So
$$Q = -15$$
 or $Q = 20$.

- 6. Given the $TU = 25X 0.5X^2$
 - What is the drivative of TU?

$$TU = 25 - X$$

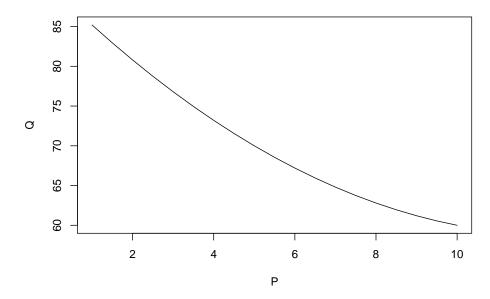
• What can we say about the utility of X?

There are diminishing returns.

Given a demand curve

$$Q_d = 90 - 5P - 0.2P^2$$

Demand Curve



What is the elasticity of demand at the point P = 5, Q = 70?

The equation for elasticity is

$$\varepsilon_d = \frac{d(Q)}{d(P)} \times \frac{P}{Q}$$

$$= \frac{-5 - 0.4 \times 5}{\times} \frac{5}{70}$$

$$= -5 - 2 \times \frac{5}{70}$$

$$= -0.5$$

Therefore the demand is inelastic