

ASSIGNMENT #3

EPsy 8252

This assignment covers vector geometry and matrix algebra. Please submit your responses to each of the questions below in a printed document. Please adhere to the following guidelines for formatting your assignment:

- All graphics should be resized so that they do not take up more room than necessary and all should have an appropriate caption.
- Any typed mathematics (equations, matrices, vectors, etc.) should be appropriately typeset within the document using Equation Editor, Markdown, or \LaTeX .
- All syntax included should be typeset in a monospaced font, appropriately commented and follow the DataCamp Style Guide (<https://teach.datacamp.com/style-guide>).

There are 10 points possible for the assignment. Each question is worth one point, unless otherwise noted.

Regression

Use the following data to answer the questions below.

```
##  Y X1 X2
##  74  3  0
##  57  4  1
##  62  4  1
##  45  2  0
##  54  2  0
```

1. Write out the design matrix for the model $Y \sim 1 + X1 + X2$. Use an equation editor to write that matrix into your word-processed document.
2. What are the dimensions of the design matrix?
3. Use R to compute $(X'X)^{-1}$. Use an equation editor to write that matrix into your word-processed document.
4. Use matrix algebra and R to compute the **b** vector (vector of the regression coefficients). Use an equation editor to write that vector into your word-processed document.
5. Using matrices, compute the vector of fitted values. Use an equation editor to write that vector into your word-processed document.
6. Draw the model triangle for this model. Label all vectors and compute the values of all of the angles in the triangle. (2pts.)

Regression through the Origin

Consider a regression of the same data, but this time, we will force the regression line through the origin.

7. Write out the design matrix for the model $Y \sim X1 + X2 - 1$. Use an equation editor to write that matrix into your word-processed document.

8. Use R to compute $(\mathbf{X}^t\mathbf{X})^{-1}$. Use an equation editor to write that matrix into your word-processed document.
9. Use matrix algebra and R to compute the \mathbf{b} vector (vector of the regression coefficients). Use an equation editor to write that vector into your word-processed document.