

Introduction to the Course

ESS 575 Models

small change

ata

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January 22, 2019



Department of Ecosystem
Science and Sustainability

Colorado
State
University®

What is this course about?

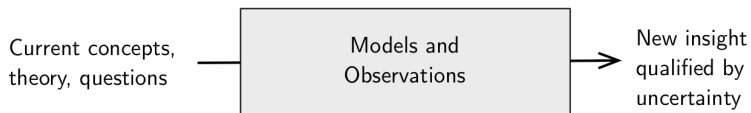
Gaining new insight about ecological processes using models and observations in the Bayesian framework.

$[z_i | \boldsymbol{\theta}_p]$ A model of a process

$[y_i | z_i, \boldsymbol{\theta}_d]$ A model of the data that arise from the process

$[\boldsymbol{\theta}_p][\boldsymbol{\theta}_d]$ Models of parameters

What is this course about?



Why this course?

KEY TO STATISTICAL METHODS

	Design or Purpose	Measurement Variables	Ranked Variables	Attributes
1 variable 1 sample	Examination of a single sample	Procedure for grouping a frequency distribution, Box 2.1; stem-and-leaf display, Section 2.5; testing for outliers, Section 13.4 Computing median of frequency distribution, Box 4.1 Computing arithmetic mean: unordered sample, Box 4.2; frequency distribution, Box 4.3 Computing standard deviation: unordered sample, Box 4.2; frequency distribution, Box 4.3 Setting confidence limits: mean, Box 7.2; variance, Box 7.3 Computing g_1 and g_2 , Box 6.2		Confidence limits for a percentage, Section 17.1 Runs test for randomness in dichotomized data, Box 18.3
	Comparison of a single sample with an expected frequency distribution	Normal expected frequencies, Box 6.1 Goodness of fit tests: parameters from an extrinsic hypothesis, Box 17.1; from an intrinsic hypothesis, Box 17.2 Kolmogorov-Smirnov test of goodness of fit, Box 17.3 Graphic "tests" for normality: large sample sizes, Box 6.3; small sample sizes (rankit test), Box 6.4 Test of sample statistic against expected value, Box 7.4		Binomial expected frequencies, Box 5.1 Poisson expected frequencies, Box 5.2 Goodness of fit tests: parameters from an extrinsic hypothesis, Box 17.1; from an intrinsic hypothesis, Box 17.2
1 variable ≥ 2 samples	Single classification	Single classification anova: unequal sample sizes, Box 9.1; equal sample sizes, Box 9.4 Planned comparison of means in anova, Box 9.8; single degree of freedom comparisons of means, Box 14.10 Unplanned comparison of means: T-method, equal sample sizes, Box 9.9; T, GT2, and Tukey-Kramer, unequal sample sizes, Box 9.10; Welch step-up, Box 9.11; STP test, Section 9.7; contrasts using Scheffé, T, and GT2, Box 9.12; multiple confidence limits, Section 14.10 Estimate variance components: unequal sample sizes, Box 9.2; equal sample sizes, Box 9.3 Setting confidence limits to a variance component, Box 9.3 Tests of homogeneity of variances, Box 13.1 Tests of equality of means when variances are heterogeneous, Box 13.2	Kruskal-Wallis test, Box 13.5 Unplanned comparison of means by a nonparametric STP, Box 17.5	G-test for homogeneity of percentages, Boxes 17.5 and 17.8 Comparison of several samples with an expected frequency distribution, Box 17.4; unplanned analysis of replicated tests of goodness of fit, Box 17.5
	Nested classification	Two-level nested anova: equal sample sizes, Box 10.1; unequal sample sizes, Box 10.4 Three-level nested anova: equal sample sizes, Box 10.3; unequal sample sizes, Box 10.5		
	Two-way or multi-way classification	Two-way anova: with replication, Box 11.1; without replication, Box 11.2; unequal but proportional subclass sizes, Box 11.4; with a single missing observation, Box 11.5 Three-way anova, Box 12.1 More than three-way classification, Section 12.3 and Box 12.2 Test for nonadditivity in a two-way anova, Box 13.4	Friedman's method for randomized blocks, Box 13.9	Three-way log-linear model, Box 17.9 Randomized blocks for frequency data (repeated testing of the same individuals), Box 17.11

Why this course?



3 A	5 B	1 B	4 B	2 A	1 A	4 A	3 B	5 A	Block 1
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2 A	5 B	4 B	2 B	4 A	3 A	1 A	1 B	3 B	5 A	Block 2
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1 A	3 B	4 B	5 B	3 A	4 A	2 A	2 B	1 B	5 A	Block 3
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5 A	2 A	1 A	4 A	3 A	1 B	3 B	5 B	4 B	2 B	Block 1
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5 B	3 B	1 B	2 B	4 B	4 A	3 A	2 A	1 A	5 A	Block 2
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4 A	3 A	5 A	1 A	2 A	2 B	1 B	3 B	5 B	4 B	Block 3
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Factorial
Arrangement of
Treatments in a
Randomized
Complete Block
Design

Factorial
Arrangement of
Treatments in a
Split-Plot Design

Why this course?

Fleishman, E., et al., 2011. Top 40 Priorities for Science to Inform US Conservation and Management Policy. *Bioscience* 61:290-300.

Why this course?

Problems poorly suited to traditional approaches

- ▶ Multiple sources of data
- ▶ Multiple sources of uncertainty
- ▶ Inference across scales
- ▶ Unobservable quantities
- ▶ Missing data
- ▶ Derived quantities
- ▶ Forecasting

Why this course?

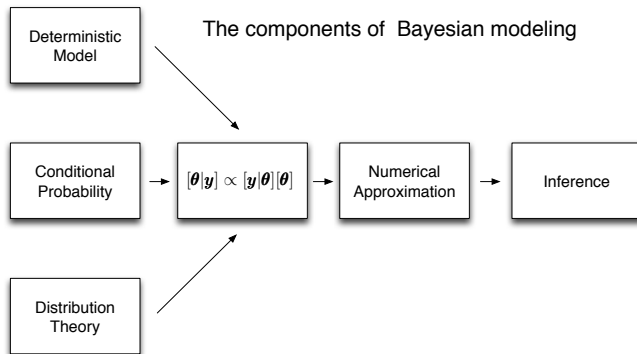
Recent ESS 575 alumni

Student	Position
Ann Raiho	Ph.D., Notre Dame
Megan Vahsen	Ph.D., Notre Dame
Nathan Galloway	Biologist, National Park Service
Nell Campbell	Research Scientist, Univ. New Hampshire
Katie Renwick	Post-doc, Univ. Montana
Alison Ketz	Post-doc, USGS, University of Wisconsin
Zhongqi Miao	Ph.D., Berkeley
Greg Wann	Post-doc, USGS
Vincent Landau	Analyst, Conservation Science Partners

Goals

- ▶ Provide *principles* based understanding
- ▶ Enhance intellectual satisfaction
- ▶ Foster collaboration
- ▶ Build a foundation for self-teaching

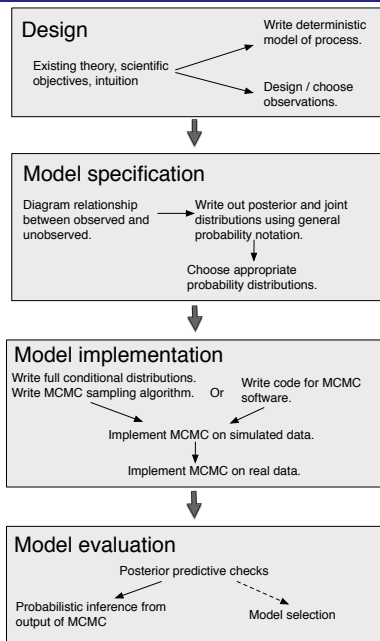
Learning outcomes



Learning outcomes

1. Explain basic principles of Bayesian inference.
2. Diagram and write out mathematically correct posterior and joint distributions for Bayesian models.
3. Explain basics of the Markov chain Monte Carlo (MCMC) algorithm and be able to write an MCMC sampler.
4. Use software for implementing MCMC.
5. Develop and implement hierarchical models.
6. Evaluate model fit.
7. Appreciate possibilities for model selection.
8. Understand consequences of spatial and temporal autocorrelation.
9. Understand papers and proposals using Bayesian methods.

Learning outcomes



Course topics

Principles

- Laws of probability
- Distribution theory
- Moment matching
- Bayes' theorem
- Conjugacy

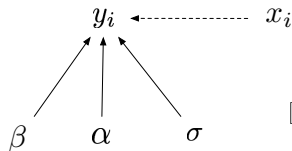
Implementation and inference

- MCMC
- JAGS
- Inference from single and multiple models
- Model checking

Hierarchical models

- Introduction
- Multi-level regression
- Mixture and occupancy
- State-space
- Spatial

Cross cutting theme



$$\mu_i = \frac{mx_i^a}{h^a + x_i^a}$$

$$[a, h, m, \sigma^2 \mid y] \propto \prod_{i=1}^n [y_i \mid \mu_i, \sigma^2] [a] [h] [m] [\sigma^2]$$

```

model{

  for(i in 1:length(y)){

    mu[i] <- (m*x[i]^a)/(h^a+x[i]^a)
    y[i] ~ dgamma(mu[i]^2/sigma^2,mu[i]/sigma^2)

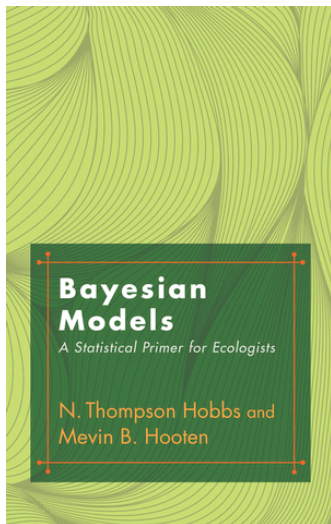
  }

  a ~ dnorm(0,.0001)
  m ~ dgamma(.01,.01)
  h ~ dgamma(.01,.01)
  sigma ~ dunif(0,5)
}
  
```

Teaching philosophy

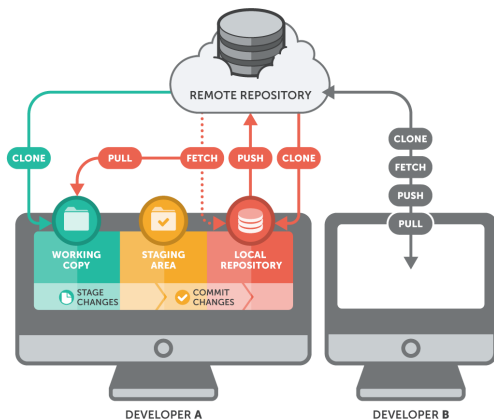
- ▶ Principles are primary
- ▶ Everyone learns, everyone teaches
- ▶ Teaching trumps evaluation.
- ▶ The best learning comes from solving problems.
- ▶ Whenever possible, I teach in the first person voice.

Text



Errata: http://warnercnr.colostate.edu/~hooten/papers/pdf/Hobbs-Hooten-Bayesian-Models-2015_errata.pdf

Accessing course materials on GitHub



Learn Version Control with Git: A step-by-step course for the complete beginner

<https://www.git-tower.com/learn/>

Accessing course materials on GitHub

Show possible file structure for course materials on board.

Housekeeping

- ▶ Lab in Natural Resources 254
 - ▶ You will need a laptop
 - ▶ Bring long power cords.
- ▶ Lecture in NESB A302 starting promptly at 9:30

Housekeeping

- ▶ R primer for first laboratory available on GitHub
- ▶ Lecture notes: download morning of class (after 8:30)
- ▶ Some board work, so be prepared to take notes.

R markdown

The screenshot shows the RStudio interface. The left pane displays the R Markdown source code for 'DiscreteLogistic.Rmd'. The code includes a style block to hide the number of publications, a script block for MathJax, and a plot command. The right pane shows the rendered HTML output, which is a document titled 'ESS 575: Models for Ecological Data' with the subtitle 'Programming in R' and the date 'January 11, 2017'. The document contains an 'Objective' section stating the purpose of the lab is to test R programming skills, followed by a list of tasks: writing functions, creating data structures, looping, sub-setting matrices, and plotting. Below this is a section titled 'Exploring chaos with the discrete logistic', which references a 1976 paper by Robert May and includes the equation $x_{t+1} = \lambda x_t(1 - x_t)$. The console at the bottom shows the execution of the R code, including the plot command and the resulting file path.

```

1 <style>
2
3 /* uncomment out this to generate exercise */
4 .hider {display: none;}
5
6 /* uncomment out this to generate key */
7 /* .hider {display: inline;} */
8
9 </style>
10
11 <script type="text/x-mathjax-config">
12 MathJax.Hub.Config({
13   Text: {
14     equationNumbers: {
15
16       autoNumber: "all",
17       formatNumber: function (n) {return +n}
18     }
19   }
20 })
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```

Console

```

~ /
> unknwn argument (unknown = 0)
> barplot(y.names.arg-as.character(x), ylab="Number of publications", as=
> dev.off()
null device
1
> barplot(y.names.arg-as.character(x), ylab="Number of publications", as=
> pdf(file="/Users/Tom/Documents/NSF Statistics Workshop/Pre-proposal201
h=6, height=4)
> barplot(y.names.arg-as.character(x), ylab="Number of publications", as=
> dev.off()
RStudioGD
2
>

```

ESS 575: Models for Ecological Data
Programming in R
January 11, 2017

Objective

The purpose of this lab is to test what you have learned about some important topics in R programming:

1. writing functions
2. creating data structures
3. looping
4. sub-setting matrices
5. plotting

Exploring chaos with the discrete logistic

In 1976, Robert May authored a classic paper (May 1976) revealing chaotic dynamics in discrete time mc logistic,

$$x_{t+1} = \lambda x_t(1 - x_t)$$

where λ is the per capita rate of population growth and x_t is the population size at time t . This form of the unfamiliar to you because it lacks the parameter, K . May used a mathematical trick to rescale the equation focus our attention on the effect of λ on the population's dynamics. In your first exercise, you will vary λ ; trajectory of a simulated population.

Evaluation

- ▶ Eleven laboratory exercises worth 50 - 100 points each. (80% of grade)
- ▶ A capstone problem done individually (20% of grade)
- ▶ You are graded relative to material, not relative to each other.
- ▶ Relax. You will get an A if you do the assignments carefully and thoughtfully.
- ▶ See syllabus for details.

Individual projects

- ▶ Purpose
- ▶ Process
- ▶ Product

Getting help

- ▶ From me: Tuesday-Thursday 11:00 - 12:00 or by appointment, NESB B227 or by email (tom.hobbs@colostate.edu). Please put ESS 575 in subject line.
- ▶ From TA, Brian Avila: Fridaya 12:30-2:30 or by appointment, Wagar 203, mlvahsen@gmail.com.

Chores

- ▶ Fill out Google doc spreadsheet if you have not already done so.
- ▶ Get account on GitHub and pull repository ESS_575_2019 to your local machine. See instructions in `Accessing course material.html`.
- ▶ Install R and R studio before lab tomorrow. See instructions in R primer on class repository.
- ▶ Install the R package ESS575 containing course data library. See instructions in `Accessing course material.html`.
- ▶ Print R primer for first laboratory.
- ▶ Read materials in Admin folder of ESS_575_2019.

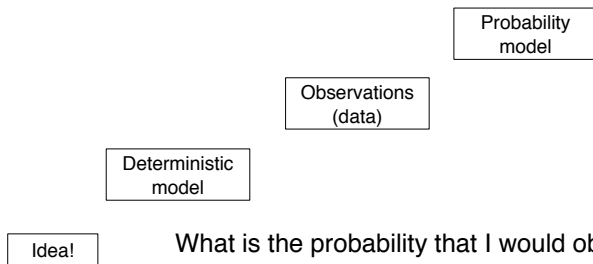
First assignment

- ▶ Read the syllabus.
- ▶ Prepare ≤ 2 minute presentation about yourself: background, what are you studying, who is your major professor, why you are taking this class.
- ▶ Prepare a 1-2 paragraph description of an important non-linear, static, deterministic model in your field of ecology. See `FirstAssignment.pdf` in Admin folder of ESS_575_2019. Due Friday.
- ▶ Dust off your calculus book. Review the definite integral and how it is derived.

Discussion topic (if time)

What do you think of when someone is described as an “ecological modeler?” Mevin and I say in our book that all ecological researchers are modelers. Why do you suppose we say that? Describe your ideas about the relationships among observations, mathematical models, and statistical models in ecology.

We are all ecological modelers



What is the probability that I would observe the data if my model is a faithful representation of the processes that gave rise to the data?