

What sets Bayes apart?

ESS 575 Models for Ecological Data

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Today

- ▶ A high elevation view of approaches for statistical inference
- ▶ Some motivation for learning
- ▶ The basic ideas of Bayesian inference

Exercise

What sets statements of scientists apart from statements made by journalists, lawyers, and logicians?

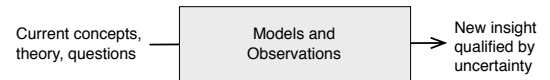
Exercise

Write the definition of a frequentist, 95% confidence interval on a parameter of interest, θ .

Frequentist confidence interval

In frequentist statistics, a 95% confidence interval represents an interval of a specified width such that if the experiment or sample were repeated many times, 95% of the intervals would contain the true parameter value.

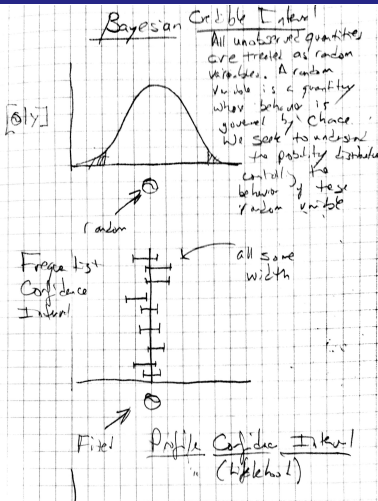
A line of inference



Some notation

- ▶ y data
- ▶ θ a parameter or other unknown quantity of interest
- ▶ $[y|\theta]$ The probability distribution of y conditional on θ
- ▶ $[\theta|y]$ The probability distribution of θ conditional on y
- ▶ $[y|\theta] = P(y|\theta) = p(y|\theta) = f(y|\theta) = f(y, \theta)$, different notation that means the same thing.

Board work on confidence envelopes



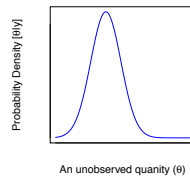
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Exercise

Describe how Bayesian analysis differs from other types of statistical analysis.

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What sets Bayes apart?



- ▶ Bayesians divide the world into things that are observed (y) and unobserved (θ).
- ▶ All unobserved quantities are treated as *random variables*.
- ▶ A random variable is a quantity whose behavior is governed by chance.
- ▶ Probability distributions are mathematical abstractions of "governed by chance."
- ▶ We seek to understand the characteristics of these probability distributions, particularly $[\theta|y]$.

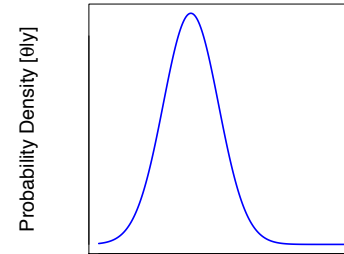
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What sets Bayes apart?

Treating unobserved quantities as random variables is profound.

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- ▶ Parameters
- ▶ Latent states
- ▶ Missing data
- ▶ Censored data
- ▶ Predictions
- ▶ Forecasts



An unobserved quantity (θ)



Prior results from the “Define a confidence interval” exercise from faculty, researchers, and graduate students at:

- ▶ Swedish Agricultural University
- ▶ University of Alaska Anchorage
- ▶ Woods Hole Research Institute
- ▶ Conservation Science Partners
- ▶ National Socio-environmental Synthesis Center (3 courses)
- ▶ ESS 575 (2 courses)

Cut to R to illustrate updating with today's data.

[illegible]

You can understand it.

P value:
~~A number that shows the likelihood~~
A number that shows the likelihood
that a value is the same as
another

Confidence Interval - shows A range of values
that we have a certain level of confidence
our value of interest falls in.

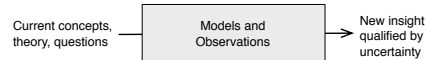
1) Definition of P value
The probability of the significant
difference between measured/observed
value & other measured values

2) What is confidence interval?
The range of measured/observed
value true population mean
can occur within it

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You can understand it.

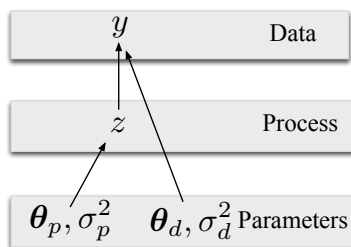
- Rules of probability
 - Conditioning and independence
 - Law of total probability
 - Factoring joint probabilities
- Distribution theory
- Markov chain Monte Carlo



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One approach applies to many problems

- An unobservable state of interest, z
- A deterministic model of a process, $g(\theta, x)$, controlling the state.
- A model of the data
- Models of parameters



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