ESS 575 Models for Ecological Data

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Today

- ▶ A high elevation view of approaches for statistical inference
- Some motivation for learning
- ▶ The basic ideas of Bayesian inference

Exercise

What sets statements of scientists apart from statements made by journalists, lawyers, and logicians?

Exercise

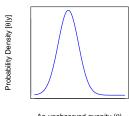
Write out the definition of a frequentist, 95% confidence interval on a parameter of interest, θ .

Frequentist confidence interval

- 1. In frequentist statistics, a 95% confidence interval represents an interval such that if the experiment were repeated 100 times, 95% of the resulting confidence intervals (e.g.. average + or 1.96 * standard error) would contain the true parameter value.
- 2. In a narrower sense, a CI for a population parameter is an interval with an associated proportion p that is generated from a random sample of an underlying population such that if the sampling was (sic) repeated numerous times and the confidence interval recalculated from each sample according to the same method, a proportion p of the confidence intervals would contain the population parameter in question.

Exercise

Describe how Bayesian analysis differs from other types of statistical analysis.



An unobserved quanity (θ)

- All unobserved quantities are treated as random variables.
- ▶ A random variable is a quantity whose behavior is governed by chance.
- Probability distributions are mathematical abstractions of "governed by chance."
- We seek to understand the characteristics of these probability distributions.

Some notation

- y data
- lacktriangledown heta a parameter or other unknown quantity of interest
- lackbox[y| heta] The probability distribution of y conditional on heta
- $lackbox{ } [\theta|y]$ The probability distribution of θ conditional on y
- ▶ $[y|\theta] = P(y|\theta) = p(y|\theta) = f(y|\theta) = f(y,\theta)$, different notation that means the same thing.

Board work on confidence envelopes

Define a confidence interval

Prior data on the exercise from faculty, researchers, and graduate students at:

Swedish Agricultural University

University of Alaska Anchorage

Woods Hole Research Institute

Conservation Science Partners

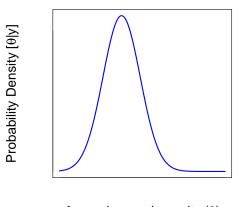
► ESS 575 2017

- ▶ We divide the world into things that are observed (y) and things that unobserved (θ) .
- ▶ The unobserved quantities (θ) are random variables. The data are random variables before they are observed and fixed after they have been observed.
- ▶ We seek to understand the probability distribution of θ using fixed observations, i.e., $[\theta|y]$.
- ▶ Those distributions quantify our uncertainty about θ .

Treating unobserved quantities as random variables is profound.

All unobserved quantities are treated in exactly the same way.

- Parameters
- Latent states
- Missing data
- Censored data
- Predictions
- Forecasts



An unobserved quanity (θ)



You can understand it.

	Design or Purpose	Measurement Variables	Ranked Variables	Attributes
1 variable 1 sample	Examination of a single sample	Procedure for grouping a frequency distribution, Bix 3.1: stem and leaf display, Section 2.5: (stein for orditine, Section 13.4 Computing medium of frequency distribution, Bix 4.1 Computing arthritism ional: frequency distribution, Bix 4.3 computing arthritism ional: frequency distribution, Bix 4.3 unnotated sample, Bix 4.2: frequency distribution, Bix 4.3 Setting confidence limits: mean, Bix 7.2: variance, Bix 7.3 Computing, and ag., Bix 6.2		Confidence limits for a percentage, Section 17.1 Runs test for randomness in dichotomized data, Box 18.3
	Comparison of a single sample with an expected frequency distribution	Normal expected frequencies, Box 6.1 Goodness of fit tests parameters from an extrinsic hypothesis, Box 17.1; from an intrinsic hypothesis, Box 17.2 Kolmogorov-Smitrov test of goodness of fit, Box 17.3 Graphic Tests for normality: large sample sizes, Box 6.3; small sample sizes irrankit testil, Box 6.4 Test of sample statistic against expected value, Box 7.4		Binomial expected frequencies, Box 5.1 Poisson expected frequencies, Box 5.2 Goodness of fit tests: parameters from an extrinsic hypothesis, Box 17.1; from an intrinsic hypothesis, Box 17.2
11 11 21 32 32 33 34 34 34 34 34 34 34 34 34 34 34 34	Single classification	Single, charaffaction storus: uniqual sample sizes, Box 91, equal sample sizes, Box 9.4 Planned comparison of means in anova, Box 9.8 single degree of refeoden comparisons of means, Box 14.10 Unplanned comparison of means: T-method, equal sample sizes, Box 9.9, T., GT2, and Tquey-Karmen, unequal sample sizes, Box 9.9, T., GT2, and Tquey-Karmen, unequal sample sizes, Box 9.9, T., and GT2, Box 9.12, multiple confidence limits. Section 14.10 meths. T. and GT2, Box 9.12, multiple confidence limits. Section 14.10 meths. Section 24, 200, 200, 200, 200, 200, 200, 200,	Kruskal-Wallis text, Box 13.5 Unplanned comparison of means by a nonparametric STP, Box 17.5	G test for homogeneity of percentages, Boxes 17.5 and 17.8 Comparison of several samples with an expected frequency distribution. Box 17. unplanned analysis of replicated tests of goodness of fir, Box 17.3.
		Tests of homogeneity of variances, Box 13.1 Tests of equality of means when variances are heterogeneous, Box 13.2		
	Nested classification	Two level nested anova: equal sample sizes, Box 10.1; unequal sample sizes, Box 10.4 Three-level nested anova: equal sample sizes, Box 10.3; unequal sample sizes, Box 10.5		
	Two way or multi-way classification	Two way anova: wth replication, Box 11.1: without replication, Box 11.2: unequal but proportional subcless sizes, Box 11.4: with a single missing observation, Box 11.5. Three way anova, Box 12.1: More than three way classification, Section 12.3 and Box 12.2. Test for nonadistricts in a law way anova, Box 13.1.4.	Friedman's method for randomized blocks. Box 13.9	Three way log-linear model, Box 17.9 Randomized blocks for frequency data frepeated testing of the same individuals Box 17.11

You can understand it.

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another

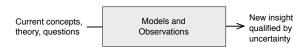
Confidence Interval— Shows A range of values that we have a certain level of confidence our value of interest falls in.

- Definition of Prolue
 The probability of the tignificant
 difference between measured (chrorusd)
 value & other measured values
- The range of measured (chserved)

 rather can occur within it

You can understand it.

- Rules of probability
 - Conditioning and independence
 - Law of total probability
 - Factoring joint probabilities
- Distribution theory
- Markov chain Monte Carlo



One approach applies to many problems

- An unobservable state of interest, z
- ▶ A deterministic model of a process, $g(\theta, x)$, controlling the state.
- A model of the data
- Models of parameters

