An R Companion to Introduction to Statistical Investigations Preliminary Edition

Randall Pruim and Lana Park

May 19, 2015

Contents

U	Prei	iminaries	7
	0.0	Getting Started with R and RStudio	7
	0.1	Introduction to the Six-Step Method	9
	0.2	Exploring Data	13
	0.3	Exploring random Processes	17
	0.4	Other Visualizations	19
1	Sign	nificance: How strong is the evidence?	21
	1.1	Introduction to Chance Models	21
	1.2	Measuring the Strength of Evidence	24
	1.3	Alternative Measure of Strength of Evidence	27
	1.4	What Impacts Strength of Evidence?	32
	1.5	Inference on a single proportion: Theory-based approach	39
2	Gen	eralization: How Broadly Do the Results Apply?	51
	2.1	Sampling from a Finite Population	51
	2.2	Inference for a Single Quantitative Variable	59
	2.3	Errors and Significance	71
3	Esti	mation: How Large is the Effect?	75
	3.1	Statistical Inference - Confidence Intervals	75
	3.2	2SD and Theory-Based Confidence Intervals for a Single Proportion	83

	3.3	2SD and Theory-Based Confidence Intervals for a Single Mean	91	
	3.4	Factors That Affect the Width of a Confidence Interval	94	
	3.5	Cautions When Conducting Inference	100	
4	Cau	sation: Can We Say What Caused the Effect?	109	
	4.1	Association and Confounding	109	
	4.2	Observational studies versus experiments	110	
5	Con	nparing Two Proportions	111	
	5.1	Comparing Two Groups: Categorical Response	111	
	5.2	Comparing Two Properties: Simulation-Based Approach	115	
	5.3	Comparing Two Proportions: Theory-Based Approach	219	
6	Con	nparing Two Means	259	
	6.1	Comparing Two Groups: Quantitative Response	259	
	6.2	Comparing Two Means: Simulation-Based Approach	262	
	6.3	Comparing Two Means: Theory-Based Approach	268	
	Paired Data: One Quantitative Variable			
7	Pair	ed Data: One Quantitative Variable	275	
7	Pair 7.1	Paired Designs		
7			275	
7	7.1	Paired Designs	275 275	
8	7.1 7.2 7.3	Paired Designs	275 275	
	7.1 7.2 7.3	Paired Designs	275 275 283 289	
	7.1 7.2 7.3	Paired Designs	275 275 283 289 289	
	7.1 7.2 7.3 Con 8.1 8.2	Paired Designs	275 275 283 289 289	
8	7.1 7.2 7.3 Con 8.1 8.2	Paired Designs	275 275 283 289 289 293	
8	7.1 7.2 7.3 Com 8.1 8.2	Paired Designs	275 283 289 289 293 305	
8	7.1 7.2 7.3 Con 8.1 8.2 Con 9.1 9.2	Paired Designs Simulation-Based Approach for Analyzing Paired Data Theory-Based Approach to Analyzing Data from Paired Samples Inparing More Than Two Proportions Simulation-Based Approach to Compare Multiple Proportions Theory-Based Approach to Compare Multiple Proportions Theory-Based Approach to Compare Multiple Proportions Inparing More than Two Means Simulation-Based Approach for Comparing More than Two Groups with a Quantitative Respons	275 283 289 289 293 305	
8	7.1 7.2 7.3 Con 8.1 8.2 Con 9.1 9.2 Two	Paired Designs Simulation-Based Approach for Analyzing Paired Data Theory-Based Approach to Analyzing Data from Paired Samples Inparing More Than Two Proportions Simulation-Based Approach to Compare Multiple Proportions Theory-Based Approach to Compare Multiple Proportions Inparing More than Two Means Simulation-Based Approach for Comparing More than Two Groups with a Quantitative Response Theory-based Approach to Comparing More than Two Groups with a Quantitative Response	275 275 283 289 289 293 305 308	
8	7.1 7.2 7.3 Con 8.1 8.2 Con 9.1 9.2 Two	Paired Designs	275 283 289 289 293 305 308 315	

10.4 Inference for Regression Slope: Simulation-Based Approach	328
10.5 Inference for the Regression Slope: Theory-Based Approach	331

 θ

Preliminaries

0.0 Getting Started with R and RStudio

R is divided up into packages. A few of these are loaded every time you run R, but most have to be selected. This way you only have as much of R as you need.

In the Packages tab, check the boxes next to the following packages to load them:

- mosaic (a package from Project MOSAIC)
- Tintle1 (data sets)

RStudio provides several ways to create documents that include text, R code, R output, graphics, even mathematical notation all in one document. The simplest of these is R Markdown.

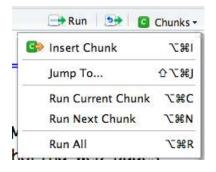
To create a new R Markdown document, go to "File", "New", then "R Markdown."

When you do this, a file editing pane will open with a template inserted. If you click on "Knit HTML", RStudio will turn this into an HTML file and display it for you. Give it a try. You will be asked to name your file if you haven't already done so. If you are using the RStudio server in a browser, then your file will live on the server ("in the cloud") rather than on your computer.

If you look at the template file you will see that the file has two kinds of sections. Some of this file is just normal text (with some extra symbols to make things bold, add in headings, etc.) You can get a list of all of these mark up options by selecting the "Mardown Quick Reference" in the question mark menu.



The second type of section is an R code chunk. These are colored differently to make them easier to see. You can insert a new code chunk by selecting "Insert Chunk" from the "Chunks" menu:



(You can also type ``` $\{r\}$ to begin and ``` to end the code chunk if you would rather type.) You can put any R code in these code chunks and the results (text output or graphics) as well as the R code will be displayed in your HTML file.

There are options to do things like (a) run R code without displaying it, (b) run R code without displaying the output, (c) controlling size of plots, etc., etc. But for starting out, this is really all you need to know.

R Markdown files are self-contained, meaning they do not have access to things you have done in your console. (This is good, else your document would change based on things not in the file.) This means that you must explicitly load data, and require packages *in the R Markdown file* in order to use them. For this text, this means that most of your R Markdown files will have a chunk near the beginning that includes

```
require(mosaic) # load the mosaic package
```

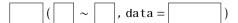
Functions in R use the following syntax:

```
functionname(argument1, argument2, ...)
```

The arguments are always surrounded by (round) parentheses and separated by commas.

Some functions (like data()) have no required arguments, but you still need the parentheses.

Most of what we will do in the subsequent chapters makes use of a single R template:



It is useful if we name the slots in this template:

$$[goal](y \sim x, data = mydata)$$

However, there are some variations on this template:

```
### Simpler version
goal(~x, data = mydata)
### Fancier version:
goal(y ~ x | z, data = mydata)
### Unified version:
goal(formula, data = mydata)
```

To use the template, you just need to know what goes in each slot. This can be determined by asking yourself two questions:

- 1. What do you want R to do?
 - this determines what function to use (goal).
- 2. What must R know to do that?
 - this determines the inputs to the function
 - for describing data, must must identify which data frame and which variable(s).

Further, if you begin a command and hit the TAB key, R will show you a list of possible ways to complete the command. If you hit TAB after the opening parenthesis of a function, it will show you the list of arguments it expects. The up and down arrows can be used to retrieve past commands.

Additional R functionality will be introduced as we go along. The mosaic package includes several vignettes with additional information about using the package and using R.

0.1 Introduction to the Six-Step Method

Example P.1: Organ Donations

Now that we've explained a few basics for using R, let's take a look at a data set.

Data sets in R are usually stored as **data frames** in a rectangular arrangement with rows corresponding to **observational units** and columns corresponding to **variables**. A number of data sets are built into R and its packages. The package for our text is **Tintle1** which comes with a number of data sets.

```
require(Tintle1) # tell R to use the package for our textbook
data(OrganDonor) # load the OrganDonor dataset
```

If you want a list of all data sets available to you in loaded packages, use data() without any arguments. If you want to view the entire data set, just typing the name will show the details in the console.

```
data() # list all datasets available in loaded packages
OrganDonor # show entire dataset in console
```

For large data sets, it may be more practical to look at different types of summaries or subsets of the data.

```
head(OrganDonor)
                      # first six cases of the dataset
  default choice
1 opt-in donor
2 opt-in donor
3 opt-in donor
4 opt-in donor
5 opt-in donor
6 opt-in donor
summary(OrganDonor)
                      # summary of each variable
  default
                      choice
                  Length: 161
 Length: 161
 Class :character Class :character
 Mode :character Mode :character
```

Now that we have a general sense of how the data is structured, we can take a more detailed look by using the R template. Let's say we want a count of observational units of each variable. We can tally the number by using the tally() function.

```
tally(~choice, data = OrganDonor)

donor not
   108   53

tally(~default, data = OrganDonor)

neutral opt-in opt-out
   56   55   50
```

This didn't really show us any more information than the summary() from above so instead, let's tally the variables together.

```
tally(~choice + default, data = OrganDonor)
      default
choice neutral opt-in opt-out
 donor
           44
                   23
                          41
            12
                   32
 not
tally(~choice + default, data = OrganDonor, margins = TRUE)
      default
choice neutral opt-in opt-out Total
 donor
            44
                   23
                           41 108
            12
                   32
                           9
                                 53
 not
 Total
          56
                   55
                           50
                               161
```

Notice that the default for tally() was to exclude the total counts of each row and column. You could have used either tab completion or search tally() in the help section to find margins and set margins=TRUE. There will be many instances where you will need to change the default settings of a function.

Moreover, we can change the organization of the variables for a slightly different output:

```
tally(choice ~ default, data = OrganDonor)
      default
choice neutral opt-in opt-out
            44
                   23
                           41
 donor
                            9
            12
                   32
 not
tally(choice ~ default, data = OrganDonor, format = "percent")
      default
choice
        neutral
                 opt-in opt-out
 donor 78.57143 41.81818 82.00000
 not 21.42857 58.18182 18.00000
```

This may be a little confusing now (proportions will be covered in chapter 2) but let's focus more on the the changed organization of the variables in the tally() function. This version of tallying calculated the proportions (and percentages) of participants who agreed and did not agree to become organ donors (choice) in each of the groups opt-in, opt-out, and neutral (default).

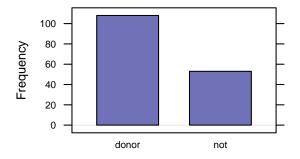
R also has many tools to visualize data. The general syntax for making a graph of one variable in a data frame is

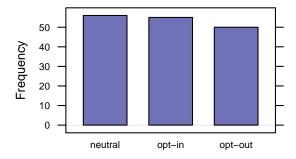
```
plotname(~variable, data = dataName)
```

In other words, there are three pieces of information we must provide to R in order to get the plot we want:

- The kind of plot (histogram(), bargraph(), densityplot(), bwplot(), etc.)
- The name of the variable
- The name of the data frame this variable is a part of.

```
bargraph(~choice, data = OrganDonor)
bargraph(~default, data = OrganDonor)
```

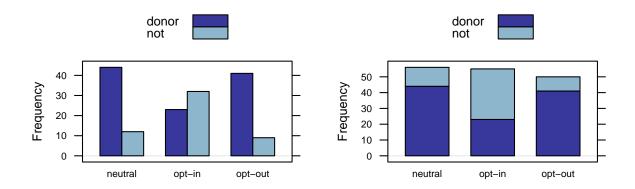




Notice that the bargraph() uses the frequency, or counts.

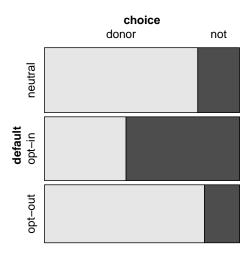
In order to graph the variable default and show what choice each option made, we can utilize the argument groups=.

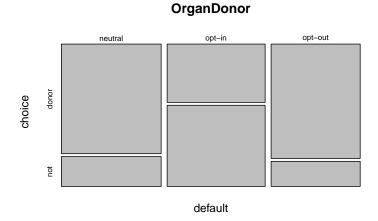
```
bargraph(~default, groups = choice, data = OrganDonor, auto.key = TRUE)
bargraph(~default, groups = choice, data = OrganDonor, auto.key = TRUE, stack = TRUE)
```



Although the bargraph is useful, the y-axis shows counts and not the percentages as in the text. The function mosiac() or mosaicplot() plots the variables relative to each other, in a way that reveals porportions, or percentages.

```
mosaic(choice ~ default, data = OrganDonor)
mosaicplot(default ~ choice, data = OrganDonor)
```





0.2 Exploring Data

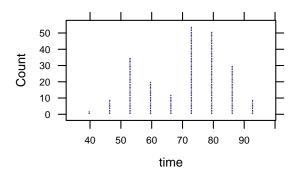
Example P.2: Old Faithful

Everytime you use a new data set, it is beneficial to look at a some key summary statistics.

```
head(0ldFaithful1)
  time
    55
2
    58
3
   56
   50
    51
    60
summary(OldFaithful1)
     time
 Min. :42.00
 1st Qu.:60.00
 Median :75.00
 Mean :71.01
 3rd Qu.:81.00
 Max. :95.00
```

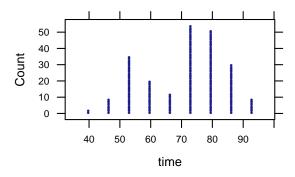
Another useful graph for examining the **shape**, **center**, and **variability** is the **dotplot**:

dotPlot(~time, data = OldFaithful1)



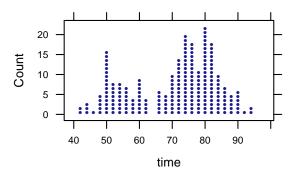
The dots in this plot are a bit small. The defaults for dotPlot() may not be the best way to examine a particular data set. We can increase the size of the dots using the cex argument. (cex stands for "character expansion" and is used to scale up or down the size of plotting characters – in this case the dots.)

dotPlot(~time, data = OldFaithful1, cex = 2)



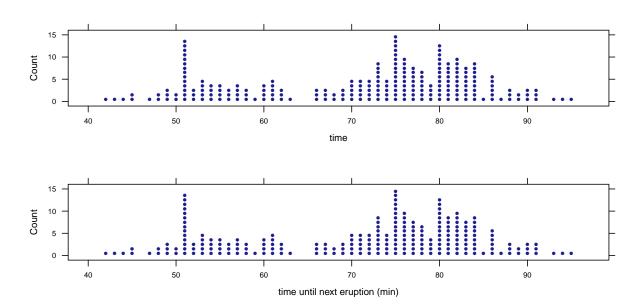
Or we can change the distance between columns of dots

dotPlot(~time, data = OldFaithful1, width = 2)



Notice that the dots have been automatically resized when we do this.

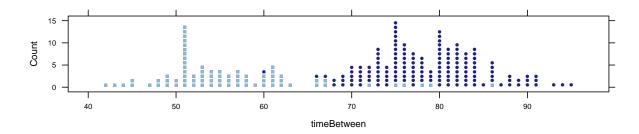
The appropriate choice may depend on the intended size and shape of the plot. The plots below are much wider, allowing us to present a finer view of the data. In the second plot, we have also added a more informative label.



Similar to the bargraph, we can organize the variables a little differently for the dotplot to graph them in relation to one another.

```
head(01dFaithful2)
  eruptionType timeBetween
                         55
1
         short
2
                         58
         short
3
         short
                        56
4
         short
                         50
5
                         51
         short
6
                         60
         short
summary(OldFaithful2)
 eruptionType
                      timeBetween
 Length:222
                    Min. :42.00
 Class :character
                     1st Qu.:60.00
 Mode :character
                    Median :75.00
                    Mean :71.01
                    3rd Qu.:81.00
                    Max. :95.00
```

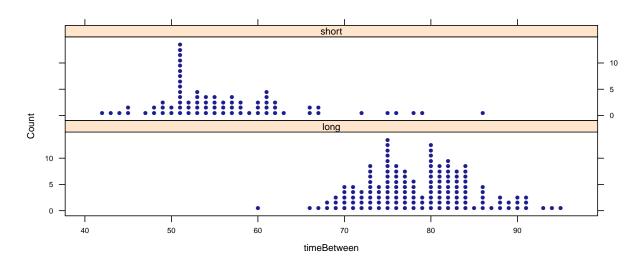
```
dotPlot(~timeBetween, groups = eruptionType, data = 0ldFaithful2, width = 1)
```



The formula for a lattice plot can be extended to create multiple panels (sometimes called facets) based on a "condition", often given by another variable. This is another way to look at multiple groups simultaneously. The general syntax for this becomes

```
plotname(~variable | condition, data = dataName)
```

```
dotPlot(~timeBetween | eruptionType, data = OldFaithful2, width = 1, layout = c(1, 2))
```



For more key numerical summaries of the data set, we can use the favestats() for "favorite" statistics.

```
TableP.1
favstats(~timeBetween, data = OldFaithful2)
min 01 median 03 max
                                          n missing
                         mean
                                     sd
 42 60
           75 81 95 71.00901 12.79918 222
favstats(timeBetween ~ eruptionType, data = 0ldFaithful2)
 eruptionType min Q1 median
                                                      sd
                                                           n missing
                                           mean
          long 60 75
                        78.5 83.00 95 78.69178 6.251692 146
        short 42 51
                       54.0 60.25 86 56.25000 8.457147 76
```

Here are ways to find the mean and the standard deviation separately:

```
mean(~timeBetween, data = 01dFaithful2)

[1] 71.00901

sd(~timeBetween, data = 01dFaithful2)

[1] 12.79918
```

```
mean(timeBetween ~ eruptionType, data = OldFaithful2)

long    short
78.69178 56.25000

sd(timeBetween ~ eruptionType, data = OldFaithful2)

long    short
6.251692 8.457147
```

0.3 Exploring random Processes

Exploration P.3: Cars or Goats

The mosaic package has a function rflip() that simulates coin tosses. We define arguments n (the number of flips) and prob (the probability of heads).

```
rflip(n = 1, prob = 0.5)
Flipping 1 coin [ Prob(Heads) = 0.5 ] ...

H
Number of Heads: 1 [Proportion Heads: 1]

rflip(n = 5, prob = 0.5)
```

```
Flipping 5 coins [ Prob(Heads) = 0.5 ] ...
H H H H H

Number of Heads: 5 [Proportion Heads: 1]
```

Although rflip() simulates coin tosses, where the probability of heads should be 0.5, we can also simulate any **random process** by changing the **probability**.

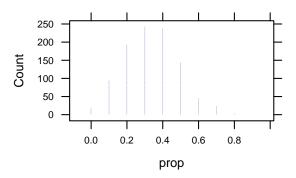
This is equivalent to the playing 15 games (flips), each game having a 1/3 chance of picking the car (heads).

Further, we can repeat each simulation many times by multiplying it by do(). When using do(), you should assign the simulation a name by using an arrow (<-) so that you are creating a new data set with all of the repetitions. In this case, we are naming the simulation GameSims.

```
\# 1000 samples, each of size 200 and proportion 1/3
GameSims \leftarrow do(1000) * rflip(n = 10, prob = 1/3)
head(GameSims)
   n heads tails prop
1 10
         6
                4 0.6
2 10
         5
                5
                   0.5
                   0.4
  10
                6
         4
4 10
         4
                6
                   0.4
5 10
         7
                3
                   0.7
6 10
                5
                   0.5
         5
```

Now we can create a dotplot of the proportion of wins but note that because of there are so many observations (1000), we will not be able to see the individual dots.

```
dotPlot(~prop, data = GameSims, width = 0.1)
```

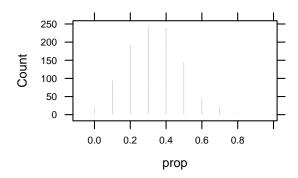


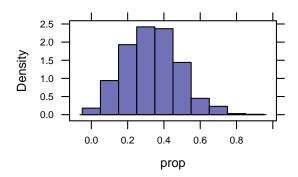
0.4 Other Visualizations

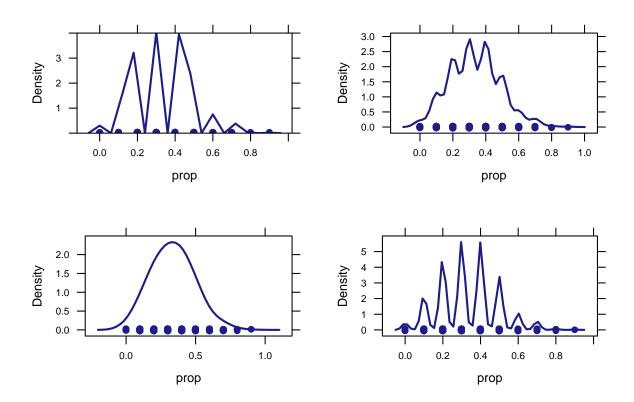
Several other types of plots can be used in place of dot plots to visualize the distribution of a single quantitative variable. The most familiar of these is the histogram, which replaces the dots of a histogram with rectangles and stacks them up touching each other to form bars. If instead we draw lines connecting the tops of each bar in a histogram (and then erase the bars), the result in a frequency polygon. A density plot is a smoother version of this idea.

Notice that to create these plots (and various numerical summaries), all we have to change is the name of the R function – all of them follow the same general template.

```
dotPlot(~ prop, data = GameSims, width = 0.1)
  histogram(~ prop, data = GameSims, width = 0.1)
freqpolygon(^{\sim} prop, data = GameSims, width = 0.1, ylim=c(0,4))
densityplot(~ prop, data = GameSims)
densityplot(~ prop, data = GameSims, adjust=2)
                                                      # "smoother"
densityplot(~ prop, data = GameSims, adjust=0.5) # less "smooth"
   favstats(~ prop, data = GameSims)
 min 01 median 03 max
                                                n missing
                            mean
                                         sd
   0 0.2
             0.3 0.4 0.9 0.3338 0.1521865 1000
       mean(~ prop, data = GameSims)
[1] 0.3338
         sd(~ prop, data = GameSims)
[1] 0.1521865
```





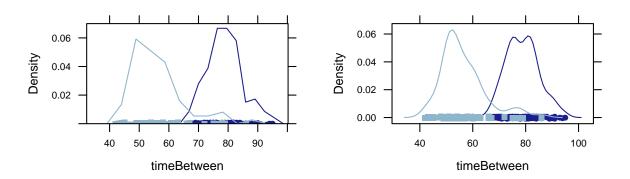


For this data set, a histogram is probably best. This is in part due to the discreteness of the data – there are only 11 possible values for prop.

Compared to dot plots, histograms, frequency polygons, and density plots handle a wider range of data sizes. The "sweet spot" for dot plots is around 100–1000 observations. Also, frequency polygons and density plot have the advantage that they can be overlaid.

```
freqpolygon(\tilde{t}imeBetween, groups = eruptionType, data = 0ldFaithful2, ylim = c(0, 0.07))

densityplot(\tilde{t}imeBetween, groups = eruptionType, data = 0ldFaithful2)
```



(The current version of freqpolygon() is not too clever about choosing the limits for the y-axis – sometimes you need to give it a hand.)

1

Significance: How strong is the evidence?

1.1 Introduction to Chance Models

Example 1.1: Can Dolphins Communicate?

The Chance Model

```
rflip(n = 16, prob = 0.5) # a sequence of 16 coin flips
Flipping 16 coins [ Prob(Heads) = 0.5 ] ...

T H H T H T T T T T H T T H T H

Number of Heads: 6 [Proportion Heads: 0.375]

Figure 1.3

Figure 1.3
```

```
rflip(n = 16, prob = 0.5) # another sequence of 16 coin flips
Flipping 16 coins [ Prob(Heads) = 0.5 ] ...
T T T T T H T H H T T T T H T T

Number of Heads: 4 [Proportion Heads: 0.25]
```

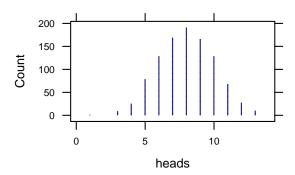
Using and evaluating the coin flip chance model

```
sim \leftarrow do(1000) * rflip(16, 0.5) # 1000 samples, each of size 16 and proportion 0.5 head(sim, 3)

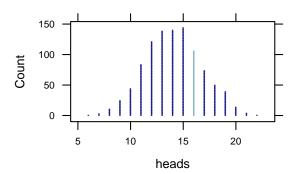
n heads tails prop
```

```
1 16 12 4 0.7500
2 16 11 5 0.6875
3 16 8 8 0.5000

dotPlot(~heads, data = sim, width = 1, cex = 3)
```



Another Doris and Buzz study

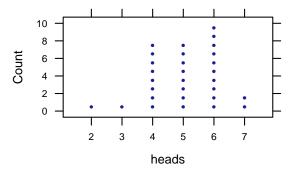


Notice the way we defined groups as (groups = (heads == 16)) in order to differentiate the observations where heads equals 16. The == operator means "are equal to". (We could also have used groups = (heads != 16) and the colors would be reversed.)

Exploration 1.1: Can Dogs Understand Human Cues?

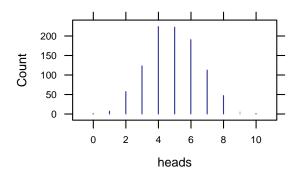
The Chance Model

```
Exploration1.1.13
sim.harley \leftarrow do(1) * rflip(10, 0.5)
sim.harley
  n heads tails prop
1 10 3 7 0.3
sim.class \leftarrow do(30) * rflip(10, 0.5)
head(sim.class, 3)
  n heads tails prop
1 10
      5 5 0.5
2 10
         6 4 0.6
3 10
              4 0.6
         6
dotPlot(~heads, data = sim.class, width = 1, cex = 0.5)
```



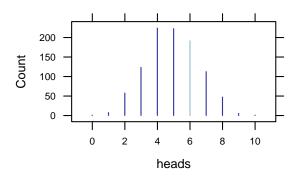
```
sim.harley2 <- do(1000) * rflip(10, 0.5)
head(sim.harley2, 3)

n heads tails prop
1 10 6 4 0.6
2 10 3 7 0.3
3 10 3 7 0.3
dotPlot(~heads, data = sim.harley2, width = 1, cex = 3, groups = (heads == 9))</pre>
dotPlot(~heads, data = sim.harley2, width = 1, cex = 3, groups = (heads == 9))
```



Another Study

```
dotPlot(~heads, data = sim.harley2, width = 1, cex = 3, groups = (heads == 6))
Exploration1.1.23
```



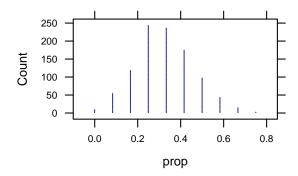
1.2 Measuring the Strength of Evidence

Example 1.2: Rock Paper Scissors

```
1. H_0: \pi = 1/3
H_a: \pi < 1/3
```

Test statistic: $\hat{p} = 0.167$ (the sample proportion of 1/6)

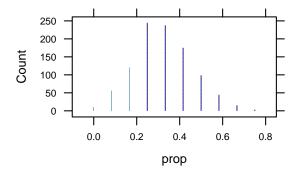
2. We simulate a world in which $\pi = 1/3$:



3. Strength of evidence:

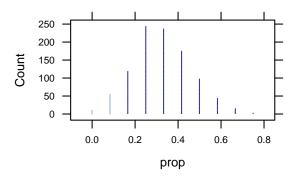
For the **p-value**, you can use the prop() function and input ($prop \le 1/6$) to find the proportion of samples that is less than or equal to the observed proportion in the data set sim.sci.

```
dotPlot(~prop, data = sim.sci, cex = 3, width = 1/12, groups = (prop <= 1/6))
prop(~(prop <= 1/6), data = sim.sci)</pre>
TRUE
0.184
```



Conclusions

```
dotPlot(~prop, data = sim.sci, cex = 3, width = 1/12, groups = (prop <= 1/12))
prop(~(prop <= 1/12), data = sim.sci)</pre>
TRUE
0.065
```



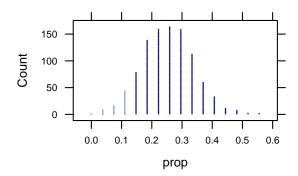
Exploration 1.2: Tasting Water

1. H_0 : $\pi = 1/4$ H_a : $\pi < 1/4$

Test statistic: $\hat{p} = 0.111$ (the sample proportion of 3/27)

2. We simulate a world in which $\pi = 1/4$:

```
Exploration1.2.18
sample.tap \leftarrow do(1) * rflip(27, 1/4)
sample.tap
   n heads tails
                        prop
               20 0.2592593
        7
sim.tap <- do(1000) * rflip(27, 1/4)
head(sim.tap, 3)
   n heads tails
1 27
               16 0.4074074
        11
2 27
               17 0.3703704
         10
3 27
               21 0.2222222
dotPlot(~prop, data = sim.tap, width = 1/27, cex = 3, groups = (prop <= 3/27))</pre>
```



3. Strength of evidence:

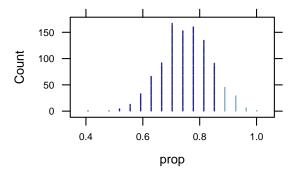
```
prop(~(prop <= 3/27), data = sim.tap)</pre>
TRUE
0.07
```

Alternate Analysis

1. H_0 : $\pi = 3/4$ H_a : $\pi > 3/4$

Test statistic: $\hat{p} = 0.889$ (the sample proportion of 24/27)

2. We simulate a world in which $\pi = 3/4$:



3. Strength of evidence:

```
prop(~(prop >= 24/27), data = sim.bottled)

TRUE
0.081
Exploration1.2.26b
```

1.3 Alternative Measure of Strength of Evidence

Example 1.3: Heart Transplant Operations

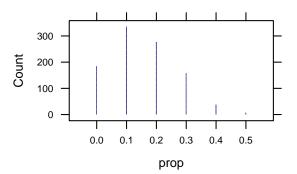
1. H_0 : $\pi = 0.15$

 H_a : $\pi > 0.15$

Test statistic: $\hat{p} = 0.80$ (the sample proportion of 8/10)

2. We simulate a world in which $\pi = 0.15$:

```
Figure1.10
sim.heart <- do(1000) * rflip(10, 0.15)
head(sim.heart, 3)
   n heads tails prop
1 10
              10 0.0
2 10
         3
               7 0.3
3 10
         1
               9 0.1
mean(~prop, data = sim.heart)
[1] 0.155
sd(~prop, data = sim.heart)
[1] 0.1116578
favstats(~prop, data = sim.heart)
 min Q1 median Q3 max mean
                                     sd
                                           n missing
            0.1 0.2 0.5 0.155 0.1116578 1000
dotPlot(~prop, data = sim.heart, width = 0.1, cex = 3, groups = (prop >= 8/10))
```



3. Strength of evidence:

```
prop(~(prop >= 8/10), data = sim.heart)
TRUE
0
```

Digging deeper into the St. George's mortality data

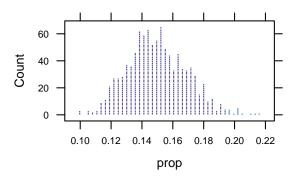
1. H_0 : $\pi = 0.15$

 H_a : $\pi > 0.15$

Test statistic: $\hat{p} = 0.197$ (the sample proportion of 71/361)

2. We simulate a world in which $\pi = 0.15$:

```
Figure1.11
sim.1986 \leftarrow do(1000) * rflip(361, 0.15)
head(sim.1986, 3)
    n heads tails
                        prop
      56 305 0.1551247
1 361
2 361
         54
             307 0.1495845
3 361
         44
            317 0.1218837
favstats(~prop, data = sim.1986)
                    01
                          median
        min
                                        Q3
                                                                               n missing
                                                  max
0.09972299\ 0.1357341\ 0.1495845\ 0.1634349\ 0.2160665\ 0.1498726\ 0.01907189\ 1000
dotPlot("prop, data = sim.1986, width = 1/361, groups = (prop >= 71/361))
```



3. Strength of evidence:

```
prop(~(prop >= 71/361), data = sim.1986)
TRUE
0.014
```

An alternative to the p-value: Standardized value of a statistic

R can be used as a calculator so we can compute the **z-score** manually:

```
z <- (71/361 - 0.15) / 0.018; z # z-score for sample size 361

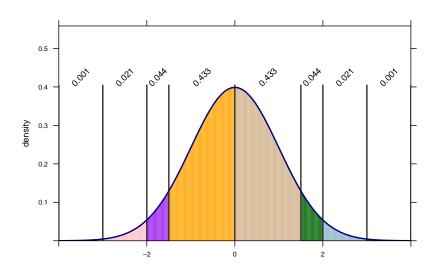
[1] 2.593106

z <- (8/10 - 0.15) / 0.113; z # z-score for sample size 10

[1] 5.752212
```

A very simple way to calculate the standardized statistic, find the p-value, and plot the bell-shaped curve is with the xpnorm() function. We'll examine xpnorm() in more detail later but for now, we just define a vector of quantiles (z-scores), mean, and sd.

```
Figure1.12
xpnorm(c(-3, -2, -1.5, 0, 1.5, 2, 3), mean = 0, sd = 1)
If X \sim N(0,1), then
P(X \le -3) = P(Z \le -3) = 0.0013
  P(X \le -2) = P(Z \le -2) = 0.0228
  P(X \le -1.5) = P(Z \le -1.5) = 0.0668
 P(X \le 0) = P(Z \le 0) = 0.5
 P(X \le 1.5) = P(Z \le 1.5) = 0.9332
 P(X \le 2) = P(Z \le 2) = 0.9772
  P(X \le 3) = P(Z \le 3) = 0.9987
P(X > -3) = P(Z > -3) = 0.9987
  P(X > -2) = P(Z > -2) = 0.9772
  P(X > -1.5) = P(Z > -1.5) = 0.9332
  P(X > 0) = P(Z > 0) = 0.5
  P(X > 1.5) = P(Z > 1.5) = 0.0668
  P(X > 2) = P(Z > 2) = 0.0228
  P(X > 3) = P(Z > 3) = 0.0013
[1] 0.001349898 0.022750132 0.066807201 0.500000000 0.933192799 0.977249868 0.998650102
```



In the example above, we input standardized values. However, we can input non-standardized statistics (observed statistic) with a new mean and sd in order to calculate the z-score.

```
xpnorm(71/361, mean = 0.15, sd = 0.018, plot = FALSE)
If X ~ N(0.15,0.018), then
P(X <= 0.196675900277008) = P(Z <= 2.593) = 0.9952
P(X > 0.196675900277008) = P(Z > 2.593) = 0.0048
```

```
[1] 0.9952443

xpnorm(8/10, mean = 0.15, sd = 0.113, plot = FALSE)

If X ~ N(0.15,0.113), then

P(X <= 0.8) = P(Z <= 5.752) = 1
P(X > 0.8) = P(Z > 5.752) = 0
[1] 1
```

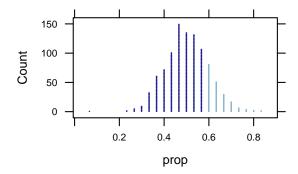
We'll ignore the p-values and plots for now and just realize that xpnorm() has computed the z-score for us so that we do not need to manually compute z by using R as a calculator.

Exploration 1.3: Do People Use Facial Prototyping?

1. H_0 : $\pi = 0.5$ H_a : $\pi > 0.5$

Test statistic: $\hat{p} = 0.6$ (the sample proportion of 18/30 for a fictitious class)

2. We simulate a world in which $\pi = 0.5$:



3. Strength of evidence:

```
prop(~(prop >= 18/30), data = sim.tim)
TRUE
0.191
```

```
mean(~prop, data = sim.tim)

[1] 0.5013667

sd <- sd(~prop, data = sim.tim)
sd # assign the standard deviation to sd

[1] 0.09525104

z <- (0.6 - 0.5)/sd
z # z-score using the assigned sd

[1] 1.049857
```

Again, we can input the observed statistic, mean, and standard deviation to xpnorm() for the standardized statistic:

```
 \begin{array}{l} \textbf{xpnorm}(0.6, \text{ mean = 0.5, sd = sd, plot = FALSE}) \\ \\ \textbf{If X} & N(0.5, 0.0952510395655401), \text{ then} \\ \\ P(X <= 0.6) &= P(Z <= 1.05) = 0.8531 \\ P(X > 0.6) &= P(Z > 1.05) = 0.1469 \\ \textbf{[1] 0.8531081} \\ \end{array}
```

1.4 What Impacts Strength of Evidence?

Example 1.4: Predicting Elections from Faces?

```
1. H_0: \pi=0.5 H_a: \pi>0.5 Test statistic: \hat{p}=0.719 (the sample proportion of 23/32)
```

2. We simulate a world in which $\pi = 0.5$:

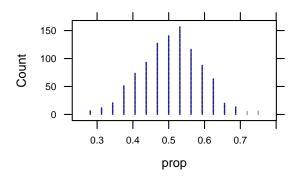
```
sim.senate <- do(1000) * rflip(32, 0.5)
head(sim.senate, 3)

n heads tails prop
1 32    15    17    0.46875
2 32    17    15    0.53125
3 32    18    14    0.56250

favstats(~prop, data = sim.senate)</pre>
Figure1.14
```

```
min Q1 median Q3 max mean sd n missing
0.28125 0.4375 0.5 0.5625 0.75 0.5064375 0.08466908 1000 0

dotPlot(~prop, data = sim.senate, groups = (prop >= 23/32), width = 1/32, cex = 3)
```



3. Strength of evidence:

```
prop(~(prop >= 23/32), data = sim.senate)

TRUE
0.011
```

Strength of evidence with the standardized statistic:

```
mean(~prop, data = sim.senate)

[1] 0.5064375

sd <- sd(~prop, data = sim.senate)

[1] 0.08466908

xpnorm(23/32, 0.5, sd, plot = FALSE)

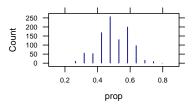
If X ~ N(0.5,0.0846690760915471), then

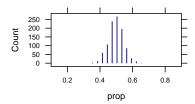
P(X <= 0.71875) = P(Z <= 2.584) = 0.9951
P(X > 0.71875) = P(Z > 2.584) = 0.0049
[1] 0.9951111
```

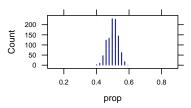
What impacts strength of evidence?

```
senate.32 <- do(1000) * rflip(32, 0.5)
dotPlot(~prop, data = senate.32, xlim = c(0.1, 0.9), cex = 5)
senate.128 <- do(1000) * rflip(128, 0.5)</pre>
```

```
dotPlot(~prop, data = senate.128, xlim = c(0.1, 0.9), cex = 5)
senate.256 <- do(1000) * rflip(256, 0.5)
dotPlot(~prop, data = senate.256, xlim = c(0.1, 0.9), cex = 5)</pre>
```







```
sd(~prop, data = senate.32)

[1] 0.09114295

sd(~prop, data = senate.128)

[1] 0.04479749

sd(~prop, data = senate.256)

[1] 0.03158375
```

```
prop(~(prop >= 23/32), data = senate.32)

TRUE
0.011

prop(~(prop >= 23/32), data = senate.128)

TRUE
0

prop(~(prop >= 23/32), data = senate.256)

TRUE
0
```

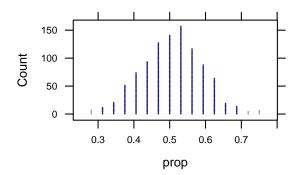
1. H_0 : $\pi = 0.5$

 H_a : $\pi \neq 0.5$

Test statistic: $\hat{p} = 0.719$ (the sample proportion of 23/32)

2. We use the simulated world in which $\pi = 0.5$:

```
dotPlot(~ prop, data = sim.senate, groups = (prop >= 23/32 | prop <= 9/32),
    width = 1/32, cex = 3)</pre>
```



Notice that because we are doing a two-sided test, we differentiate the samples with proportions greater than or equal to 23/32 and proportions less than or equal to 9/32 (the proportion that is as extreme as 23/32) by using the bar |.

3. Strength of evidence:

```
prop(~(prop <= 9/32 | prop >= 23/32), data = sim.senate)
TRUE
0.018
```

Follow-up Study

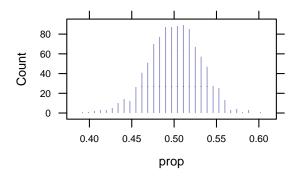
1. H_0 : $\pi = 0.5$

 H_a : $\pi \neq 0.5$

Test statistic: $\hat{p} = 0.677$ (the sample proportion of 189/279)

2. We simulate a world in which $\pi = 0.5$:

```
Figure1.17
sim.house <- do(1000) * rflip(279, 0.5)
head(sim.house, 3)
    n heads tails
             133 0.5232975
1 279
        146
2 279
        135
               144 0.4838710
3 279
        124
              155 0.4444444
favstats(~prop, data = sim.house)
                   01
                         median
                                         03
 0.3942652\ 0.4802867\ 0.5017921\ 0.5197133\ 0.5985663\ 0.5002939\ 0.0307716\ 1000
dotPlot(\ \tilde{p}rop, data = sim.house, groups = (prop >= 189/279 \mid prop <= 90/279), width = 0.007)
```



3. Strength of evidence:

```
prop(~(prop >= 189/279 | prop <= 90/279), data = sim.house)</pre>
TRUE
0
```

Strength of evidence with the standardized statistic:

```
mean(~prop, data = sim.house)

[1] 0.5002939

sd <- sd(~prop, data = sim.house)

sd

[1] 0.0307716

xpnorm(189/279, 0.5, sd, plot = FALSE)

If X ~ N(0.5,0.0307716025296676), then

P(X <= 0.67741935483871) = P(Z <= 5.766) = 1
P(X > 0.67741935483871) = P(Z > 5.766) = 0

[1] 1
```

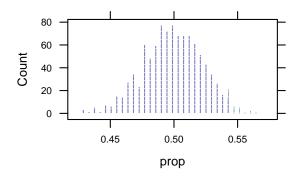
Exploration 1.4: Competitive Advantage to Uniform Colors?

```
1. H_0: \pi=0.5 H_a: \pi>0.5 Test statistic: \hat{p}=0.543 (the sample proportion of 248/457)
```

2. We simulate a world in which $\pi = 0.5$:

```
sim.red <- do(1000) * rflip(457, 0.5)
head(sim.red, 3)
```

```
n heads tails
                        prop
1 457
        239
              218 0.5229759
2 457
        230
              227 0.5032823
              222 0.5142232
3 457
        235
favstats(~prop, data = sim.red)
                  Q1
                                       Q3
       min
                         median
                                                max
                                                          mean
                                                                              n missing
0.4266958\ 0.4857768\ 0.5010941\ 0.5164114\ 0.5667396\ 0.5003173\ 0.02300691\ 1000
dotPlot(~prop, data = sim.red, groups = (prop >= 0.543), width = 2/457)
```



3. Strength of evidence:

```
prop(~(prop >= 0.543), data = sim.red)

TRUE
0.023
Exploration1.4.3b
```

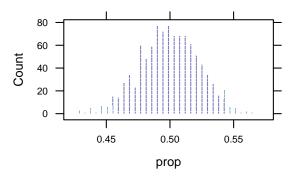
1. H_0 : $\pi = 0.5$

 H_a : $\pi \neq 0.5$

Test statistic: $\hat{p} = 0.543$ (the sample proportion of 248/457)

2. We use the simulated world in which $\pi = 0.5$ from the one-sided test:

```
\frac{\text{dotPlot}(\text{prop, data = sim.red, groups = (prop <= 0.457 | prop >= 0.543), width = 2/457)}{\text{Exploration1.4.5}}
```



3. Strength of evidence:

```
prop(~(prop <= 0.457 | prop >= 0.543), data = sim.red)

TRUE
0.053

Exploration1.4.5b
```

Difference between statistic and null hypothesis parameter value

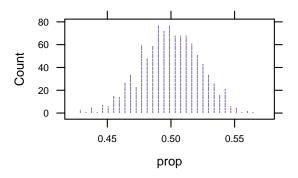
1. H_0 : $\pi = 0.5$

 H_a : $\pi > 0.5$

Test statistic: $\hat{p} = 0.57$ (the sample proportion)

2. We use the simulated world in which $\pi = 0.5$:

```
dotPlot(~prop, data = sim.red, groups = (prop >= 0.57), width = 2/457)
```



3. Strength of evidence:

```
prop(~(prop >= 0.57), data = sim.red)
TRUE
0
```

Sample size

1. H_0 : $\pi = 0.5$

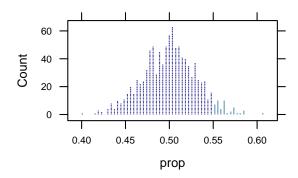
 H_a : $\pi > 0.5$

Test statistic: $\hat{p} = 0.551$ (the sample proportion of 150/272)

2. We simulate a world in which $\pi = 0.5$:

```
sim.box \leftarrow do(1000) * rflip(272, 0.5)

head(sim.box, 3)
```



3. Strength of evidence

```
prop(~(prop >= 0.551), data = sim.box)
TRUE
0.045
```

1.5 Inference on a single proportion: Theory-based approach

Example 1.5: Halloween Treats

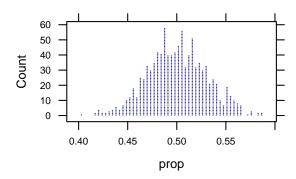
```
1. H_0: \pi = 0.5
H_a: \pi \neq 0.5
```

Test statistic: $\hat{p} = 0.523$ (the sample proportion of 148/283)

2. We simulate a world in which $\pi = 0.5$:

```
sim.candy <- do(1000) * rflip(283, 0.5)
head(sim.candy, 3)

n heads tails prop
1 283 130 153 0.4593640
2 283 137 146 0.4840989
3 283 148 135 0.5229682
```



Theory-based approach (One proportion z test)

Calculating predicted standard deviation:

```
mean <- 0.5

n <- 283

sd <- sqrt(mean * (1 - mean)/n)

sd
```

Calculating z-score:

```
Z <- (0.523 - mean)/sd

Z [1] 0.7738398

xpnorm(148/283, 0.5, sd, plot = FALSE)

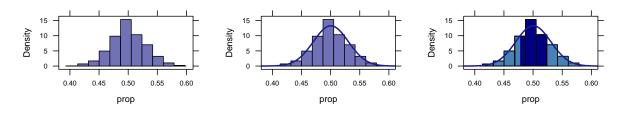
If X ~ N(0.5,0.0297219149138882), then

P(X <= 0.522968197879859) = P(Z <= 0.773) = 0.7802

P(X > 0.522968197879859) = P(Z > 0.773) = 0.2198

[1] 0.7801707
```

To overlay a normal approximation, let's graph a histogram using histogram() instead of a dotplot:



The two main functions we need for working with normal distributions are pnorm() and qnorm(). pnorm() computes the proportion of a normal distribution below a specified value:

```
pnorm(x,mean=\mu, sd=\sigma) = Pr(X \le x)
```

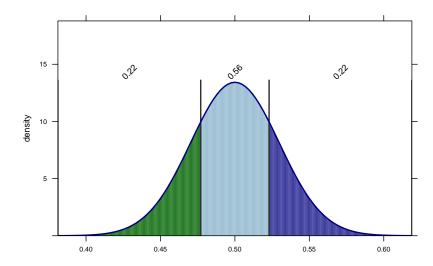
when $X \sim \text{Norm}(\mu, \sigma)$.

We can obtain arbitrary probabilities using pnorm() We can now examine the rest of the output from xpnorm(), which is an augmented version of pnorm(). Because it's a two-sided test, we can input both the observed statistic (148/283) and the statistic that is as extreme as the observed (135/283).

```
xpnorm(c(135/283, 148/283), 0.5, sd)

If X ~ N(0.5,0.0297219149138882), then

P(X <= 0.477031802120141) = P(Z <= -0.773) = 0.2198
   P(X <= 0.522968197879859) = P(Z <= 0.773) = 0.7802
P(X > 0.477031802120141) = P(Z > -0.773) = 0.7802
   P(X > 0.522968197879859) = P(Z > 0.773) = 0.7802
   P(X > 0.522968197879859) = P(Z > 0.773) = 0.2198
[1] 0.2198293 0.7801707
```



The output gives the z-scores for both statistics and the p-value. We know now that this p-value is found using the predicted standard deviation and normal approximation. The p-value for the two-sided test is the sum of $P(Z \le -0.773)$ and P(Z > 0.773).

We can also use the just observed statistic as we have done before but only we will need to change the lower.tail to FALSE.

```
xpnorm(148/283, 0.5, sd, lower.tail = FALSE, plot = FALSE)

If X ~ N(0.5,0.0297219149138882), then

P(X <= 0.522968197879859) = P(Z <= 0.773) = 0.7802
P(X > 0.522968197879859) = P(Z > 0.773) = 0.2198
[1] 0.2198293

2 * xpnorm(148/283, 0.5, sd, lower.tail = FALSE, plot = FALSE)

If X ~ N(0.5,0.0297219149138882), then

P(X <= 0.522968197879859) = P(Z <= 0.773) = 0.7802
P(X > 0.522968197879859) = P(Z > 0.773) = 0.2198
[1] 0.4396586
```

This results in the p-value of the alternative hypothsis that π is greater than the observed statistic (the default is the alternative hypothsis that π is less than the observed statistic). For the two-sided test, we have multiplied the resulting p-value by two.

The function pnorm() can be used just to find the p-value:

```
2 * pnorm(148/283, 0.5, sd, lower.tail = FALSE)

[1] 0.4396586
```

Further, we can input the standardized statistic (z-score) to find the p-value:

```
2 * pnorm(z, 0, 1, lower.tail = FALSE)

[1] 0.4390255
```

The most convenient way to find the p-value for a proportion using normal approximation is to use prop. test() by inputing the number of sucesses and the number of samples:

```
prop.test(148, n = 283)

1-sample proportions test with continuity correction

data: 148 out of 283

X-squared = 0.50883, df = 1, p-value = 0.4756
alternative hypothesis: true p is not equal to 0.5

95 percent confidence interval:
    0.4631063 0.5821963

sample estimates:
    p
0.5229682
```

Note that the default for the prop test is with a $\pi = 0.5$, two-sided test, and a continuity correction. The continuity correction results in a more accurate p-value but if you want the p-value found with pnorm() we can change the default.

```
prop.test(148, 283, correct = FALSE)

1-sample proportions test without continuity correction

data: 148 out of 283

X-squared = 0.59717, df = 1, p-value = 0.4397
alternative hypothesis: true p is not equal to 0.5

95 percent confidence interval:
    0.4648584 0.5804628

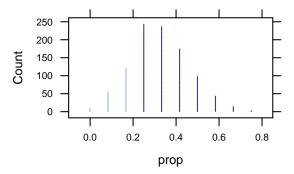
sample estimates:
    p
0.5229682
```

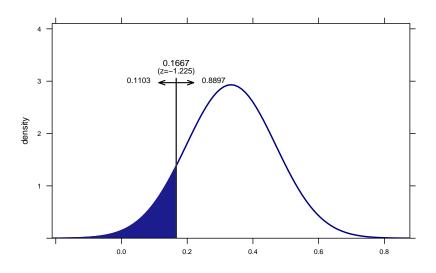
A situation where a theory-based approach doesn't work

```
mean <- 1/3
n <- 12
sd <- sqrt(mean * (1 - mean)/n)
sd
```

```
[1] 0.1360828
```

```
dotPlot(~prop, data = sim.sci, group = (prop <= 1/6), width = 1/12, cex = 3)
prop(~(prop <= 1/6), data = sim.sci)</pre>
TRUE
0.184
```





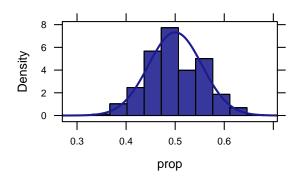
Exploration 1.5: Calling Heads or Tails

```
1. H_0: \pi = 0.5
H_a: \pi > 0.5
```

Test statistic: $\hat{p} = 0.651$ (the sample proportion of 54/83)

2. We simulate a world in which $\pi = 0.5$:

```
Exploration1.5.5
sim.heads <- do(1000) * rflip(83, 0.5)
head(sim.heads, 3)
   n heads tails
       37 46 0.4457831
2 83
        42
             41 0.5060241
3 83
        43
            40 0.5180723
favstats(~prop, data = sim.heads)
                                                                           n missing
                 01
                       median
                                     Q3
                                                       mean
                                                                    sd
      min
                                              max
 0.313253 0.4578313 0.4939759 0.5421687 0.6626506 0.5001084 0.05449511 1000
histogram(~prop, data = sim.heads, groups = (prop >= 54/83), fit = "normal")
```



3. Strength of evidence

```
prop(~(prop >= 54/83), data = sim.heads)

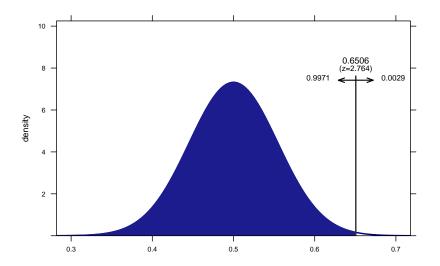
TRUE
0.002
Exploration1.5.5b
```

Normal approximation using simulated sd:

```
sd <- sd(~prop, data = sim.heads)
xpnorm(54/83, 0.5, sd, lower.tail = FALSE)

If X ~ N(0.5,0.0544951058293514), then

P(X <= 0.650602409638554) = P(Z <= 2.764) = 0.9971
P(X > 0.650602409638554) = P(Z > 2.764) = 0.0029
[1] 0.002858421
```



Formulas

```
sd <- sqrt(0.5 * (1 - 0.5)/83)
sd
```

Follow-up Analysis #1

1. H_0 : $\pi = 0.5$ H_a : $\pi \neq 0.5$ Test statistic: $\hat{p} = 0.70$ (the sample proportion)

2. Normal approximation using predicted sd:

```
sd <- sqrt(0.5 * (1 - 0.5)/83)

sd

[1] 0.05488213

2 * xpnorm(0.7, 0.5, sd, plot = FALSE, lower.tail = FALSE)

If X ~ N(0.5,0.0548821299948452), then

P(X <= 0.7) = P(Z <= 3.644) = 0.9999

P(X > 0.7) = P(Z > 3.644) = 1e-04

[1] 0.0002682525
```

Approximate test for proportions without continuity correction:

```
prop.test(58.1, 83, correct = FALSE) # 58.1 = 0.70 * 83
1-sample proportions test without continuity correction

data: 58.1 out of 83
X-squared = 13.28, df = 1, p-value = 0.0002683
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
    0.5943661 0.7879397
sample estimates:
    p
0.7
```

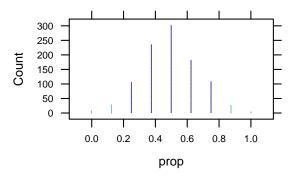
Follow-up Analysis # 2

```
1. H_0: \pi = 0.5

H_a: \pi \neq 0.5

Test statistic: \hat{p} = 0.875 (the sample proportion of 7/8)
```

2. We simulate a world in which $\pi = 0.5$:



3. Strength of evidence:

```
prop(~(prop <= 0.125 | prop >= 0.875), data = sim.small)
TRUE
0.065
```

Approximate test for proportions without continuity correction:

```
prop.test(7, 8, correct = FALSE)

1-sample proportions test without continuity correction

data: 7 out of 8
X-squared = 4.5, df = 1, p-value = 0.03389
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
    0.5291118    0.9775825
sample estimates:
    p
0.875
```

There is also another test that will compute the p-value for a proportion and that the binomial test. binom.test() utilizes a binomial probability distribution while prop.test() utilizes a normal probability distribution. The tests are similar but the binomial test will result in the most accurate p-value.

```
Exact binomial test (with Score CI)

data: 7 out of 8
number of successes = 7, number of trials = 8, p-value = 0.07031
alternative hypothesis: true probability of success is not equal to 0.5
95 percent confidence interval:
0.4734903 0.9968403
sample estimates:
probability of success
0.875
```

```
binom.test(58, 83)

Exact binomial test (with Score CI)

data: 58 out of 83
number of successes = 58, number of trials = 83, p-value = 0.0003783
alternative hypothesis: true probability of success is not equal to 0.5

95 percent confidence interval:
    0.5882227 0.7946876
sample estimates:
probability of success
    0.6987952
```

2

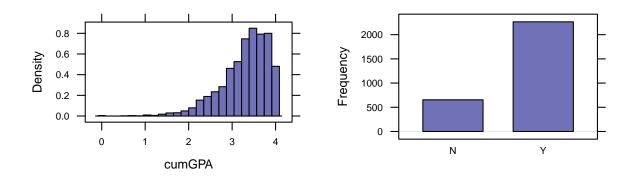
Generalization: How Broadly Do the Results Apply?

2.1 Sampling from a Finite Population

Example 2.1A: Sampling Students

In chapter one, we used **histograms** a few times instead of dotplots and changed their widths. You can also control the number of bins by defining nint, or n for short.

```
histogram(~cumGPA, data = CollegeMidwest, n = 24)
bargraph(~onCampus, data = CollegeMidwest)
```



Simple Random Samples

For a **simple random sample** of a data set, we use sample() and define the size of the same we want.

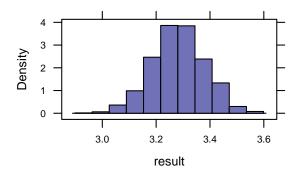
```
Table2.2
sample1 <- sample(CollegeMidwest, 30)</pre>
sample1
     onCampus cumGPA orig.ids
540
                  2.72
                              540
                  4.00
1803
              Υ
                             1803
2878
             Υ
                  3.41
                             2878
              N
                  3.63
425
                              425
              Υ
                             1707
1707
                  3.79
886
              Υ
                  3.81
                              886
2451
              Υ
                  2.85
                             2451
1954
             Ν
                  2.38
                             1954
2026
             Υ
                  3.50
                             2026
1156
              Υ
                  3.90
                             1156
2714
             Υ
                  3.89
                             2714
1885
             Ν
                  2.83
                             1885
832
              Υ
                  3.06
                              832
745
             Ν
                  3.58
                              745
470
             Ν
                  3.09
                              470
1650
              Υ
                  3.68
                             1650
1021
              Υ
                  3.52
                             1021
579
              Υ
                  2.84
                              579
2288
             Ν
                  3.76
                             2288
1083
              Υ
                  4.00
                             1083
1105
              Υ
                  2.66
                             1105
816
              Υ
                  3.57
                              816
1848
              Υ
                  3.09
                             1848
1804
              Υ
                  2.99
                             1804
568
             Ν
                  3.18
                              568
828
              Υ
                  3.33
                              828
                  2.89
193
              Υ
                              193
2245
             Ν
                  3.75
                             2245
2212
             Υ
                  3.49
                             2212
2230
                             2230
             Ν
                  2.76
sample2 <- sample(CollegeMidwest, 30)</pre>
sample3 <- sample(CollegeMidwest, 30)</pre>
```

```
sample4 <- sample(CollegeMidwest, 30)</pre>
sample5 <- sample(CollegeMidwest, 30)</pre>
                                                                                                    Table2.3
mean(~cumGPA, data = sample1)
[1] 3.331667
mean(~cumGPA, data = sample2)
[1] 3.449667
mean(~cumGPA, data = sample3)
[1] 3.325
mean(~cumGPA, data = sample4)
[1] 3.381333
mean(~cumGPA, data = sample5)
[1] 3.435667
prop(~onCampus, level = "Y", data = sample1)
0.7
prop(~onCampus, level = "Y", data = sample2)
 Υ
0.7
prop(~onCampus, level = "Y", data = sample3)
0.7333333
prop(~onCampus, level = "Y", data = sample4)
0.8333333
prop(~onCampus, level = "Y", data = sample5)
0.7666667
```

Notice the level in order to find the proportion of students who said "yes" instead of the default "no".

Similar to the simulation of random processes in chapter one, we can repeat taking different simple random samples. Conveniently, R will let you set data= to a simple random sample so we can repeat finding the mean or the proportion of a different simple random sample many times.

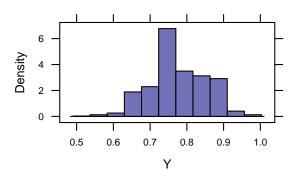
```
Figure 2.2
sample.gpa <- do(1000) * mean(cumGPA, data = sample(CollegeMidwest, 30))
head(sample.gpa)
    result
1 3.311667
2 3.388667
3 3.091333
4 3.116000
5 3.216667
6 3.238000
favstats(~result, data = sample.gpa)
      min
              01
                   median
                                 03
                                         max
                                                  mean
                                                                sd
                                                                      n missina
 2.950667 3.2175 3.282167 3.347833 3.587667 3.282172 0.09871397 1000
histogram(~result, data = sample.gpa)
```



```
sample.campus <- do(1000) * prop(~onCampus, level = "Y", data = sample(CollegeMidwest, 30))
head(sample.campus)

Y
1 0.7666667
2 0.8333333
3 0.9000000
4 0.5666667
5 0.8000000
6 0.9000000
favstats(~Y, data = sample.campus)</pre>
```

```
min Q1 median Q3 max mean sd n missing 0.5 0.7333333 0.7666667 0.8333333 0.9666667 0.7769 0.07483159 1000 0 histogram(~Y, data = sample.campus)
```



Exploration 2.1A: Sampling Words

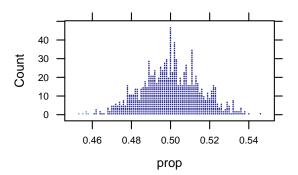
```
head(GettysburgAddress)
   word
  Four
2 score
3
    and
4 seven
5 years
    ago
Words <- sample(GettysburgAddress, 10)</pre>
Words %>% mutate(length = nchar(word))
        word orig.ids length
                  243
1
                            3
         God
2
                   57
                             3
         met
3
         are
                    33
4
         Now
                    31
5
      nation
                   241
                             6
6
                    97
                             6
      proper
7
                   246
8
                   167
                             6
      rather
9
                    62
                             2
10 conceived
```

Example 2.1B: Should Supersize Drinks be Banned?

```
1. H_0: \pi=0.5 H_a: \pi<0.5 Test statistic: \hat{p}=0.46 (the sample proportion of 503/1093)
```

2. We simulate a world in which $\pi = 0.5$:

```
Figure 2.3
sim.ban <- do(1000) * rflip(1093, 0.5)
head(sim.ban, 3)
     n heads tails
                         prop
         547
               546 0.5004575
1 1093
2 1093
         560
               533 0.5123513
3 1093
               540 0.5059469
         553
favstats(~prop, data = sim.ban)
      min
                 01
                       median
                                      Q3
                                                max
                                                         mean
                                                                              n missing
0.452882\ 0.4903934\ 0.5004575\ 0.5105215\ 0.5462031\ 0.5001372\ 0.01511847\ 1000
dotPlot(~prop, data = sim.ban, groups = (prop <= 0.46), width = 0.001)</pre>
```



3. Strength of evidence:

```
prop(~(prop <= 0.46), data = sim.ban)</pre>
TRUE
0.005
```

Normal approximation using predicted standard deviation:

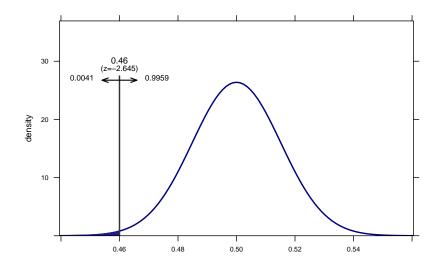
```
sd <- sqrt(0.5 * (1 - 0.5)/1093)
sd

[1] 0.01512377

xpnorm(0.46, 0.5, sd)

If X ~ N(0.5,0.0151237651004726), then

P(X <= 0.46) = P(Z <= -2.645) = 0.0041
P(X > 0.46) = P(Z > -2.645) = 0.9959
[1] 0.004086429
```



Approximate test for proportions with continuity correction:

Exact test for proportions:

```
binom.test(503, 1093, alt = "less")

Exact binomial test (with Score CI)

data: 503 out of 1093
number of successes = 503, number of trials = 1093, p-value = 0.004628
alternative hypothesis: true probability of success is less than 0.5

95 percent confidence interval:
    0.0000000   0.4855139
sample estimates:
probability of success
    0.4602013
```

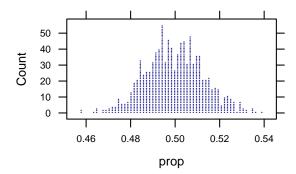
Exploration 2.1B: Banning Smoking in Cars?

```
1. H_0: \pi = 0.5
H_a: \pi > 0.5
```

Test statistic: $\hat{p} = 0.55$ (the sample proportion)

2. We simulate a world in which $\pi = 0.5$:

```
Exploration 2.1B.10
sim.smoke <- do(1000) * rflip(1421, 0.5)
head(sim.smoke, 3)
     n heads tails
                         prop
               694 0.5116115
1 1421
         727
2 1421
         706
                715 0.4968332
3 1421
               715 0.4968332
         706
favstats(~prop, data = sim.smoke)
                   01
                         median
                                        Q3
                                                                             n missing
       min
                                                max
                                                         mean
                                                                       sd
 0.4574243\ 0.4912034\ 0.4996481\ 0.5087966\ 0.539057\ 0.499912\ 0.01304541\ 1000
dotPlot(~prop, data = sim.smoke, groups = (prop >= 0.55), width = 0.0014)
```



3. Strength of evidence:

```
prop(~(prop >= 0.55), data = sim.smoke)
TRUE
0
```

Normal approximation using predicted standard deviation:

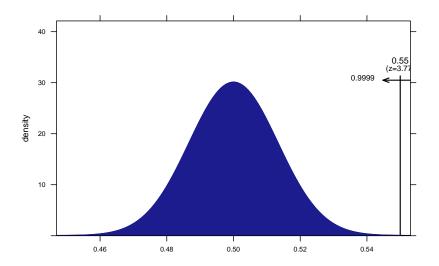
```
sd <- sqrt(0.5 * (1 - 0.5)/1421)
sd

[1] 0.01326395

xpnorm(0.55, 0.5, sd, lower.tail = FALSE)

If X ~ N(0.5,0.0132639527269323), then

P(X <= 0.55) = P(Z <= 3.77) = 0.9999
P(X > 0.55) = P(Z > 3.77) = 1e-04
[1] 8.174966e-05
```



Approximate test for proportions with continuity correction:

```
prop.test(782, 1421, alt = "greater") # 782 = 1421 * 0.55

1-sample proportions test with continuity correction

data: 782 out of 1421

X-squared = 14.19, df = 1, p-value = 8.262e-05
alternative hypothesis: true p is greater than 0.5
95 percent confidence interval:
0.5281822 1.0000000

sample estimates:

p
0.5503167
```

Exact test for proportions:

```
binom.test(782, 1421, alt = "greater")

Exact binomial test (with Score CI)

data: 782 out of 1421
number of successes = 782, number of trials = 1421, p-value = 8.166e-05
alternative hypothesis: true probability of success is greater than 0.5

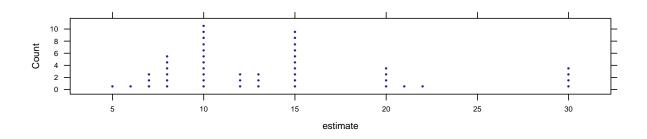
95 percent confidence interval:
0.5281957 1.0000000

sample estimates:
probability of success
0.5503167
```

2.2 Inference for a Single Quantitative Variable

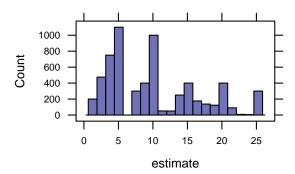
Example 2.2: Estimating Elapsed Time

```
head(TimeEstimate)
  estimate
        10
2
        12
3
         6
4
        13
5
        15
        10
favstats(~estimate, data = TimeEstimate)
 min Q1 median Q3 max
                          mean
                                     sd n missing
   5 10 12 15 30 13.70833 6.500273 48
dotPlot(~estimate, data = TimeEstimate, width = 1, cex = 0.5)
```

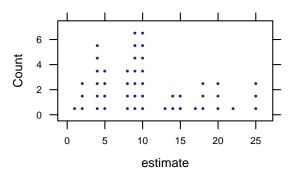


```
Table2.5
TimeEstimate %>% mutate(Rank = rank(estimate, ties.method = "random")) %>% arrange(Rank)
   estimate Rank
1
           5
2
           6
                2
3
           7
                3
4
                4
5
                5
6
                6
           8
7
           8
                7
8
           8
                8
9
           8
                9
10
           8
               10
           8
               11
11
12
          10
               12
          10
13
               13
14
          10
               14
15
          10
               15
16
          10
               16
17
          10
               17
          10
               18
18
19
          10
               19
20
          10
               20
21
          10
               21
22
          10
               22
```

```
23
       12 23
24
       12 24
25
       12 25
26
       13 26
27
       13 27
28
       13 28
29
       15 29
30
       15 30
31
       15 31
       15 32
32
33
       15
           33
34
       15
           34
35
       15
           35
36
       15
           36
37
       15 37
38
       15 38
39
       20 39
40
       20 40
41
       20 41
42
       20 42
43
       21 43
       22 44
44
       30 45
45
       30 46
46
47
       30
           47
48
       30 48
```



```
Figure 2.7
sample1 <- sample(TimePopulation, 48)</pre>
head(sample1, 3)
     estimate orig.ids
5599
            2
                   5599
308
            4
                    308
5006
           20
                   5006
favstats(~estimate, data = sample1)
 min Q1 median Q3 max
                           mean
                                       sd n missing
             9 15 25 10.72917 6.584119 48
dotPlot("estimate, data = sample1, width = 1, cex = 0.3)
```

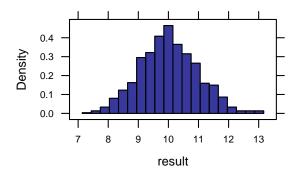


```
1. H_0: \mu = 10
H_a: \mu \neq 10
```

Test statistic: $\bar{x} = 13.71$ (the sample mean)

2. We simulate random samples from a finite population:

```
sim.time <- do(1000) * mean(~estimate, data = sample(TimePopulation, 48))
head(sim.time, 3)</pre>
```



3. Strength of evidence:

```
prop(~(result <= 6.29 | result >= 13.71), data = sim.time)

TRUE
   0
```

Strength of evidence with the standardized statistic:

```
mean(~result, data = sim.time)

[1] 10.02562

sd <- sd(~result, data = sim.time)
sd

[1] 0.9602245

xpnorm(13.71, 10, sd, lower.tail = FALSE, plot = FALSE)

If X ~ N(10,0.960224460941498), then

P(X <= 13.71) = P(Z <= 3.864) = 0.9999
P(X > 13.71) = P(Z > 3.864) = 1e-04
[1] 5.584577e-05
```

Theory-based approach: One-sample t-test

```
xbar <- 13.71

mu <- 10

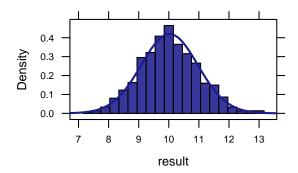
s <- 6.5

n <- 48

t <- (xbar - mu)/(s/sqrt(n))

t
```

```
histogram(~result, data = sim.time, groups = (result <= 6.29 | result >= 13.71), nint = 20,
center = 10, fit = "t")
```



```
2 * pt(t, df = 47, lower.tail = FALSE)

[1] 0.0002570976
```

Alternative Analysis: What about the median?

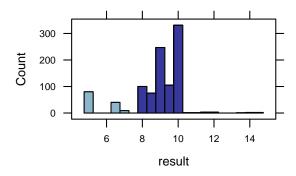
```
sim.median <- do(1000) * median(~estimate, data = sample(TimePopulation, 48))
head(sim.median, 3)

result
1    9.5
2    8.0
3    10.0

histogram(~result, data = sim.median, groups = (result < 8 | result > 12), width = 0.5, type = "count")
prop(~(result < 8 | result > 12), data = sim.median)

target level: TRUE; other levels: FALSE

TRUE
0.134
```



Exploration 2.2: Sleepless Nights?

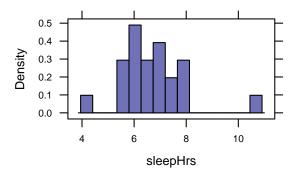
```
head(SleepTimes, 3)

sleepHrs
1 7.0
2 5.5
3 8.0
```

Shape

```
histogram(~sleepHrs, data = SleepTimes, nint = 15)

Exploration2.2.10
```



Center

```
mean(~sleepHrs, data = SleepTimes)
[1] 6.704545
```

```
median(~sleepHrs, data = SleepTimes)
[1] 6.5
```

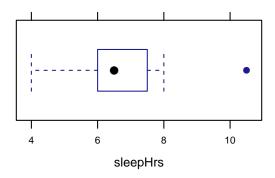
Variability

```
sd(~sleepHrs, data = SleepTimes)
[1] 1.297058
```

Unusual observations

We could examine the entire data set to find any outliers, but there is a quicker way to see if there potential outliers. The bwplot() function plots a box-and-whisker plot which identifies *possible* outliers with a dot beyond the whiskers.

```
bwplot(~sleepHrs, data = SleepTimes)
```

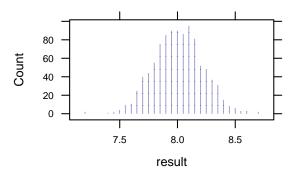


Instead of using the hypothetical population provided in the applet, we can create our own hypothetical population by assigning a variable (sleepHrs) a random normal distribution (rnorm()) of count (18000), mean (8 hrs), and standard deviation (1.5 hrs). Additionally, let's round each value to the nearest hundredth (2) using round()

```
Pop1 <- data.frame(sleepHrs = round(rnorm(18000, 8, 1.5), 2))
head(Pop1)

sleepHrs
1 6.10
2 7.27
3 10.84
```

```
Exploration2.2.25
mean(~sleepHrs, data = SleepTimes) # test statistic
[1] 6.704545
sim.pop1 \leftarrow do(1000) * mean(~sleepHrs, data = sample(Pop1, 48))
head(sim.pop1, 3)
    result
1 8.248125
2 8.114792
3 7.731250
dotPlot(~result, data = sim.pop1, width = 0.05)
favstats(~result, data = sim.pop1)
               01 median
                                  Q3
     min
                                           max
                                                   mean
                                                               sd
                                                                     n missing
7.20125 7.862604 8.004062 8.142708 8.694583 8.006431 0.2112868 1000
```



```
prop(~(result <= 6.705), data = sim.pop1)</pre>
TRUE
0
```

```
Exploration2.2.27

sd <- sd(~result, data = sim.pop1)
xpnorm(6.705, 8, sd, plot = FALSE)

If X ~ N(8,0.211286837881223), then

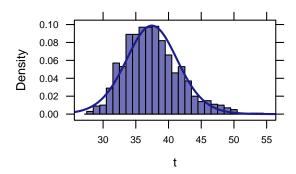
P(X <= 6.705) = P(Z <= -6.129) = 0
P(X > 6.705) = P(Z > -6.129) = 1
[1] 4.418636e-10
```

```
t <- (6.705 - 8)/(1.5/sqrt(48))
t

[1] -5.981349
```

```
sim.t <- do(1000) * stat(t.test(~sleepHrs, data = sample(Pop1, 48)))
head(sim.t, 3)

t
1 36.77293
2 48.02783
3 33.31042
histogram(~t, data = sim.t, width = 1, fit = "t")</pre>
```



```
prop(~(t <= 5.981), data = sim.t)</pre>
TRUE
0
```

```
t.test(~sleepHrs, data = Pop1)

One Sample t-test

data: data$sleepHrs

t = 715.65, df = 17999, p-value < 2.2e-16

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

7.987704 8.031579

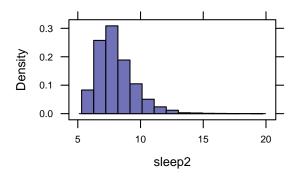
sample estimates:

mean of x

8.009642
```

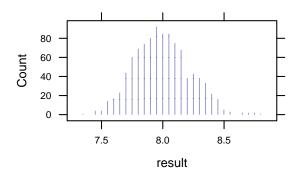
Follow-up # 1

```
Exploration2.2.40
head(Pop)
  sleep1 sleep2 sleep3
   6.50
          8.50
                 5.00
2
    6.00
         10.00
                 4.75
3
   6.00
           6.75
                  2.75
   6.75
          10.00
                 4.50
5
    9.00
           7.75
                 14.00
   7.75
           7.00
                10.25
favstats(~sleep2, data = Pop)
 min Q1 median Q3 max
                             mean
                                               n missing
                                        sd
   6 7 7.75 8.75 19.5 7.999458 1.501079 18000
histogram(~sleep2, data = Pop)
```



```
mean(~sleepHrs, data = SleepTimes) # test statistic
Exploration2.2.40b
```

```
[1] 6.704545
sim.pop2 \leftarrow do(1000) * mean(~sleep2, data = sample(Pop, 48))
head(sim.pop2, 3)
    result
1 7.947917
2 8.088542
3 7.890625
dotPlot(~result, data = sim.pop2, width = 0.05)
favstats(~result, data = sim.pop2)
                Q1 median
                                   Q3
                                           max
                                                   mean
                                                                sd
 7.369792 7.838542 7.984375 8.145833 8.822917 7.997401 0.2252886 1000
prop("(result <= 6.705)), data = sim.pop2)
TRUE
0
```



```
t.test(~sleep2, data = Pop)

One Sample t-test

data: data$sleep2
t = 714.98, df = 17999, p-value < 2.2e-16
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
7.977528 8.021389
sample estimates:
mean of x
7.999458</pre>
```

Follow-up # 2

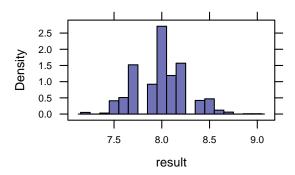
```
median(~sleepHrs, data = SleepTimes) # test statistic

[1] 6.5

sim.pop1med <- do(1000) * median(~sleep1, data = sample(Pop, 48))
head(sim.pop1med, 3)

result
1  8.25
2  8.00
3  7.75

histogram(~result, data = sim.pop1med, width = 0.1)
prop(~(result <= 6.5), data = sim.pop1med)</pre>
TRUE
0
```



2.3 Errors and Significance

Exploration 2.3: Parapsychology Studies

1. H_0 : $\pi = 0.25$ H_a : $\pi > 0.25$

Test statistic: $\hat{p} = 0.333$ (the sample proportion of 709/2124)

2. We simulate a world in which $\pi = 0.25$:

```
sim.esp <- do(1000) * rflip(2124, 0.25)
head(sim.esp, 3)

n heads tails prop
1 2124 562 1562 0.2645951
2 2124 536 1588 0.2523540
3 2124 582 1542 0.2740113
```

3. Strength of evidence:

```
prop(~(prop >= 0.333), data = sim.esp)
TRUE
0
```

Approximate test for proportions:

```
prop.test(709, 2124, p = 0.25, alt = "greater")

1-sample proportions test with continuity correction

data: 709 out of 2124
X-squared = 79.112, df = 1, p-value < 2.2e-16
alternative hypothesis: true p is greater than 0.25
95 percent confidence interval:
    0.3169623 1.0000000
sample estimates:
    p
0.3338041</pre>
```

Approximate test for $\hat{p} = 15/50$ if $\pi = 0.25$:

```
prop.test(15, 50, p = 0.25, alt = "greater")

1-sample proportions test with continuity correction

data: 15 out of 50
X-squared = 0.42667, df = 1, p-value = 0.2568
alternative hypothesis: true p is greater than 0.25
95 percent confidence interval:
    0.1974083 1.0000000
sample estimates:
    p
0.3
```

Approximate test for $\hat{p} = 15/50$ if $\pi = 0.33$:

```
prop.test(15, 50, p = 0.33, alt = "greater")

1-sample proportions test with continuity correction

data: 15 out of 50

X-squared = 0.090457, df = 1, p-value = 0.6182
alternative hypothesis: true p is greater than 0.33

95 percent confidence interval:
```

```
0.1974083 1.0000000
sample estimates:
    p
0.3
```



Estimation: How Large is the Effect?

3.1 Statistical Inference - Confidence Intervals

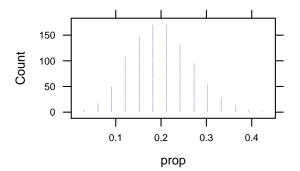
Example 3.1: Can Dogs Sniff Out Cancer?

```
1. H_0: \pi = 0.20

H_a: \pi > 0.20

Test statistic: \hat{p} = 0.909 (the sample proportion of 30/33)
```

2. We simulate a world in which $\pi = 0.20$:



3. Strength of evidence:

1. H_0 : $\pi = 0.70$

 H_a : $\pi \neq 0.70$

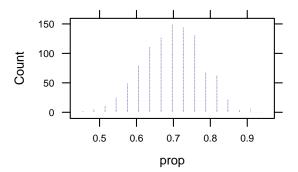
Test statistic: $\hat{p} = 0.909$ (the sample proportion of 30/33)

2. We simulate a world in which $\pi = 0.70$:

```
sim.cancer2 <- do(1000) * rflip(33, 0.7)
head(sim.cancer2, 3)

n heads tails    prop
1 33     25     8 0.7575758
2 33     18     15 0.5454545
3 33     22     11 0.6666667

dotPlot(~prop, data = sim.cancer2, groups = (prop <= 0.4545 | prop >= 0.909), width = 0.001)
```



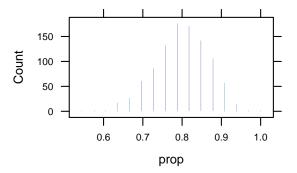
3. Strength of evidence:

```
1. H_0: \pi = 0.80

H_a: \pi \neq 0.80

Test statistic: \hat{p} = 0.909 (the sample proportion of 30/33)
```

2. We simulate a world in which $\pi = 0.80$:



3. Strength of evidence:

Results of testing different values of probabilities under the null hypothesis:

```
pval(binom.test(30, 33, p = 0.93))

p.value
0.500728

pval(binom.test(30, 33, p = 0.94))
```

```
p.value
0.4474364
pval(binom.test(30, 33, p = 0.95))
 p.value
0.2271931
pval(binom.test(30, 33, p = 0.96))
  p.value
0.1442113
pval(binom.test(30, 33, p = 0.97))
  p.value
0.0756354
pval(binom.test(30, 33, p = 0.98))
   p.value
0.02792949
pval(binom.test(30, 33, p = 0.99))
    p.value
0.004360339
```

Exploration 3.1: Kissing Right?

```
1. H_0: \pi = 0.5
H_a: \pi > 0.5
```

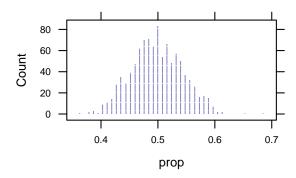
Test statistic: $\hat{p} = 0.645$ (the sample proportion of 80/124)

2. We simulate a world in which $\pi = 0.5$:

```
sim.kiss <- do(1000) * rflip(124, 0.5)
head(sim.kiss, 3)

n heads tails    prop
1 124    60    64 0.4838710
2 124    61    63 0.4919355
3 124    70    54 0.5645161

dotPlot(~prop, data = sim.kiss, groups = (prop >= 0.645), width = 0.001)
```



3. Strength of evidence:

Approximate test for proportions:

```
prop.test(80, 124, alt = "greater")

1-sample proportions test with continuity correction

data: 80 out of 124

X-squared = 9.879, df = 1, p-value = 0.0008359
alternative hypothesis: true p is greater than 0.5
95 percent confidence interval:
0.5679583 1.0000000
sample estimates:

p
0.6451613
```

Exact test for proportions:

```
binom.test(80, 124, alt = "greater")

Exact binomial test (with Score CI)

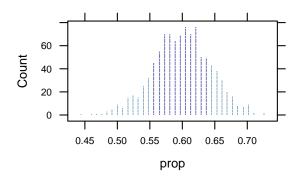
data: 80 out of 124
number of successes = 80, number of trials = 124, p-value = 0.0007824
alternative hypothesis: true probability of success is greater than 0.5
95 percent confidence interval:
0.5683679 1.0000000
sample estimates:
probability of success
0.6451613
```

1. H_0 : $\pi = 0.6$

 H_a : $\pi \neq 0.6$

Test statistic: $\hat{p} = 0.645$ (the sample proportion of 80/124)

2. We simulate a world in which $\pi = 0.6$:



3. Strength of evidence:

Approximate test for proportions:

```
prop.test(80, 124, p = 0.6)

1-sample proportions test with continuity correction

data: 80 out of 124

X-squared = 0.87399, df = 1, p-value = 0.3499
alternative hypothesis: true p is not equal to 0.6

95 percent confidence interval:
0.5536318 0.7275562
```

```
sample estimates:
    p
0.6451613
```

Exact test for proportions:

```
binom.test(80, 124, p = 0.6)

Exact binomial test (with Score CI)

data: 80 out of 124
number of successes = 80, number of trials = 124, p-value = 0.3151
alternative hypothesis: true probability of success is not equal to 0.6

95 percent confidence interval:
0.5542296 0.7289832
sample estimates:
probability of success
0.6451613
```

```
Exploration3.1.11
pval(binom.test(80, 124, p = 0.54))
   p.value
0.01914928
pval(binom.test(80, 124, p = 0.55))
   p.value
0.03756733
pval(binom.test(80, 124, p = 0.56))
   p.value
0.05778438
pval(binom.test(80, 124, p = 0.57))
  p.value
0.1023575
pval(binom.test(80, 124, p = 0.58))
 p.value
0.1464801
pval(binom.test(80, 124, p = 0.59))
 p.value
0.2354593
```

```
pval(binom.test(80, 124, p = 0.6))

p.value
0.3150598
```

```
Exploration3.1.11b
pval(binom.test(80, 124, p = 0.7))
  p.value
0.2023599
pval(binom.test(80, 124, p = 0.71))
 p.value
0.1139799
pval(binom.test(80, 124, p = 0.72))
   p.value
0.07145753
pval(binom.test(80, 124, p = 0.73))
   p.value
0.04242023
pval(binom.test(80, 124, p = 0.74))
   p.value
0.01849757
pval(binom.test(80, 124, p = 0.75))
    p.value
0.009268747
pval(binom.test(80, 124, p = 0.76))
    p.value
0.004281263
```

3.2 2SD and Theory-Based Confidence Intervals for a Single Proportion

Example 3.2: The Afforable Care Act

An easy way to find a confidence interval in R is to use prop.test() or binom.test() which by default calculates a 95% confidence interval in its results.

```
binom.test(713, 1034) # 713 = 1034 * 0.69

Exact binomial test (with Score CI)

data: 713 out of 1034
number of successes = 713, number of trials = 1034, p-value < 2.2e-16
alternative hypothesis: true probability of success is not equal to 0.5
95 percent confidence interval:
0.6603601 0.7176665
sample estimates:
probability of success
0.6895551
```

Theory-Based Approach

```
xpnorm(c(-1.645, 1.645), 0, 1)
If X ~ N(0,1), then

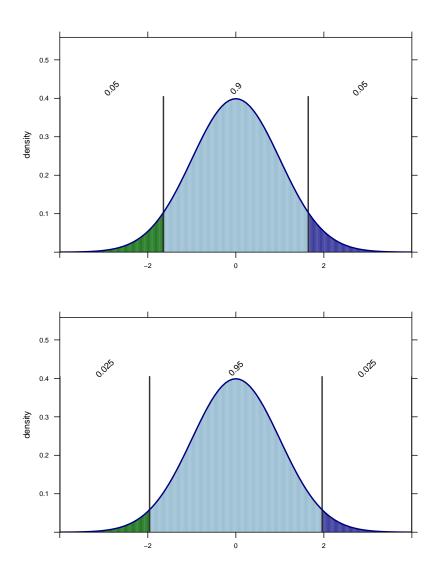
P(X <= -1.645) = P(Z <= -1.645) = 0.05
  P(X <= 1.645) = P(Z <= 1.645) = 0.95
  P(X > -1.645) = P(Z > -1.645) = 0.95
  P(X > 1.645) = P(Z > 1.645) = 0.05
[1] 0.04998491 0.95001509

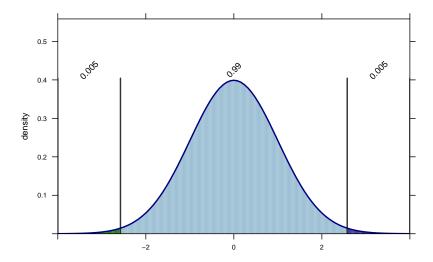
xpnorm(c(-1.96, 1.96), 0, 1)
```

```
If X = N(0,1), then

P(X <= -1.96) = P(Z <= -1.96) = 0.025
P(X <= 1.96) = P(Z <= 1.96) = 0.975
P(X > -1.96) = P(Z > -1.96) = 0.975
P(X > 1.96) = P(Z > 1.96) = 0.025
[1] \ 0.0249979 \ 0.9750021
xpnorm(c(-2.576, 2.576), 0, 1)

If X = N(0,1), then
P(X <= -2.576) = P(Z <= -2.576) = 0.005
P(X <= 2.576) = P(Z <= 2.576) = 0.995
P(X > -2.576) = P(Z > -2.576) = 0.995
P(X > 2.576) = P(Z > 2.576) = 0.995
P(X > 2.576) = P(Z > 2.576) = 0.005
[1] \ 0.004997532 \ 0.995002468
```





Using 2SD method and standard error of the observed sample proportion (Theory-Based Inference applet):

```
| Tigure 3.7 | No. 1034 | Public 2 | Public 2 | Public 2 | Public 3 | Public 3 | Public 3 | Public 4 | Public
```

Exploration 3.2: American Exceptionalism

```
1. H_0: \pi=0.775 H_a: \pi\neq0.775 Test statistic: \hat{p}=0.80 (the sample proportion of 85/1019)
```

2. We simulate a world in which $\pi = 0.775$:

```
sim.amer <- do(1000) * rflip(1019, 0.775)
head(sim.amer, 3)
```

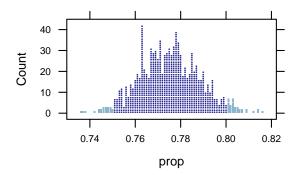
```
n heads tails prop

1 1019 817 202 0.8017664

2 1019 793 226 0.7782139

3 1019 779 240 0.7644750

dotPlot(~prop, data = sim.amer, groups = (prop <= 0.75 | prop >= 0.8), width = 0.001)
```



3. Strength of evidence:

Approximate test for proportions:

```
prop.test(815, 1019, p = 0.775)

1-sample proportions test with continuity correction

data: 815 out of 1019

X-squared = 3.4544, df = 1, p-value = 0.06308
alternative hypothesis: true p is not equal to 0.775
95 percent confidence interval:
0.7736183 0.8236924
sample estimates:

p
0.7998037
```

Exact test for proportions:

```
binom.test(815, 1019, p = 0.775)
```

```
Exact binomial test (with Score CI)

data: 815 out of 1019
number of successes = 815, number of trials = 1019, p-value = 0.06064
alternative hypothesis: true probability of success is not equal to 0.775
95 percent confidence interval:
0.7738936 0.8239686
sample estimates:
probability of success
0.7998037
```

1. H_0 : $\pi = 0.5$

 H_a : $\pi \neq 0.5$

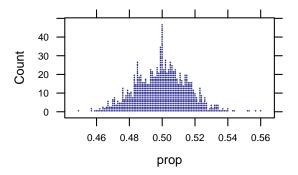
Test statistic: $\hat{p} = 0.80$ (the sample proportion of 815/1019)

2. We simulate a world in which $\pi = 0.5$:

```
sim.amer2 <- do(1000) * rflip(1019, 0.5)
head(sim.amer2, 3)

n heads tails prop
1 1019 515 504 0.5053974
2 1019 495 524 0.4857704
3 1019 494 525 0.4847890

dotPlot(~prop, data = sim.amer2, groups = (prop <= 0.2 | prop >= 0.8), width = 0.001)
```



3. Strength of evidence:

Approximate test for proportions:

```
prop.test(815, 1019)

1-sample proportions test with continuity correction

data: 815 out of 1019

X-squared = 365.16, df = 1, p-value < 2.2e-16
alternative hypothesis: true p is not equal to 0.5

95 percent confidence interval:
0.7736183 0.8236924

sample estimates:

p
0.7998037
```

Exact test for proportions:

```
binom.test(815, 1019)

Exact binomial test (with Score CI)

data: 815 out of 1019
number of successes = 815, number of trials = 1019, p-value < 2.2e-16
alternative hypothesis: true probability of success is not equal to 0.5
95 percent confidence interval:
0.7738936 0.8239686
sample estimates:
probability of success
0.7998037
```

Finding the standard deviation using simulated deviation:

```
sd <- sd(~prop, data = sim.amer)
sd

[1] 0.01311552

z <- (0.8 - 0.775)/sd

z

[1] 1.906138

xpnorm(0.8, 0.775, sd, lower.tail = FALSE, plot = FALSE)

If X ~ N(0.775,0.0131155233362715), then

P(X <= 0.8) = P(Z <= 1.906) = 0.9717
P(X > 0.8) = P(Z > 1.906) = 0.0283
[1] 0.02831614
```

Determining a 95% confidence interval using the 2SD Method and standard deviation of the null distribution:

```
p.hat <- 0.80  # given sample proportion  # previously found simulated standard deviation

[1] 0.01311552

MoE <- 2 * sd; MoE  # margin of error for 95% CI

[1] 0.02623105

p.hat - MoE  # lower limit of 95% CI

[1] 0.773769

p.hat + MoE  # upper limit of 95% CI

[1] 0.826231
```

Determining a 95% confidence interval using the 2SD Method and standard error of the observed sample proportion:

```
n <- 1019
p.hat <- 0.80  # given sample proportion
SE <- sqrt(p.hat * (1 - p.hat) / n); SE

[1] 0.01253063

MoE <- 2 * SE; MoE  # margin of error for 95% CI

[1] 0.02506126
p.hat - MoE  # lower limit of 95% CI

[1] 0.7749387
p.hat + MoE  # upper limit of 95% CI
```

Determining a 95% confidence interval using more accurate multipliers and standard error of the observed sample proportion (Theory-Based Inference applet):

Another way to create a 95% confidence interval is to use the middle 95% of the simulated null distribution. This is not exactly the same as the interval found by the 2SD Method, but it is very close.

```
cdata(0.95, prop, data = sim.amer)

low          hi central.p
0.7507360 0.8017664 0.9500000
```

The binom.test() calculates the exact confidence interval for any confidence level:

```
binom.test(815, 1019, p = 0.775, conf.level = 0.95)

Exact binomial test (with Score CI)

data: 815 out of 1019
number of successes = 815, number of trials = 1019, p-value = 0.06064
alternative hypothesis: true probability of success is not equal to 0.775
95 percent confidence interval:
0.7738936 0.8239686
sample estimates:
probability of success
0.7998037

binom.test(815, 1019, p = 0.775, conf.level = 0.99)

Exact binomial test (with Score CI)
```

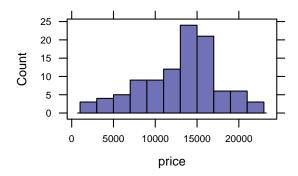
```
data: 815 out of 1019
number of successes = 815, number of trials = 1019, p-value = 0.06064
alternative hypothesis: true probability of success is not equal to 0.775
99 percent confidence interval:
0.7656447 0.8311121
sample estimates:
probability of success
            0.7998037
binom.test(815, 1019, p = 0.775, conf.level = 0.9)
Exact binomial test (with Score CI)
data: 815 out of 1019
number of successes = 815, number of trials = 1019, p-value = 0.06064
alternative hypothesis: true probability of success is not equal to 0.775
90 percent confidence interval:
0.7780614 0.8202524
sample estimates:
probability of success
       0.7998037
```

Note that the specified π , the p = 0.775, only matters in calculating the p-value and does not affect the confidence interval.

3.3 2SD and Theory-Based Confidence Intervals for a Single Mean

Example 3.3: Used Cars

```
head(UsedCars)
                                                                                                 Figure3.9
price
1 21990
2 21990
3 21987
4 20955
5 20955
6 19995
favstats(~price, data = UsedCars)
                            Q3 max
            01 median
                                                    sd n missing
 min
                                         mean
 1200 10067.25 13992 15998.75 21990 13292.33 4534.568 102
histogram(~price, data = UsedCars, type = "count", width = 2000)
```



Determining a 95% confidence interval using the 2SD Method and standard error of the sample population:

```
Example3.3
n <- nrow(UsedCars); n</pre>
[1] 102
mean <- mean(~ price, data = UsedCars); mean</pre>
[1] 13292.33
sd <- sd(~ price, data = UsedCars); sd</pre>
[1] 4534.568
SE <- sd / sqrt(n)
MoE <- 2 * SE; MoE
                        # margin of error for 95% CI
[1] 897.9782
mean - MoE
                        # lower limit of 95% CI
[1] 12394.36
mean + MoE
                        # upper limit of 95% CI
[1] 14190.31
```

Theory-based approach

```
confint(t.test(~price, data = UsedCars))
mean of x lower upper level
13292.33 12401.66 14183.01 0.95
```

Exploration 3.3: Sleepless Nights? (continued)

```
Exploration3.3.1
head(SleepTimes)
  sleepHrs
      7.0
2
      5.5
3
      8.0
      7.0
5
      7.5
6
      6.0
favstats(~sleepHrs, data = SleepTimes)
min Q1 median
                 Q3 max
                             mean
                                     sd n missing
4 6 6.5 7.375 10.5 6.704545 1.297058 22
```

Determining a 95% confidence interval using the 2SD Method and standard error of the sample population:

```
Exploration3.3.6

n <- nrow(SleepTimes); n

[1] 22

mean <- mean(~ sleepHrs, data = SleepTimes); mean

[1] 6.704545

sd <- sd(~ sleepHrs, data = SleepTimes); sd

[1] 1.297058

SE <- sd / sqrt(n)
MoE <- 2 * SE; MoE # margin of error for 95% CI</pre>
```

```
[1] 0.5530674

mean - MoE  # lower limit of 95% CI

[1] 6.151478

mean + MoE  # upper limit of 95% CI

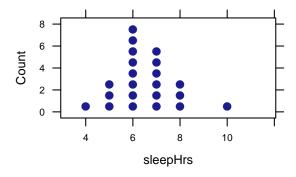
[1] 7.257613
```

Theory-based approach

```
confint(t.test(~sleepHrs, data = SleepTimes))

mean of x lower upper level
6.704545 6.129462 7.279629 0.950000
```

```
dotPlot(~sleepHrs, data = SleepTimes, width = 1) # to check the distribution
```



3.4 Factors That Affect the Width of a Confidence Interval

Example 3.4: The Afforable Care Act (continued)

```
confint(binom.test(713, 1034, conf.level = 0.95))
probability of success
                                        lower
                                                                upper
             0.6895551
                                    0.6603601
                                                            0.7176665
                 level
             0.9500000
confint(binom.test(713, 1034, conf.level = 0.99))
probability of success
                                        lower
                                                                upper
                                    0.6511883
             0.6895551
                                                            0.7261507
                 level
             0.9900000
```

Sample size

```
confint(binom.test(70, 100))
                                                                                                    Figure3.12
probability of success
                                          lower
                                                                  upper
             0.7000000
                                     0.6001853
                                                              0.7875936
                 level
             0.9500000
confint(binom.test(140, 200))
probability of success
                                          lower
                                                                  upper
             0.7000000
                                     0.6313501
                                                              0.7626104
                 level
             0.9500000
confint(binom.test(280, 400))
probability of success
                                          lower
                                                                  upper
                                     0.6524781
             0.7000000
                                                              0.7445333
                 level
             0.9500000
```

Optional: Effect of sample proportion

Sample proportions will affect confidence intervals calculated by using accurate multipliers and the standard error of the observed sample proportion (Theory-Based Inference applet). However, the sample proportions will not affect confidence intervals found by using the exact test for proportions, binom.test().

```
confint(binom.test(838, 1034))
probability of success lower upper
```

```
0.8104449
                                     0.7852004
                                                             0.8339078
                 level
             0.9500000
MoE838 <- 0.8339078 - 0.7852004
MoE838
[1] 0.0487074
confint(binom.test(196, 1034))
probability of success
                                         lower
                                                                 upper
             0.1895551
                                     0.1660922
                                                             0.2147996
                 level
             0.9500000
MoE196 <- 0.2147996 - 0.1660922
MoE 196
[1] 0.0487074
```

Exploration 3.4: Holiday Spending Habits

Determining a 95% confidence interval using the 2SD Method and standard error of the sample population:

```
n <- 1039
mean <- 704
sd <- 150
SE <- sd / sqrt(n)
MoE <- 2 * SE; MoE  # margin of error for 95% CI

[1] 9.307081

mean - MoE  # lower limit of 95% CI

[1] 694.6929

mean + MoE  # upper limit of 95% CI

[1] 713.3071</pre>
```

```
n <- 1039
mean <- 704
sd <- 300
SE <- sd / sqrt(n)
MoE <- 2 * SE; MoE # margin of error for 95% CI
```

```
[1] 18.61416

mean - MoE  # lower limit of 95% CI

[1] 685.3858

mean + MoE  # upper limit of 95% CI

[1] 722.6142
```

The impact of sample size

```
n <- 477
mean <- 704
sd <- 300
SE <- sd / sqrt(n)
MoE <- 2 * SE; MoE  # margin of error for 95% CI

[1] 27.47211

mean - MoE  # lower limit of 95% CI

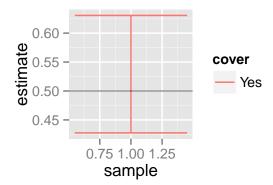
[1] 676.5279

mean + MoE  # upper limit of 95% CI

[1] 731.4721</pre>
```

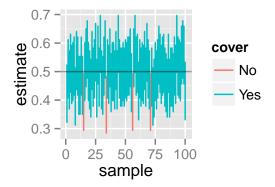
Exploration 3.4B: Reese's Pieces

Simulate 1 sample proportion and calculate the 95% confidence interval:



Simulate 100 sample proportions and calculate the 95% confidence intervals:

```
sim.CI <- CIsim(100, samples = 100, rdist = rbinom, args = list(size = 1, prob = 0.5), method = binom.test, method.args = list(success = 1), verbose = FALSE, estimand = 0.5)
```



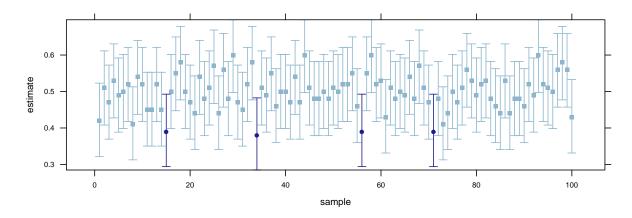
Proportion of intervals produced that do not contain $\pi = 0.5$:

```
prop(~cover, data = sim.CI)

No
0.04
Exploration3.4B.5b
```

Plot the 95% confidence intervals of the simulation of 100 sample proportions:

```
require(Hmisc)
xYplot(Cbind(estimate, lower, upper) ~ sample, data = sim.CI, par.settings = col.mosaic(),
    groups = cover)
```



Simulate 1000 sample proportions and calculate the 95% confidence intervals:

Proportion of intervals produced that do not contain $\pi = 0.5$:

```
prop(~cover, data = sim.CI2)

No
0.04
Exploration3.4B.5e
```

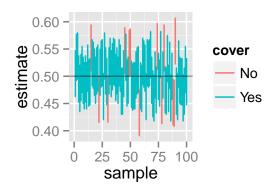
Simulate 1000 sample proportions and calculate the 90% confidence intervals:

Proportion of intervals produced that do not contain $\pi = 0.5$:

```
prop(~cover, data = sim.CI3)

No
0.101
Exploration3.4B.6b
```

Simulate 1000 sample proportions and calculate the 90% confidence intervals (sample size = 400):



Proportion of intervals produced that do not contain $\pi = 0.5$:

```
prop(~cover, data = sim.CI4)
No
0.13
```

3.5 Cautions When Conducting Inference

```
1. H_0: \pi = 0.3645
```

 H_a : $\pi > 0.3645$

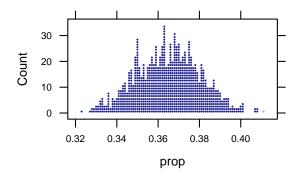
Test statistic: $\hat{p} = 0.41$ (the sample proportion)

2. We simulate a world in which $\pi = 0.3645$:

```
sim.obama <- do(1000) * rflip(1000, 0.3645)
head(sim.obama, 3)

n heads tails prop
1 1000    365    635    0.365
2 1000    376    624    0.376
3 1000    375    625    0.375

dotPlot(~prop, data = sim.obama, groups = (prop >= 0.41), width = 0.001)
```



3. Strength of evidence:

Exploration 3.5A: Voting for President

Finding the 99% confidence interval using the exact test for proportions:

Another famous case of problems in Presidential election polling

Finding the 99% confidence interval using the exact test for proportions:

Example 3.5B: Parapsychology Studies (continued)

```
confint(binom.test(709, 2124, conf.level = 0.95))
                                                                                                   Example3.5B
probability of success
                                          lower
                                                                  upper
             0.3338041
                                     0.3137548
                                                              0.3543132
                 level
             0.9500000
confint(binom.test(709, 2124, conf.level = 0.99))
probability of success
                                          lower
                                                                  upper
             0.3338041
                                     0.3076114
                                                              0.3607496
                 level
             0.9900000
```

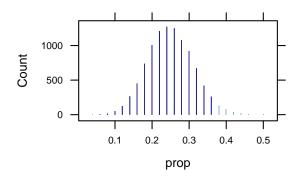
1. H_0 : $\pi = 0.25$

 H_a : $\pi > 0.25$

Test statistic: $\hat{p} = 0.38$ (the sample proportion of 19/50)

2. We simulate a world in which $\pi = 0.25$:

```
Figure3.15
sim.esp2 \leftarrow do(10000) * rflip(50, 0.25)
head(sim.esp2, 3)
   n heads tails prop
            40 0.20
1 50
      10
2 50
              38 0.24
        12
3 50
        15
              35 0.30
dotPlot(\tilde{p}rop, data = sim.esp2, groups = (prop >= 0.38), width = 0.01, cex = 10)
prop(~(prop >= 0.38), data = sim.esp2)
    target level: TRUE; other levels: FALSE
  TRUE
0.0257
```



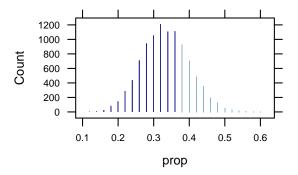
1. H_0 : $\pi = 1/3$

$$H_a$$
: $\pi > 1/3$

Test statistic: $\hat{p} = 0.38$ (the sample proportion of 19/50)

2. We simulate a world in which $\pi = 1/3$:

```
Figure3.16
sim.esp3 <- do(10000) * rflip(50, 1/3)
head(sim.esp3, 3)
  n heads tails prop
1 50
        19
              31 0.38
2 50
        13
              37 0.26
3 50
        23
              27 0.46
dotPlot("prop, data = sim.esp3, groups = (prop >= 0.38), width = 0.01, cex = 10)
prop(~(prop >= 0.38), data = sim.esp3)
    target level: TRUE; other levels: FALSE
  TRUE
0.2872
```



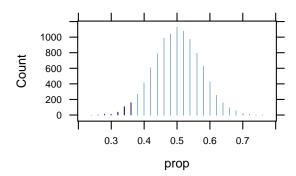
1. H_0 : $\pi = 1/2$

 H_a : $\pi > 1/2$

Test statistic: $\hat{p} = 0.38$ (the sample proportion of 19/50)

2. We simulate a world in which $\pi = 1/2$:

```
sim.esp4 <- do(10000) * rflip(50, 1/2)
                                                                                             Figure3.17
head(sim.esp4, 3)
   n heads tails prop
1 50
        27
              23 0.54
2 50
              20 0.60
        30
3 50
        29
              21 0.58
dotPlot("prop, data = sim.esp4, groups = (prop >= 0.38), width = 0.01, cex = 10)
prop(~(prop >= 0.38), data = sim.esp4)
    target level: TRUE; other levels: FALSE
  TRUE
0.9664
```



3.5.1 Exploration 3.5B: Cat Households

1. H_0 : $\pi = 1/3$ H_a : $\pi < 1/3$

Test statistic: $\hat{p} = 0.324$ (the sample proportion of 15228/47000)

2. Exact test for proportions:

```
Exploration3.5B.3
binom.test(15228, 47000, p = 1/3, conf.level = 0.999, alt = "less")
Exact binomial test (with Score CI)
data: 15228 out of 47000
number of successes = 15228, number of trials = 47000, p-value = 8.654e-06
alternative hypothesis: true probability of success is less than 0.3333333
99.9 percent confidence interval:
0.0000000 0.3307064
sample estimates:
probability of success
                 0.324
binom.test(15228, 47000, p = 1/3, alt = "less")
Exact binomial test (with Score CI)
data: 15228 out of 47000
number of successes = 15228, number of trials = 47000, p-value = 8.654e-06
alternative hypothesis: true probability of success is less than 0.3333333
95 percent confidence interval:
0.0000000 0.3275694
sample estimates:
probability of success
                 0.324
```

3. We simulate a world in which $\pi = 1/3$:

```
sim.pets <- do(1000) * rflip(100, 1/3)
head(sim.pets, 3)
```

```
n heads tails prop
1 100 29 71 0.29
2 100 33 67 0.33
3 100 40 60 0.40
```

We could use trial-and-error to determine values of the sample proportion that would produce a p-value of less than 0.05. R can quickly calculate try possible values that would result in the significance level of 0.05 but we can also have R calculate them for us.

```
cdata(0.95, prop, data = sim.pets)

low     hi central.p
     0.25     0.42     0.95
```

1. H_0 : $\pi = 0.30$

 H_a : $\pi < 0.30$

Test statistic: $\hat{p} = 0.243$ (the sample proportion)

2. We simulate a world in which $\pi = 0.30$:

```
sim.pets2 <- do(1000) * rflip(100, 0.3)
head(sim.pets2, 3)

    n heads tails prop
1 100     31     69 0.31
2 100     36     64 0.36
3 100     28     72 0.28

prop(~(prop <= 0.243), data = sim.pets2)

    target level: TRUE; other levels: FALSE

TRUE
0.093</pre>
```

```
cdata(0.9, prop, data = sim.pets2)

low     hi central.p
0.23     0.38     0.90
```

```
Exact binomial test (with Score CI)
data: 24 out of 100
number of successes = 24, number of trials = 100, p-value = 0.1136
alternative hypothesis: true probability of success is less than 0.3
95 percent confidence interval:
0.0000000 0.3206028
sample estimates:
probability of success
                  0.24
confint(binom.test(33, 100, p = 1/3, conf.level = 0.9))
probability of success
                                        lower
                                                                upper
             0.3300000
                                    0.2523035
                                                            0.4154543
                 level
             0.9000000
binom.test(25, 100, p = 0.3, alt = "less", conf.level = 0.9)
Exact binomial test (with Score CI)
data: 25 out of 100
number of successes = 25, number of trials = 100, p-value = 0.1631
alternative hypothesis: true probability of success is less than 0.3
90 percent confidence interval:
0.0000000 0.3140311
sample estimates:
probability of success
                  0.25
confint(binom.test(167, 500, p = 1/3))
probability of success
                                        lower
                                                                upper
             0.3340000
                                    0.2927472
                                                            0.3772297
                 level
             0.9500000
binom.test(146, 500, p = 0.3, alt = "less")
Exact binomial test (with Score CI)
data: 146 out of 500
number of successes = 146, number of trials = 500, p-value = 0.3685
alternative hypothesis: true probability of success is less than 0.3
95 percent confidence interval:
0.0000000 0.3273078
sample estimates:
probability of success
                 0.292
confint(binom.test(33, 100, p = 1/3))
```

```
probability of success
                                       lower
                                                             upper
            0.3300000
                                   0.2391985
                                                          0.4311728
                level
            0.9500000
binom.test(24, 100, p = 0.2, alt = "less")
Exact binomial test (with Score CI)
data: 24 out of 100
number of successes = 24, number of trials = 100, p-value = 0.8686
alternative hypothesis: true probability of success is less than 0.2\,
95 percent confidence interval:
0.0000000 0.3206028
sample estimates:
probability of success
        0.24
```

4

Causation: Can We Say What Caused the Effect?

4.1 Association and Confounding

Example 4.1: Night Lights and Near-Sightedness

Often, when a dataset has only categorical variables, it may come in the form of a table and not a frame. Here is a way to create a data frame in R.

```
Darkness NightLight RoomLight
Near 18 78 41
Not 154 154 34

NightLight <- rbind(
do(18) * data.frame(light = "Darkness", nearsight = "Near"),
do(154) * data.frame(light = "Darkness", nearsight = "Not"),
do(78) * data.frame(light = "NightLight", nearsight = "Near"),
do(154) * data.frame(light = "NightLight", nearsight = "Not"),
do(154) * data.frame(light = "NightLight", nearsight = "Not"),
do(41) * data.frame(light = "RoomLight", nearsight = "Near"),
do(34) * data.frame(light = "RoomLight", nearsight = "Not")
)
```

```
head(NightLight)
    light nearsight .row .index
1 Darkness
             Near 1 1
2 Darkness
             Near
                   1
3 Darkness
             Near 1
                           3
4 Darkness
             Near
                   - 1
                           4
5 Darkness
                           5
             Near
                    1
6 Darkness
             Near
```

```
tally(nearsight ~ light, data = NightLight)
```

```
light
nearsight Darkness NightLight RoomLight
    Near 18 78 41
            154
                      154
                                34
    Not
tally(~nearsight | light, data = NightLight)
       light
nearsight Darkness NightLight RoomLight
             18
                      78
                           41
    Near
    Not
             154
                      154
                                34
tally(~nearsight + light, data = NightLight, margins = TRUE)
       light
nearsight Darkness NightLight RoomLight Total
   Near
             18
                      78
                               41 137
             154
                      154
                                34
                                    342
   Total
         172
                      232
                                75
                                    479
```

4.2 Observational studies versus experiments

Exploration 4.2: Have a Nice Trip

Comparing Two Proportions

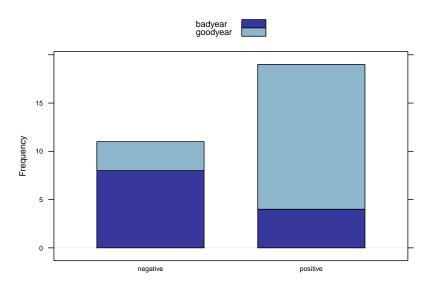
5.1 Comparing Two Groups: Categorical Response

Example 5.1: Good and Bad Perceptions

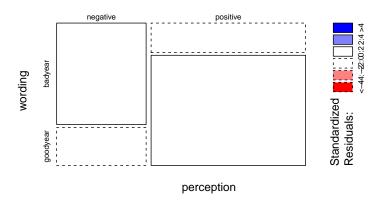
```
head(GoodandBad, 30)
                                                                                        Table5.1
   wording perception
1 goodyear positive
2 goodyear negative
3 badyear positive
4 goodyear positive
5 goodyear negative
6 badyear positive
7 goodyear positive
8 goodyear positive
9 goodyear positive
10 badyear
            negative
11 goodyear
            negative
12 badyear
            negative
13 goodyear
            positive
14 badyear negative
15 goodyear positive
16 goodyear positive
17 badyear positive
18 goodyear positive
19 goodyear positive
20 goodyear
            positive
21 badyear
            negative
22 goodyear
            positive
23 badyear
            negative
24 goodyear
            positive
25 badyear
            negative
26 goodyear
            positive
27 badyear
            negative
28 goodyear
            positive
29 badyear
            positive
30 badyear
            negative
```

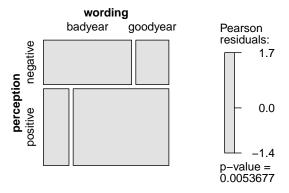
```
Table5.2
tally(perception ~ wording, data = GoodandBad, margins = TRUE)
         wording
perception badyear goodyear
 negative
                8
                        3
 positive
                4
                        15
               12
                        18
 Total
tally(perception ~ wording, data = GoodandBad, format = "prop")
         wording
perception badyear goodyear
 negative 0.6666667 0.1666667
 positive 0.3333333 0.8333333
prop(perception ~ wording, data = GoodandBad)
negative.badyear negative.goodyear
       0.6666667
                        0.1666667
prop(perception ~ wording, level = "positive", data = GoodandBad)
positive.badyear positive.goodyear
```

```
bargraph(~perception, groups = wording, data = GoodandBad, stack = TRUE, auto.key = TRUE)
mosaicplot(~perception + wording, data = GoodandBad, shade = TRUE)
mosaic(~perception + wording, data = GoodandBad, shade = TRUE)
```



GoodandBad





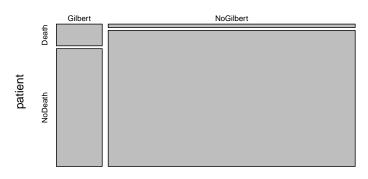
Summarizing the data

Exploration 5.1: Murderous Nurse?

```
mosaicplot(shift ~ patient, data = Nurse)
```

Nurse

shift



prop(patient ~ shift, data = Nurse)

Death.Gilbert Death.NoGilbert
 0.15564202 0.02456647

diffprop(patient ~ shift, data = Nurse)

diffprop
-0.1310755

Further Analysis

```
Nurse2 <- rbind(
```

```
Exploration 5.1.18b
tally(patient ~ shift, data = Nurse2, margin = TRUE)
        shift
patient Gilbert NoGilbert
 Death
           100 357
 NoDeath
             157
                      1027
  Total
             257
                      1384
tally(patient ~ shift, data = Nurse2, format = "prop")
        shift
patient
        Gilbert NoGilbert
 Death 0.3891051 0.2579480
 NoDeath 0.6108949 0.7420520
diffprop(patient ~ shift, data = Nurse2) # diff in conditional prop
 diffprop
-0.1311571
```

5.2 Comparing Two Properties: Simulation-Based Approach

Example 5.2: Swimming with Dolphins

```
head(Dolphin)
                                                                                        Table5.3
 swimming response
1 Dolphin Improve
2 Dolphin Improve
3 Dolphin Improve
4 Dolphin Improve
5 Dolphin Improve
6 Dolphin Improve
tally(response ~ swimming, data = Dolphin, margin = TRUE)
          swimming
          Control Dolphin
response
 Improve 3
                     10
 NotImprove
               12
Total
               15
                       15
```

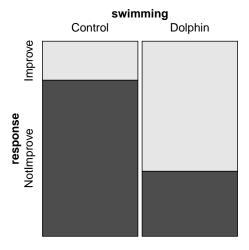
```
tally(response ~ swimming, data = Dolphin, format = "prop")

swimming
response Control Dolphin
Improve 0.2000000 0.6666667
NotImprove 0.8000000 0.33333333
```

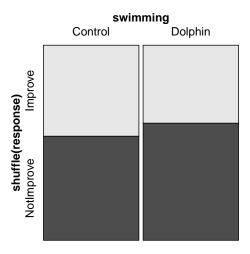
```
diffprop(response ~ swimming, data = Dolphin)

diffprop
0.4666667

mosaic(response ~ swimming, data = Dolphin, dir = "v")
```



```
mosaic(shuffle(response) ~ swimming, data = Dolphin, dir = "v")
```



```
Figure5.5
tally(shuffle(response) ~ swimming, data = Dolphin, margins = TRUE)
               swimming
shuffle(response) Control Dolphin
      Improve 6
                          7
      NotImprove
                      9
                              8
      Total
                     15
                             15
tally(shuffle(response) ~ swimming, data = Dolphin, margins = TRUE)
                swimming
shuffle(response) Control Dolphin
      Improve
                      4 9
                              6
      NotImprove
                      11
      Total
                     15
                             15
tally(shuffle(response) ~ swimming, data = Dolphin, margins = TRUE)
                swimming
shuffle(response) Control Dolphin
      Improve
                  6
      NotImprove
                     9
                              8
      Total
                     15
                             15
diffprop(response ~ swimming, data = Dolphin)
diffprop
0.4666667
diffprop(shuffle(response) ~ swimming, data = Dolphin)
 diffprop
0.06666667
```

1. H_0 : $\pi_{dolphins} - \pi_{control} = 0$ H_a : $\pi_{dolphins} - \pi_{control} > 0$ Test statistic: $\hat{p}_{dolphins} - \hat{p}_{control} = 0.4667$ (the difference in the conditional sample proportions)

2. We simulate a world in which $\pi_{dolphins} - \pi_{control} = 0$:

```
Figure 5.6
sim.dol <- do(1000) * diffprop(shuffle(response) ~ swimming, data = Dolphin)</pre>
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                              other levels:
                   Improve;
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
                   Improve;
    target level:
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                             other levels:
                                             NotImprove
                   Improve;
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                             other levels:
                   Improve;
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                             other levels:
                   Improve;
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
                   Improve;
    target level:
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                                             NotImprove
                             other levels:
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                                             NotImprove
                             other levels:
    target level:
                   Improve;
                                             NotImprove
                             other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
                         other levels:
                                         NotImprove
target level:
              Improve;
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
                         other levels:
                                         NotImprove
target level:
              Improve;
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                         other levels:
                                         NotImprove
target level:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
target level:
              Improve;
                         other levels:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
                         other levels:
                                         NotImprove
target level:
              Improve;
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

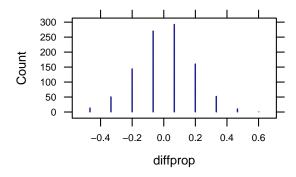
```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
                         other levels:
                                         NotImprove
target level:
              Improve;
```

```
Improve;
                                             NotImprove
    target level:
                             other levels:
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                                             NotImprove
                   Improve;
                             other levels:
    target level:
                   Improve;
                              other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                                             NotImprove
                             other levels:
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                              other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                             other levels:
                                             NotImprove
                                             NotImprove
    target level:
                   Improve;
                             other levels:
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                                             NotImprove
                             other levels:
    target level:
                   Improve;
                             other levels:
                                             NotImprove
    target level:
                   Improve;
                              other levels:
                                             NotImprove
    target level:
                                             NotImprove
                   Improve;
                              other levels:
    target level:
                   Improve;
                             other levels:
                                             NotImprove
head(sim.dol, 3)
dotPlot(~diffprop, data = sim.dol, groups = (diffprop >= 0.4667), width = 1/15, cex = 5)
```



3. Strength of evidence:

Approximate test for difference in proportions:

Estimation

Determining a 95% confidence interval using the 2SD Method and simulated standard deviation of the null distribution:

```
# given difference in sample proportions
diff <- diffprop(response ~ swimming, data = Dolphin)
# simulated standard deviation
sd <- sd(~diffprop, data = sim.dol)
# margin of error for 95% CI</pre>
```

```
MoE <- 2 * sd
MoE

[1] 0.3584312

# lower limit of 95% CI
diff - MoE

diffprop
0.1082355

# upper limit of 95% CI
diff + MoE

diffprop
0.8250979
```

Determining a 95% confidence interval using the approximate test for proportions:

Follow-up Analysis

```
Dolphin2 <- rbind(
  do(8) * data.frame(response = "Improve", swimming = "Control"),
  do(5) * data.frame(response = "Improve", swimming = "Dolphin"),
  do(7) * data.frame(response = "NotImprove", swimming = "Control"),
  do(10) * data.frame(response = "NotImprove", swimming = "Dolphin")
  )</pre>
```

```
tally(response ~ swimming, data = Dolphin2, margin = TRUE, format = "prop")

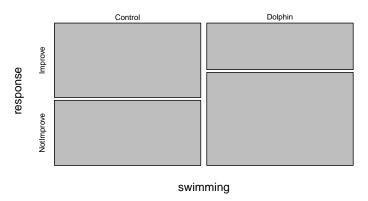
swimming
response Control Dolphin
Improve 0.5333333 0.3333333
NotImprove 0.4666667 0.6666667
Total 1.0000000 1.0000000

diffprop(response ~ swimming, data = Dolphin2)

diffprop
-0.2
```

```
mosaicplot(swimming ~ response, data = Dolphin2)
```

Dolphin2



- 1. H_0 : $\pi_{dolphins} \pi_{control} = 0$ H_a : $\pi_{dolphins} \pi_{control} > 0$ Test statistic: $\hat{p}_{dolphins} \hat{p}_{control} = 0.20$ (the difference in the conditional sample proportions)
- 2. We simulate a world in which $\pi_{dolphins} \pi_{control} = 0$:

```
Figure5.7d
sim.dol2 <- do(1000) * diffprop(shuffle(response) ~ swimming, data = Dolphin2)
                                            NotImprove
    target level: Improve;
                             other levels:
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                                            NotImprove
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                             other levels:
                   Improve;
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                             other levels:
                                            NotImprove
                   Improve;
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels:
                                            NotImprove
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                         other levels:
                                         NotImprove
target level:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                         other levels:
                                         NotImprove
target level:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

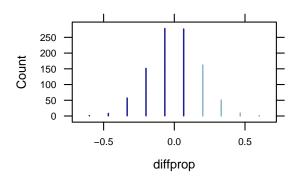
```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level: Improve;
                                         NotImprove
                         other levels:
```

```
target level: Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                         other levels:
                                         NotImprove
               Improve;
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                                         NotImprove
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
target level:
                                         NotImprove
               Improve;
                         other levels:
target level:
               Improve;
                         other levels:
                                         NotImprove
               Improve;
                                         NotImprove
target level:
                         other levels:
              Improve;
                         other levels:
                                         NotImprove
target level:
```

```
target level: Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                                            NotImprove
                             other levels:
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels:
                                            NotImprove
    target level:
                   Improve;
                             other levels:
                                            NotImprove
    target level:
                  Improve;
                             other levels: NotImprove
head(sim.dol2, 3)
dotPlot(~diffprop, data = sim.dol2, groups = (diffprop >=0.20),
       width = 1/15, cex = 5)
```



3. Strength of evidence:

Approximate test for difference in proportions:

Relative Risk

Exploration 5.2: Is Yawning Contagious?

```
Exploration5.2.9
head(Yawning, 3)
 yawnSeed response
   Seeded
              Yawn
2 Seeded
              Yawn
   Seeded
              Yawn
tally(response ~ yawnSeed, data = Yawning, margin = TRUE)
       yawnSeed
response Control Seeded
 NoYawn 13
             3
                    11
 Yawn
 Total
             16
                    34
```

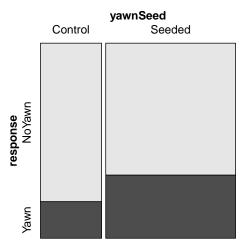
```
tally(response ~ yawnSeed, data = Yawning, format = "prop")

yawnSeed
response Control Seeded
NoYawn 0.8125000 0.6764706
Yawn 0.1875000 0.3235294

diffprop(response ~ yawnSeed, level = "Yawn", data = Yawning)

diffprop
0.1360294
```

```
mosaic(response ~ yawnSeed, data = Yawning, dir = "v")
Exploration5.2.11
```



```
tally(shuffle(response) ~ yawnSeed, data = Yawning, margins = TRUE)

yawnSeed
shuffle(response) Control Seeded
NoYawn 9 27
Yawn 7 7
Total 16 34
```

```
1. H_0: \pi_{seeded} - \pi_{control} = 0
```

$$H_a$$
: $\pi_{seeded} - \pi_{control} > 0$

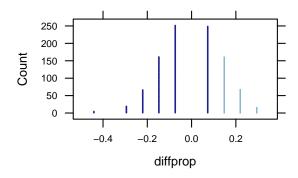
Test statistic: $\hat{p}_{seeded} - \hat{p}_{control} = 0.136$ (the difference in the conditional sample proportions)

2. We simulate a world in which $\pi_{seeded} - \pi_{control} = 0$:

```
sim.yawn <-
    do(1000) * diffprop(shuffle(response) ~ yawnSeed, level = "Yawn", data = Yawning)
head(sim.yawn, 3)

diffprop
1 -0.2316176
2  0.1360294
3  0.2279412

dotPlot(~diffprop, data = sim.yawn, groups = (diffprop >= 0.136), cex = 5)
```



3. Strength of evidence:

Approximate test for difference in proportions:

```
prop.test(response ~ yawnSeed, data = Yawning, alt = "greater")

Warning in stats::prop.test(t(table_from_formula), p = p, conf.level = conf.level, : Chi-squared approximation may be incorrect

2-sample test for equality of proportions with continuity correction

data: tally(response ~ yawnSeed)
X-squared = 0.43786, df = 1, p-value = 0.2541
alternative hypothesis: greater
95 percent confidence interval:
    -0.1177157    1.0000000
sample estimates:
    prop 1    prop 2
0.8125000    0.6764706
```

```
Yawning2 <- rbind(
do(12) * data.frame(response = "NoYawn", yawnSeed = "Control"),
do(24) * data.frame(response = "NoYawn", yawnSeed = "Seeded"),
do(4) * data.frame(response = "Yawn", yawnSeed = "Control"),
do(10) * data.frame(response = "Yawn", yawnSeed = "Seeded")
)
```

```
Exploration5.2.21b
head(Yawning2, 3)
 response yawnSeed .row .index
1 NoYawn Control
   NoYawn Control
                              2
   NoYawn Control
                              3
tally(response ~ yawnSeed, data = Yawning2, margin = TRUE)
        yawnSeed
response Control Seeded
  NoYawn
             12
                    24
              4
  Yawn
Total
        16
```

```
tally(response ~ yawnSeed, data = Yawning2, format = "prop")

yawnSeed
response Control Seeded
NoYawn 0.7500000 0.7058824
Yawn 0.2500000 0.2941176

diffprop(response ~ yawnSeed, level = "Yawn", data = Yawning2)

diffprop
0.04411765
```

- 1. H_0 : $\pi_{seeded} \pi_{control} = 0$ H_a : $\pi_{seeded} \pi_{control} > 0$ Test statistic: $\hat{p}_{seeded} \hat{p}_{control} = 0.0441$ (the difference in the conditional sample proportions)
- 2. We simulate a world in which $\pi_{seeded} \pi_{control} = 0$:

```
sim.yawn2 <-
do(1000) * diffprop(shuffle(response) ~ yawnSeed, level = "Yawn", data = Yawning2)

target level: Yawn; other levels: NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                     NoYawn
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                     NoYawn
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                     NoYawn
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

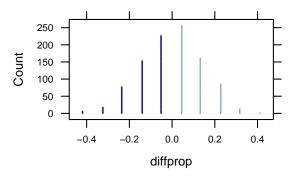
```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                          other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                          other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                          other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level: Yawn; other levels: NoYawn
head(sim.yawn2, 3)
dotPlot(~diffprop, data = sim.yawn2, groups = (diffprop >= 0.0441),
       cex = 5, width = 1/136)
```



3. Strength of evidence:

Approximate test for difference in proportions:

```
prop.test(response ~ yawnSeed, data = Yawning2, alt = "greater")

2-sample test for equality of proportions with continuity correction

data: tally(response ~ yawnSeed)
X-squared = 3.853e-31, df = 1, p-value = 0.5
alternative hypothesis: greater
95 percent confidence interval:
    -0.2196049   1.0000000
sample estimates:
    prop 1    prop 2
0.7500000   0.7058824
```

Estimation

```
sd <- sd(~diffprop, data = sim.yawn2)
sd

[1] 0.1417443</pre>
```

Determining a 95% confidence interval using the 2SD Method and simulated standard deviation of the null distribution:

```
# given difference in sample proportions
diff <- diffprop(response ~ yawnSeed, level = "Yawn", data = Yawning2)
# previously found simulated standard deviation
sd

[1] 0.1417443

# margin of error for 95% CI
MoE <- 2 * sd
MoE

[1] 0.2834887
```

```
# lower limit of 95% CI
diff - MoE

diffprop
-0.239371

# upper limit of 95% CI
diff + MoE

diffprop
0.3276063
```

Determining a 95% confidence interval using the approximate test for proportions:

Effect of Sample Size

```
Yawning3 <- rbind(
do(240) * data.frame(response = "NoYawn", yawnSeed = "Control"),
do(120) * data.frame(response = "NoYawn", yawnSeed = "Seeded"),
do(100) * data.frame(response = "Yawn", yawnSeed = "Control"),
do(40) * data.frame(response = "Yawn", yawnSeed = "Seeded")
)
```

```
Exploration5.2.31b
head(Yawning3, 3)
 response yawnSeed .row .index
1 NoYawn Control 1 1
2 NoYawn Control
                            2
                   1
3 NoYawn Control
                   1
                            3
tally(response ~ yawnSeed, data = Yawning3, margin = TRUE)
       yawnSeed
response Control Seeded
  NoYawn
            240
                 120
  Yawn
            100
                   40
 Total
          340
                   160
```

```
1. H_0: \pi_{seeded} - \pi_{control} = 0
H_a: \pi_{seeded} - \pi_{control} > 0
Test statistic: \hat{p}_{seeded} - \hat{p}_{control} = 0.0441 (the difference in the conditional sample proportions)
```

2. We simulate a world in which $\pi_{seeded} - \pi_{control} = 0$:

```
Exploration5.2.32
sim.yawn3 <-
 do(1000) * diffprop(shuffle(response) ~ yawnSeed, level = "Yawn",
                       data = Yawning3)
    target level:
                   Yawn; other levels:
                                          NoYawn
    target level:
                   Yawn;
                          other levels:
                                          NoYawn
    target level:
                           other levels:
                                          NoYawn
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
    target level:
                   Yawn:
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                          other levels:
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
                                          NoYawn
    target level:
                           other levels:
                   Yawn;
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                          other levels:
                                          NoYawn
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
                                          NoYawn
    target level:
                   Yawn;
                          other levels:
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
    target level:
                           other levels:
                                          NoYawn
                   Yawn;
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                          other levels:
                           other levels:
                                          NoYawn
    target level:
                   Yawn;
                                          NoYawn
    target level:
                   Yawn;
                           other levels:
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
               Yawn;
                      other levels:
                                      NoYawn
target level:
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                     NoYawn
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

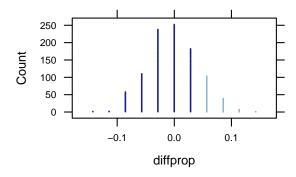
```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                     NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                      NoYawn
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                     NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level: Yawn; other levels:
                                     NoYawn
```

```
NoYawn
target level: Yawn; other levels:
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
               Yawn;
                      other levels:
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
                                      NoYawn
target level:
                      other levels:
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
                      other levels:
                                      NoYawn
               Yawn;
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
                                     NoYawn
               Yawn;
                      other levels:
                      other levels:
                                      NoYawn
target level:
               Yawn;
                      other levels:
                                      NoYawn
target level:
               Yawn;
target level: Yawn; other levels:
                                     NoYawn
```

```
target level: Yawn; other levels:
                                         NoYawn
    target level:
                  Yawn;
                         other levels:
                                         NoYawn
    target level:
                  Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                         other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
    target level:
                         other levels:
                                         NoYawn
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                         other levels:
                                         NoYawn
                  Yawn;
                         other levels:
    target level:
                   Yawn;
                                         NoYawn
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
    target level:
                         other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
    target level:
                         other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
                                         NoYawn
    target level:
                  Yawn:
                         other levels:
    target level:
                         other levels:
                                         NoYawn
                   Yawn;
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
    target level:
                   Yawn;
                          other levels:
                                         NoYawn
                                         NoYawn
    target level:
                          other levels:
                   Yawn;
    target level:
                   Yawn;
                         other levels:
                                         NoYawn
                                         NoYawn
    target level:
                   Yawn;
                         other levels:
    target level:
                         other levels:
                                         NoYawn
                   Yawn;
    target level: Yawn;
                         other levels:
                                         NoYawn
    target level: Yawn; other levels: NoYawn
head(sim.yawn3, 3)
dotPlot(~diffprop, data = sim.yawn3, groups = (diffprop >= 0.0441), cex = 5)
```



3. Strength of evidence:

Approximate test for difference in proportions:

```
prop.test(response ~ yawnSeed, data = Yawning3, alt = "greater")

2-sample test for equality of proportions with continuity correction

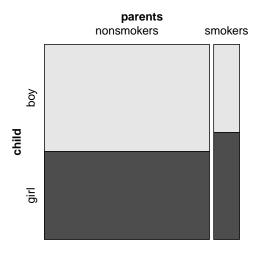
data: tally(response ~ yawnSeed)
X-squared = 0.84298, df = 1, p-value = 0.8207
alternative hypothesis: greater
95 percent confidence interval:
    -0.1181584    1.0000000
sample estimates:
    prop 1    prop 2
0.7058824    0.7500000
```

Relative risk

5.3 Comparing Two Proportions: Theory-Based Approach

Example 5.3: Smoking and Birth Gender

```
head(Smoking, 3)
                                                                                       Figure 5.9
 parents child
1 smokers girl
2 smokers girl
3 smokers girl
summary(Smoking)
  parents
                    child
Length: 4167
                 Length: 4167
 Mode :character Mode :character
tally(parents ~ child, data = Smoking, margin = TRUE)
          child
parents
           boy girl
 nonsmokers 1975 1627
           255 310
 smokers
 Total
           2230 1937
mosaic(child ~ parents, data = Smoking, dir = "v")
```



```
tally(child ~ parents, data = Smoking, format = "prop", margins = TRUE)

parents

child nonsmokers smokers

boy 0.5483065 0.4513274

girl 0.4516935 0.5486726

Total 1.0000000 1.0000000
```

```
diffprop(child ~ parents, data = Smoking)

diffprop
-0.09697906
```

1. H_0 : $\pi_{smoker} - \pi_{nonsmoker} = 0$

 H_a : $\pi_{smoker} - \pi_{nonsmoker} \neq 0$

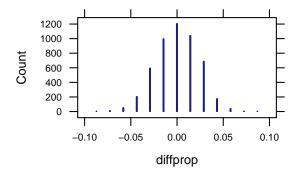
Test statistic: $\hat{p}_{smoker} - \hat{p}_{nonsmoker} = -0.097$ (the difference in the conditional sample proportions)

2. We simulate a world in which $\pi_{smoker} - \pi_{nonsmoker} = 0$:

```
sim.smoke <- do(5000) * diffprop(shuffle(child) ~ parents, data = Smoking)
head(sim.smoke, 3)

diffprop
1  0.023825505
2  -0.002792451
3  0.027920575

dotPlot(~diffprop, data = sim.smoke, cex = 25)</pre>
```



3. Strength of evidence:

Normal approximation (using simulated standard deviation):

```
sd <- sd(~diffprop, data = sim.smoke)

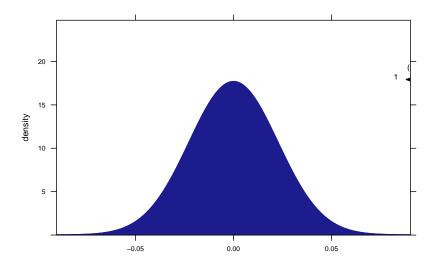
2 * xpnorm(0.097, 0, sd, lower.tail = FALSE) # 2 times because two-sided

If X ~ N(0,0.0225622971246741), then

P(X <= 0.097) = P(Z <= 4.299) = 1

P(X > 0.097) = P(Z > 4.299) = 0

[1] 1.714098e-05
```



Approximate test for difference in proportions:

```
prop.test(child ~ parents, data = Smoking)

2-sample test for equality of proportions with continuity correction

data: tally(child ~ parents)

X-squared = 18.077, df = 1, p-value = 2.122e-05

alternative hypothesis: two.sided

95 percent confidence interval:
    0.05182158    0.14213654

sample estimates:
    prop 1    prop 2
    0.5483065    0.4513274
```

Estimation

Formulas

```
prop(child ~ parents, data = Smoking)

boy.nonsmokers boy.smokers
    0.5483065    0.4513274

p.1 <- 0.548
p.2 <- 0.451
p.hat <- prop(~child, data = Smoking)
p.hat # pooled prop of success

boy
0.5351572

n.1 <- 565
n.2 <- 3602</pre>
```

```
z <- (p.1 - p.2)/sqrt((p.hat * (1 - p.hat) * (1/n.1 + 1/n.2)))
z

boy
4.29796
```

```
SE <- sqrt(p.1 * (1 - p.1)/n.1 + p.2 * (1 - p.2)/n.2)
SE [1] 0.02251975
```

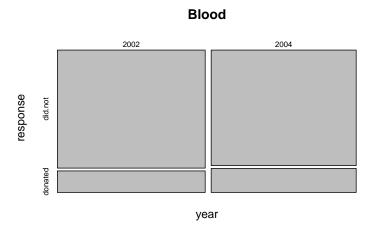
```
MoE <- 2 * SE
MoE

[1] 0.04503951
```

Exploration 5.3: Donating Blood

```
sample(Blood, 5)
                                                                                         Exploration5.3.2
    year response orig.ids
206 2002 donated
                   206
482 2002 did.not
                      482
2327 2004 did.not
                      2327
                   1712
1712 2004 did.not
146 2002 donated
                      146
tally(response ~ year, data = Blood, format = "count", margin = TRUE)
        year
response 2002 2004
 did.not 1152 1106
 donated 210 230
Total 1362 1336
```

```
mosaicplot(year ~ response, data = Blood)
```



- 1. H_0 : $\pi_{2004} \pi_{2002} = 0$ H_a : $\pi_{2004} - \pi_{2002} \neq 0$ Test statistic: $\hat{p}_{2004} - \hat{p}_{2002} = 0.0180$ (the difference in the conditional sample proportions)
- 2. We simulate a world in which $\pi_{2004} \pi_{2002} = 0$:

```
Exploration5.3.6
sim.blood <-
 do(5000) * diffprop(shuffle(response) ~ year, level = "donated", data = Blood)
    target level:
                   donated; other levels:
                                            did.not
    target level:
                             other levels:
                                             did.not
                   donated;
    target level:
                   donated;
                             other levels:
                                             did.not
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                   donated;
                             other levels:
                                            did.not
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                   donated;
                             other levels:
                                            did.not
    target level:
                   donated;
                             other levels:
                                             did.not
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                   donated;
                             other levels:
                                            did.not
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                             other levels: did.not
                   donated;
    target level:
                   donated;
                             other levels:
                                            did.not
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                                            did.not
                   donated;
                             other levels:
                                            did.not
    target level:
                             other levels:
                   donated;
    target level:
                             other levels:
                                            did.not
                   donated;
    target level:
                             other levels:
                   donated;
                                            did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                                      did.not
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                                      did.not
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                                      did.not
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

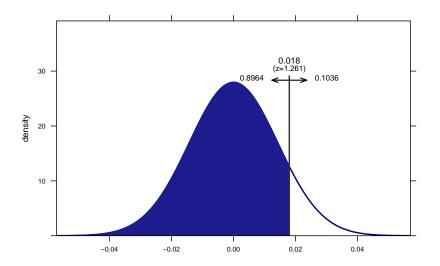
```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated; other levels: did.not
         target level: donated;
                                 other levels:
         target level: donated; other levels: did.not
         target level: donated;
                                 other levels: did.not
         target level: donated;
                                 other levels: did.not
         target level:
                                 other levels: did.not
                       donated;
         target level:
                       donated;
                                 other levels:
                                                did.not
         target level:
                       donated;
                                 other levels:
                                                did.not
                                 2001e1
         target level:
                                                did.not
                       donated;
                                       levels:
                                                did not
         target level:
                       donated<u>:</u>
                                 1550he<u>r</u>
                                       levels:
         target level:
                       donate \overline{B}
                                 1000he<u>r</u>
                                       levels:
         target level:
                                       levels:
                       donated;
                                 odher
         target level:
                                       levels: did not
                       donated;
                                 other
                                 other levels:
                                                did.no
         target level:
                       donated;
                                                     0.00
                                                           0.02
                                                                 0.04
                                         -0.04
                                               -0.02
         target level:
                       donated;
                                 other levels:
                                                did.not
                                                diffprop
         target level: donated;
                                 other levels:
         target level: donated;
                                 other levels:
         target level: donated;
                                 other levels: did.not
         target level:
                       donated:
                                 other levels: did.not
  3. Strength of evidence: donated;
                                 other levels: did.not
         target level: donated; other levels: did.not
                                                                                           Exploration 5.3.6b
     favstats(~diffprop, data = sim.blood)
                                  median
                                                  03
                                                           max
                                                                        mean
                                                                                     sd
      missing
     prop(~(diffprop \le -0.018 \mid diffprop \ge 0.018), data = sim.blood)
      TRUE
     0.1948
         target level: donated; other levels: did.not
         target level: donated; other levels: did.not
         target level: donated; other levels: did.not
     Normal approximation (using simulated standard deviation):
         target level: donated; other levels: did.not
         taraat lawal. danatad. athan lawala.
                                                                                           Exploration5.3.8
     sd <- sd(~diffprop, data = sim.blood)</pre>
     2 * xpnorm(0.018, 0, sd, lower.tail = FALSE) # 2 times because two-sided
     If X ^{\sim} N(0,0.0142690163196014), then
     P(X \le 0.018) = P(Z \le 1.261) = 0.8964
     P(X > 0.018) = P(Z > 1.261) = 0.1036
     [1] 0.2071379
         target level: donated; other levels: did.not
Last Modified May 19,2019 nated; other levels: did.not
                                                                                             ©2014
         target level: donated;
                                 other levels:
```

target level: donated;

other levels:

did.not



Approximate test for difference in proportions:

```
prop.test(response ~ year, data = Blood)

2-sample test for equality of proportions with continuity correction

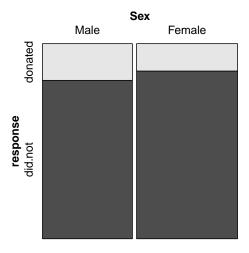
data: tally(response ~ year)
X-squared = 1.4668, df = 1, p-value = 0.2258
alternative hypothesis: two.sided
95 percent confidence interval:
    -0.01065634    0.04659768
sample estimates:
    prop 1    prop 2
0.8458150    0.8278443
```

```
Blood2 <- rbind(
do(239) * data.frame(response = "donated", Sex = "Male"),
do(201) * data.frame(response = "donated", Sex = "Female"),
do(1032) * data.frame(response = "did.not", Sex = "Male"),
do(1226) * data.frame(response = "did.not", Sex = "Female")
)
```

```
tally(response ~ Sex, data = Blood2, margin = TRUE)
```

```
Sex
response Male Female
  donated 239
                  201
 did.not 1032
                 1226
 Total 1271
                 1427
tally(response ~ Sex, data = Blood2, format = "prop")
        Sex
response
              Male
                      Female
  donated 0.1880409 0.1408549
  did.not 0.8119591 0.8591451
diffprop(response ~ Sex, data = Blood2)
   diffprop
-0.04718597
```

```
mosaic(response ~ Sex, data = Blood2, dir = "v")
```



- 1. H_0 : $\pi_{female} \pi_{male} = 0$ H_a : $\pi_{female} \pi_{male} \neq 0$ Test statistic: $\hat{p}_{female} \hat{p}_{male} = -0.0472$ (the difference in the conditional sample proportions)
- 2. We simulate a world in which $\pi_{female} \pi_{male} = 0$:

```
sim.blood2 <- do(5000) * diffprop(shuffle(response) ~ Sex, data = Blood2)

target level: donated; other levels: did.not
target level: donated; other levels: did.not</pre>
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                                      did.not
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                                      did.not
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels: did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated; other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

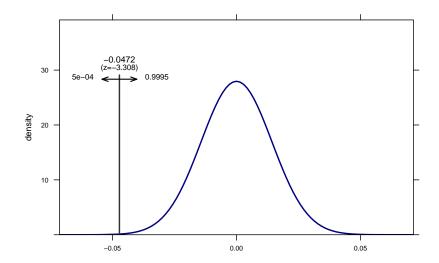
```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level: donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                       did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level: donated; other levels: did.not
```

```
target level: donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                       did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated:
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
                        other levels: did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels:
                                       did.not
              donated;
target level:
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
target level:
                        other levels:
                                      did.not
              donated;
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels:
                                      did.not
              donated;
                                      did.not
target level:
              donated;
                        other levels:
target level:
              donated;
                        other levels:
                                      did.not
                        other levels: did.not
target level:
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
              donated;
                        other levels:
                                      did.not
target level:
                        other levels: did.not
              donated;
target level:
                        other levels: did.not
              donated;
target level:
                        other levels:
                                      did.not
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
                        other levels: did.not
target level:
              donated;
target level: donated;
                        other levels: did.not
```

```
target level: donated; other levels: did.not
         target level:
                        donated;
                                  other levels:
                                                 did.not
         target level: donated; other levels: did.not
         target level:
                        donated: other levels:
                                                 did.not
                                                                                            Exploration 5.3.15e
     favstats(~donated.Female, data = sim.blood2)
     Error in eval(expr, envir, enclos): object 'donated.Female' not found
     prop(~(donated.Female <= -0.0472 | donated.Female >= 0.0472), data = sim.blood2)
     Error in eval(expr, envir, enclos): object 'donated.Female' not found
         target level: donated; other levels: did.not
     Normal approximation (using simulated standard deviation): target level: donated; other levels: did.not
                                                                                            Exploration5.3.15f
     sd <- sd(~donated.Female, data = sim.blood2)</pre>
     Error in eval(expr, envir, enclos): object 'donated.Female' not found
     2 * xpnorm(-0.0472, 0, sd, xlim = 0 + c(-5, 5) * sd) # 2 times because two-sided
     If X ^{\sim} N(0,0.0142690163196014), then
    P(X \le -0.0472) = P(Z \le -3.308) = 5e-04
    P(X > -0.0472) = P(Z > -3.308) = 0.9995
     [1] 0.0009400964
         target level: donated; other levels: did.not
        target level: donated; other levels: did.not
©2014
                                                                           Last Modified: May 19, 2015
         target level: donated; other levels: did.not
```

target level: donated; other levels: did.not



Approximate test for difference in proportions:

```
prop.test(response ~ Sex, data = Blood2)

2-sample test for equality of proportions with continuity correction

data: tally(response ~ Sex)
X-squared = 10.623, df = 1, p-value = 0.001117
alternative hypothesis: two.sided
95 percent confidence interval:
    0.01838452    0.07598742
sample estimates:
    prop 1    prop 2
0.1880409    0.1408549
```

6

Comparing Two Means

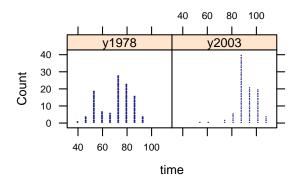
6.1 Comparing Two Groups: Quantitative Response

Example 6.1: Geyser Eruptions

```
head(OldFaithful, 3)

year time
1 y1978    78
2 y1978    74
3 y1978    68

dotPlot(~time | year, data = OldFaithful)
```



```
fivenum(~time, data = OldFaithful)

[1] 42 73 84 91 110

fivenum(time ~ year, data = OldFaithful)
```

```
y19781 y19782 y19783 y19784 y19785 y20031 y20032 y20033 y20034 y20035
42.0 59.0 75.0 80.5 95.0 56.0 87.0 91.0 97.0 110.0
```

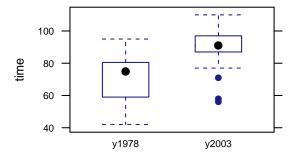
```
IQR(~time, data = OldFaithful)

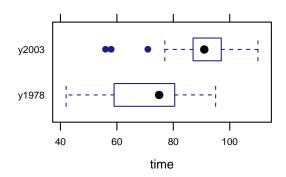
[1] 18

IQR(~time | year, data = OldFaithful)

y1978 y2003
20.75 10.00
```

```
bwplot(time ~ year, data = OldFaithful)
bwplot(year ~ time, data = OldFaithful, horizontal = TRUE)
```



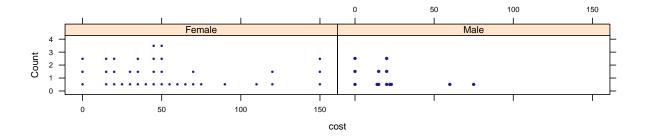


Exploration 6.1A: Haircut Prices

```
head(Haircuts)

sex cost
1 Female 50
2 Male 20
3 Female 60
4 Male 75
5 Female 150
6 Male 23
```

```
Exploration6.1A.4
dotPlot(~cost | sex, data = Haircuts, width = 1, cex = 0.25)
```



```
favstats(~cost | sex, data = Haircuts)

sex min 01 median 03 max mean sd n missing
1 Female 0 25  45 70 150 54.05405 41.61393 37 0
2 Male 0 14  20 22 75 21.84615 22.13536 13 0
```

```
diffmean(cost ~ sex, data = Haircuts)

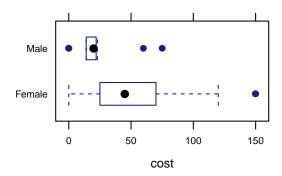
diffmean
-32.2079
Exploration6.1A.10
```

Further Analyses

```
median(cost ~ sex, data = Haircuts)

Female Male
    45    20
```

```
bwplot(sex ~ cost, data = Haircuts, horizontal = TRUE)
```



```
IQR(cost ~ sex, data = Haircuts)
Female Male
45 8
```

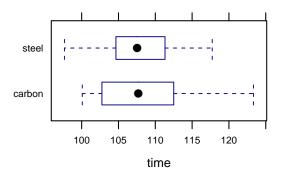
6.2 Comparing Two Means: Simulation-Based Approach

Example 6.2: Bicycling to Work

```
head(BikeTimes)

frame time
1 steel 115.7500
2 steel 115.6667
3 steel 108.7333
4 steel 117.7333
5 steel 112.6167
6 steel 109.5667
```

```
bwplot(frame ~ time, data = BikeTimes, horizontal = TRUE)
```

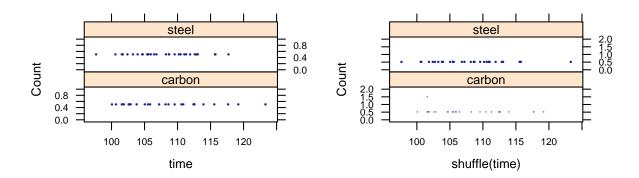


```
dotPlot(~time | frame, data = BikeTimes, width = 0.01, cex = 0.1, layout = c(1, 2))
diffmean(time ~ frame, data = BikeTimes)

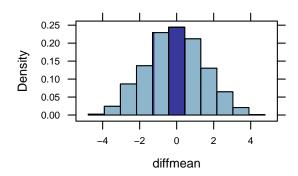
diffmean
-0.5347007

dotPlot(~shuffle(time) | frame, data = BikeTimes, width = 0.01, cex = 0.1, layout = c(1, 2))
diffmean(shuffle(time) ~ frame, data = BikeTimes)

diffmean
-0.9355555
```



- 1. H_0 : $\mu_{carbon} \mu_{steel} = 0$ H_a : $\mu_{carbon} \mu_{steel} \neq 0$ Test statistic: $\bar{x}_{carbon} \bar{x}_{steel} = 0.53$ (the difference in the sample means)
- 2. We simulate a world in which $\mu_{carbon} \mu_{steel} = 0$:



3. Strength of evidence:

Estimating a confidence interval

Determining a 95% confidence interval using the 2SD Method and standard deviation of the null distribution:

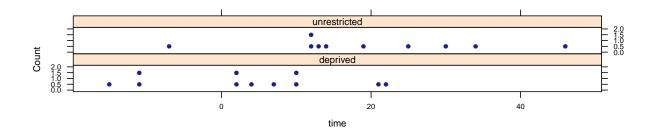
```
diff <- -diffmean(time ~ frame, data = BikeTimes) # note the negative sign
sd <- sd(~diffmean, data = sim.bike)
diff - 2 * sd # lower limit of 95% CI

diffmean
-2.501939
diff + 2 * sd # upper limit of 95% CI</pre>
diffmean
3.57134
```

Exploration 6.2: Lingering Effects of Sleep Deprivation

```
head(Sleep)
```

```
sleep time
1 unrestricted -7.0
2 unrestricted 11.6
3 unrestricted 12.1
4 unrestricted 12.6
5 unrestricted 14.5
6 unrestricted 18.6
```



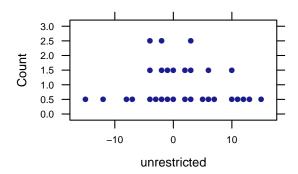
```
diff(mean(shuffle(time) ~ sleep, data = Sleep))

unrestricted
    3.95

sample <- do(30) * diff(mean(shuffle(time) ~ sleep, data = Sleep))
head(sample, 3)

unrestricted
1    -0.5936364
2    10.7463636
3    14.9463636

dotPlot(~unrestricted, data = sample, width = 1, cex = 0.25)</pre>
```



- 1. H_0 : $\mu_{unrestricted} \mu_{deprived} = 0$
 - H_a : $\mu_{unrestricted} \mu_{deprived} > 0$

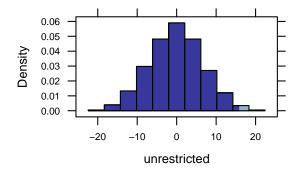
Test statistic: $\bar{x}_{unrestricted} - \bar{x}_{deprived} = 15.92$ (the difference in the sample means)

2. We simulate a world in which $\mu_{unrestricted} - \mu_{deprived} = 0$:

```
sim.sleep <- do(1000) * diff(mean(shuffle(time) ~ sleep, data = Sleep))
head(sim.sleep, 3)

unrestricted
1    3.377273
2    8.570000
3    -4.755455

histogram(~ unrestricted, data = sim.sleep,
    groups = (unrestricted >= 15.92))
```



3. Strength of evidence:

Determining a 95% confidence interval using the 2SD Method and standard deviation of the null distribution:

```
diff <- diff(mean(time ~ sleep, data = Sleep))
sd <- sd(~unrestricted, data = sim.sleep)
diff - 2 * sd # lower limit of 95% CI

unrestricted
    2.371878

diff + 2 * sd # upper limit of 95% CI

unrestricted
    29.46812
```

Another statistic

```
median(time ~ sleep, data = Sleep)

deprived unrestricted
    4.50     16.55

diff(median(time ~ sleep, data = Sleep))

unrestricted
    12.05
```

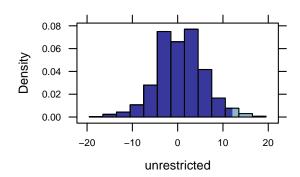
- 1. H_0 : median_{unrestricted} median_{deprived} = 0 H_a : median_{unrestricted} median_{deprived} > 0

 Test statistic: median_{unrestricted} median_{deprived} = 12.05 (the difference in the sample medians)
- 2. We simulate a world in which median_{unrestricted} median_{deprived} = 0:

```
sim.med <- do(1000) * diff(median(shuffle(time) ~ sleep, data = Sleep))
head(sim.med, 3)

unrestricted
1     3.05
2     3.95
3     2.10

histogram(~ unrestricted, data = sim.med,
     groups = (unrestricted >= 12.05),
     width = 3)
```



3. Strength of evidence:

```
favstats(~unrestricted, data = sim.med)

min Q1 median Q3 max mean sd n missing
-16.5 -2.3 -0.5 3.55 17.05 0.4765 5.19492 1000 0

prop(~(unrestricted >= 12.05), data = sim.med)

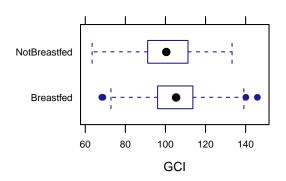
TRUE
0.021
```

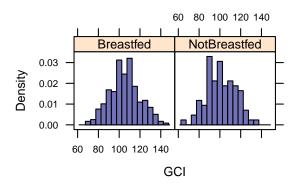
6.3 Comparing Two Means: Theory-Based Approach

Example 6.3: Breastfeeding and Intelligence

```
head(BreastFeedIntell)
                                                                                                  Table6.4
    feeding
                GCI
1 Breastfed 126.701
2 Breastfed 124.692
3 Breastfed 99.787
4 Breastfed 104.966
5 Breastfed 97.252
6 Breastfed 131.276
favstats(GCI ~ feeding, data = BreastFeedIntell)
       feeding
                  min
                          Q1 median
                                          Q3
                                                 max mean
                                                                  sd
                                                                       n missing
    Breastfed 68.330 96.083 105.366 113.677 145.889 105.3 14.49998 237
2 NotBreastfed 63.408 91.127 100.485 111.243 133.226 100.9 13.99997 85
diffmean(GCI ~ feeding, data = BreastFeedIntell)
diffmean
-4.40005
```

```
bwplot(feeding ~ GCI, horizontal = TRUE, data = BreastFeedIntell)
histogram(~GCI | feeding, data = BreastFeedIntell, width = 5)
```





- 1. H_0 : $\mu_{breastfed} \mu_{not} = 0$
 - H_a : $\mu_{breastfed} \mu_{not} \neq 0$

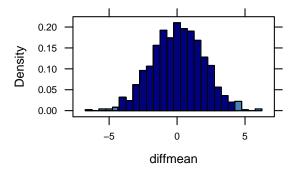
Test statistic: $\bar{x}_{breastfed} - \bar{x}_{not} = 4.40$ (the difference in the sample means)

2. We simulate a world in which $\mu_{breast fed} - \mu_{not} = 0$:

```
sim.GCI <- do(1000) * diffmean(shuffle(GCI) ~ feeding, data = BreastFeedIntell)
head(sim.GCI, 3)

diffmean
1    3.511704
2    -1.579765
3    -2.509369

histogram(~ diffmean, data = sim.GCI, width = 0.5,
    group = cut(diffmean, c(-7, -4.40, 4.40, 7)),
    fcol = c("steelblue", "navy", "steelblue"))</pre>
```



3. Strength of evidence:

Determining a 95% confidence interval using the 2SD Method and standard deviation of the null distribution:

```
diff <- -diffmean(GCI ~ feeding, data = BreastFeedIntell) # note the negative sign
sd <- sd(~diffmean, data = sim.GCI)
sd

[1] 1.884651

diff - 2 * sd # lower limit of 95% CI

diffmean
0.6307471

diff + 2 * sd # upper limit of 95% CI</pre>
```

Exploration 6.3: Close Friends

```
head(CloseFriends)
                                                                                  Exploration6.3.1
 sex friends
1 Men
          0
2 Men
         0
3 Men
4 Men
        0
5 Men
          0
6 Men
          0
tally(~friends + sex, data = CloseFriends, margin = TRUE)
      sex
friends Men Women Total
       196 201 397
 1
       135
            146
                  281
 2
       108 155 263
 3
       100 132 232
 4
       42 86 128
 5
       40 56 96
            37 70
 6
       33
Total 654 813 1467
```

```
favstats(friends ~ sex, data = CloseFriends)

sex min Q1 median Q3 max mean sd n missing

1 Men 0 0 1 3 6 1.860856 1.777147 654 0

2 Women 0 1 2 3 6 2.088561 1.760130 813 0

diffmean(friends ~ sex, data = CloseFriends)

diffmean

0.2277046
```

```
1. H_0: \mu_{men} - \mu_{women} = 0
H_a: \mu_{men} - \mu_{women} \neq 0
Test statistic: \bar{x}_{men} - \bar{x}_{women} = -0.228 (the difference in the sample means)
```

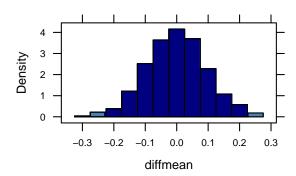
2. We simulate a world in which $\mu_{men} - \mu_{women} = 0$:

```
sim.fri <- do(1000) * diffmean(friends ~ shuffle(sex), data = CloseFriends)

head(sim.fri, 3)

diffmean
1 -0.012333977
2 -0.153046255
3 -0.006815848
```

```
histogram(~ diffmean, data = sim.fri, width = 0.05,
     group = cut(diffmean, c(-0.4, -0.228, 0.228, 0.4)),
     fcol = c("steelblue", "navy", "steelblue"))
```



3. Strength of evidence:

```
t.test(friends ~ sex, data = CloseFriends)

Welch Two Sample t-test

data: friends by sex
t = -2.4497, df = 1392.8, p-value = 0.01442
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
-0.41004255 -0.04536669
sample estimates:
mean in group Men mean in group Women
1.860856 2.088561

stat(t.test(friends ~ sex, data = CloseFriends))
```

```
pval(t.test(friends ~ sex, data = CloseFriends))

p.value
0.01441824
```

Validity Conditions

Paired Data: One Quantitative Variable

7.1 Paired Designs

7.2 Simulation-Based Approach for Analyzing Paired Data

Example 7.2: Rounding First Base (continued)

Let's begin by creating a data frame that organizes this data differently. We'll call the new data frame First-Base2.

```
6 5.55 5.60

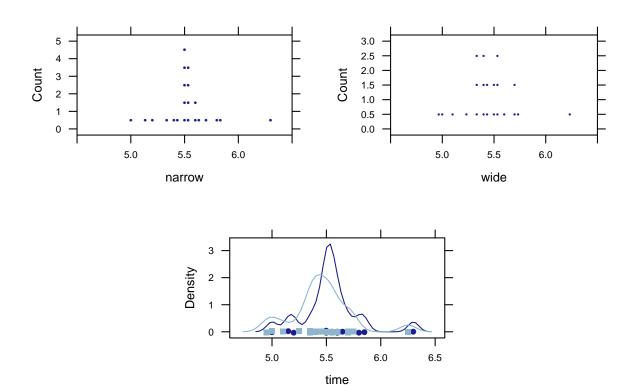
7 5.40 5.35

8 5.50 5.35

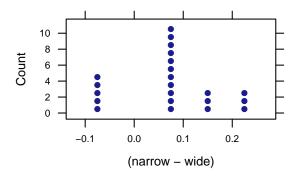
9 5.15 5.00

10 5.80 5.70
```

```
dotPlot(~narrow, data = FirstBase, nint = 40, cex = 0.2, xlim = c(4.5, 6.5))
dotPlot(~wide, data = FirstBase, nint = 40, cex = 0.1, xlim = c(4.5, 6.5))
densityplot(~time, groups = angle, data = FirstBase2)
```



```
dotPlot(~(narrow - wide), data = FirstBase)
```



```
Table7.3
Swap.Base <- swap(FirstBase, c("narrow", "wide"))</pre>
Swap.Base
   narrow wide
1
     5.50 5.55
2
     5.70 5.75
3
     5.60 5.50
     5.40 5.50
4
5
     5.85 5.70
6
     5.55 5.60
7
     5.40 5.35
8
     5.50 5.35
9
     5.00 5.15
     5.80 5.70
10
     5.10 5.20
11
12
     5.55 5.45
13
     5.35 5.45
14
     5.00 4.95
15
     5.40 5.50
16
     5.55 5.50
17
     5.35 5.55
18
     5.50 5.55
19
     5.45 5.25
20
     5.40 5.60
21
     5.55 5.65
22
     6.30 6.25
mean(~(narrow - wide), data = Swap.Base)
[1] -0.01136364
```

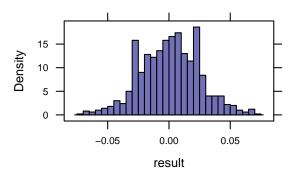
We simulate a world in which $\mu_d = 0$:

```
Sim.Base <- do(1000) * mean(~ (narrow - wide), data = swap(FirstBase, c("narrow", "wide")))
head(Sim.Base, 3)

result
1 0.002272727
```

```
2 -0.006818182
3 -0.020454545

histogram(~ result, data = Sim.Base, width = 0.005, center = 0.0025)
```



```
histogram(~result, data = Sim.Base, width = 0.005, center = 0.0025, groups = (result >= 0.075))

sd <- sd(~result, data = Sim.Base)

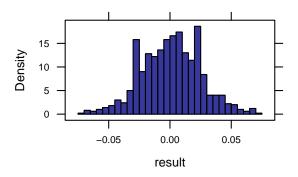
sd

[1] 0.02417083

0.075 - 2 * sd

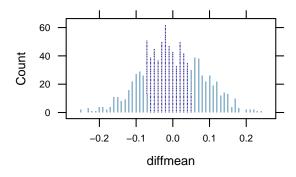
[1] 0.02665835

0.075 + 2 * sd
```



```
sim.firstbase <- do(1000) * diffmean(time ~ shuffle(angle), data = FirstBase2)
head(sim.firstbase, 3)</pre>
```

```
diffmean
1 -0.01590909
2 0.04318182
3 0.03409091
favstats(~diffmean, data = sim.firstbase)
                Q1
                       median
                                   Q3
                                          max
                                                   mean
missing
     0
dotPlot(~diffmean, data = sim.firstbase, nint = 50, groups = (diffmean <= -0.075 | diffmean >=
prop(~(diffmean <= -0.075 | diffmean >= 0.075), data = sim.firstbase)
   target level: TRUE; other levels: FALSE
TRUE
0.384
```



Exploration 7.2: Exercise and Heart Rate

```
favstats(~JJ, data = JJvsBicycle)
Exploration7.2.7
```

```
min Q1 median Q3 max mean sd n missing
70 102.25 115 129.25 146 114.6364 19.5705 22 0

favstats(~bicycle, data = JJvsBicycle)

min Q1 median Q3 max mean sd n missing
70 87.25 97.5 121.75 143 102.6818 20.65911 22 0

mean(~(JJ - bicycle), data = JJvsBicycle)

[1] 11.95455
```

```
swap.bike <- swap(JJvsBicycle, c("JJ", "bicycle"))
mean(~(JJ - bicycle), data = swap.bike)

[1] -2.954545

sd(~(JJ - bicycle), data = swap.bike)

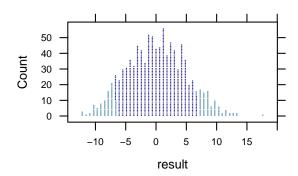
[1] 23.33499</pre>
```

1. H_0 : $\mu_d = 0$

 H_a : $\mu_d \neq 0$

Test statistic: $\bar{x}_d = -6.773$ (the mean difference in sample)

2. We simulate a world in which $\mu_d = 0$:



3. Strength of evidence:

Standarized statistic:

```
sd <- sd(~result, data = sim.bike)
xpnorm(-6.773, 0, sd, plot = FALSE)

If X ~ N(0,4.82659265076836), then

P(X <= -6.773) = P(Z <= -1.403) = 0.0803
P(X > -6.773) = P(Z > -1.403) = 0.9197
[1] 0.08026856
```

95% confidence interval using 2SD Method:

```
sd <- sd(~result, data = sim.bike)

-6.773 - 2 * sd

[1] -16.42619

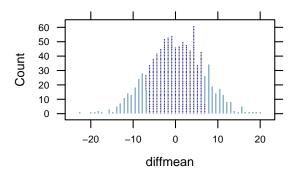
-6.773 + 2 * sd

[1] 2.880185
```

Let's again create the stacked data.

```
Exploration7.2.17
require(tidyr)
JJvsBicycle2 <- JJvsBicycle %>% gather(key = exercise, value = heartrate, JJ:bicycle)
sample(JJvsBicycle2, 5)
   exercise heartrate orig.ids
32 bicycle
                   82
                             32
27 bicycle
                   111
                             27
1
         JJ
                   118
                              1
12
         JJ
                    99
                             12
25 bicycle
                    92
                             25
```

```
Exploration7.2.17b
sim.bike2 <- do(1000) * diffmean(heartrate ~ shuffle(exercise), data = JJvsBicycle2)</pre>
head(sim.bike2, 3)
      diffmean
1 -8.95454545
2 -12.50000000
3 -0.04545455
favstats(~diffmean, data = sim.bike2)
              01
                      median
                                    Q3
                                                                         n missing
                                                                   sd
                                            max
                                                       mean
 -22.86364 \ -4.25 \ 0.04545455 \ 4.409091 \ 19.68182 \ 0.02490909 \ 6.401086 \ 1000
dotPlot(~diffmean, data = sim.bike2, nint = 50, groups = (diffmean <= -6.773 | diffmean >=
    6.773))
prop("(diffmean <= -6.773 | diffmean >= 6.773), data = sim.bike2)
TRUE
0.29
```



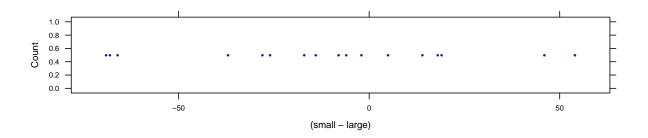
7.3 Theory-Based Approach to Analyzing Data from Paired Samples

Example 7.3: How Many M&Ms Would You Like?

```
head(BowlsMMs)
                                                                                                         Table7.4
  small large
     33
           41
     24
2
           92
3
     35
           61
4
     24
           19
5
     40
           21
     33
           35
```

```
Table7.5
favstats(~small, data = BowlsMMs)
min Q1 median Q3 max
                        mean
                                   sd n missing
           34 40 88 38.58824 16.89696 17
favstats(~large, data = BowlsMMs)
min Q1 median Q3 max
                                  sd n missing
                        mean
          42 62 104 49.47059 27.20781 17
favstats(~(small - large), data = BowlsMMs)
min Q1 median Q3 max
                          mean
                                    sd n missing
-69 -28 -8 14 54 -10.88235 36.30062 17
```

```
dotPlot(~(small - large), data = BowlsMMs, width = 1, cex = 0.05)
```



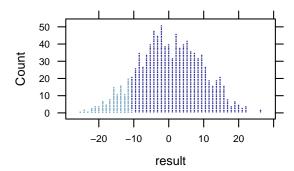
```
1. H_0: \mu_d=0 H_a: \mu_d<0 Test statistic: \bar{x}_d=-10.88 (the mean difference in paired samples)
```

2. We simulate a world in which $\mu_d = 0$:

```
sim.mm <- do(1000) * mean(~ (small - large), data = swap(BowlsMMs, c("small", "large")))
head(sim.mm, 3)

result
1 -2.294118
2 -1.352941
3 -9.941176

dotPlot(~ result, data = sim.mm, nint = 50, groups = (result <= -10.88))</pre>
```



3. Strength of evidence:

Theory-based approach

```
t.test(small, large, data = BowlsMMs, paired = TRUE, alt = "less")

Paired t-test

data: small and large
t = -1.236, df = 16, p-value = 0.1171
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
    -Inf 4.488747
sample estimates:
mean of the differences
    -10.88235
```

Exploration 7.3: comparing Auction Formats

```
head(Auction)

dutch FP
1 25 26.25
2 24 25.25
3 26 27.00
4 20 20.75
5 20 20.75
6 15 15.25
```

```
dutch FP
Min.: 0.150 Min.: 0.100
1st Qu.: 2.000 1st Qu.: 1.188
Median: 3.000 Median: 2.275
Mean: 5.162 Mean: 4.779
3rd Qu.: 7.000 3rd Qu.: 6.050
Max.: 26.000 Max.: 27.000

favstats(~(dutch - FP), data = Auction)

min Q1 median Q3 max mean sd n missing
-1.25 0 0.25 0.5 2.4 0.3835227 0.6752063 88 0
```

```
1. H_0: \mu_d = 0
```

 H_a : $\mu_d \neq 0$

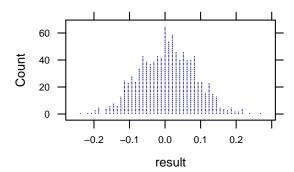
Test statistic: $\bar{x}_d = 0.384$ (the mean difference in paired samples)

2. We simulate a world in which $\mu_d = 0$:

```
sim.auction <- do(1000) * mean(~ (dutch - FP), data = swap(Auction, c("dutch", "FP")))
head(sim.auction, 3)

result
1  0.02897727
2  0.02556818
3  -0.06988636

dotPlot(~ result, data = sim.auction, groups = (result <= -0.384 | result >= 0.384), nint = 50)
```



3. Strength of evidence:

4. t-test for paired samples (theory-based approach):

```
Exploration7.3.7
t.test(Auction$dutch, Auction$FP, paired = TRUE)
Paired t-test
data: Auction$dutch and Auction$FP
t = 5.3284, df = 87, p-value = 7.692e-07
alternative hypothesis: true difference in means is not equal to {\bf 0}
95 percent confidence interval:
0.2404602 0.5265853
sample estimates:
mean of the differences
              0.3835227
t.test(~(dutch - FP), data = Auction)
One Sample t-test
data: data$(dutch - FP)
t = 5.3284, df = 87, p-value = 7.692e-07
alternative hypothesis: true mean is not equal to {\bf 0}
95 percent confidence interval:
0.2404602 0.5265853
sample estimates:
mean of x
0.3835227
```

95% confidence interval using the t-test:

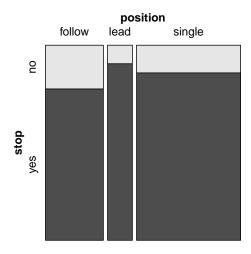


Comparing More Than Two Proportions

8.1 Simulation-Based Approach to Compare Multiple Proportions

Example 8.1: Coming to a Stop

```
Table8.1
require(vcd)
sample(Stop, 5)
   position stop orig.ids
215 lead no 215
166 single no 166
238 follow yes 238
300 follow no 300
147 single yes 147
tally(~stop + position, data = Stop, margins = TRUE)
      position
stop follow lead single Total
 no 22 4 25 51
yes 76 38 151 265
  Total 98 42 176 316
tally(stop ~ position, data = Stop)
    position
stop follow lead single
       22 4 25
 no
         76 38 151
  yes
mosaic(stop ~ position, data = Stop, direction = "v")
```



Mean Absolute Difference (MAD)

We can input the proportions to compute MAD:

```
MAD(prop(stop ~ position, data = Stop))

[1] 0.0861678
```

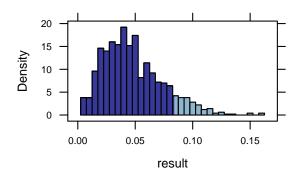
Then we can shuffle the response variable:

```
MAD(prop(shuffle(stop) ~ position, data = Stop))
[1] 0.03834261
```

- 1. H_0 : $\pi_{Single} = \pi_{Lead} = \pi_{Follow}$ H_a : At least one of the three long-run probabilities is different from the others Test statistic: MAD = 0.086 (the absolute mean difference)
- 2. We simulate a world in which MAD = 0:

```
sim.stop <- do(1000) * MAD(prop(shuffle(stop) ~ position, data = Stop))
head(sim.stop, 3)

    result
1 0.01839827
2 0.04336735
3 0.08390023
histogram(~result, data = sim.stop, width = 0.005, groups = (result >= 0.086))
```



3. Strength of evidence:

Exploration 8.1: Recruiting Organ Donors

```
head(OrganDonor)

default choice
1 opt-in donor
2 opt-in donor
3 opt-in donor
4 opt-in donor
5 opt-in donor
6 opt-in donor
```

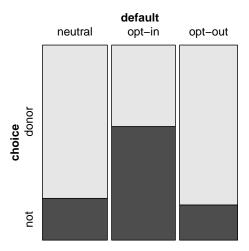
```
default

choice neutral opt-in opt-out

donor 44 23 41

not 12 32 9

mosaic(choice ~ default, data = OrganDonor, direction = "v")
```



```
MAD(prop(choice ~ default, data = OrganDonor))

[1] 0.2678788
```

1. H_0 : $\pi_{opt-in} = \pi_{opt-out} = \pi_{neutral}$

 H_a : At least one of the three long-run probabilities is different from the others

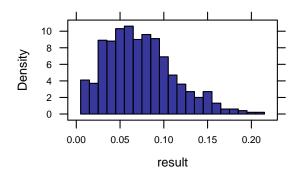
Test statistic: MAD = 0.268 (the absolute mean difference)

2. We simulate a world in which MAD = 0:

```
sim.donor <- do(1000) * MAD(prop(shuffle(choice) ~ default, data = OrganDonor))
head(sim.donor, 3)

result
1 0.13212121
2 0.11190476
3 0.09212121

histogram(~result, data = sim.donor, width = 0.01, groups = (result >= 0.268))
```



3. Strength of evidence:

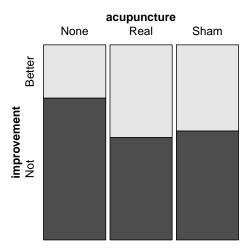
8.2 Theory-Based Approach to Compare Multiple Proportions

Example 8.2: Sham Acupuncture

```
Table8.2
sample(Acupuncture, 5)
    acupuncture improvement orig.ids
335
           Sham
                      Better
444
           None
                      Better
                                 444
352
           Sham
                      Better
                                 352
1005
           None
                        Not
                                 1005
433
           None
                      Better
                                 433
tally(~improvement + acupuncture, data = Acupuncture, margins = TRUE)
          acupuncture
improvement None Real Sham Total
    Better 106 184 171
                             461
    Not
            282 203
                      216
                             701
    Total
            388 387 387
                           1162
tally(improvement ~ acupuncture, data = Acupuncture)
```

```
acupuncture
improvement None Real Sham
Better 106 184 171
Not 282 203 216
```

```
mosaic(improvement ~ acupuncture, data = Acupuncture, direction = "v")
MAD(prop(improvement ~ acupuncture, data = Acupuncture))
[1] 0.1348375
```



1. H_0 : $\pi_{real} = \pi_{sham} = \pi_{none}$

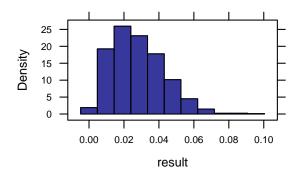
 H_a : At least one of the three long-run probabilities is different from the others

Test statistic: MAD = 0.135 (the absolute mean difference)

2. We simulate a world in which MAD = 0:

```
sim.acu <- do(1000) * MAD(prop(shuffle(improvement) ~ acupuncture, data = Acupuncture))
head(sim.acu, 3)

    result
1 0.02583979
2 0.01961516
3 0.01307973
histogram(~result, data = sim.acu, groups = (result >= 0.135))
```



3. Strength of evidence:

Theory-based approach: The chi-square test

For the chi-square test, data must be tabulated.

```
acu.table <- tally(~improvement + acupuncture, data = Acupuncture)
acu.table

acupuncture
improvement None Real Sham
Better 106 184 171
Not 282 203 216

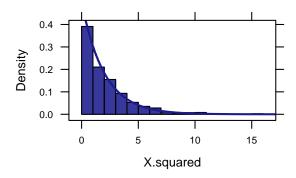
chisq.test(acu.table)

Pearson's Chi-squared test
data: acu.table
X-squared = 38.054, df = 2, p-value = 5.453e-09
```

```
sim.acuX2 <- do(1000) * chisq.test(tally(~shuffle(improvement) + acupuncture, data = Acupuncture))$statistic
head(sim.acuX2, 3)</pre>
```

```
X.squared
1    1.347661
2    3.420586
3    2.489779

histogram(~X.squared, data = sim.acuX2, width = 1, center = 0.5, groups = X.squared >= 38.05)
plotDist("chisq", df = 2, add = TRUE)
```



```
Figure8.8
xchisq.test(acu.table) # with cell contributions and expected counts
Pearson's Chi-squared test
X-squared = 38.054, df = 2, p-value = 5.453e-09
 106
         184
                  171
(153.93) (153.53) (153.53)
[14.92] [6.05] [1.99]
<-3.86> < 2.46> < 1.41>
  282
          203
                   216
(234.07) (233.47) (233.47)
[ 9.82] [ 3.98] [ 1.31]
< 3.13> <-1.99> <-1.14>
key:
observed
(expected)
[contribution to X-squared]
<residual>
```

Exploration 8.2: Conserving Hotel Towels

```
head(Towels)

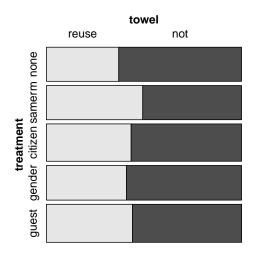
Exploration8.2.2
```

```
towel none samerm citizen gender guest
reuse 113 151 145 127 150
not reuse 192 155 189 183 190
```

Here, we can see that the data set is already in table format. But let's also store it as a data frame for future use.

```
Towels
          treatment
towe1
           none samerm citizen gender guest
           113 151 145 127
 reuse
                                      150
 not reuse 192
                  155
                                 183
                                       190
                          189
Towels1 <- rbind(
 do(113) * data.frame(treatment = "none",
                                              towel = "reuse"),
 do(192) * data.frame(treatment = "none",
                                              towel = "not"),
 do(151) * data.frame(treatment = "samerm",
                                              towel = "reuse"),
 do(155) * data.frame(treatment = "samerm",
                                             towel = "not"),
 do(145) * data.frame(treatment = "citizen", towel = "reuse"),
 do(189) * data.frame(treatment = "citizen", towel = "not"),
 do(127) * data.frame(treatment = "gender", towel = "reuse"),
 do(183) * data.frame(treatment = "gender",
                                              towel = "not"),
                                              towel = "reuse"),
 do(150) * data.frame(treatment = "guest",
 do(190) * data.frame(treatment = "guest",
                                              towel = "not")
```

```
Exploration8.2.5
prop.table(Towels, margin = 2)
           treatment
towe1
                 none
                         samerm citizen
                                              gender
            0.3704918 \ 0.4934641 \ 0.4341317 \ 0.4096774 \ 0.4411765
  not reuse 0.6295082 0.5065359 0.5658683 0.5903226 0.5588235
tally(towel ~ treatment, data = Towels1)
       treatment
towel none samerm citizen gender guest
 reuse 113
              151
                       145
                               127
                                    150
         192
                155
                        189
                               183
                                    190
 not
mosaic(towel ~ treatment, data = Towels1)
```



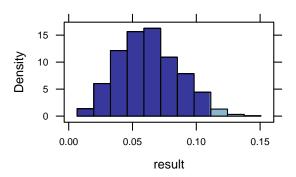
```
MAD(prop(towel ~ treatment, data = Towels1))

[1] 0.1109774

sim.towel <- do(1000) * MAD(prop(shuffle(towel) ~ treatment, data = Towels1))
head(sim.towel, 3)

    result
1 0.00687602
2 0.05258570
3 0.04466305

histogram(~result, data = sim.towel, groups = (result >= 0.111))
prop(~(result >= 0.111), data = sim.towel)
TRUE
0.024
```



```
prop(~towel, data = Towels1)
    reuse
0.430094
Exploration8.2.7
```

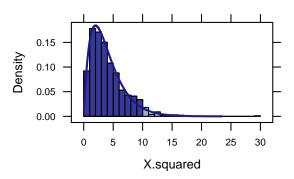
```
chisq.test(Towels)

Pearson's Chi-squared test
data: Towels
X-squared = 10.153, df = 4, p-value = 0.03792

sim.towelX2 <- do(1000) * chisq.test(tally(~shuffle(towel) + treatment, data = Towels1))$statistic head(sim.towelX2, 3)

X.squared
1  7.782173
2  2.882825
3  2.127759

histogram(~X.squared, data = sim.towelX2, width = 1, center = 0.5, groups = X.squared >= 10.153)
plotDist("chisq", df = 4, add = TRUE)
```



Follow-up Analysis

Exploration 8.2b: Near-sightedness and Nighlights revisited

```
NightLight1

Darkness NightLight RoomLight
Near 18 78 41
Not 154 154 34
```

Alternative formula for chi-square statistic

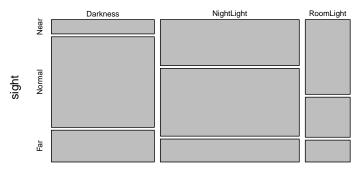
```
xchisq.test(NightLight1)
                                                                                              Exploration 8.2b.4
Pearson's Chi-squared test
data: x
X-squared = 55.519, df = 2, p-value = 8.795e-13
            78
                     41
(49.19) (66.35) (21.45)
[19.78] [ 2.04] [17.82]
<-4.45> < 1.43> < 4.22>
          154
  154
                   34
(122.81) (165.65) (53.55)
[7.92] [0.82] [7.14]
< 2.81> <-0.90> <-2.67>
key:
observed
(expected)
[\hbox{contribution to $X$-squared}]
<residual>
```

We can see that NightLight1 is in table format. Let's create new data frame it for some easier analysis.

```
NightLight2
               light
sight
                Darkness NightLight RoomLight
                                                41
  Nearsighted
                      18
                                   78
                                                22
  Normal
                      114
                                   115
  Farsighted
                       40
                                    39
                                                12
NightLight <- rbind(</pre>
  do(18) * data.frame(light = "Darkness", sight = "Near"),
  do(114) * data.frame(light = "Darkness", sight = "Normal"),
  do(40) * data.frame(light = "Darkness", sight = "Far"),
do(78) * data.frame(light = "NightLight", sight = "Near"),
do(115) * data.frame(light = "NightLight", sight = "Normal"),
  do(39) * data.frame(light = "NightLight", sight = "Far"),
  do(41) * data.frame(light = "RoomLight", sight = "Near"),
  do(22) * data.frame(light = "RoomLight", sight = "Normal"),
  do(12) * data.frame(light = "RoomLight", sight = "Far")
```

```
mosaicplot(light ~ sight, data = NightLight)
```

NightLight



light

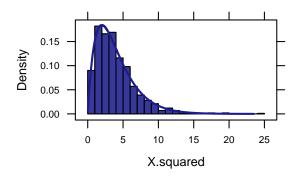
```
chisq.test(tally(~sight + light, data = NightLight))
Pearson's Chi-squared test

data: tally(~sight + light, data = NightLight)
X-squared = 56.513, df = 4, p-value = 1.565e-11
```

```
sim.nightX2 <- do(1000) * chisq.test(tally(~shuffle(light) + sight, data = NightLight))$statistic
head(sim.nightX2, 3)

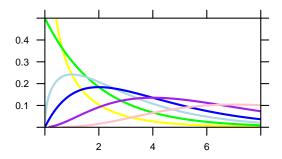
X.squared
1 2.383670
2 1.775620
3 1.571492

histogram(~X.squared, data = sim.nightX2, width = 1, center = 0.5, groups = X.squared >= 56.514)
plotDist("chisq", df = 4, add = TRUE)
```



```
Exploration8.2b.12
xchisq.test(NightLight2)
Pearson's Chi-squared test
X-squared = 56.513, df = 4, p-value = 1.565e-11
  18
           78
                    41
(49.19) (66.35) (21.45)
[19.78] [ 2.04] [17.82]
<-4.45> < 1.43> < 4.22>
  114
          115
(90.13) (121.57) (39.30)
[ 6.32] [ 0.36] [ 7.62]
< 2.51> <-0.60> <-2.76>
  40
           39
                    12
(32.68) (44.08) (14.25)
[ 1.64] [ 0.58] [ 0.35]
< 1.28> <-0.76> <-0.60>
key:
observed\\
(expected)
[contribution to X-squared]
<residual>
```

```
plotDist("chisq", params = list(df = 1), col = "yellow", ylim = c(0, 0.5), xlim = c(0, 8))
plotDist("chisq", params = list(df = 2), col = "green", add = TRUE)
plotDist("chisq", params = list(df = 3), col = "lightblue", add = TRUE)
plotDist("chisq", params = list(df = 4), col = "blue", add = TRUE)
plotDist("chisq", params = list(df = 6), col = "purple", add = TRUE)
plotDist("chisq", params = list(df = 9), col = "pink", add = TRUE)
```



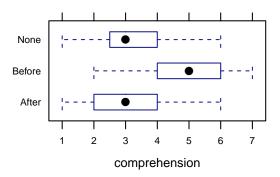
9

Comparing More than Two Means

9.1 Simulation-Based Approach for Comparing More than Two Groups with a Quantitative Response

Example 9.1: Comprehending Ambiguous Prose

```
bwplot(condition ~ comprehension, data = Comprehension, horizontal = TRUE)
Figure 9.2
```



```
MAD(mean(comprehension ~ condition, data = Comprehension))
[1] 1.157895
```

1. H_0 : $\pi_{After} = \pi_{Before} = \pi_{None}$

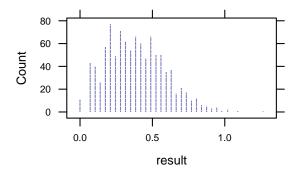
 H_a : At least one of the three long-run probabilities is different from the others Test statistic: MAD = 1.16 (the mean absolute difference)

2. We simulate a world in which MAD = 0:

```
sim.comp <- do(1000) * MAD(mean(shuffle(comprehension) ~ condition, data = Comprehension))
head(sim.comp, 3)

result
1 0.3859649
2 0.5263158
3 0.4912281

dotPlot(~result, data = sim.comp, width = 0.005, groups = (result >= 1.16))
```

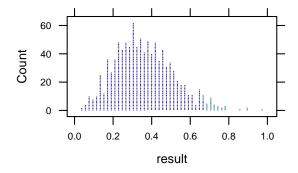


3. Strength of evidence:

Exploration 9.1: Exercise and Brain Volume

```
head(Brain)
                                                                                                         Exploration 9.1.3
  treatment brain_change
     TaiChi
                     0.987
2
     TaiChi
                     1.960
3
     TaiChi
                     0.304
4
     TaiChi
                     0.005
5
     TaiChi
                    -1.829
     TaiChi
                     1.227
```

```
Exploration 9.1.6
favstats(brain_change ~ treatment, data = Brain)
  treatment
               min
                          Q1 median
                                         Q3 max
                                                                     sd n missing
                                                         mean
       None -2.034 -1.16875 -0.585 0.9725 2.011 -0.2401250 1.2584309 24
     Social -1.359 0.00750 0.596 0.8060 1.796 0.4056296 0.6968969 27
                                                                                  0
     TaiChi -1.829 0.00500 0.449 0.9870 2.201 0.4710690 0.8557466 29
                                                                                  0
4 Walking -3.470 -1.05850 -0.026 0.9710 1.833 -0.1503333 1.3868388 27
                                                                                  0
                                                                                                 Exploration9.1.13
MAD(mean(brain_change ~ treatment, data = Brain))
[1] 0.6723862
                                                                                                 Exploration9.1.16
MAD(mean(shuffle(brain_change) ~ treatment, data = Brain))
[1] 0.4693284
                                                                                                  Exploration9.1.19
sim.brain <- do(1000) * MAD(mean(shuffle(brain_change) ~ treatment, data = Brain))</pre>
head(sim.brain, 3)
     result
1 0.3482152
2 0.2412166
3 0.4617909
```



dotPlot(~result, data = sim.brain, n = 50, groups = (result >= 0.672))

```
prop(~(result >= 0.672), data = sim.brain)
TRUE
0.034
```

```
sim.10000 <- do(10000) * MAD(mean(shuffle(brain_change) ~ treatment, data = Brain))
head(sim.10000, 3)

    result
1 0.4116506
2 0.2878076
3 0.3137294

prop(~(result >= 0.672), data = sim.10000)

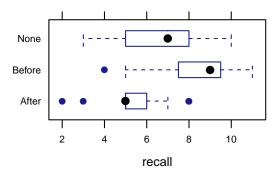
    target level: TRUE; other levels: FALSE

TRUE
0.0325
```

9.2 Theory-based Approach to Comparing More than Two Groups with a Quantitative Response

Example 9.2: Recalling Ambiguous Prose

```
bwplot(condition ~ recall, data = Recall, horizontal = TRUE)
                                                                                                Figure 9.4
favstats(recall ~ condition, data = Recall)
  condition min Q1 median Q3 max
                                                  sd n missing
                                       mean
      After
              2 5.0
                     5 6.0 8 5.368421 1.460994 19
                                                              0
2
              4 7.5
                         9 9.5 11 8.263158 1.820931 19
     Before
                                                              0
3
              3 5.0
                                                              0
       None
                         7 8.0 10 6.631579 2.005839 19
MAD(mean(recall ~ condition, data = Recall))
[1] 1.929825
```

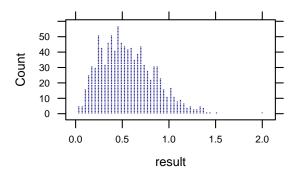


- 1. H_0 : $\pi_{After} = \pi_{Before} = \pi_{None}$
 - H_a : At least one of the three long-run probabilities is different from the others Test statistic: MAD = 1.93 (the mean absolute difference)
- 2. We simulate a world in which MAD = 0:

```
sim.recall <- do(1000) * MAD(mean(shuffle(recall) ~ condition, data = Recall))
head(sim.recall, 3)

    result
1 0.8421053
2 0.5964912
3 0.1403509

dotPlot(~result, data = sim.recall, width = 0.005, groups = (result >= 1.93))
```

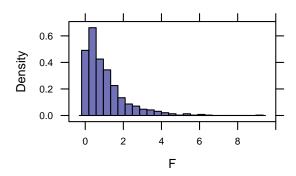


3. Strength of evidence:

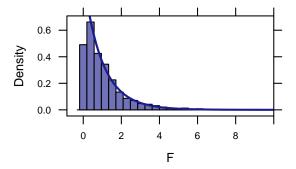
```
Figure 9.8
sim.recallF <- do(1000) * anova(lm(shuffle(recall) ~ condition, data = Recall))</pre>
head(sim.recallF, 3)
              source df
                               SS
                                                          pval .row .index
condition condition 2 10.77193 5.385965 1.212906 0.3053025
                                                                  1
                                                                         1
Residuals Residuals 54 239.78947 4.440546
                                                                          1
                                                  NA
                                                            NA
condition1 condition 2 10.77193 5.385965 1.212906 0.3053025
                                                                   1
                                                                          2
histogram(~F, data = sim.recallF, n = 25)
prop(~(F \ge 12.67), data = sim.recallF)
```

```
TRUE

0
```



```
histogram(~F, data = sim.recallF, n = 25)
plotDist("f", df1 = 2, df2 = 52, add = TRUE)
```



```
anova(lm(recall ~ condition, data = Recall))

Analysis of Variance Table

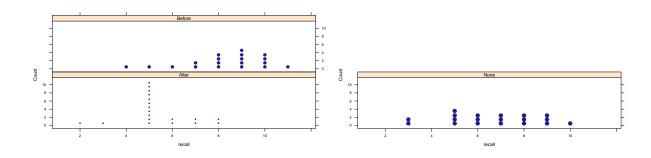
Response: recall

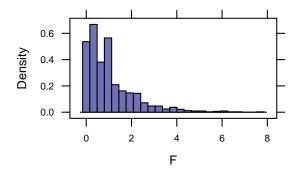
Df Sum Sq Mean Sq F value Pr(>F)
condition 2 80.035 40.018 12.672 3.074e-05 ***
Residuals 54 170.526 3.158

---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
Figure 9.11

dotPlot(~recall | condition, data = Recall, cex = 0.5, width = 1, layout = c(1, 2))
```



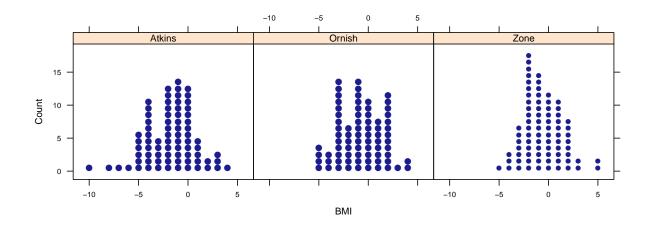


Exploration 9.2: Comparing Popular Diets

```
head(Diets1)

diet BMI
1 Atkins 0.1
```

```
2 Atkins -1.0
3 Atkins -5.4
4 Atkins -6.2
5 Atkins -4.1
6 Atkins -1.7
```



```
MAD(mean(BMI ~ diet, data = Diets1))

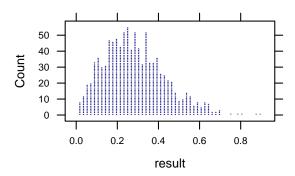
[1] 0.7468464

sim.diet <- do(1000) * MAD(mean(shuffle(BMI) ~ diet, data = Diets1))
head(sim.diet, 3)

result
1 0.5271083
2 0.2121364
3 0.2165300

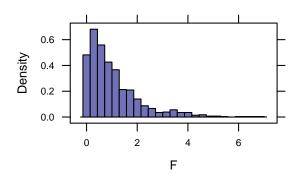
dotPlot(~result, data = sim.diet, n = 50, groups = (result >= 0.747))
prop(~(result >= 0.747), data = sim.diet)

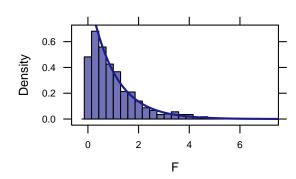
TRUE
0.005
```



```
Exploration9.2.8
anova(lm(BMI ~ diet, data = Diets1))
Analysis of Variance Table
Response: BMI
          Df Sum Sq Mean Sq F value Pr(>F)
           2
              53.96 26.9814 5.3916 0.005151 **
Residuals 229 1146.00 5.0044
Signif. codes: 0 \ '***' \ 0.001 \ '**' \ 0.05 \ '.' \ 0.1 \ ' \ '
sim.dietF \leftarrow do(1000) * anova(lm(shuffle(BMI) ~ diet, data = Diets1))
head(sim.dietF, 3)
             source df
                               SS
                                         MS
                                                   F
                                                           pval .row .index
diet
              diet 2 24.27956 12.139781 2.364591 0.09627892
                                                                 1
                                                                        1
Residuals Residuals 229 1175.68315 5.133988
                                                  NA
                                                                          1
diet1
              diet 2 16.54297 8.271487 1.600591 0.20402629
prop(~(F >= 5.392), data = sim.dietF)
TRUE
0.005
```

```
histogram(~F, data = sim.dietF, n = 25)
plotDist("f", df1 = 2, df2 = 229, add = TRUE)
```





10

Two Quantitative Variables

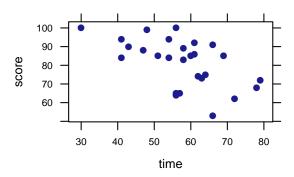
10.1 Summarizing the Relationship Between Two Quantitative Variables Using the Correlation Coefficient

Example 10.1: Exam Times and Exam Scores

Exploring the Data: Graphical Summary

Figure 10.1 plots data that have been modified to exclude 3 observations, so we will take the subset of Exam-TimesScores.

```
scores <- subset(ExamTimesScores, time < 90)
xyplot(score ~ time, data = scores)</pre>
```



Exploring the Data: Numerical Summary

```
cor(score ~ time, data = scores)

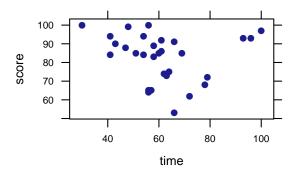
[1] -0.5636557
```

```
cor(score ~ time, data = ExamTimesScores)
[1] -0.124997
```

Caution: Influential Observations

```
xyplot(score ~ time, data = ExamTimesScores)
cor(score ~ time, data = ExamTimesScores)

[1] -0.124997
```



Exploration 10.1: Are Dinner Plates Getting Larger?

```
head(PlateSize)

year size
1 1950 10.000
2 1956 10.750
3 1957 10.125
4 1958 10.000
5 1963 10.625
6 1964 10.750
```

```
PlateSize

year size
1 1950 10.000
2 1956 10.750
3 1957 10.125
4 1958 10.000
5 1963 10.625
6 1964 10.750
```

```
7 1969 10.625

8 1974 10.000

9 1975 10.500

10 1978 10.125

11 1980 10.375

12 1986 10.750

13 1990 10.375

14 1995 11.000

15 2004 10.750

16 2004 10.125

17 2007 11.500

18 2008 11.000

19 2008 11.125

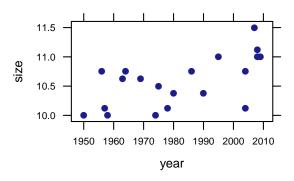
20 2009 11.000
```

Graphical summary of two-quantitative variables: Scatterplots

```
cor(size ~ year, data = PlateSize)

[1] 0.6037724

xyplot(size ~ year, data = PlateSize)
Exploration10.1.8
```



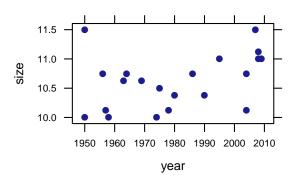
Numerical Summaries

```
cor(size ~ year, data = PlateSize)

[1] 0.6037724
Exploration10.1.15
```

Here is one way to add a new observation to an existing data frame:

```
Exploration10.1.16
PlateSize2 <- PlateSize # make a copy of data with different name
PlateSize2[21, ] <- c(1950, 11.5) # assigning values to the 21st row of data frame
PlateSize2
         size
   year
  1950 10.000
2 1956 10.750
3 1957 10.125
4 1958 10.000
   1963 10.625
6 1964 10.750
7 1969 10.625
8 1974 10.000
9 1975 10.500
10 1978 10.125
11 1980 10.375
12 1986 10.750
13 1990 10.375
14 1995 11.000
15 2004 10.750
16 2004 10.125
17 2007 11.500
18 2008 11.000
19 2008 11.125
20 2009 11.000
21 1950 11.500
xyplot(size ~ year, data = PlateSize2)
cor(size ~ year, data = PlateSize2)
[1] 0.3697467
```

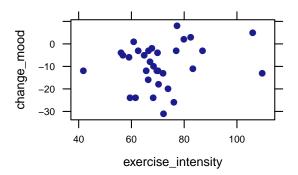


10.2 Inference for the Correlation Coefficient: A Simulation-based Approach

Example 10.2: Exercise Intensity and Mood Changes

```
ExerciseMood
                                                                                                           Table10.2
   exercise_intensity change_mood
                   72.2
                                 -31
2
                   76.1
                                 -26
3
                   68.3
                                 -24
4
                                 -24
                   61.6
5
                                  -24
                   59.5
6
                   73.9
                                 -20
7
                   70.3
                                 -18
8
                   66.4
                                 -16
9
                   65.6
                                 -12
10
                                 -12
                   69.7
11
                   70.1
                                 -12
                   72.0
12
                                 -13
13
                   83.3
                                 -11
14
                  109.6
                                 -13
                   68.4
15
                                 -10
16
                   67.1
                                  -8
17
                   59.1
                                   -6
                   41.8
                                  -12
18
19
                   56.8
                                   -5
20
                   56.1
                                   -4
21
                   62.6
                                   -3
22
                   64.9
                                   -5
23
                   66.5
                                   -3
24
                   69.9
                                   -4
25
                                   -3
                   77.0
26
                   87.0
                                   -3
                   67.8
27
                                   -2
28
                   60.9
                                   1
29
                   79.9
                                   2
30
                   82.5
                                   3
31
                   77.3
                                   8
32
                  106.0
                                   5
```

```
xyplot(change_mood ~ exercise_intensity, data = ExerciseMood)
cor(change_mood ~ exercise_intensity, data = ExerciseMood)
[1] 0.186898
```



1. H_0 : $\rho = 0$

 H_a : $\rho \neq 0$

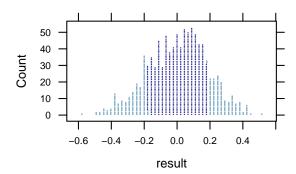
Test statistic: r = 0.187 (the sample correlation)

2. We simulate a world in which $\rho = 0$:

```
sim.mood <- do(1000) * cor(shuffle(change_mood) ~ exercise_intensity, data = ExerciseMood)
head(sim.mood, 3)

result
1 0.13900806
2 0.02069769
3 0.26876050

dotPlot(~result, data = sim.mood, n = 50, groups = (result <= -0.187 | result >= 0.187))
```

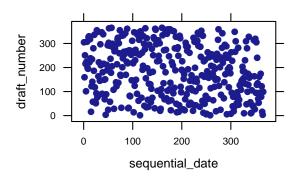


3. Strength of evidence:

Exploration 10.2: Draft Lottery

```
5 5 101
6 6 224

xyplot(draft_number ~ sequential_date, data = DraftLottery)
```



You can identify the specific row in a data set to examine a specific observation like so:

```
Exploration10.2.3
DraftLottery[32, ] # draft number for Feb 1
   sequential_date draft_number
      32 86
                                                                                               Exploration10.2.4
median(~draft_number, data = subset(DraftLottery, sequential_date >= 1 & sequential_date <=</pre>
    31)) # Jan median
[1] 215
median(~draft_number, data = subset(DraftLottery, sequential_date >= 32 & sequential_date <=</pre>
    60)) # Feb median
[1] 210
median(~draft_number, data = subset(DraftLottery, sequential_date >= 61 & sequential_date <=</pre>
    91)) # Mar median
[1] 256
median(~draft_number, data = subset(DraftLottery, sequential_date >= 92 & sequential_date <=</pre>
    121)) # Apr median
[1] 225
median(~draft_number, data = subset(DraftLottery, sequential_date >= 122 & sequential_date <=</pre>
152))  # May median
```

```
[1] 226
median(~draft_number, data = subset(DraftLottery, sequential_date >= 153 & sequential_date <=</pre>
    182))  # Jun median
[1] 207.5
median(~draft number, data = subset(DraftLottery, sequential date >= 183 & sequential date <=</pre>
    213))  # Jul median
[1] 188
median(~draft_number, data = subset(DraftLottery, sequential_date >= 214 & sequential_date <=</pre>
    243)) # Aug median
[1] 149.5
median(~draft_number, data = subset(DraftLottery, sequential_date >= 244 & sequential_date <=</pre>
    274)) # Sep median
[1] 161
median(~draft_number, data = subset(DraftLottery, sequential_date >= 275 & sequential_date <=</pre>
    304)) # Oct median
[1] 201.5
median(~draft_number, data = subset(DraftLottery, sequential_date >= 305 & sequential_date <=</pre>
    335)) # Nov median
[1] 131
median(~draft_number, data = subset(DraftLottery, sequential_date >= 336 & sequential_date <=</pre>
    366)) # Dec median
[1] 100
```

```
cor(draft_number ~ sequential_date, data = DraftLottery)
[1] -0.2260414
```

```
1. H_0: \rho = 0

H_a: \rho \neq 0

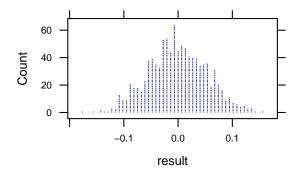
Test statistic: r = -0.226 (the sample correlation)
```

2. We simulate a world in which $\rho = 0$:

```
sim.draft <- do(1000) * cor(shuffle(draft_number) ~ sequential_date, data = DraftLottery)
head(sim.draft, 3)

result
1 -0.06224926
2 0.02188976
3 0.02020080

dotPlot(~result, data = sim.draft, n = 50, groups = (result <= -0.226 | result >= 0.226))
```



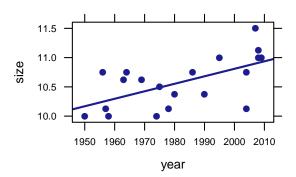
3. Strength of evidence:

10.3 Least Squares Regression

R provides the simple command 1m() to find the least squares line.

```
xyplot(size ~ year, data = PlateSize, type = c("p", "r"))
lm(size ~ year, data = PlateSize)
Call:
lm(formula = size ~ year, data = PlateSize)
```

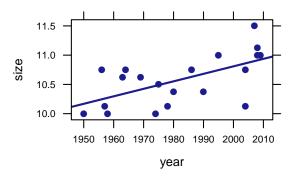
```
Coefficients:
(Intercept) year
-14.8003 0.0128
```



Note that type = c("p", "r") adds the least squares regression line to the scatterplot.

For just the coefficients:

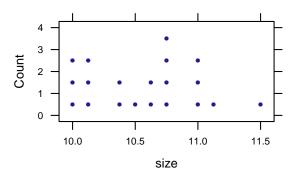
```
Figure10.8
 xyplot(size ~ year, data = PlateSize, type = c("p", "r"))
 resid(lm(size ~ year, data = PlateSize)) # residuals for each point
                                                                                                                                                                                                                                                                         2
                                                                                                                                                                                                                                                                                                                                                                                                                            3
 -0.16845690 \quad 0.50471606 \quad -0.13308845 \quad -0.27089295 \quad 0.29008451 \quad 0.40228000 \quad 0.21325747 \quad 0.40228000 \quad 0.40228000 \quad 0.21325747 \quad 0.40228000 \quad 
                                                                                                                                                                                                                                                                         9
                                                                                                                                                                                                                                                                                                                                                                                                               10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        13
 -0.47576507 \quad 0.01143042 \ -0.40198310 \ -0.17759211 \quad 0.12058084 \ -0.30563718 \quad 0.25534028 \ -0.40198310 \ -0.17759211 \ -0.12058084 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.30563718 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.25534028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.2554028 \ -0.255402
                                                                                                            15
                                                                                                                                                                                                                                                           16
                                                                                                                                                                                                                                                                                                                                                                                                             17
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  18
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         19
-0.10990028 \ -0.73490028 \ \ 0.60168619 \ \ 0.08888169 \ \ 0.21388169 \ \ 0.07607718
```

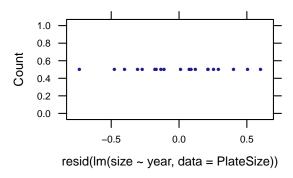


For more information, including the **coefficient of determination**, use the summary() function on the linear model.

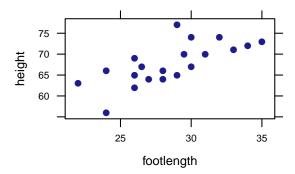
```
Figure10.8b
summary(lm(size ~ year, data = PlateSize))
Call:
lm(formula = size ~ year, data = PlateSize)
Residuals:
     Min
              10
                  Median
                                 30
                                         Max
-0.73490 -0.20092 0.04375 0.22425 0.60169
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -14.800332 7.897098 -1.874 0.07724 .
              0.012805
                        0.003985
                                    3.213 0.00482 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.3521 on 18 degrees of freedom
Multiple R-squared: 0.3645, Adjusted R-squared: 0.3292
F-statistic: 10.33 on 1 and 18 DF, p-value: 0.004818
rsquared(lm(size ~ year, data = PlateSize)) # just the r-squared
[1] 0.3645411
```

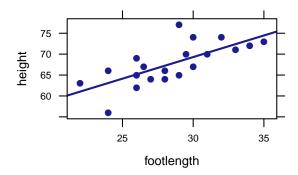
```
dotPlot(~size, data = PlateSize, width = 0.005, cex = 0.25)
dotPlot(~resid(lm(size ~ year, data = PlateSize)), width = 0.001, cex = 0.05)
```





```
xyplot(height ~ footlength, data = FootHeight)
```





```
# sum of the absolute values of the residuals of the linear model
sum(abs(resid(lm(height ~ footlength, data = FootHeight))))

[1] 54.59867
```

```
# sum of the squared residuals
deviance(lm(height ~ footlength, data = FootHeight))
[1] 235.0006
```

```
coef(lm(height ~ footlength, data = FootHeight))

(Intercept) footlength
    38.302106    1.033259
Exploration10.3.8
```

To make predictions, we can make a function out of the linear model by using the makeFun() function.

```
# assigning function of the linear model the name fh
fh <- makeFun(lm(height ~ footlength, data = FootHeight))
fh(footlength = 28) # predicted height for foot length 28

1
67.23337

fh(footlength = 29) # predicted height for foot length 29
```

```
fh(footlength = 0) # predicted height for foot length 0
1
38.30211
```

Coefficient of Determination (r^2)

```
cor(height ~ footlength, data = FootHeight)^2

[1] 0.5060419

rsquared(lm(height ~ footlength, data = FootHeight))

[1] 0.5060419
```

10.4 Inference for Regression Slope: Simulation-Based Approach

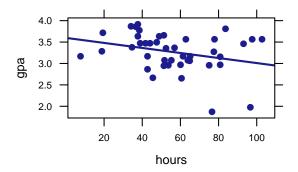
Example 10.4: Do students who spend more time in non-academic activities, tend to have lower GPAs?

```
xyplot(gpa ~ hours, data = GPA, type = c("p", "r"))
cor(gpa ~ hours, data = GPA)

[1] -0.290021

coef(lm(gpa ~ hours, data = GPA))

(Intercept) hours
3.597690950 -0.005883873
```



1. H_0 : slope = 0

 H_a : slope < 0

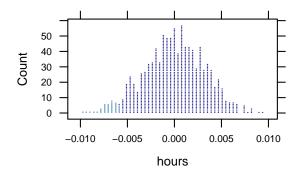
Test statistic: slope = -0.00588 (the sample slope coefficient)

2. We simulate a world in which slope = 0:

```
sim.gpa <- do(1000) * coef(lm(shuffle(gpa) ~ hours, data = GPA))
head(sim.gpa, 3)

Intercept hours
1  3.104523  0.002844396
2  3.037118  0.004037358
3  3.442636 -0.003139649

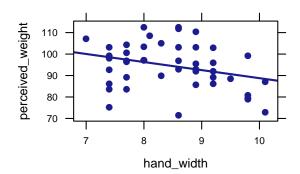
dotPlot(~hours, data = sim.gpa, n = 50, groups = (hours <= -0.00588))</pre>
```



3. Strength of evidence:

Exploration 10.4: Perceptions of Heaviness

```
Table10.4
head(Handwidth, 10)
   hand_width perceived_weight
           7.4
1
                            75.2
2
           7.4
                            83.6
3
           7.4
                            86.2
4
           7.4
                            92.6
5
           7.4
                            98.1
           7.4
6
                            99.2
7
           7.4
                            103.1
8
           7.0
                            107.2
9
           7.7
                            104.3
10
                            100.6
```



```
coef(lm(perceived_weight ~ hand_width, data = Handwidth))

(Intercept) hand_width
126.333411 -3.756255
```

1. H_0 : slope = 0

 H_a : slope < 0

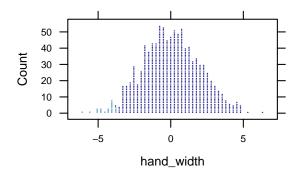
Test statistic: slope = -3.756 (the sample slope coefficient)

2. We simulate a world in which slope = 0:

```
sim.hand <- do(1000) * coef(lm(shuffle(perceived_weight) ~ hand_width, data = Handwidth))
head(sim.hand, 3)

Intercept hand_width
1 84.58420 1.17306710
2 94.14856 0.04380425
3 110.28287 -1.86117008

dotPlot(~hand_width, data = sim.hand, n = 50, groups = (hand_width <= -3.756))</pre>
```

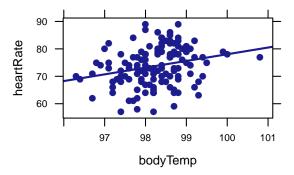


3. Strength of evidence:

10.5 Inference for the Regression Slope: Theory-Based Approach

Example 10.5A: Predicting Heart Rate from Body Temperature

```
Figure10.13
head(TempHeart)
  bodyTemp heartRate
      96.3
                   70
2
      96.7
                   71
3
      96.9
                   74
      97.0
4
                   80
5
      97.1
                   73
6
      97.1
                   75
xyplot(heartRate ~ bodyTemp, data = TempHeart, type = c("p", "r"))
```



```
coef(lm(heartRate ~ bodyTemp, data = TempHeart))

(Intercept) bodyTemp
-166.284719 2.443238
```

1. H_0 : slope = 0

 H_a : slope $\neq 0$

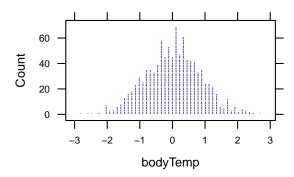
Test statistic: slope = 2.443 (the sample slope coefficient)

2. We simulate a world in which slope = 0:

```
sim.rate <- do(1000) * coef(lm(shuffle(heartRate) ~ bodyTemp, data = TempHeart))
head(sim.rate, 3)

Intercept bodyTemp
1 207.04719 -1.3566075
2 140.17331 -0.6759521
3 -92.32675 1.6904793

dotPlot(~bodyTemp, data = sim.rate, n = 50, groups = (bodyTemp <= -2.443 | bodyTemp >= 2.443))
```



3. Strength of evidence:

```
Figure 10.15

sim.ratet <- do(1000) * coef(summary(lm(shuffle(heartRate) ~ bodyTemp, data = TempHeart)))

head(sim.ratet, 10)

Estimate Std..Error t.value Pr.>|t|
(Intercept) 43.2628666 83.6046573 0.517469576 0.6057215
bodyTemp 0.3104215 0.8509211 0.364806406 0.7158580
(Intercept).1 15.2098429 83.4878494 0.182180317 0.8557294
bodyTemp.1 0.5959507 0.8497323 0.701339342 0.4843644
(Intercept).2 93.1349087 83.6305785 1.113646591 0.2675177
bodyTemp.2 -0.1971860 0.8511850 -0.231660546 0.8171716
```

```
      (Intercept).3
      -0.2334883
      83.3920153
      -0.002799888
      0.9977704

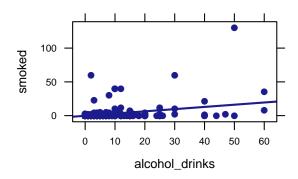
      bodyTemp.3
      0.7531359
      0.8487569
      0.887340005
      0.3765601

      (Intercept).4
      98.8021862
      83.6188202
      1.181578332
      0.2395637

      bodyTemp.4
      -0.2548686
      0.8510653
      -0.299470137
      0.7650671
```

Example 10.5B: Smoking and Drinking

```
xyplot(smoked ~ alcohol_drinks, data = AlcoholSmoke, type = c("p", "r"))
Figure 10.18
```



Caution: Outliers and Influential Observations

```
cor(smoked ~ alcohol_drinks, data = AlcoholSmoke)

[1] 0.3703078

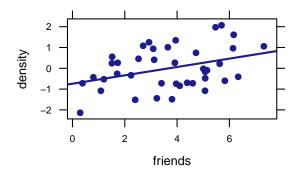
cor(smoked ~ alcohol_drinks, data = subset(AlcoholSmoke, smoked < 125))

[1] 0.3014187</pre>
```

Exploration 10.5: Predicting Brain Density from Number of Facebook Friends

```
head(Facebook)
                                                                                                    Table10.5
  friends density
     0.30
           -2.14
2
           -1.09
     1.09
3
           -0.72
     0.39
           -0.53
4
     1.20
5
     0.80
            -0.43
     1.71
          -0.26
```

```
xyplot(density ~ friends, data = Facebook, type = c("p", "r"))
```



1. H_0 : slope = 0

 H_a : $slope \neq 0$

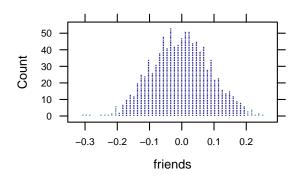
Test statistic: slope = 0.201 (the sample slope coefficient)

2. We simulate a world in which slope = 0:

```
sim.face <- do(1000) * coef(lm(shuffle(density) ~ friends, data = Facebook))
head(sim.face, 3)

Intercept    friends
1    0.14535911 -0.04008954
2  -0.28238865    0.07628066
3    0.04101383 -0.01170206

dotPlot(~friends, data = sim.face, n = 50, groups = (friends <= -0.201 | friends >= 0.201))
```



3. Strength of evidence:

```
cor(density ~ friends, data = Facebook)
[1] 0.3655156
Exploration10.5.6
```

```
summary(lm(density ~ friends, data = Facebook))

Call:
lm(formula = density ~ friends, data = Facebook)

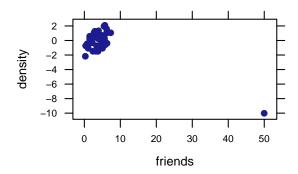
Residuals:
    Min    10  Median    30  Max
```

```
confint(lm(density ~ friends, data = Facebook))

2.5 % 97.5 %
(Intercept) -1.42767560 -0.05320521
friends 0.03288886 0.36890148
```

```
Facebook2 <- Facebook # make a copy of data with different name
Facebook2[41, ] <- c(50, -10) # assigning values to the 41st row of data frame
xyplot(density ~ friends, data = Facebook2)
cor(density ~ friends, data = Facebook2)

[1] -0.7735351
```



Bibliography

Index

ExamTimesScores., 313 tally, 9 FirstBase2, 273 GameSims., 16 NightLight1, 298 Tintle1, 5, 7 bargraph(), 9 bargraph, 10 binom.test(), 46, 81binom.test, 88, 93 bwplot(), 9, 64 data(), 6, 7 densityplot(),9 do(),16 dotPlot(), 12 do, 16 favestats, 14 freqpolygon(), 18 histogram(), 9, 38 lattice, 14 1m(), 321 makeFun(),325 mosaicplot, 10mosaic, 5, 7, 15 mosiac, 10 pnorm(), 40, 41 pnorm, 39 prop(), 23 prop.test(), 41, 46, 81 qnorm, 39 rflip(), 15rflip, 16 rnorm, 64 round(), 64 sample(),50 sim.sci,23 summary(),8 summary, 323 tally(),8

tally, 9 xpnorm(), 28, 30 xpnorm, 28, 29, 39