## **Mathematics for Political Science**

Lecture 5: Probability & Looking Ahead Exercise Solutions

1. 
$$36 * 35 * 5 * 12 * 13 * 6 = 5896800$$

2.

- 1. {Reagan, Bush31, Dole, Bush43, McCain, Perot, Nader}
- 2. (graph all the area outside the circle around L)
- 3. U, V
- 4. [0, .7]
- 5. {1,2,3,4,5,6}
- 6. (.7, .8)
- 7. (graph the region where circles L and M overlap)
- 8. {∅}
- 3.  $A \cup A = A$  and  $A \cap A = A$ . The intersection or union of any set with itself is itself.

4.

$$\begin{array}{c|cccc}
2 & \frac{1}{16} \\
3 & \frac{2}{16} = \frac{1}{8}
\end{array}$$

$$4 \begin{vmatrix} \frac{3}{16} \\ \frac{3}{16} \end{vmatrix}$$

$$5 \mid \frac{4}{16} = \frac{1}{4}$$

$$7 \mid \frac{2}{16} = \frac{1}{8}$$

5.

1. 
$$\left(\frac{1}{2}\right)^6 = \frac{1}{64}$$

2. 
$$\binom{10}{3} \left(\frac{3}{13}\right)^3 \left(\frac{10}{13}\right)^7 \approx .235$$

3. 
$$1 - \binom{9}{3} \binom{6}{3} \left(\frac{1}{6}\right)^9 \approx .99983$$

- 6.
  - 1. .53
  - $2. \approx .444$
  - 3. ≈ .396
  - $4. \approx .333$
  - 5. ≈ .595
- 7.  $\frac{2}{11}$
- 8.
  - 1.  $p(A|red) = \frac{1}{7} \approx .143$ ,  $p(B|red) = \frac{6}{7} \approx .857$
  - 2.  $p(A|blue, blue) \approx .835$ ,  $p(B|blue, blue) \approx .165$  $p(A|blue, blue, blue) \approx .919$ ,  $p(B|blue, blue) \approx .081$ .
  - 3.  $p(A|red) = \approx .310$
- 9.  $\frac{7}{31} \approx .226$