

PLSC 308: Introduction to Political Research

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The Margin of Error (MOE)

Sampling error is the (random) difference between the value you want to know in the population and its respective value in the sample.

Characteristics:

- Intuition: “Repeated samples”
- A function of:
 - The sample size,
 - The sampling design, and
 - The size of the population.

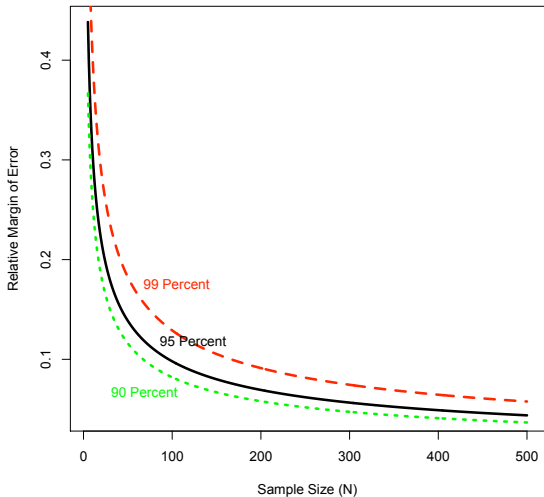
MOE Example

Consider the proportion Q of observations in the population that have some (binary) trait. For a simple random sample of size N , the margin of error (sampling error) for the sample proportion q is:

$$\text{Standard error} = \sqrt{\frac{q(1 - q)}{N}}$$

We typically calculate relative sampling error for a given *level of confidence*...

MOE and Sample Size



XXX

Sampling: An Example

| | Name | sex | namegroup | score |
|----|-----------------------|-----|-----------|-------|
| 1 | ARNOLD, EMILY | F | AB | 31 |
| 2 | BERNICKER, BRENDAN | M | AB | 62 |
| 3 | CHEN, TIANGE | M | CD | 61 |
| 4 | DANIEL, ASHLEY | F | CD | 82 |
| 5 | KLARIC, ROMAN | M | KL | 86 |
| 6 | KLAVANS, JORDAN | M | KL | 64 |
| 7 | KNABB, CHRISTOPHER | M | KL | 1 |
| 8 | LAMAS, MATTHEW | M | KL | 23 |
| 9 | LEVIN, LOUIS | M | KL | 67 |
| 10 | LI, ZIYU | M | KL | 51 |
| 11 | MCCABE, MICHAEL | M | MN | 69 |
| 12 | MCDONNELL, HANNAH | F | MN | 74 |
| 13 | NAHVI, SUSAN | F | MN | 48 |
| 14 | PARIKH, YASH | M | OP | 92 |
| 15 | PELOSI, OLIVER | M | OP | 29 |
| 16 | RANKIN-WAHLERS, JADEN | F | QR | 104 |
| 17 | SALVESEN, BRIAN | M | ST | 29 |
| 18 | SHAFFER, JOHN | M | ST | 27 |
| 19 | SHIPMAN, MATTHEW | M | ST | 19 |
| 20 | THOMAS, CORY | M | ST | 23 |
| 21 | WAGNER, SEAMUS | M | WX | 32 |
| 22 | WESTERFER, JOSEPH | M | WX | 30 |

Sampling Example (continued)

Population characteristics:

- **Overall mean = 50.2** ($N = 22$)
- Mean for males = 45 ($N_M = 17$)
- Mean for females = 67.8 ($N_F = 5$)
- No differences by last name

Simple Random Sampling via Random Numbers

| | Name | sex | namegroup | score | rando |
|----|-----------------------|-----|-----------|-------|------------|
| 2 | BERNICKER, BRENDAN | M | AB | 62 | 0.03999592 |
| 8 | LAMAS, MATTHEW | M | KL | 23 | 0.04577026 |
| 1 | ARNOLD, EMILY | F | AB | 31 | 0.15904600 |
| 13 | NAHVI, SUSAN | F | MN | 48 | 0.18109621 |
| 15 | PELOSI, OLIVER | M | OP | 29 | 0.20124804 |
| 3 | CHEN, TIANGE | M | CD | 61 | 0.21879954 |
| 16 | RANKIN-WAHLERS, JADEN | F | QR | 104 | 0.25880982 |
| 10 | LI, ZIYU | M | KL | 51 | 0.26518667 |
| 11 | MCCABE, MICHAEL | M | MN | 69 | 0.30467220 |
| 21 | WAGNER, SEAMUS | M | WX | 32 | 0.31182431 |
| 9 | LEVIN, LOUIS | M | KL | 67 | 0.45609148 |
| 12 | MCDONNELL, HANNAH | F | MN | 74 | 0.50730687 |
| 5 | KLARIC, ROMAN | M | KL | 86 | 0.52569755 |
| 19 | SHIPMAN, MATTHEW | M | ST | 19 | 0.55333359 |
| 22 | WESTERFER, JOSEPH | M | WX | 30 | 0.62181920 |
| 20 | THOMAS, CORY | M | ST | 23 | 0.64640609 |
| 14 | PARIKH, YASH | M | OP | 92 | 0.75967064 |
| 18 | SHAFFER, JOHN | M | ST | 27 | 0.80735234 |
| 4 | DANIEL, ASHLEY | F | CD | 82 | 0.81059855 |
| 7 | KNABB, CHRISTOPHER | M | KL | 1 | 0.83134505 |
| 6 | KLAVANS, JORDAN | M | KL | 64 | 0.91465817 |
| 17 | SALVESEN, BRIAN | M | ST | 29 | 0.99215042 |

Simple Random Sample ($N = 10$)

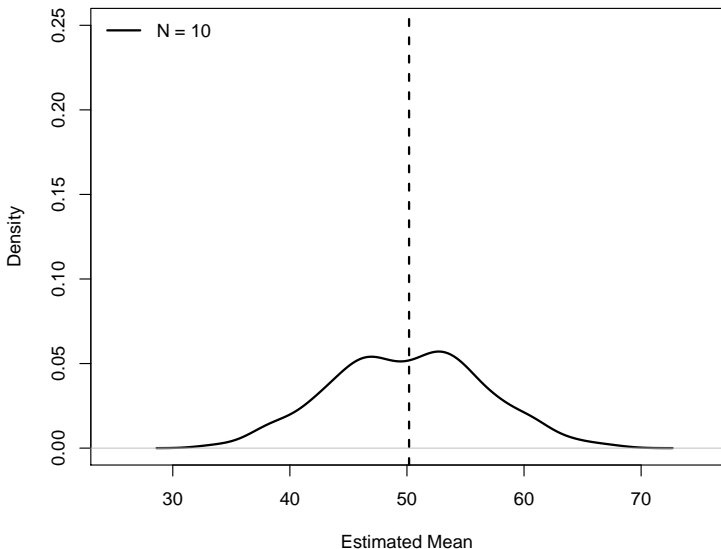
Sample characteristics:

- **Overall mean = 51** ($N = 10$)
- Mean for males = 46.7 ($N_M = 7$)
- Mean for females = 61 ($N_F = 3$)
- No differences by last name

$$\text{Overall MOE} = \sqrt{\frac{0.51(1 - 0.51)}{10}} = 0.158 \text{ (15.8 percent)}$$

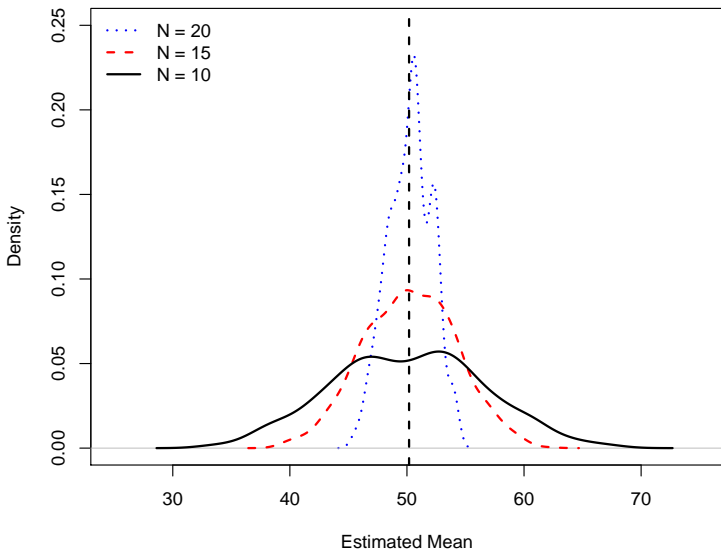
Simple Random Sampling, repeated

Sample Means, $N=10$ (1000 replications)



Vary Sample Sizes

Sample Means, Various Ns (1000 replications)



Stratified Sampling

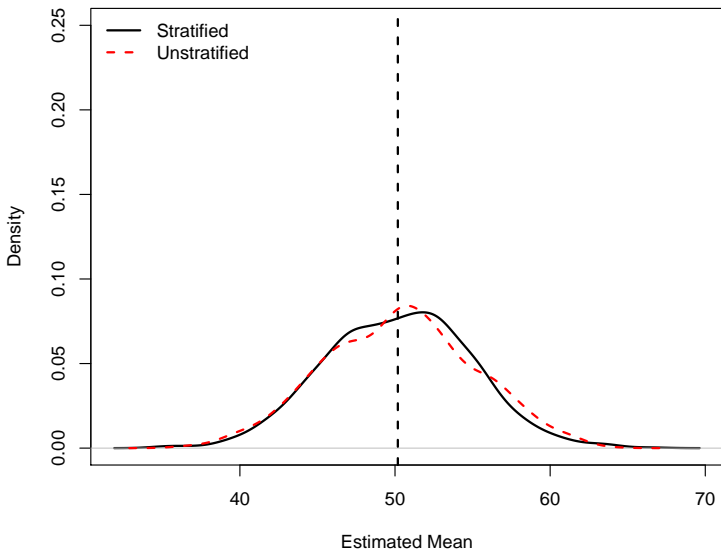
Women are 22.7 percent of the population...

Proportional stratified sampling (say, select 3 women and 10 men randomly):

| | Name | sex | namegroup | score | rando |
|----|-----------------------|-----|-----------|-------|------------|
| 1 | ARNOLD, EMILY | F | AB | 31 | 0.26093924 |
| 13 | NAHVI, SUSAN | F | MN | 48 | 0.79497190 |
| 16 | RANKIN-WAHLERS, JADEN | F | QR | 104 | 0.72192125 |
| 10 | LI, ZIYU | M | KL | 51 | 0.64051016 |
| 2 | BERNICKER, BRENDAN | M | AB | 62 | 0.30613168 |
| 3 | CHEN, TIANGE | M | CD | 61 | 0.43401093 |
| 5 | KLARIC, ROMAN | M | KL | 86 | 0.50771100 |
| 17 | SALVESEN, BRIAN | M | ST | 29 | 0.14978794 |
| 8 | LAMAS, MATTHEW | M | KL | 23 | 0.12362789 |
| 9 | LEVIN, LOUIS | M | KL | 67 | 0.62641954 |
| 6 | KLAVANS, JORDAN | M | KL | 64 | 0.05987933 |
| 21 | WAGNER, SEAMUS | M | WX | 32 | 0.08098174 |
| 22 | WESTERFER, JOSEPH | M | WX | 30 | 0.79409840 |

Proportional Stratification: Results

Proportional (Stratified) Sample Means, N=13 (1000 replications)



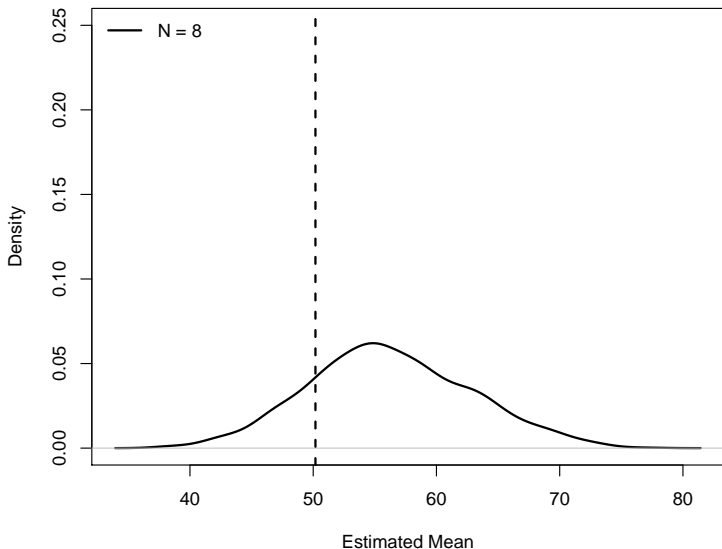
Stratified Sampling

Oversampling women (say, a 50-50 male-female split):

| | Name | sex | namegroup | score | rando |
|----|-----------------------|-----|-----------|-------|-----------|
| 1 | ARNOLD, EMILY | F | AB | 31 | 0.0939031 |
| 13 | NAHVI, SUSAN | F | MN | 48 | 0.2346178 |
| 16 | RANKIN-WAHLERS, JADEN | F | QR | 104 | 0.4263274 |
| 4 | DANIEL, ASHLEY | F | CD | 82 | 0.5336345 |
| 10 | LI, ZIYU | M | KL | 51 | 0.1426833 |
| 2 | BERNICKER, BRENDAN | M | AB | 62 | 0.1178203 |
| 3 | CHEN, TIANGE | M | CD | 61 | 0.5439105 |
| 5 | KLARIC, ROMAN | M | KL | 86 | 0.7212281 |

Oversampling: Results

Female Oversampled Sample Means, N=8 (1000 replications)



Cluster Sampling

Sample on namegroup with $N_c = 3$

| | Name | sex | namegroup | score |
|----|--------------------|-----|-----------|-------|
| 3 | CHEN, TIANGE | M | CD | 61 |
| 4 | DANIEL, ASHLEY | F | CD | 82 |
| 5 | KLARIC, ROMAN | M | KL | 86 |
| 6 | KLAVANS, JORDAN | M | KL | 64 |
| 7 | KNABB, CHRISTOPHER | M | KL | 1 |
| 8 | LAMAS, MATTHEW | M | KL | 23 |
| 9 | LEVIN, LOUIS | M | KL | 67 |
| 10 | LI, ZIYU | M | KL | 51 |
| 17 | SALVESEN, BRIAN | M | ST | 29 |
| 18 | SHAFFER, JOHN | M | ST | 27 |
| 19 | SHIPMAN, MATTHEW | M | ST | 19g |
| 20 | THOMAS, CORY | M | ST | 23 |

Mean score = 44.1...

Midterm Matters...

- In-class (75 minutes), 3/1/2016
- Closed-book / closed-notes / etc.
- Materials:
 - Chapters 1 - 7 of the text
 - Class lecture material
- Format:
 - Definitions
 - Short answer questions
 - A short “essay”
- **Worth 20% of course grade (200 points)**