

a) given a data set X, ..., Xn, then you.

(b) assume a DGP, then you

c) define one (or many) interential target parameters of, then
compute  $\theta = w(x_1, ..., x_n)$  and then you
make a colorum a test at size alpha Let's examine (b). How do you just "assume a DGP"? Sometimes you really do know the DGP e.g. a coin flipped repeatedly is ited Bernoulli (d), a die rolled repeatedly is ited uniform discrete But what about "daily wind speeds at IFK airport" or "rat survival times" (like on midterm) or "daily percentage returns of the SLP 500"? The DGP's for the last three are very complicated and they're unknown What It we wanted to guess" the DGP's?
This is actually a really big part of what statisticians do This is called "model fitting". DGP = model Models you kinda make up 2 hope fully they're useful for whatever you're doing Why don't we proceed as follows let's guess M candidate models. DGPs m = 1, 2, ..., N and (1) Pick the "best" model out of my M guesses and maybe (2) provide a weighting score to each of the M guesses (low scores indicate bad guesses and high scores indicate good guesses). Goal (1) is famous and called "model selection". In 3H2, We do a little of this atheoretically there we'll do it more theoretically

Model selection is more fundamental than you realize. It's actually the entire problem of all of science for example, let's say you have some astronomical data on movement of different planets, stars, etc.
You want to fit a model (guess Dap) for the
force on two celestial boolies with masses
m, m, at a distance i from each other
(1.e. "gravity"). Consider the following models: Mod 1: F=G Min/2 Newton's law Mod 2: F=G, W, W, + G, M, W, Newton's extension Mod 3: P=G, M, N, e Laplace's extension Which model is the best? We know all these are wrong because Finstein came and disproved them with general relativity Let's talk about model selection techniques!
Our data X, Xn comes from an unknown
DGP. Here are M candidate models Mod 1: [(X,,..., Xn', 0,,..., 0, K) = &, (0,,..., 0, K, X, Xp) Mod 2: 1 (X, , , , Xn; Oa, , , Oak) = lo (Oa, , , de X, X, X) Mod m: Im (x, xn; Am, -.. Amkm) - In (Am, Bukm; X, ... Yn) K, is the # of parameters in model 1, ka is the number of parameters in model 2, \_\_, KM is the number of parameters in model M. Each Km could be different Why don't we just select the model that has the highest likelihood? m = avgmax [ & (0m,,...,0mkm; X,,...xn)} = augmax [lm(0mi, -.. Omkm; Xi, - - iXn)] The problem with this is we don't know the value of a for any of the models! 50 let's richardize k, + k, + - + km times! We'll estimate each of the parameters using MLE's and plug them all in and then my = cugmax { ( fine full ) X1, xn)} You could do this. But it will not give you the best model. Why? (AMLE AMLE , XI, ..., Xn) is an estimator for (9m, , 9mk , X, ..., Xn) and it's brased

aith many assumptions, you can prove that.

asymptotically -- meaning as n gets large 
Bigs I (AMLE AMLE) There is positive bias (meaning that log-likelihood would appear higher on average) and this bias condidate models. This was figured out by H. Akaike, a Jopanese statistician, and published It in 1974. Once you have the you just use it to correct your estimate! 1(0m, 1.0mkm) ~ 1 (1 mkm; X1...Xn) - Km Recall that log likelihood is always negative for discrete DGP's and almost always negative for continuous DGP's. So let's flip its sign and multiply by two. , 9 mkm ; X1, 2 ... , X0) + 8K (Akaike's Information Criterion) So The "best" log likelihood is the largest i.e closest to zero so once negated, the "best" negative log likelihood is the smallest i.e closest M, := argmin [ARC]