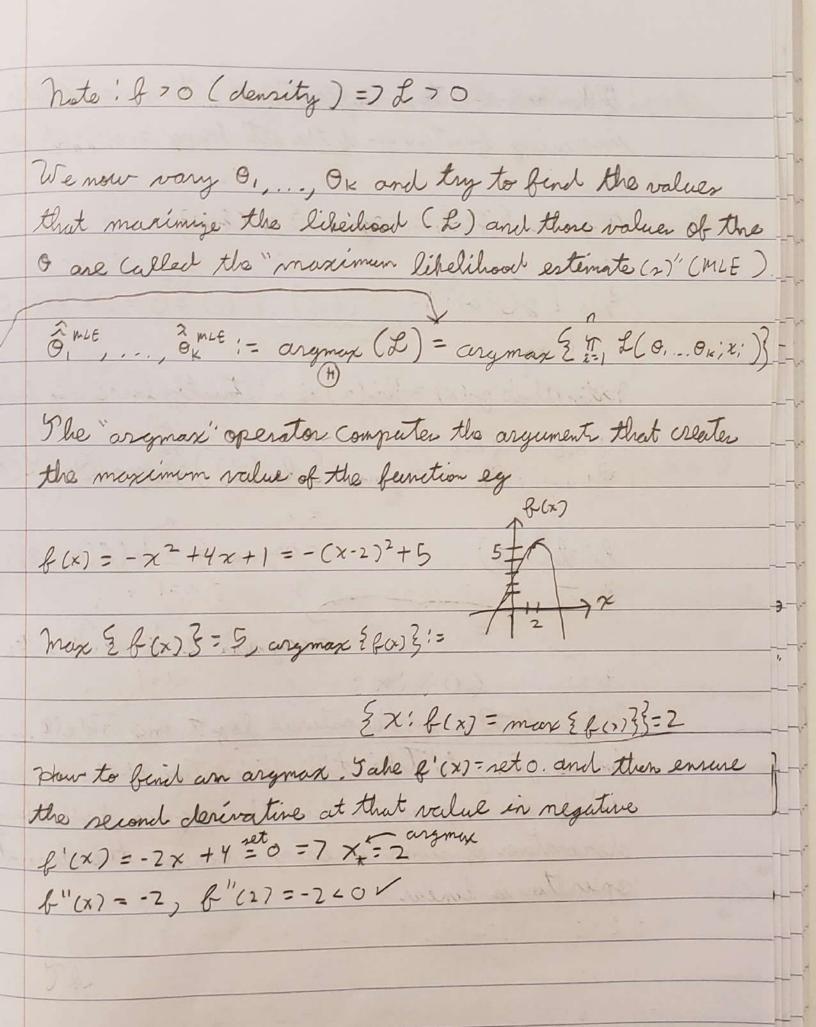
9/23/20 06P: 20 U(0,0), 1] We want to find the MM estimator for o $u_{i} = E[X] = \frac{0+\theta}{2} = \frac{\theta}{2} = \alpha_{i}(\theta) = 7\theta = 2u = 8, (u_{i})$ =) $\hat{g}^{MM} = 2\hat{u}_{1} = 2\bar{x}$ Date : = 21,2,3,107, 0 = 2 x = 2(4) = 8 This is an absurd estimate, We're saying the true populties maximum is 8 but we've already seen x4=10,8!? So this is clearly monsensical another method for binding estimates / esterator goes lad. to the 180 o'r but was popularized by Fisher between 1912-1922 and its called "maximum likethood" χ , χ_n in $DfP(\theta_1, \theta_2)$ preferent χ f(xi, O, ..., ox) if contino Dere to endependence and identical distributedness liberheed = $L(0, \dots, 0, 1, 1, \dots, X_n) = f(x_1, \dots, x_n, 0, \dots, 0, x_n)^2$ "stat pupitie // inputs / givens inputs givens "f(xi;o,, 9) L' variables varibles



The argmox is unaffected by taking a strictly inversing function of of the set being analyzed is arymon { f wi} = arymon { g (fix)} 4/3x [g(f(x))]= g'(f(x)) f'(x)=0=7f'(x)=0=7x, note that g(x) = ln(x) is a strictly increasing beention x70 $\frac{2}{9}$, $\frac{2}{9}$ = argmax $\frac{2}{9}$ lm (2) $\frac{1}{9}$ = argmax $\frac{1}{9}$ ln $\frac{1}{1}$ $\frac{1$ l'ilm (L) = $argmax \{ \sum In(L(0, -0, x_i)) \}$ = arginax { { { (0, ..., 0 k j xi)}} Why do this whole natural log thing? Well ... because we're going to Take the derivative of the expression inside the argmax to find The argmax and taking derivatives of sums is easy because the derivative operator is linear

To get the MLE's, we solved the bollowing system of equations; € = [l(0, ... 0 k', XL)] = 0 precede section de [l(0,...0€; xi)] =0 2 Jok [l (0, ... 0 x ; x i)]=0 Ut's also possible, there is no maximum that corresponds to a critical points. So there you have to check the Edger" of the parameter space manually DGP: X, , ... , x, in Bern (0), Find of MLE

n (2(0;x;)) - ln(r(xi;0)) $\frac{d}{de} \left[x : |n(e) + (1-x;)|_{n(1-e)} \right] = \frac{x_i}{e} - \frac{1-x_i}{1-e} = \frac{\xi x_i'}{e} - \frac{n-\xi x_i'}{1-e} = 0$ 1 $\frac{\xi \times i}{\Theta} = \frac{n - \xi \times i}{1 - \Theta} = 7(1 - \Theta) \frac{\xi \times i}{2} = \Theta(n - \xi \times i)$

Q = w(x, xn) <= 7 0 = w(x, xn) likelihood estimator Maximum likelihood estimate 3 mm = w(x, ..., xn) (= > 6 mm = w(x,,.., xn) DGP: Y, ,, x, i'd-U(O, 6), ômm=27, ôm=? ₹ = [l(o; x;)] = ₹ = [ln(β(x; θ))] = ₹] [ln(β(x; θ))] = ₹ 3 = [-In (6)] $= \underbrace{\xi - \frac{1}{6}}_{=} = -\frac{n}{6} = 0 = 7 \text{ no rolution } \text{The } (x_i'_i 6) = \underbrace{\text{The } (x_i'_i 6)}_{i=1} = \underbrace{\text{The } (x_i'_$ >= (or it 0 = x: = 0 \fix: \)

