1111120 Milhael Velez Here's a relevant fact about p-values that's important in our discussion about multiple comparisons - If Ho is true, what is the distribution of the p-volue? Consider a right Olto sided rest Proof for why p-values under the north hypothesis are realizations from U(0,1) distribution. Assume left-sided test. The proof for right-sized and two-sized is similar. P-Va1 = = Fâlto (8) =7 a.v. moder for pronis Let's examone the CDF of p-val to try and Egre out is distribution. This is a proof from Fever (Pron) = P(Pron & pron) = P(Follio (6) & pron)

= P(0 = Formo (pval)) = Fétho (Fortho (PVAI)) = PVAI = 7 PVAI ~ V(Q) We will rema to testing now. We previously Proved...

O MLE - B

Test / RET = [00 + Z1 - a SE(0)]

TEST | WAVE CE

(RETORDATED) CION-25 [@ MLE + Z 1- 2 [\$(0)-1] we'll now derive a related means of testing that Recall for it DGP, S(0; X1,..., Xn) = \(\frac{2}{1'(0; \times)} \) det 8, 1009 $= \frac{1}{n} S(\Theta; X_{1,...}, X_{n}) = \overline{W} \frac{S(\Theta; X_{1,...}, X_{n})}{\sqrt{n T(\Theta)}} drM(0)$ E[Wi]=0 (Fact 16) lec 9 Var[Wi]= I(0) lec 9-10 (=7 th S(0; X1, -1, XD)

= W-ELX] & MO,1) Jos (Oo; X,, ,, Xn) in wing his as a

In I (Oo) ~ M(O,1) Z-test statistic was discovered by Bao, 1948 (100 XIIII) C [-1.96,1.96] and it is called the "Score test" but others call it the "lagrange" milliplier test" More This is "one domensional", There's only one o being sight for con derve the generalizeation with multiple 0's but we won't in this class. This test statistic is really strange, where is the estimator, QZ It's not there! And it you just want to kest Hai- 0 + Do you don't really need an estimentor or an estimate. You usually find an estimable that gauges he deformer from to, and and approxits distribution (the sampling distribution) and the Check of 9 looks werd. It so, resect-But he don't do may here, he estimenter is not in the expression! And it you just won't to test that 0 #00, you don't need on estimate lessimator.

mary somes, it is me some as the world best wer you acmally algebracially solve for me lest statistic. (It w you'll use Bernault). Here's on ex who you core about this: DGP: 10 LOGISTIC (0,1):= e-(x-6) L=Te-xieto e-Exietno
1=1 (1+exe-0)2 = e (1+exe-0)2 1=-Exi+no-22In(1+e* e+0) 5=1'=-n-22 e e To get the MLE I set the above equal to 0 and some for O- Good luck? It's not pussible in Gosele forme You can use a comparer to do a innerton solve it you wish.

$$|| (0; x) = 1 - 2 e^{-x} e^{-\theta}$$

$$|| (0; x) = 2 (1 + e^{-x} e^{\theta}) e^{-x} e^{\theta} - (e^{-x} e^{\theta})^{2}$$

$$|| (1 + e^{-x} e^{\theta})^{2} - (1 + e^{-x} e^{\theta})^{2} - (1 + e^{-x} e^{\theta})^{2}$$

$$|| (1 + e^{-x} e^{\theta})^{2} - (1 + e^{-x} e^{\theta})^{2} - (1 + e^{-x} e^{\theta})^{2} + (1 + e^$$

In are down example, we get = 4.77 £ [-1-96,1.96] =7 Reject Ho Here's mother also related testing procedure to the hald and Score. Here too we wish to test against Ito : 0 = 00. Remember, we want an estmak mat ganges departure from mos. How a barr... 112 OGR LR:= L(ÔME; X,,, Xn) (FIL(ÔME; Xi) 1 L(0, X, Xn) = # L(0, Xi) Likelihood Ratio. It 11's signaturally >1, then Now we sust need IT L (GALE, X.) & LB, the samping distribution int L(Oo;Xi) we can grove that: 1==21 (LB) -d, X; Recall Fx2 (3.84) = 95%

$$\frac{1}{2} = \frac{1}{1} \frac{1}{2} \frac$$