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Survey: Who has an iPhone?

Standard $X_1 = 0$ $X_2 = 0$, $X_3 = 1$, $X_4 = 1$, $X_5 = 0$, 1, 1, 1,

for a first "NO" 0,0,1,1,1,1,0,0,1,1,0
"datum string

n = 20 is our "Sample" 12 15, 8 0's

Do we believe this survey is a "sample" of N=20 elements from a superset called the "population"? If we do, this is called the "population model sampling assumption.

If So, what is that population?
- All people on Earth?

- All People in America?

- All college Students?

-All college students in NYC?

-All Public college Students in NYC? -All QC Students?

Is this sample representative of the population?

This is typical. Given a sample, assume a population model, then identify the representative population. This happens in data science all the time.

In classical statistics, this goes in the opposite direction. You begin by defining the population clearly and then sample n elements from that population.

Population has size N. You have some idea of what N is. If population = all Americans $\Rightarrow N = 330$ million

population)

Sample (n)

We see the data

X1, X2, ..., Xn in the

Sample (n) Sample but not other

data in the population

Can we learn about the population from the Sample ?

This is called inference. We use the sample to vinfer properties about the population. Usually the properties are parameters of the random variable which creates the population the population.

"Infer means to make an educated guess from specific things to Universal properties, A synonym is "induction."

The opposite is deduction which is Universal => particular. You can *never* be sure your inference is correct

How is inference done w/ data?

You generate "Statistics" which are functions of the data!

$$\frac{\hat{\Lambda}}{\hat{\Theta}} = W(X_1, \dots, X_n) \text{ e.g. } \frac{\hat{\Lambda}}{\hat{\Theta}} = \frac{1}{n} \sum_{i=1}^{n} X_i$$
Statistic
$$\hat{X} \text{ or } \hat{\rho}$$
(Usually Scalar)

= 0.6 our iphone Survey

What can you infer w/ this Statistic? Usually, you infer &, the population parameter which is the "true proportion" Of iPhones. "Statistical inference" - Using Statistics to make inferences.

What is 0 ?

 $\theta = X \rightarrow \#$ of people in the population that have iphones (unknown) # of elements in the population (known)

Parameter (Unknown Property)

 $\Theta \in \Theta = \{0, \frac{1}{N}, \frac{2}{N}, \dots, \frac{N-1}{N}, 1\}$, the parameter space

Convention is that greek letters represent unknown quantities and roman letters represent known quantities

Theta. "Point estimate" for the unknown theta. "Point" meaning one specific value which you believe is a good guess for the value of theta.

(1) "Point estimation" is one of the goals of
Statistical inference. The other two are
(2) Confidence set creation and (3) theory
testing (testing a theory about a specific
Value of theta at a "certainty level"
alpha)

Let's Sample One element from the population and do one survey.

Population

How should this element be chosen if I want a "representative"

Sample ?

N=1 Randomly but specifically,

Uniform meaning every element

has probability of 1 of being chosen. That's called " a "Simple random Sample" (SRS).

What is the probability that X, =1?

 $P(X_1 = X_1 = 1) = X = 0$ the r.v. the specific

modeling realization
the Survey (a value
in the support
of X,)