Comparing von Bertalanffy Growth Functions

Derek H. Ogle, Northland College 20-Aug-2016

Preliminaries

```
> library(FSAdata)  # for Croaker2 data
> library(FSA)  # for vbStarts(), residPlot(), extraSS(), lrt(), vbFuns(), filterD(), col2rbgt()
> library(dplyr)  # for mutate()
```

Loading the Data and Some Preparations

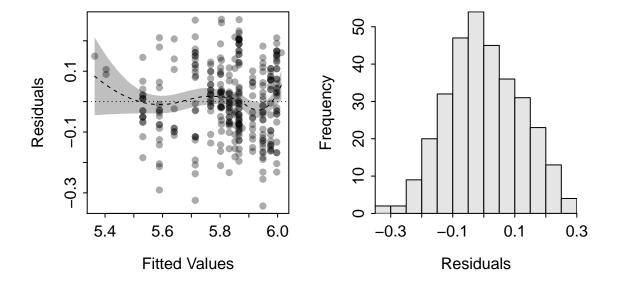
```
> data(Croaker2)
> str(Croaker2)
'data.frame': 318 obs. of 3 variables:
$ age: int 1 1 1 2 2 2 2 2 2 2 2 ...
$ t1 : int 243 247 248 330 320 285 280 265 260 248 ...
$ sex: Factor w/ 2 levels "F", "M": 1 1 2 1 1 1 1 1 1 ...
> Croaker2 <- mutate(Croaker2, logTL=log(t1))</pre>
```

Fitting Most Complex Model and Checking Assumptions

```
> ( sv0m <- vbStarts(tl~age,data=Croaker2) )</pre>
$Linf
[1] 434.697
$K
[1] 0.1837369
$t0
[1] -3.541856
> (svLKt \leftarrow Map(rep, svOm, c(2,2,2)))
$Linf
[1] 434.697 434.697
[1] 0.1837369 0.1837369
$t0
[1] -3.541856 -3.541856
> vbLKt <- tl~Linf[sex]*(1-exp(-K[sex]*(age-t0[sex])))</pre>
> fitLKt <- nls(vbLKt,data=Croaker2,start=svLKt)</pre>
> residPlot(fitLKt,col=col2rgbt("black",1/3))
```

```
100
                                                         9
                                                         50
      20
Residuals
                                                   Frequency
                                                         4
      0
                                                         30
                                                         20
                                                         10
      -100
               250
                        300
                                350
                                        400
                                                             -100
                                                                              0
                                                                                     50
                                                                                            100
                    Fitted Values
                                                                         Residuals
```

```
> vbLKt <- logTL~log(Linf[sex]*(1-exp(-K[sex]*(age-t0[sex]))))
> fitLKt <- nls(vbLKt,data=Croaker2,start=svLKt)
> residPlot(fitLKt,col=col2rgbt("black",1/3))
```



Are There Any Differences?

```
> vb0m <- logTL~log(Linf*(1-exp(-K*(age-t0))))
> fit0m <- nls(vb0m,data=Croaker2,start=sv0m)

> extraSS(fit0m,com=fitLKt,sim.name="{0mega}",com.name="{Linf,K,t0}")

Model 1: {0mega}

Model A: {Linf,K,t0}

Df0 RSS0 DfA RSSA Df SS F Pr(>F)

1vA 315 5.23971 312 4.44264 3 0.79707 18.659 3.705e-11

> lrt(fit0m,com=fitLKt,sim.name="{0mega}",com.name="{Linf,K,t0}")

Model 1: {0mega}

Model A: {Linf,K,t0}
```

```
DfO logLikO DfA logLikA Df logLik Chisq Pr(>Chisq)
1vA 315 201.597 312 227.835 3 -26.238 52.476 2.372e-11
```

Is the Most Complex Model Warranted?

> svK \leftarrow Map(rep,svOm,c(1,2,1))

> fitK <- nls(vbK,data=Croaker2,start=svK)</pre>

```
> vbLK <- logTL~log(Linf[sex]*(1-exp(-K[sex]*(age-t0))))
> (svLK \leftarrow Map(rep,svOm,c(2,2,1)))
$I.inf
[1] 434.697 434.697
[1] 0.1837369 0.1837369
$t0
[1] -3.541856
> fitLK <- nls(vbLK,data=Croaker2,start=svLK)</pre>
> vbLt <- logTL~log(Linf[sex]*(1-exp(-K*(age-t0[sex]))))</pre>
> svLt \leftarrow Map(rep,svOm,c(2,1,2))
> fitLt <- nls(vbLt,data=Croaker2,start=svLt)</pre>
> vbKt <- logTL~log(Linf*(1-exp(-K[sex]*(age-t0[sex]))))
> svKt \leftarrow Map(rep,svOm,c(1,2,2))
> fitKt <- nls(vbKt,data=Croaker2,start=svKt)</pre>
> extraSS(fitLK,fitLt,fitKt,com=fitLKt,com.name="{Linf,K,t0}",
          sim.names=c("{Linf,K}","{Linf,t0}","{K,t0}"))
Model 1: {Linf,K}
Model 2: {Linf,t0}
Model 3: {K,t0}
Model A: {Linf,K,t0}
    DfO
            RSSO DfA
                          RSSA Df
                                                  F Pr(>F)
1vA 313 4.442641 312 4.442639 1 0.000002 0.0001 0.9916
2vA 313 4.444957 312 4.442639 1 0.002318 0.1628 0.6869
3vA 313 4.476736 312 4.442639 1 0.034097 2.3946 0.1228
```

Can the Model be Reduced to Only One Parameter that Differs?

> extraSS(fitL,fitK,com=fitLK,com.name="{Linf,K}",sim.names=c("{Linf}","{K}"))

```
> vbL <- logTL~log(Linf[sex]*(1-exp(-K*(age-t0))))
> ( svL <- Map(rep,svOm,c(2,1,1)) )
$Linf
[1] 434.697 434.697

$K
[1] 0.1837369

$t0
[1] -3.541856

> fitL <- nls(vbL,data=Croaker2,start=svL)
> vbK <- logTL~log(Linf*(1-exp(-K[sex]*(age-t0))))</pre>
```

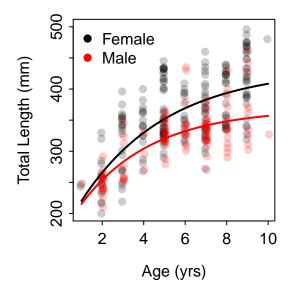
```
Model 1: {Linf}
Model 2: {K}
Model A: {Linf,K}

DfO RSSO DfA RSSA Df SS F Pr(>F)
1vA 314 4.484252 313 4.442641 1 0.041612 2.9317 0.087847
2vA 314 4.621667 313 4.442641 1 0.179027 12.6131 0.000442
```

Summarize Final Model

```
> summary(fitL,correlation=TRUE)
Formula: logTL \sim log(Linf[sex] * (1 - exp(-K * (age - t0))))
Parameters:
       Estimate Std. Error t value Pr(>|t|)
Linf1 425.37158 17.13519 24.824 < 2e-16
Linf2 384.21649 15.65097 24.549 < 2e-16
       0.24825
                  0.05315
                            4.671 4.45e-06
t0
       -2.12303
                 0.66226 -3.206 0.00149
Residual standard error: 0.1195 on 314 degrees of freedom
Correlation of Parameter Estimates:
      Linf1 Linf2 K
Linf2 0.94
      -0.95 -0.93
     -0.87 -0.85 0.97
t.0
Number of iterations to convergence: 4
Achieved convergence tolerance: 1.809e-06
> round(cbind(coef(fitL),confint(fitL)),3)
Waiting for profiling to be done...
                 2.5%
                        97.5%
Linf1 425.372 400.090 481.671
Linf2 384.216 360.721 435.082
K
       0.248 0.144 0.357
t0
   -2.123 -3.986 -1.108
> vb <- vbFuns("typical")</pre>
> # Females
> crF <- filterD(Croaker2,sex=="F")</pre>
> svF <- list(Linf=425,K=0.25,t0=-2)
> fitF <- nls(logTL~log(vb(age,Linf,K,t0)),data=crF,start=svF)</pre>
> # Males
> crM <- filterD(Croaker2,sex=="M")</pre>
> svM <- list(Linf=385,K=0.25,t0=-2)
> fitM <- nls(logTL~log(vb(age,Linf,K,t0)),data=crM,start=svM)</pre>
> clr1 <- c("black","red")</pre>
> clr2 <- col2rgbt(clr1,1/5)
> offset <- 0.04
> # Females
> plot(tl~I(age-offset),data=crF,pch=19,col=clr2[1],ylim=c(200,500),
       xlab="Age (yrs)",ylab="Total Length (mm)")
```

```
> curve(vb(x-offset,coef(fitF)),from=1,to=10,col=clr1[1],lwd=2,add=TRUE)
> # Males
> points(tl~I(age+offset),data=crM,pch=19,col=clr2[2])
> curve(vb(x+offset,coef(fitM)),from=1,to=10,col=clr1[2],lwd=2,add=TRUE)
> legend("topleft",c("Female","Male"),pch=19,col=clr1,bty="n")
```



Using Information Criterion

Fit the Only Other Model not Fit Above

```
> vbt <- logTL~log(Linf*(1-exp(-K*(age-t0[sex]))))
> svt <- Map(rep,sv0m,c(1,1,2))
> fitt <- nls(vbt,data=Croaker2,start=svt)</pre>
```

AICc Table

```
> library(AICcmodavg)
> ms <- list(fitOm,fitL,fitK,fitt,fitLK,fitLt,fitKt,fitLKt)
> mnames <- c("{Omega}","{Linf}","{K}","{t0}","{Linf,K}","{Linf,t0}","{K,t0}","{Linf,K,t0}")</pre>
> aictab(ms,mnames)
Model selection based on AICc:
            K
                  AICc Delta_AICc AICcWt Cum.Wt
{Linf,K}
            6 - 443.40
                             0.00
                                     0.31
                                            0.31 227.84
{Linf,t0}
            6 - 443.23
                             0.17
                                     0.29
                                            0.60 227.75
            5 -442.51
                                     0.20
                                            0.80 226.35
{Linf}
                             0.89
\{Linf,K,t0\} 7 -441.31
                             2.09
                                     0.11
                                            0.91 227.84
{K,t0}
            6 - 440.97
                             2.43
                                     0.09
                                           1.00 226.62
{K}
            5 -432.91
                            10.49
                                     0.00
                                            1.00 221.55
{t0}
            5 - 422.44
                            20.96
                                     0.00
                                            1.00 216.31
{Omega}
            4 -395.07
                            48.33
                                     0.00
                                            1.00 201.60
```