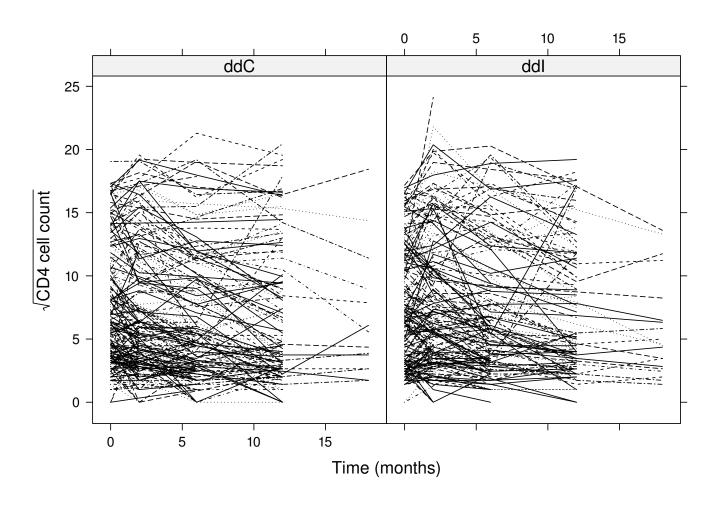
# Chapter 1 Motivating Data Sets

#### 1.1 Motivating Longitudinal Studies



- AIDS: 467 HIV infected patients who had failed or were intolerant to zidovudine therapy (AZT) (Abrams et al., NEJM, 1994)
- The aim of this study was to compare the efficacy and safety of two alternative antiretroviral drugs, didanosine (ddl) and zalcitabine (ddC)
- Outcomes of interest:
  - ▷ CD4 cell count measurements at baseline, 2, 6, 12 and 18 months
  - ▷ randomized treatment: 230 patients ddl and 237 ddC
  - > prevOI: previous opportunistic infections







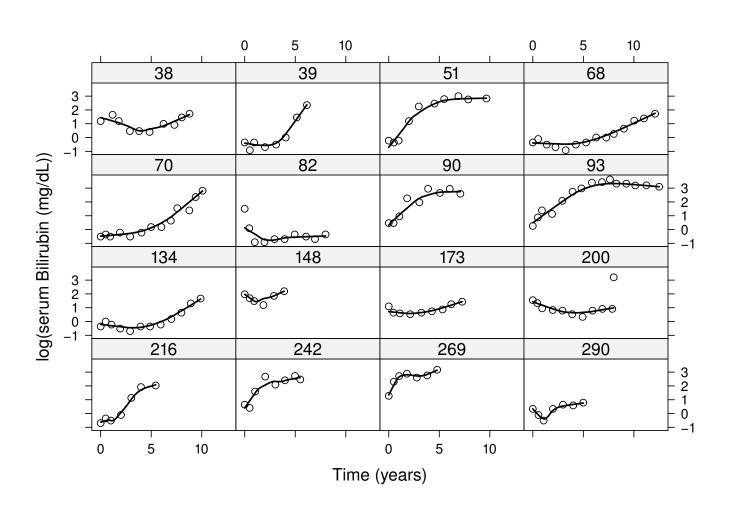
- Research Questions:

  - Does treatment improve average longitudinal evolutions?



- **PBC:** Primary Biliary Cirrhosis:
  - ▷ a chronic, fatal but rare liver disease
  - > characterized by inflammatory destruction of the small bile ducts within the liver
- Data collected by Mayo Clinic from 1974 to 1984 (Murtaugh et al., Hepatology, 1994)
- Outcomes of interest:
  - ▷ longitudinal serum bilirubin, serum cholesterol, prothrombin time
  - ▷ randomized treatment: 158 patients received D-penicillamine and 154 placebo







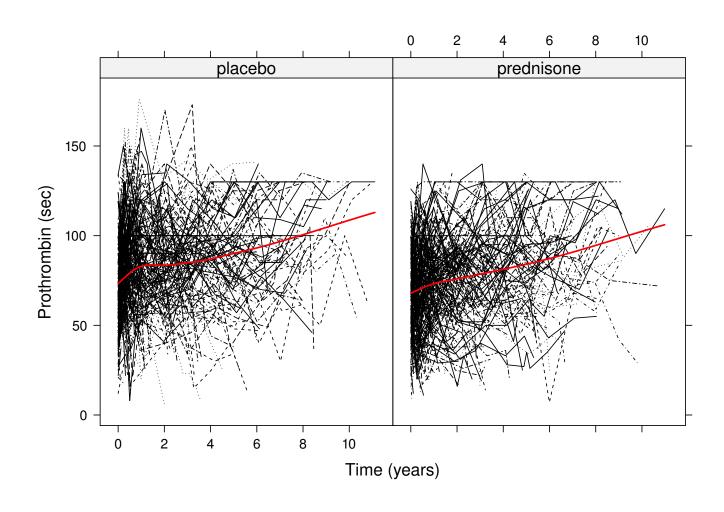
- Research Questions:
  - Do men have higher serum bilirubin during follow-up than women? 

    □ Do men have higher serum bilirubin during follow-up than women?
  - ▶ Is there a difference in the average longitudinal evolutions of serum bilirubin between the two treatments when we correct for age and gender at baseline?



- Prothro: Prednisone versus placebo in liver cirrhosis patients
  - > slowly progressing disease in which healthy liver tissue is replaced with scar tissue, eventually preventing the liver from functioning properly
- Randomized trial in Denmark (Andersen et al., Springer, 1993)
- Outcomes of interest:
  - > randomized treatment: 237 patients received prednisone and 251 placebo

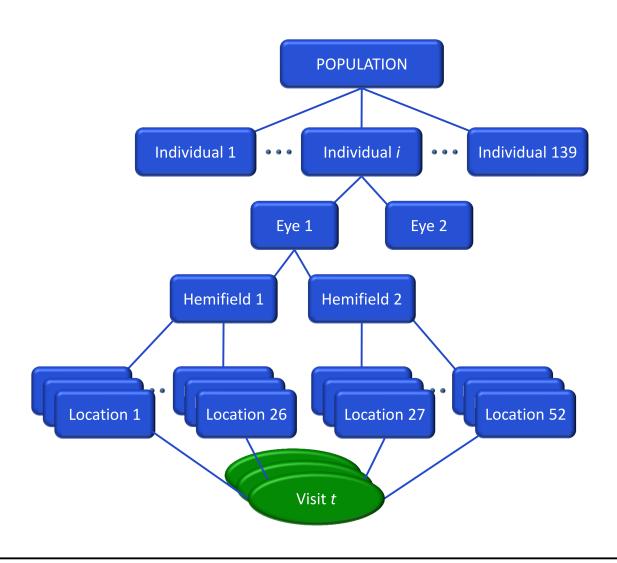




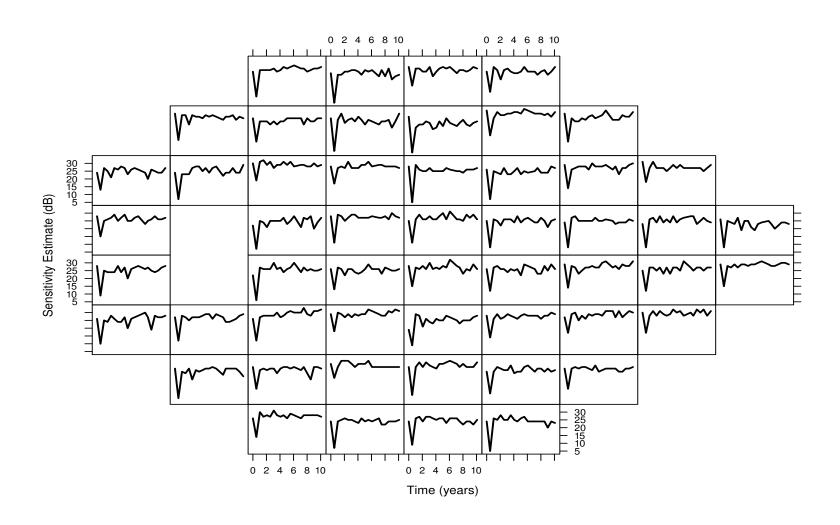


- Glaucoma: A group of eye conditions resulting in optic nerve damage, which may cause loss of vision
- Ongoing prospective cohort study on 139 patients (80% men) conducted by the Rotterdam Eye Hospital in the Netherlands http://rod-rep.com
- Outcome of interest:
  - ▷ Visual field (VF) sensitivity collected at approximately 6-months intervals











- Research Questions:
  - > Study disease progression using VF sensitivity
  - > Predict rate of progression for future patients

#### 1.2 Features of Longitudinal Data



- Repeated evaluations of the same outcome in each subject in time
  - ▷ CD4 cell count in HIV-infected patients
  - > serum bilirubin in PBC patients
- Visiting process
  - > some times fixed by design (e.g., in randomized trials) but often not everybody adheres to them
  - > completely determined by the physicians and/or the patients



Measurements on the same subject are expected to be (positively) correlated

ullet This implies that standard statistical tools, such as the t-test and simple linear regression that assume independent observations, are not optimal for longitudinal data analysis



- Let's see why: The simplest case of longitudinal data are paired data
- Example: We consider the baseline and 6-month longitudinal measurements of square root CD4 cell count from the AIDS dataset

	n	mean	sd
month = 0	294	7.73	4.69
month = 6	294	6.71	4.96



- There is an average decrease of about 1 unit
- The classical analysis of paired data is based on comparisons within subjects:

$$\Delta_i = Y_i(t=0) - Y_i(t=6), \qquad i = 1, \dots, n$$

- A positive  $\Delta_i$  corresponds to a decrease of the square root CD4 cell count, while a negative  $\Delta_i$  is equivalent to an increase
- ullet Testing for a time effect is now equivalent to testing whether the average difference  $\mu_{\Delta}$  equals zero



• The paired *t*-test yields

```
Paired t-test

data: CD4 by obstime t = 6.472, df = 293, p-value = 4.057e-10

alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval:

0.7105585 1.3315439

sample estimates: mean of the differences

1.021051
```



- What if we had ignored the paired nature of the data?
- ullet We then could have used a two-sample (unpaired) t-test to compare the average CD cell count at the two time points

```
Welch Two Sample t-test

data: CD4 by obstime t = 2.565, df = 584.229, p-value = 0.01056
alternative hypothesis: true difference in means is not equal to 0 95 percent confidence interval:
0.2392406 1.8028617
sample estimates: mean in group 0 mean in group 6
7.730128 6.709077
```



- We would still have found a significant difference (p = 0.0106), but the p-value would have been many times larger compared to the one obtained using the paired t-test
- The two-sample *t*-test does not take into account that the measurements are not independent
  - $\triangleright p$ -values **wrongly** too small for *between subjects* effects
  - $\triangleright p$ -values **wrongly** too large for *within subjects* effects
- The different effects
  - between subjects: examine differences between subjects (e.g., males vs females)

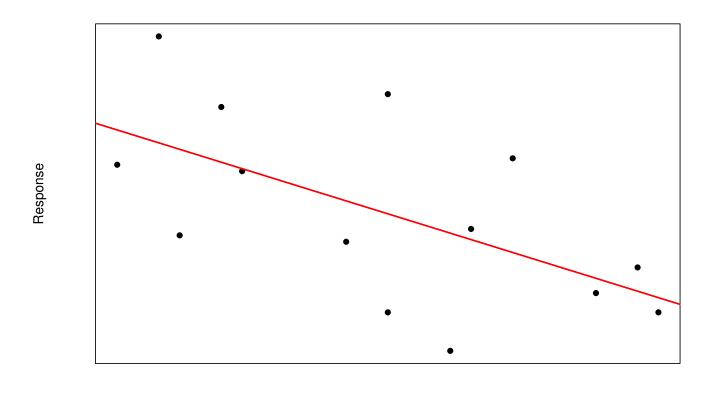


• This illustrates that classical statistical models which assume independent observations will not be optimal for the analysis of clustered data



- Longitudinal studies allow to investigate
  - 1. how treatment means differ at specific time points, e.g., at the end of the study (cross-sectional effect)
  - 2. how treatment means or differences between means of treatments change over time (*longitudinal effect*)
- ullet An example: Suppose it is of interest to study the relation between some response Y and age
  - ▷ a cross-sectional study yields the following data:



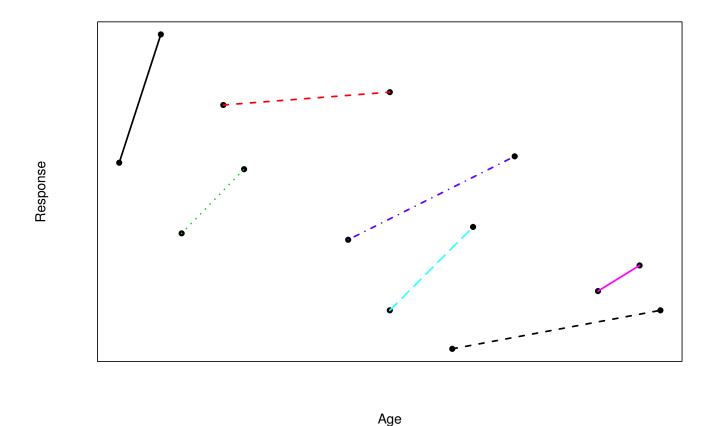


Age



- ullet The graph clearly suggests a negative relation between Y and age
- Nevertheless, exactly the same observations also could have been obtained in a longitudinal study, with 2 measurements per subject







Are we now still inclined to conclude that there is a negative relation between Y and age?

• <u>Conclusion</u>: Longitudinal data allow to distinguish differences between subjects from changes within subjects

#### 1.3 Review of Key Points



- Grouped & longitudinal data: Features
  - > measurements on the same subject are correlated
  - > allow to distinguish within and between subjects effects