## Writing Bayesian Hierarchical Models

#### Models for Socio-Environmental Data

Chris Che-Castaldo, Mary B. Collins, and N. Thompson Hobbs

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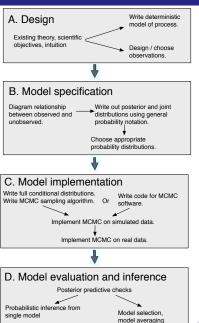
#### What is this course about?



## All modeling problems have idiosyncrasies

- Sampling error in the predictors or responses
- Calibration error for predictors or responses
- Prior knowledge of parameters
- Missing data
- Multiple scales of data (group level effects)
- Prediction and forecasting
- Spatial or temporal dependence
- Derived quantities

## The Bayesian method



### Cross cutting theme

# Things to watch for today

- Sampling error in x's and y's
- Calibration error in y's
- Derived quantities
- Group level effects
- ▶ Treatment effects

All of these will appear in the exercises.

# Things to watch for today

#### Partitioning uncertainty

- Process variance
- Sampling variance
- Calibration variance (aka observation variance)
- Group level variance

## Steps in writing Bayesian models

- 1. Write your deterministic model. Be careful about support.
- 2. Draw Bayesian network (DAG) describing relationships between observed and unobserved quantities.
- 3. Use the Bayesian network to write proportionality between posterior and joint distributions using bracket notation [|].
  - 3.1 Posterior distribution: [unobserved quantities | data]
  - 3.2 Joint distribution
    - 3.2.1 All nodes in Bayesian network at the heads of arrows (children) must be on the left hand side of a conditioning symbol |.
    - 3.2.2 All nodes in Bayesian network at the tails of arrows (parents) must be on the right hand side of a conditioning symbol |.
    - 3.2.3 All nodes at the end of an arrow with no arrow coming into them must be expressed unconditionally, i.e., they must have numeric arguments.
- 4. Assign specific PDF or PMF to each of the brackets.
- 5. Choose numeric values for parameters of prior distributions. Do this sensibly! Do not default to vague priors.