What sets Bayes apart?

Models for Socio-Environmental Data

Chris Che-Castaldo, Mary B. Collins, and N. Thompson Hobbs

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Today

- ▶ Goals
- Some motivation for learning
- ► A high elevation view of Bayesian modeling

Consider statements made by journalists, lawyers, and scientists. What do they have in common? What sets the statements of scientists apart?

Goals



Goals

- Provide principles based understanding
- Foster collaboration
- Build a foundation for self-teaching
- Enhance intellectual satisfaction

Learning objectives

- Understand basic principles of probability and distribution theory.
- 2. Explain maximum likelihood.
- 3. Explain key principles of Bayesian statistics.
- 4. Be able to diagram, write, and implement hierarchical models.
- 5. Explain the Markov chain Monte Carlo (MCMC) algorithm.
- Use software for implementing MCMC methods (i.e., JAGS, R packages).
- Understand procedures for model checking and model selection in the Bayesian framework
- 8. Be able to apply Bayesian methods to a broad array of analysis problems in ecology and social science research

Cross cutting theme

```
ahm
       [a, h, m, \sigma^2 \mid y] \propto \prod_{i=1}^{n} [y_i | \mu_i, \sigma^2][a, h, m, \sigma^2]
model{
      for(i in 1:length(y)){
            mu[i] <- (m*x[i]^a)/(h^a+x[i]^a)
            y[i] ~ dgamma(mu[i]^2/sigma^2,mu[i]/sigma^2)
           dnorm(0,.0001)
           dgamma(.01,.01)
      h ~ dgamma(.01,.01)
      sigma ~ dunif(0,5)
```

Some notation

- y data
- lacktriangledown heta a parameter or other unknown quantity of interest
- lackbox[y| heta] The probability distribution of y conditional on heta
- $lackbox{ } [\theta|y]$ The probability distribution of θ conditional on y
- ▶ $P(y|\theta) = p(y|\theta) = [y|\theta] = f(y|\theta) = f(y,\theta)$, different notation that means the same thing.

Bayesian models are stochastic.

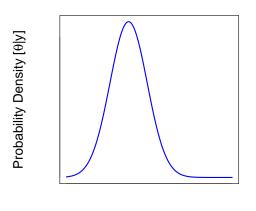
- A model is a mathematical function that returns a quantity (or quantities) given parameters and inputs.
- ► A deterministic model returns a scalar (or sometimes a vector or matrix) for any given set of parameters and inputs.
- ▶ A stochastic model returns a *probability distribution* for any given set of parameters and inputs.
- Probability distributions characterize the behavior of random variables.¹.
- In Bayesian analysis, we seek to understand the probability distributions of random variables of interest using data, models, and prior information (including limited prior information).

¹A random variable is a quantity whose behavior is governed by chance.

What do we do in Bayesian modeling?

- ▶ We divide the world into things that are observed (y) and things that unobserved (θ) .
- ▶ The unobserved quantities (θ) are random variables . The data are random variables before they are observed and fixed after they have been observed.
- ▶ We seek to understand the probability distribution of θ using fixed observations, i.e., $[\theta|y]$.
- ▶ Those distributions quantify our uncertainty about θ .

Bayesian modeling is a procedure for updating knowledge.



An unobserved quanity (θ)

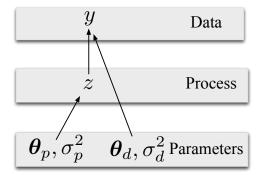


Updating knowledge

Show updating process in R

Why Bayes? One approach applies to many problems

- A deterministic model of a process
- A model of the data
- Models of parameters



Why Bayes? You can understand it.

	Design or Purpose	Measurement Variables	Ranked Variables	Attributes
l variable 1 sample	Examination of a single sample	Procedure for grouping, a Frequency distribution, Box 2.1: stem and leaf display, Section 2.1: esting for outliers, Section 13.4 Computing median of Frequency distribution, Box 4.1 Computing arthribution (Box 4.2) computing arthribution (Box 4.3) computing arthribution (Box 4.3) computing arthribution (Box 4.3) computing and page. Box 4.2: Prequency distribution, Box 4.3 computing and page, Box 6.2: Occupating a gain age, Box 6.2. Computing a gain age, Box 6.2.		Confidence limits for a percentage, Section 17.1 Runs test for randomness in dichotomized data, Box 18.3
	Comparison of a single sample with an expected frequency distribution	Normal expected frequencies, Box 6.1 Goodness of fit tests: parameters from an extrinsic hypothesis, Box 17.2; from an intrinsic hypothesis, Box 17.2 Kolimogroru-Smirrov test of goodness of fit, Box 17.3 Graphic "Test" for normality: large sample sizes, Box 6.3, small sample sizes (rankit test), Box 6.4 Test of sample statics against expected value, Box 7.4		Binomial expected frequencies, Box 5.1 Poisson expected frequencies, Box 5.2 Goodness of fit tests: parameters from an extrinsic hypothesis, Box 17.1; from an intrinsic hypothesis, Box 17.2
1 rariable ≥2 amples	Single classification	Single Classification anniva: single classification anniva: planned comparison of means in anoxa, Box 9.8; Planned comparison of means in anoxa, Box 9.8; single degree of freedom comparisons of means, Box 14.10 Umplanned comparison of means. Therethod, equal sample sizes, Box 9.9; T., GT2, and Tiday-Starmer, unqual sample sizes, Box 9.9; T., GT2, and Tiday-Starmer, unqual sample sizes, Box 9.10; T., and GT2, Box 9.12; multiple confidence limits. Section 14.10 Estimate variance components: unequal sample sizes, Box 9.2; equal sample sizes, Box 9.3 Tests of homogeneity of variances. Box 13.1 Tests of polium of means when variances are heterogeneous, Box 13.2	Kruskal-Wallis test, Bos 13.5 Unplanned comparison of months of the comparison of the comparison of the comparison of the comparison of th	Great for homogeneity of percentages, Boxes 17.3 and 17.8 Comparison of several samples with an expected frequency distribution, Box 17.4 unplanned analysis of reglicated tests of goodness of fit, Box 117.5
	Nested classification	Two-level nested anova: equal sample sizes, Box 10.1; unequal sample sizes, Box 10.4 Three-level nested anova: equal sample sizes, Box 10.3; unequal sample sizes, Box 10.5		
	Two-way or multi-way classification	Two way anous with replication, Box 111, swithout replication, Box 11.2; unequal but in proteinfoal subclass sizes. Box 11.4; with a single missing observation, Box 11.5. Three way anous, Box 12.1 More than-three way classification, Section 12.3 and Box 12.2. Test for nonadiativity in a tow way anous, Box 13.4.	Friedman's method for randomized blocks, Box 13.9	Three way log-linear model, Box 17.9 Randomized blocks for frequency data repeated testing of the same individuals, Box 17.11

Why Bayes? You can understand it.

- Rules of probability
 - Conditioning and independence
 - Law of total probability
 - Factoring joint probabilities
- Distribution theory
- Markov chain Monte Carlo

