Processing Robot and Sensor Log File

Seeking a Circular Target

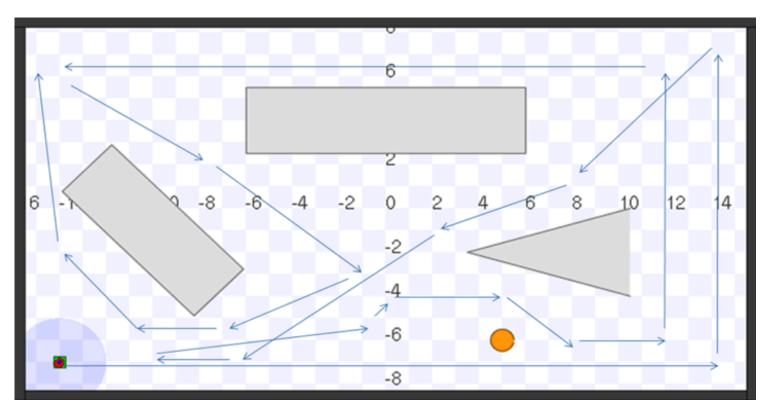


Figure 1: Robot Training Ground.

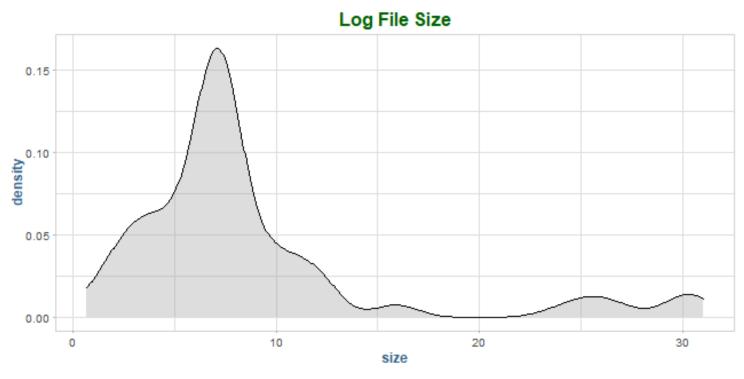
Robot Log Data

```
ff <- list.files(data.dir, full.names = T)
head(ff)</pre>
```

- [1] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/01groundTruth.log"
- [2] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/hasCircle100"
- [3] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31

```
[4] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 12 50
[5] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09
[6] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 13 29
ff <- list.files(data.dir, full.names = T,</pre>
                 pattern = "JRSPdata.*\\.log")
head(ff)
[1] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31
[2] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_50
[3] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 13 09
[4] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_29
[5] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_48
[6] "D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_28
info <- file.info(ff)</pre>
head(info)
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 13 29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_28.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 39 28.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 13 29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_28.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 12 50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 13 48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_28.log
```

```
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 12 50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_28.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 39 28.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_31.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_12_50.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_09.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_13_29.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata 2010 03 10 12 13 48.log
D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_28.log
summary(info$size/1024^2)
   Min. 1st Qu.
                 Median
                           Mean 3rd Qu.
                                           Max.
 0.6832 5.4062 7.1641 8.7556 9.3241 31.0498
file info <- data.frame( size = info$size/1024^2)
ggplot(file_info, aes(size)) +
   geom_density(fill = "darkgrey", alpha = .4) +
   labs(title = "Log File Size")
```



Read Log File

```
i <- which(iface == "position2d" & type == "001")</pre>
   i = i[ iface[i+1] == "laser" & type[i+1] == "001"]
   # Get the time, x, y, and then the range of values
   # from the laser below.
   locations \leftarrow t(sapply(els[i], `[`, c(1, 8, 9)))
   ranges \leftarrow t(sapply(els[i + 1], `[`, seq(14, by = 2, length = 361)))
   # now combine these into a data framee
   locations <- as.data.frame(lapply(1:ncol(locations),</pre>
                                    function(i)
                                        as.numeric(locations[, i])))
   ranges <- as.data.frame(lapply(1:ncol(ranges),</pre>
                                 function(i)
                                     as.numeric(ranges[, i])))
   ans <- cbind(locations, ranges)</pre>
   names(ans) <- c("time", "x", "y",</pre>
                   sprintf("range%d", 1:ncol(ranges)))
   invisible(ans)
}
log <- readLog(filename, lines)</pre>
head(log)
        x y range1 range2 range3 range4 range5 range6 range7 range8 range9
                                          1.723 1.697 1.673
1 0.2 -14 -7 1.838 1.807 1.778 1.749
                                                                1.65 1.628
2 0.4 -14 -7 1.838
                     1.807 1.778 1.749
                                          1.723 1.697 1.673
                                                                1.65 1.628
3 0.6 -14 -7 1.838 1.807 1.778 1.749
                                          1.723 1.697 1.673 1.65 1.628
4 0.8 -14 -7
             1.838
                     1.807
                            1.778 1.749
                                          1.723 1.697
                                                       1.673
                                                               1.65 1.628
5 1.0 -14 -7 1.838
                     1.807 1.778 1.749
                                          1.723 1.697 1.673
                                                                1.65
                                                                      1.628
 1.1 -14 -7 1.838 1.807 1.778 1.749 1.723 1.697 1.673
                                                                1.65 1.628
  range10 range11 range12 range13 range14 range15 range16 range17 range18
1
    1.607
           1.587
                   1.568
                             1.55
                                   1.533
                                           1.517
                                                   1.501
                                                           1.486
                                                                   1.472
   1.607
2
           1.587
                   1.568
                            1.55
                                   1.533
                                           1.517
                                                   1.501 1.486
                                                                   1.472
3
   1.607 1.587 1.568
                            1.55
                                                  1.501 1.486
                                                                   1.472
                                   1.533
                                          1.517
    1.607
4
           1.587
                   1.568
                            1.55
                                   1.533
                                           1.517
                                                   1.501
                                                          1.486
                                                                   1.472
5
    1.607
           1.587
                   1.568
                             1.55
                                   1.533
                                           1.517
                                                   1.501
                                                           1.486
                                                                   1.472
    1.607
                            1.55
                                   1.533
                                                   1.501
6
           1.587
                   1.568
                                           1.517
                                                           1.486
                                                                   1.472
  range19 range20 range21 range22 range23 range24 range25 range26 range27
    1.459
            1.446
                    1.434
                            1.423
                                    1.412
                                           1.402
                                                   1.392
                                                           1.383
                                                                   1.375
```

2	1.459	1.446	1.434	1.423	1.412	1.402	1.392	1.383	1.375
3	1.459	1.446	1.434	1.423	1.412	1.402	1.392	1.383	1.375
4	1.459	1.446	1.434	1.423	1.412	1.402	1.392	1.383	1.375
5	1.459	1.446	1.434	1.423	1.412	1.402	1.392	1.383	1.375
6	1.459	1.446	1.434	1.423	1.412	1.402	1.392	1.383	1.375
	range28	range29	range30	range31	range32	range33	range34	range35	range36
1	1.367	1.359	1.352	1.346	1.34	1.334	1.329	1.324	1.32
2	1.367	1.359	1.352	1.346	1.34	1.334	1.329	1.324	1.32
3	1.367	1.359	1.352	1.346	1.34	1.334	1.329	1.324	1.32
4	1.367	1.359	1.352	1.346	1.34	1.334	1.329	1.324	1.32
5	1.367	1.359	1.352	1.346	1.34	1.334	1.329	1.324	1.32
6	1.367	1.359	1.352	1.346	1.34	1.334	1.329	1.324	1.32
	range37	range38	range39	range40	range41	range42	range43	range44	range45
1	1.316	1.313	1.31	1.307	1.305	1.303	1.302	1.301	1.3
2	1.316	1.313	1.31	1.307	1.305	1.303	1.302	1.301	1.3
3	1.316	1.313	1.31	1.307	1.305	1.303	1.302	1.301	1.3
4	1.316	1.313	1.31	1.307	1.305	1.303	1.302	1.301	1.3
5	1.316	1.313	1.31	1.307	1.305	1.303	1.302	1.301	1.3
6	1.316	1.313	1.31	1.307	1.305	1.303	1.302	1.301	1.3
	range46	range47	range48	range49	range50	range51	range52	range53	range54
1	1.3	1.3	1.301	1.302	1.303	1.305	1.307	1.31	1.313
2	1.3	1.3	1.301	1.302	1.303	1.305	1.307	1.31	1.313
3	1.3	1.3	1.301	1.302	1.303	1.305	1.307	1.31	1.313
4	1.3	1.3	1.301	1.302	1.303	1.305	1.307	1.31	1.313
5	1.3	1.3	1.301	1.302	1.303	1.305	1.307	1.31	1.313
6	1.3	1.3	1.301	1.302	1.303	1.305	1.307	1.31	1.313
	range55	range56	range57	range58	range59	range60	range61	range62	range63
1	1.316	1.32	1.324	1.329	1.334	1.34	1.346	1.352	1.359
2	1.316	1.32	1.324	1.329	1.334	1.34	1.346	1.352	1.359
3	1.316	1.32	1.324	1.329	1.334	1.34	1.346	1.352	1.359
4	1.316	1.32	1.324	1.329	1.334	1.34	1.346	1.352	1.359
5	1.316	1.32	1.324	1.329	1.334	1.34	1.346	1.352	1.359
6	1.316	1.32	1.324	1.329	1.334	1.34	1.346	1.352	1.359
	range64	range65	range66	range67	range68	range69	range70	range71	range72
1	1.367	1.375	1.383	1.392	1.402	1.412	1.423	1.434	1.446
2	1.367	1.375	1.383	1.392	1.402	1.412	1.423	1.434	1.446
3	1.367	1.375	1.383	1.392	1.402	1.412	1.423	1.434	1.446
4	1.367	1.375	1.383	1.392	1.402	1.412	1.423	1.434	1.446
5	1.367	1.375	1.383	1.392	1.402	1.412	1.423	1.434	1.446
6	1.367	1.375	1.383	1.392	1.402	1.412	1.423	1.434	1.446
	range73	range74	range75	range76	range77	range78	range79	range80	range81
1	1.459	1.472	1.486	1.501	1.517	1.533	1.55	1.568	1.587
2	1.459	1.472	1.486	1.501	1.517	1.533	1.55	1.568	1.587
3	1.459	1.472	1.486	1.501	1.517	1.533	1.55	1.568	1.587
4	1.459	1.472	1.486	1.501	1.517	1.533	1.55	1.568	1.587

5	1.459	1.472	1.486	1.501	1.	517	1.5	533	1.5	5 1.568	1.587
6	1.459	1.472	1.486	1.501	1.	517	1.5	533	1.5	5 1.568	1.587
	range82	range83	range84	range85	rang	ge86	range	e87	range8	8 range89	range90
1	1.607	1.628	1.65	1.673	1.	697	1.7	723	1.74	9 1.778	3 1.807
2	1.607	1.628	1.65	1.673	1.	697	1.7	723	1.74	9 1.778	1.807
3	1.607	1.628	1.65	1.673	1.	697	1.7	723	1.74	9 1.778	3 1.807
4	1.607	1.628	1.65	1.673	1.	697	1.7	723	1.74	9 1.778	1.807
5	1.607	1.628	1.65	1.673		697		723	1.74		
6	1.607	1.628	1.65	1.673		697	1.7		1.74		
										7 range98	
1	1.838	1.843	1.905	1.941	_	2		2		2 2	•
2	1.838	1.843	1.905	1.941		2		2		2 2	
3	1.838	1.843	1.905	1.941		2		2		2 2	
4	1.838	1.843	1.905	1.941		2		2		2 2	
5	1.838	1.843	1.905	1.941		2		2		2 2	
6	1.838	1.843	1.905	1.941		2		2		2 2	
U					o103		ro10/		mo 105	range106	
1	2	_	71 Tange. 2	2	2	1 0116	2	ı aı	2	2	2
2	2		2	2	2		2		2	2	2
3	2		2	2	2		2		2	2	2
4	2		2	2	2		2		2	2	2
5	2		2	2	2		2		2	2	2
	2		2	2	2		2		2	2	2
6	_		_								
4	•	•	•	•		rang	-	ran	•	range114	•
1	2		2	2	2		2		2	2	2
2	2		2	2	2		2		2	2	2
3	2		2	2	2		2		2	2	2
4	2		2	2	2		2		2	2	2
5	2		2	2	2		2		2	2	2
6	2		2	2	2		2		2	2	2
						rang		ran		range122	
1	2		2	2	2		2		2	2	2
2	2		2	2	2		2		2	2	2
3	2		2	2	2		2		2	2	2
4	2		2	2	2		2		2	2	2
5	2		2	2	2		2		2	2	2
6	2		2	2	2		2		2	2	2
	range124	range12	25 range:	126 rang	e127	rang	ge128	ran	ge129	range130	range131
1	2		2	2	2		2		2	2	2
2	2		2	2	2		2		2	2	2
3	2		2	2	2		2		2	2	2
4	2		2	2	2		2		2	2	2
5	2		2	2	2		2		2	2	2
6	2		2	2	2		2		2	2	2
	range132	range13	33 range	134 rang	e135	rang	ge136	ran	ge137	range138	range139

	•		•				•	•
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	_		range142				_	
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
			range150					
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range156	range157	range158	range159	range160	range161	range162	range163
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range164	range165	range166	range167	range168	range169	range170	range171
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range172	range173	range174	range175	range176	range177	range178	range179
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
-			range182					
1	2	2	2	2	2	2	2	2
2								
_	2	2	2	2	2	2	2	2

_		_	_	_	_	_	_	_
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range188		range190		range192	range193	range194	range195
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range196	range197	range198	range199	range200	range201	range202	range203
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range204	range205	range206	range207	range208	range209	range210	range211
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range212	range213	range214	range215	range216	range217	range218	range219
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range220	range221	range222	range223	range224	range225	range226	range227
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range228	range229	range230	range231	range232	range233	range234	
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2

	range236	range237	range238	range239	range240	range241	range242	range243
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
Ü	range 244	range 245	range 246	range 247	range248	range 249	range 250	range251
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
ک ۱	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
О	2	2	2	2	2	2	2	2
	range252	_	range254	_	range256	range257	range258	range259
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range260	range261	range262	range263	range264	range265	range266	range267
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
	range268	range269	range270	range271	range272	range273	range274	range275
1	2	2	2	2	2	2	2	2
2	2	2	2	2	2	2	2	2
3	2	2	2	2	2	2	2	2
4	2	2	2	2	2	2	2	2
5	2	2	2	2	2	2	2	2
6	2	2	2	2	2	2	2	2
					range280			
1	1.958	1.93	1.904	1.878	1.854	1.831	1.809	1.789
2	1.958	1.93	1.904	1.878		1.831	1.809	1.789
3	1.958	1.93	1.904	1.878		1.831		1.789
4	1.958	1.93	1.904	1.878		1.831	1.809	1.789
5	1.958	1.93	1.904	1.878		1.831		1.789
6	1.958	1.93	1.904	1.878	1.854	1.831	1.809	1.789
O								
4	-	_	_	_	range288	_	_	_
1	1.769	1.75	1.732	1.715	1.699	1.683	1.669	1.655
2	1.769	1.75	1.732	1.715	1.699	1.683	1.669	1.655

3	1.769	1.75	1.732	1.715	1.699	1.683	1.669	1.655
4	1.769	1.75	1.732	1.715	1.699	1.683	1.669	1.655
5	1.769	1.75	1.732	1.715	1.699	1.683	1.669	1.655
6	1.769	1.75	1.732	1.715	1.699	1.683	1.669	1.655
	range292	range293	range294	range295	range296	range297	range298	range299
1	1.642	1.63	1.618	1.607	1.596	1.586	1.577	1.569
2	1.642	1.63	1.618	1.607	1.596	1.586	1.577	1.569
3	1.642	1.63	1.618	1.607	1.596	1.586	1.577	1.569
4	1.642	1.63	1.618	1.607	1.596	1.586	1.577	1.569
5	1.642	1.63	1.618	1.607	1.596	1.586	1.577	1.569
6	1.642	1.63	1.618	1.607	1.596	1.586	1.577	1.569
	range300	range301	range302	range303	range304	range305	range306	range307
1	1.56	1.553	1.546	1.539	1.534	1.528	1.523	1.519
2	1.56	1.553	1.546	1.539	1.534	1.528	1.523	1.519
3	1.56	1.553	1.546	1.539	1.534	1.528	1.523	1.519
4	1.56	1.553	1.546	1.539	1.534	1.528	1.523	1.519
5	1.56	1.553	1.546	1.539	1.534	1.528	1.523	1.519
6	1.56	1.553	1.546	1.539	1.534	1.528	1.523	1.519
	range308	range309	range310	range311	range312	range313	range314	range315
1	1.515	1.511	1.508	1.506	1.504	1.502	1.501	1.5
2	1.515	1.511	1.508	1.506	1.504	1.502	1.501	1.5
3	1.515	1.511	1.508	1.506	1.504	1.502	1.501	1.5
4	1.515	1.511	1.508	1.506	1.504	1.502	1.501	1.5
5	1.515	1.511	1.508	1.506	1.504	1.502	1.501	1.5
6	1.515	1.511	1.508	1.506	1.504	1.502	1.501	1.5
	range316	range317	range318	range319	range320	range321	range322	range323
1	1.5	1.5	1.501	1.502	1.504	1.506	1.508	1.511
2	1.5	1.5	1.501	1.502	1.504	1.506	1.508	1.511
3	1.5	1.5	1.501	1.502	1.504	1.506	1.508	1.511
4	1.5	1.5	1.501	1.502	1.504	1.506	1.508	1.511
5	1.5	1.5	1.501	1.502	1.504	1.506	1.508	1.511
6	1.5	1.5	1.501	1.502	1.504	1.506	1.508	1.511
	range324	range325	•	range327	range328	range329	range330	range331
1	1.515	1.519	1.523	1.528	1.534	1.539	1.546	1.553
2	1.515	1.519	1.523	1.528	1.534	1.539	1.546	1.553
3	1.515	1.519	1.523	1.528	1.534	1.539	1.546	1.553
4	1.515	1.519	1.523	1.528	1.534	1.539	1.546	1.553
5	1.515	1.519	1.523	1.528	1.534	1.539	1.546	1.553
6	1.515	1.519	1.523	1.528		1.539	1.546	1.553
	range332	range333	range334	range335	range336	range337	range338	range339
1	1.56	1.569	1.577	1.586	1.596	1.607	1.618	1.63
2	1.56	1.569	1.577	1.586	1.596	1.607	1.618	1.63
3	1.56	1.569		1.586				
4	1.56	1.569	1.577	1.586	1.596	1.607	1.618	1.63
5	1.56	1.569	1.577	1.586	1.596	1.607	1.618	1.63

```
6
      1.56
               1.569
                        1.577
                                  1.586
                                            1.596
                                                                          1.63
                                                      1.607
                                                               1.618
  range340 range341 range342 range343 range344 range345 range346 range347
1
     1.642
               1.655
                        1.669
                                  1.683
                                            1.701
                                                      1.716
                                                               1.738
                                                                         1.765
2
     1.642
               1.655
                        1.669
                                  1.683
                                            1.701
                                                      1.716
                                                               1.738
                                                                         1.765
3
     1.642
              1.655
                        1.669
                                  1.683
                                            1.701
                                                      1.716
                                                               1.738
                                                                         1.765
4
     1.642
              1.655
                        1.669
                                  1.683
                                            1.701
                                                      1.716
                                                               1.738
                                                                         1.765
5
     1.642
              1.655
                        1.669
                                  1.683
                                            1.701
                                                      1.716
                                                               1.738
                                                                         1.765
                                                               1.738
6
     1.642
               1.655
                        1.669
                                  1.683
                                            1.701
                                                      1.716
                                                                         1.765
  range348 range349 range350 range351 range352 range353 range354 range355
1
     1.774
               1.811
                        1.817
                                  1.852
                                            1.864
                                                      1.885
                                                               1.921
                                                                         1.941
2
     1.774
               1.811
                        1.817
                                            1.864
                                                      1.885
                                                               1.921
                                                                         1.941
                                  1.852
3
     1.774
              1.811
                                                                         1.941
                        1.817
                                  1.852
                                            1.864
                                                      1.885
                                                               1.921
4
     1.774
              1.811
                        1.817
                                  1.852
                                            1.864
                                                      1.885
                                                               1.921
                                                                         1.941
5
     1.774
               1.811
                        1.817
                                  1.852
                                            1.864
                                                               1.921
                                                                         1.941
                                                      1.885
6
     1.774
               1.811
                        1.817
                                  1.852
                                            1.864
                                                      1.885
                                                               1.921
                                                                         1.941
  range356 range357 range358 range359 range360 range361
1
     1.978
                   2
                        1.944
                                  1.889
                                            1.835
                                                      1.838
2
     1.978
                   2
                        1.944
                                  1.889
                                            1.835
                                                      1.838
3
     1.978
                   2
                        1.944
                                  1.889
                                            1.835
                                                     1.838
4
     1.978
                   2
                        1.944
                                  1.889
                                            1.835
                                                      1.838
5
     1.978
                   2
                        1.944
                                  1.889
                                            1.835
                                                      1.838
6
     1.978
                   2
                        1.944
                                  1.889
                                            1.835
                                                      1.838
```

Data Exploration

```
system.time(logs <- lapply(ff, readLog))

user system elapsed
110.86   0.83   111.74

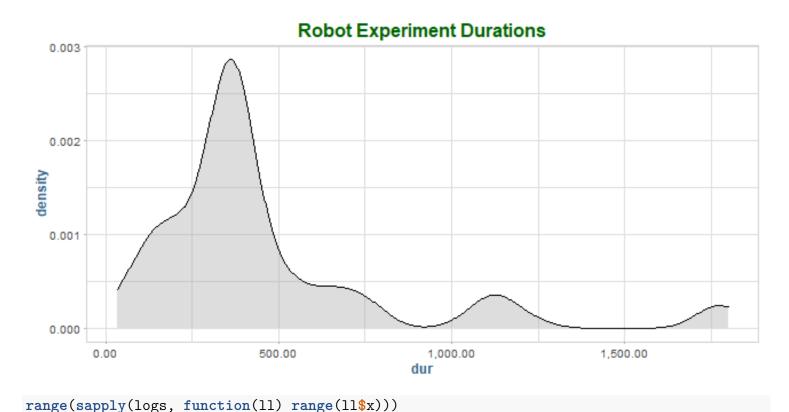
names(logs) <- ff

dur <- sapply(logs, function(x) x$time[nrow(x)] - x$time[1])

range(dur)

[1]   33.8   1799.7

ggplot(data.table(dur * 30 * 60), aes(dur)) +
   geom_density(fill = "darkgrey", alpha = .4) +
   labs(title = "Robot Experiment Durations") +
   scale_x_continuous(labels = comma)</pre>
```



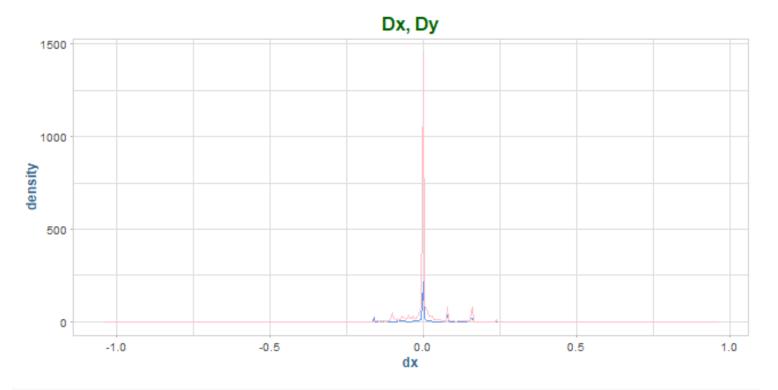
```
[1] -14.910 14.546
range(sapply(logs, function(ll) range(ll$y)))
[1] -7.713 7.316
table(sapply(logs, function(ll) all( diff(ll$time) > 0)))
TRUE
 100
deltas <- unlist(lapply(logs, function(ll) diff(ll$time)))</pre>
summary(deltas)
   Min. 1st Qu. Median
                          Mean 3rd Qu.
                                          Max.
 0.1000 0.1000 0.2000 0.1746 0.2000 8.8000
quantile(deltas, seq(.99, 1, length = 11))
  99% 99.1% 99.2% 99.3% 99.4% 99.5% 99.6% 99.7% 99.8% 99.9% 100%
  0.5
       0.5
             0.5
                   0.5
                         0.5
                                     0.5
                               0.5
                                           0.5
                                                 0.5
                                                       0.5
                                                              8.8
which.max(deltas)
```

D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_12_39_46.log2

nrow(logs[["D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_1

```
[1] 2184
```

```
summary(sapply(logs, nrow))
   Min. 1st Qu. Median
                            Mean 3rd Qu.
                                             Max.
    208
           1647
                    2182
                            2666
                                     2840
                                             9448
11 <- logs[["D:/Projects/Statistical-Computing/Case Studies/datasets/robot/JRSPdata_2010_03_10_
i <- which.max(diff(ll$time))</pre>
delta.x <- unlist(lapply(logs, function(ll) diff(ll\$x)))</pre>
delta.y <- unlist(lapply(logs, function(ll) diff(ll$y)))</pre>
delta_df <- data.table(dx = delta.x, dy = delta.y)</pre>
ggplot(delta df) +
   geom_density(aes(dx), col = "cornflowerblue") +
   geom_density(aes(dy), col = "pink") +
   labs(title = "Dx, Dy", xlab = "Distance", ylab = "Density")
```

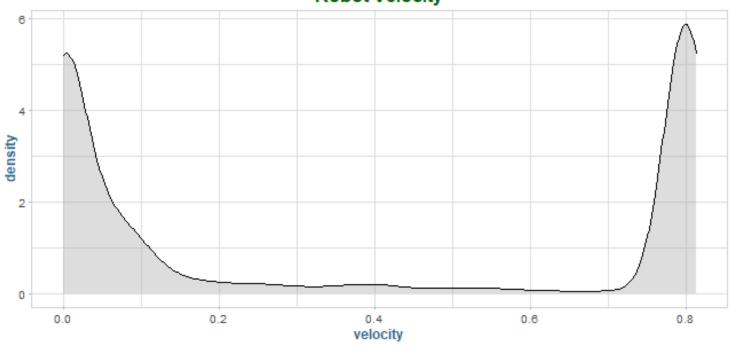


```
tail(sort(table(delta.x)))
```

delta.x

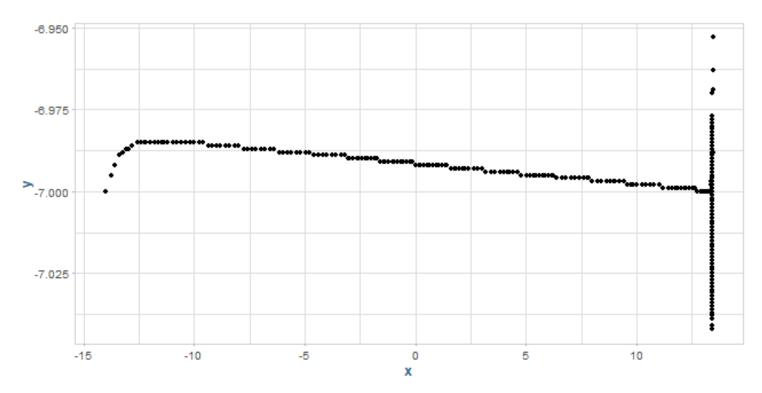
```
-0.080000000000001 0.00099999999999446
                                                           -0.16
                4220
                                      6924
                                                            8879
                0.16
                       0.0800000000000001
                                                               0
               11031
                                                          105168
                                     11701
velocity <- lapply(logs, function(ll) sqrt( diff(ll\$x)^2 + diff(ll\$y)^2)/diff(ll\$time))</pre>
velocity_df <- data.table( velocity = unlist(velocity))</pre>
summary(velocity_df$velocity)
   Min. 1st Qu. Median
                            Mean 3rd Qu.
                                            Max.
 0.0000 0.0000 0.1350 0.3708 0.8000 0.8130
ggplot(velocity_df, aes(velocity)) +
   geom_density(fill = "darkgrey", alpha = .4) +
   labs(title = "Robot Velocity")
```

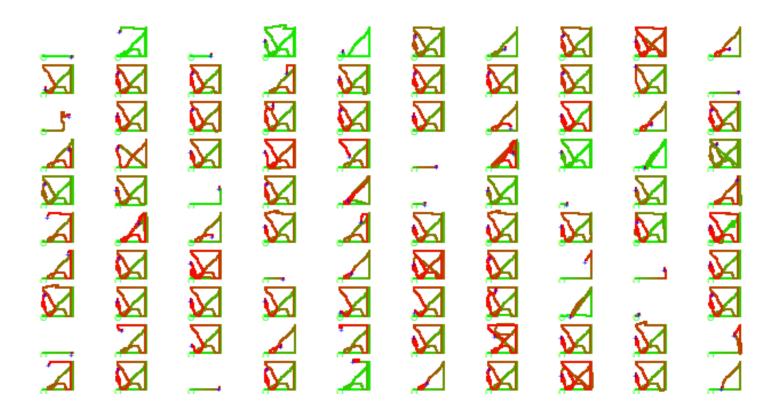
Robot Velocity



```
plot_path <- function(ll) {
    ggplot(ll, aes(x, y)) +
        geom_point()
}

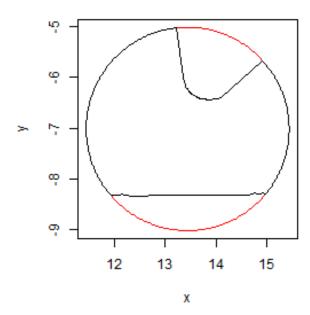
plot_path(logs[[1]])</pre>
```





Exploring a "Look"

```
plot.Look <-</pre>
   function(row, ...) {
      x \leftarrow row[1, "x"]
      y <- row[1, "y"]
      theta \leftarrow seq(0, 2*pi, length = 360) - pi/2
      r \leftarrow as.numeric(row[1, -c(1:3, 365)])
      x1 \leftarrow x + r * cos(theta)
      y1 \leftarrow y + r * sin(theta)
      par(pty = 's')
      plot(x + 2*cos(theta), y + 2*sin(theta),
            col = "red", type = "1",
            xlab = "x", ylab = "y", ...)
      points(x1, y1, type = "1")
   }
par(mfrow = c(1,1))
plot.Look(logs[[1]][ nrow(logs[[1]]), ])
```



```
par(mfrow = c(1, 1))

index <- 2
row <- logs[[index]][ nrow(logs[[index]]), ]

x <- row[1, "x"]
y <- row[1, "y"]

theta <- seq(0, 2*pi, length = 360) - pi/2
r <- as.numeric(row[1, -c(1:3, 365)])

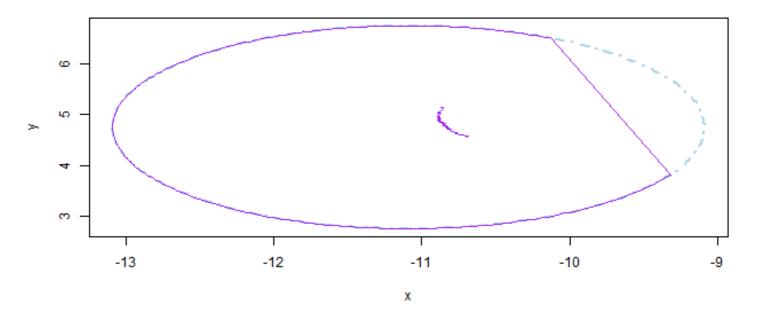
x1 <- x + r * cos(theta)</pre>
```

Warning in r * cos(theta): longer object length is not a multiple of shorter object length

```
y1 <- y + r * sin(theta)
```

```
eq2 <- cbind( x = x1[ which(r == 2) ], y = y1[ which(r == 2) ] )
lt2 <- cbind( x = x1[ which(r < 2) ], y = y1[ which(r < 2) ] )

points(eq2, type = "l", col="purple")
points(lt2, type ="l", col = "purple")</pre>
```



```
lt2 <- cbind( x = x1[ which(r < 2) ], y = y1[ which(r < 2) ] )
  points(eq2, type = "1", col="purple")
  points(lt2, type ="l", col = "purple")
}
par(mar = rep(0, 4), mfrow = c(10, 10), pty = 's')
invisible(lapply(logs, function(ll)
  plot.Look2(ll[ nrow(ll), ], axes = FALSE)))
Warning in r * cos(theta): longer object length is not a multiple of shorter
object length
Warning in r * sin(theta): longer object length is not a multiple of shorter
object length
Warning in r * cos(theta): longer object length is not a multiple of shorter
object length
Warning in r * sin(theta): longer object length is not a multiple of shorter
object length
Warning in r * cos(theta): longer object length is not a multiple of shorter
object length
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object length
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object length
Warning in r * sin(theta): longer object length is not a multiple of shorter
object length
Warning in r * cos(theta): longer object length is not a multiple of shorter
object length
Warning in r * sin(theta): longer object length is not a multiple of shorter
object length
Warning in r * cos(theta): longer object length is not a multiple of shorter
object length
Warning in r * sin(theta): longer object length is not a multiple of shorter
object length
Warning in r * cos(theta): longer object length is not a multiple of shorter
object length
Warning in r * sin(theta): longer object length is not a multiple of shorter
```

```
object length
```

Warning in r * sin(theta): longer object length is not a multiple of shorter object length

Warning in r * cos(theta): longer object length is not a multiple of shorter object length

Warning in r * sin(theta): longer object length is not a multiple of shorter object length

Warning in r * cos(theta): longer object length is not a multiple of shorter object length

Warning in r * sin(theta): longer object length is not a multiple of shorter object length

Warning in r * cos(theta): longer object length is not a multiple of shorter object length

Warning in r * sin(theta): longer object length is not a multiple of shorter object length

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Warning in r * sin(theta): longer object length is not a multiple of shorter object length

Warning in r * cos(theta): longer object length is not a multiple of shorter object length

Warning in r * sin(theta): longer object length is not a multiple of shorter object length

```
Warning in r * sin(theta): longer object length is not a multiple of shorter object length
```

Warning in r * sin(theta): longer object length is not a multiple of shorter object length

Warning in r * cos(theta): longer object length is not a multiple of shorter object length

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Warning in r * sin(theta): longer object length is not a multiple of shorter object length
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Warning in r * sin(theta): longer object length is not a multiple of shorter object length

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Warning in r * sin(theta): longer object length is not a multiple of shorter object length
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Warning in r * sin(theta): longer object length is not a multiple of shorter object length

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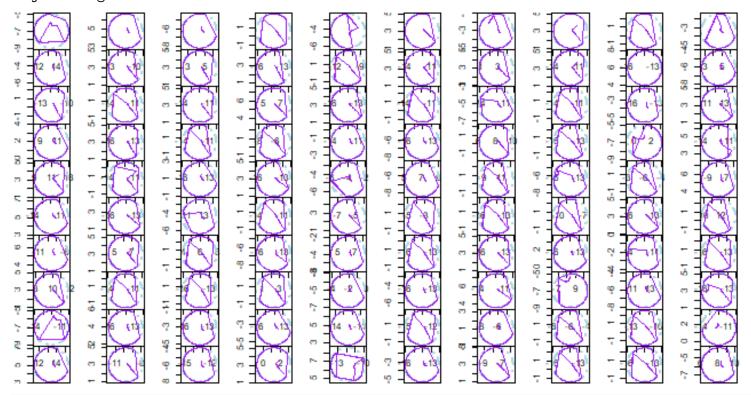
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e <- unlist(lapply(logs, function(ll) ll\$range1 - ll\$range361))
summary(e)</pre>

Min. 1st Qu. Median Mean 3rd Qu. Max.
0 0 0 0 0 0

class(11)

```
[1] "data.frame"
getRangeErrors <- function(11) {</pre>
   ll$pos <- sprintf("%.3f,%.3f", ll$x, ll$y)
   w <- duplicated(ll$pos)</pre>
   if(any(w)) {
      tmp <- 11[ 11$pos %in% 11$pos[w], ]</pre>
      errs <- unlist(by(tmp[, 4:364], tmp$pos, scale, scale = F,
                         simplify = F)
      errs
   }
}
rangeErrs <- unlist(lapply(logs, getRangeErrors))</pre>
finalLooks <- lapply(logs, function(ll) ll[nrow(ll), ])</pre>
length(finalLooks)
Γ1 100
par(mar = rep(0, 4), mfrow = c(10, 10), pty = 's')
invisible(lapply(finalLooks, function(ll)
   plot.Look2(11[ nrow(11), ], axes = F)))
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