

ETC 2420/5242 Lab 4 2016

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Week 4

Purpose

This lab is to examine different statistical distributions, fit distributions to samples by estimating the parameters by maximum likelihood and checking the fit with QQ-plots.

Reading

Read the material on maximum likelihood estimation at <https://onlinecourses.science.psu.edu/stat414/node/191>.

Read the code in the lecture notes from Week 3. Particularly look at the functions for making QQ-plots, computing and plotting the likelihood functions.

Warmup exercises

- Compute these probabilities for $X \sim N(2, 0.5)$
 - $P(X < 1.3)$
 - $P(X > 1.9)$
 - $P(1.8 < X < 2.2)$
- Compute the quantile value (X) for $X \sim N(-3, 4)$ which matches these probabilities
 - $P(X < x) = 0.53$
 - $P(X < x) = 0.12$
 - $P(X < x) = 0.84$
 - $P(X < x) = 1.2$
- Compute the value of the density function for a $N(-1.2, 0.8)$ corresponding to $X =$
 - -1.0
 - -0.2
 - -2.0
- Plot the density curves a
 - $Weibull(2.5, 2)$
 - $Weibull(2.5, 1)$
 - $Weibull(1, 1)$ on the same plot.

Question 1

1. Simulate samples of size $n = 30, 100, 500$ from these distributions
 - a. Lognormal(2, 5)
 - b. Gamma(2, 4)
2. Make a QQ-plot of each these samples.

Question 2

Using this code, generate a sample of size $n = 267$ from a $\text{Gamma}(1.2, 0.25)$ distribution.

```
set.seed(123)
X2 <- data.frame(x=rgamma(n=267, 1.2, 0.25))
```

- Plot the sample, using a histogram, describe the shape of the distribution.
- What parameters of the gamma distribution were used to simulate the sample? (α, β)
- If we are to use maximum likelihood distribution what values would we expect to get as the parameter estimates?
- Write a function to compute the likelihood function.
- Plot the likelihood function for a range of values of α, β that shows the maximum likelihood estimates for each parameter.
- Look up the function `fitdistr` from the `MASS` library. Explain what this does. Use it to find the MLE estimates for α, β . How do these compare with the values you read off your plot?

Question 3

Take a look at the data set `danishuni` from the `CASdatasets` library.

```
library(CASdatasets)
data(danishuni)
```

- Make a histogram of the `Loss`. Describe the shape.
- Fit both a gamma and lognormal distribution to the sample, i.e. find the MLEs.
- Produce a QQ-plot for each of the distributions.
- Which is the better fit to the sample?
- Re-do steps a-d after log-transforming the `Loss`.

TURN IN

- Your `.Rmd` file
- Your Word (or pdf) file that results from knitting the `Rmd`.
- Make sure your group members are listed as authors, one person per group will turn in the report
- DUE: Wednesday after the lab, by 7am, loaded into moodle

Resources

- PSU lecture notes on MLE
- `CASdatasets`