Lab1

Ludwig Thaung Elon Brange (ludth852, elobr959) 2019-04-01

Task 1

a)

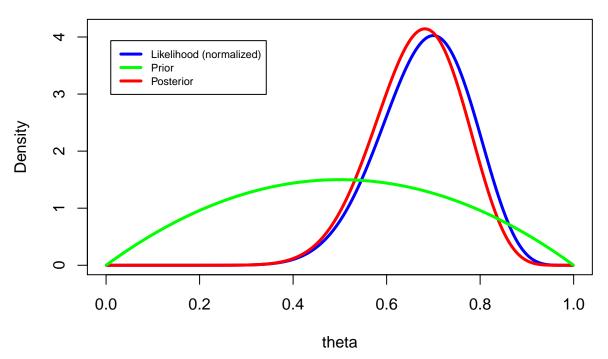
For 20 and 10000 draws repectively we get:

[1] "Posterior Mean GT: 0.66666666666667"

[1] "ground truth std: 0.0942809041582063"

[1] "std: 0.108916008104342" ## [1] "Mean: 0.693247041754232"

Bernoulli model - Beta(a,b) prior



- ## [1] "Posterior Mean GT: 0.66666666666667"
- ## [1] "ground truth std: 0.0942809041582063"
- ## [1] "std: 0.0932435668335933"

[1] "Mean: 0.66722315799665"

Posterior mean GT is the value that the posterior distribution mean is converging to.

b)

```
## [1] "propability condition with random: 0.0036"
```

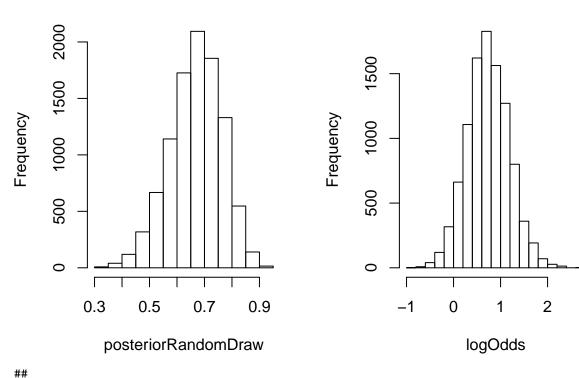
[1] "ground truth probability: 0.00397268082810898"

Looking at the plot above, the probability for theta < 0.5 | y is very small. The simulated value is relatively close to the ground truth. (Note: The further to the left on the tail, the larger sample we will need as the data points become more sparse.)

c)

Histogram of posteriorRandomDr

Histogram of logOdds



```
## Call:
    density.default(x = logOdds)
##
##
  Data: logOdds (10000 obs.); Bandwidth 'bw' = 0.06366
##
##
##
                               :0.0000071
##
           :-1.03007
                        Min.
    Min.
    1st Qu.:-0.03592
                        1st Qu.:0.0055394
##
    Median : 0.95823
                        Median :0.0783128
##
           : 0.95823
                               :0.2512249
    Mean
                        Mean
##
    3rd Qu.: 1.95239
                        3rd Qu.:0.4653388
    Max.
           : 2.94654
                               :0.9318959
                        Max.
```

Task 2

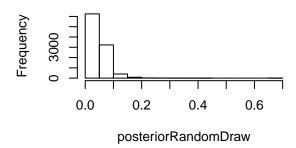
b

 \mathbf{a} ## Warning: package 'LaplacesDemon' was built under R version 3.4.4 The following objects are masked from mtcars (pos = 5): ## am, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs, wt ## **CDF** posterior random draws **Chi Posterior of Variance** Cumulative probability Density 0.4 10 0.0 2000 0.0 0.2 0.4 0.6 0.8 1.0 0 6000 10000

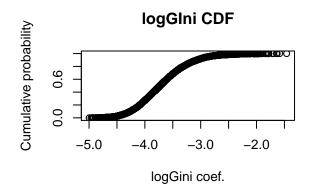
no. of draws

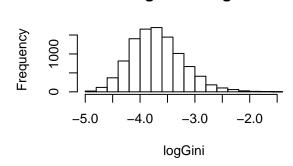
Histogram of posteriorRandomDraw

theta

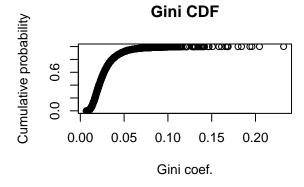


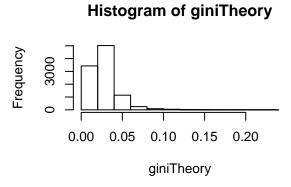
The following objects are masked from mtcars (pos = 3):
##
am, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs, wt
The following objects are masked from mtcars (pos = 6):
##
am, carb, cyl, disp, drat, gear, hp, mpg, qsec, vs, wt





Histogram of logGini





```
##
## Call:
    density.default(x = middleData)
##
## Data: middleData (9501 obs.);
                                     Bandwidth 'bw' = 0.001563
##
##
                               : 0.00192
           :0.006417
##
    Min.
                       Min.
##
    1st Qu.:0.023728
                       1st Qu.: 2.21714
    Median :0.041039
                       Median: 7.78380
##
    Mean
           :0.041039
                       Mean
                               :14.42745
    3rd Qu.:0.058350
                       3rd Qu.:25.56459
##
           :0.075661
                               :43.48395
   Max.
                       Max.
## [1] 0.01110461
## [1] 0.070973
```

Task 3

 \mathbf{a}

 \mathbf{c}

b