

# Applied Bayesian Statistics

## Class Assignment 2

*Simon Roth*

*nomis.roth@gmx.net*

*14.01.2019*

## Packages

**Note** This is Rmarkdown document which combines the entire code, outputs and text. If you don't have *pacman* installed, just get it once from CRAN and it will manage all the rest of the dependencies (for ever).

```
# install.packages("pacman")
pacman::p_load(
  tidyverse, rjags, purrr, tidyr, broom,
  texreg, ggthemes, janitor, knitr
)
ggplot2::theme_set(theme_bw())
set.seed(2018)
```

## Helper

## Data

A reduced dataset of Student Panel Survey during the Lecture in Introduction to Political Methodology Winter term 2016/2017 at the University of Konstanz

- **poleff** Political Efficacy (Likert Score based on 7 items) A larger value = higher level of efficacy
- **friend** Number of alteri in friendship network
- **poldisc** Number of alteri in political discussion network
- **lr.self** Ideological orientation (left right self-placement) 1: Left <- -> 11: Right
- **lr.self.2** Ideological orientation (left right self-placement, second measurement) 1: Left <- -> 11: Right
- **univ.election** Vote intention at the next university election. 1: Yes; 0: other (No and DK)
- **polint** interest at university politics 1: not interested at all <- -> 5 strongly interested
- **tuition** opinion on the general tuition fee for German universities 1: support; 2: reject; 3: indifferent
- **acceptable** acceptable level of the tuition fee (in Euro per Semester) (Only those who support the tuition fee or indifferent)
- **protest1 - protest6** willingness to participate a protest action against the general tuition fee 1: yes; 0: no
  - **protest1** demonstration in Konstanz
  - **protest2** demonstration in Stuttgart
  - **protest3** giving signature at petitions
  - **protest4** strike
  - **protest5** occupation of university buildings
  - **protest6** legal dispute at courts

```
dat <- get(load("data/Bayes_Student_Survey.RData")) %>%
  drop_na(univ.election, lr.self)

dat %>% glimpse
```

```
## Observations: 158
## Variables: 17
## $ id          <dbl> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 1...
## $ male        <dbl> 1, 0, 1, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 1, 0, 0, ...
## $ friend      <dbl> 5, 4, 6, 6, 0, 6, 9, 0, 0, 2, 0, 0, 9, 4, 1, 1, ...
## $ poldisc     <dbl> 7, 2, 1, 1, 0, 7, 3, 0, 0, 2, 0, 0, 11, 4, 0, 1, ...
## $ poleff      <dbl> 25, 23, 23, 22, 23, 26, 26, 22, 21, 28, 13, 24, ...
## $ lr.self     <dbl> 2, 3, 8, 5, 8, 4, 6, 5, 7, 5, 6, 7, 2, 6, 5, 3, ...
## $ lr.self.2   <dbl> 3, NA, 8, 5, 7, 4, 6, 5, NA, 7, 8, NA, 3, 6, 6, ...
## $ univ.election <dbl> 1, 1, 0, 1, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 0, 1, ...
## $ polint      <dbl> 4, 4, 2, 3, 1, 4, 4, 3, 1, 4, 3, 3, 3, 3, 3, 2, ...
## $ tuition     <dbl> 2, NA, 2, 2, 3, 2, 2, 2, NA, 3, 2, NA, 2, 2, 2, ...
## $ acceptable  <dbl> NA, NA, NA, NA, 25, NA, NA, NA, NA, 150, NA, NA, ...
## $ protest1    <dbl> 1, NA, 0, 0, NA, 1, 1, 0, NA, NA, 0, NA, 1, 1, 0...
## $ protest2    <dbl> 0, NA, 0, 0, NA, 1, 0, 0, NA, NA, 0, NA, 1, 1, 1...
## $ protest3    <dbl> 1, NA, 1, 1, NA, 1, 1, 1, NA, NA, 1, NA, 1, 1, 1...
## $ protest4    <dbl> 0, NA, 0, 0, NA, 1, 0, 0, NA, NA, 0, NA, 1, 1, 0...
## $ protest5    <dbl> 0, NA, 0, 1, NA, 1, 0, 1, NA, NA, 0, NA, 1, 1, 0...
## $ protest6    <dbl> 0, NA, 0, 0, NA, 0, 0, 1, NA, NA, 0, NA, 1, 1, 1...
```

## 1 Estimate the parameters of a binary logit model.

You can choose a dependent variable and one independent variable from the dataset for yourself.

```
binary_model1 <- "model{
  for (i in 1:N){
    y[i] ~ dbern(p[i])
    logit(p[i]) <- ystar[i]
    ystar[i] <- alpha + beta * x[i]
  }

  alpha ~ dnorm(0,0.0001)
  beta ~ dnorm(0,0.0001)
}"

write(binary_model1, "bivariate_binary_model1.bug")
```

```
jags.data <- list(
  y = dat$univ.election,
  x = dat$lr.self,
  N = nrow(dat)
)

jags.inits <- 1:5 %>%
  map(~ list(beta = runif(1, min = 0, max = 1)))
```

```
fit_binary_1 <- jags.model(
  file = "bivariate_binary_model1.bug",
  inits = jags.inits,
  data = jags.data,
  n.chains = length(jags.inits)
)
```

```
## Compiling model graph
##   Resolving undeclared variables
##   Allocating nodes
## Graph information:
##   Observed stochastic nodes: 158
##   Unobserved stochastic nodes: 2
##   Total graph size: 351
##
## Initializing model
```

## 2 Calculate DIC of the logit model above by computing the log-likelihood value by using JAGS.

You can orient yourself the code on the slide 7.18, but you have to care about which distribution the logit model assumes.

```
binary_model2 <- "model{
  for (i in 1:N){
    y[i] ~ dbern(p[i])
    logit(p[i]) <- ystar[i]
    ystar[i] <- alpha + beta * x[i]
    ### LL for Binary Data - From: https://data.princeton.edu/wws509/notes/c3.pdf
    ll[i] <- y[i]*log(p[i]) + (1 - y[i]) * log(1 - p[i])
  }

  alpha ~ dnorm(0,0.0001)
  beta ~ dnorm(0,0.0001)

  LL <- sum(ll[])
}"

write(binary_model2, "bivariate_binary_model2.bug")

fit_binary_2 <- jags.model(
  file = "bivariate_binary_model2.bug",
  inits = jags.inits,
  data = jags.data,
  n.chains = length(jags.inits)
)
```

```
## Compiling model graph
##   Resolving undeclared variables
```

```
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 158
## Unobserved stochastic nodes: 2
## Total graph size: 443
##
## Initializing model

fit_binary_2_list <- coda.samples(
  fit_binary_2,
  variable.names = c("alpha", "beta", "LL"),
  n.iter = 5000,
  thin = 5
)

## Average LL and Deviance
LL <- fit_binary_2_list %>% map(~.x[, "LL"])
LL %>% map_dbl(mean)

## [1] -98.23319 -98.26477 -98.26811 -98.26949 -98.25403

Deviiances <- LL %>% map(~.x * -2)
Deviiances %>% map_dbl(mean)

## [1] 196.4664 196.5295 196.5362 196.5390 196.5081
```

### 3 Calculate DIC of the logit model above by using dic.samples().

```
binary_dic <- dic.samples(fit_binary_1, n.iter = 2000, thin = 1)
binary_dic
```

```
## Mean deviance: 196.6
## penalty 2.063
## Penalized deviance: 198.6
```

```
binary_dic_list <- coda.samples(
  fit_binary_1,
  variable.names=c("alpha", "beta", "deviance", "LL"),
  n.iter = 2000,
  thin = 1
)
```

```
## Warning in FUN(X[[i]], ...): Failed to set trace monitor for LL
## Variable LL not found
```

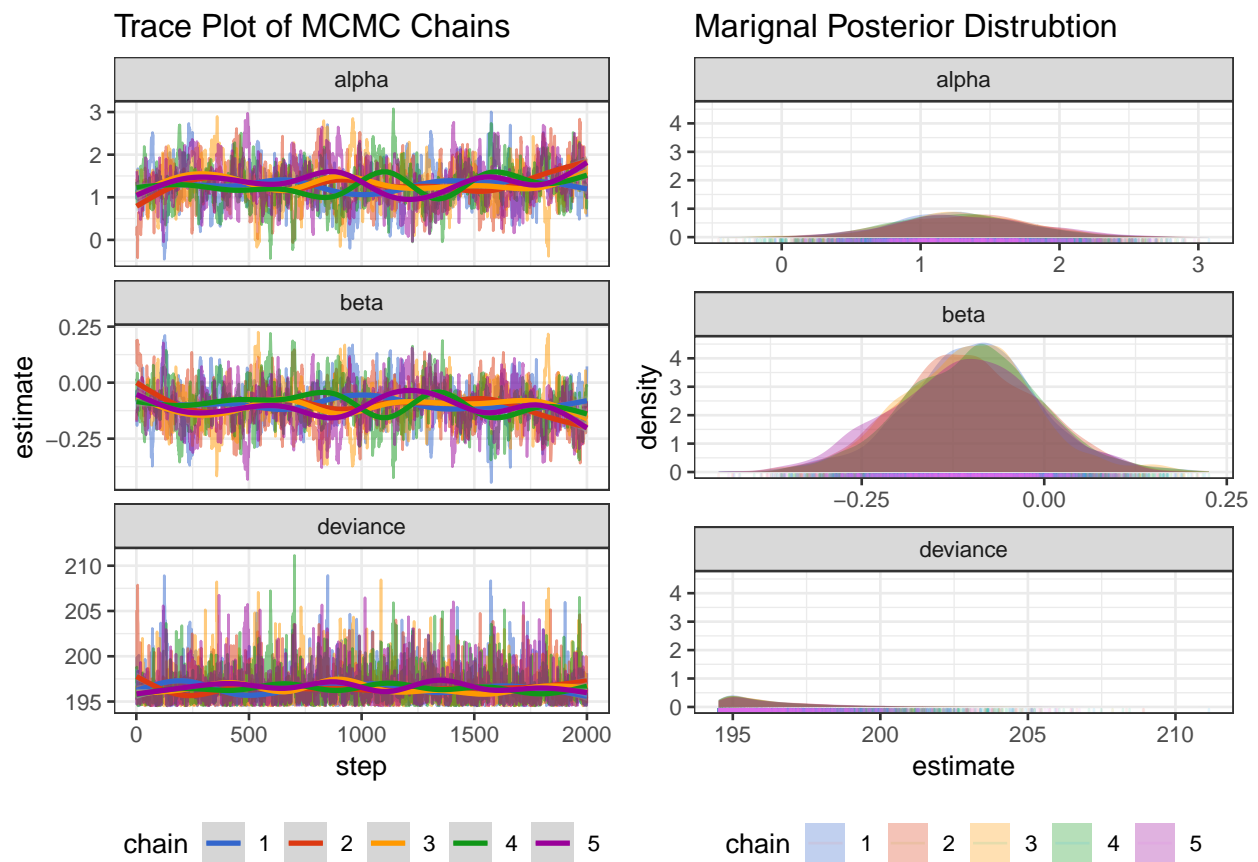
```
# No LL available?
# binary_dic_list %>%
#   map(~mean(.x[, "LL"]))

binary_dic_list %>%
  map(~mean(.x[, "deviance"]))
```

```
## [[1]]
## [1] 196.4438
##
## [[2]]
## [1] 196.4428
##
## [[3]]
## [1] 196.4557
##
## [[4]]
## [1] 196.4345
##
## [[5]]
## [1] 196.6067
```

```
plot_jags_model(binary_dic_list, terms = c("alpha", "beta", "deviance"))
```

```
## `geom_smooth()` using method = 'gam' and formula 'y ~ s(x, bs = "cs")'
```



```
sessionInfo()
```

```
## R version 3.5.1 (2018-07-02)
```

```

## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS High Sierra 10.13.6
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/3.5/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.5/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
##
## attached base packages:
## [1] stats      graphics  grDevices  utils      datasets  methods    base
##
## other attached packages:
## [1] bindrcpp_0.2.2  knitr_1.20      janitor_1.1.1   ggthemes_4.0.1
## [5] texreg_1.36.23  broom_0.5.0     rjags_4-8       coda_0.19-2
## [9] forcats_0.3.0   stringr_1.3.1   dplyr_0.7.8     purrr_0.2.5
## [13] readr_1.1.1     tidyr_0.8.2     tibble_2.0.0    ggplot2_3.1.0
## [17] tidyverse_1.2.1
##
## loaded via a namespace (and not attached):
## [1] tidyselect_0.2.5 haven_1.1.2      lattice_0.20-35  colorspace_1.3-2
## [5] htmltools_0.3.6 mgcv_1.8-24     yaml_2.2.0       utf8_1.1.4
## [9] rlang_0.3.0.1    pillar_1.3.1    glue_1.3.0       withr_2.1.2
## [13] modelr_0.1.2     readxl_1.1.0    bindr_0.1.1      plyr_1.8.4
## [17] munsell_0.5.0    gtable_0.2.0    cellranger_1.1.0 rvest_0.3.2
## [21] evaluate_0.12    labeling_0.3     fansi_0.4.0      Rcpp_1.0.0
## [25] scales_1.0.0     backports_1.1.3 jsonlite_1.6      gridExtra_2.3
## [29] hms_0.4.2        digest_0.6.18   stringi_1.2.4    grid_3.5.1
## [33] rprojroot_1.3-2  cli_1.0.1        tools_3.5.1      magrittr_1.5
## [37] lazyeval_0.2.1   pacman_0.5.0     crayon_1.3.4     pkgconfig_2.0.2
## [41] Matrix_1.2-14    xml2_1.2.0       lubridate_1.7.4  assertthat_0.2.0
## [45] rmarkdown_1.10   httr_1.4.0       rstudioapi_0.8   R6_2.3.0
## [49] nlme_3.1-137     compiler_3.5.1

```