Discussion 1

CUNY MSDS DATA 605

Duubar Villalobos Jimenez February 1, 2018

C17 † Page 42

Book: Beezer: A First Course in Linear Algebra

Exercise

Find all solutions to the system of linear equations. Use your favorite computing device to row-reduce the augmented matrices for the systems, and write the solutions as a set, using correct set notation.

$$-x_1 + 5x_2 = -8$$

$$-2x_1 + 5x_2 + 5x_3 + 2x_4 = 9$$

$$-3x_1 - x_2 + 3x_3 + x_4 = 3$$

$$7x_1 + 6x_2 + 5x_3 + x_4 = 30$$

Preparation

In oder to solve this linear system, we need to set up our square matrix by taking the left side values from the equal sign and I will call it C; our right side values of the equal sign will be represented in a vector, I will call it d.

```
C = matrix(data = c(-1,-2,-3,7,5,5,-1,6,0,5,3,5,0,2,1,1), nrow=4, ncol = 4)

d = c(-8,9,3,30)
```

Matrix C.

```
## [,1] [,2] [,3] [,4]
## [1,] -1 5 0 0
## [2,] -2 5 5 2
## [3,] -3 -1 3 1
## [4,] 7 6 5 1
```

Vector d.

Solving in R using 'solve'

We can solve this equation by using the following command.

solve(C,d)

```
## [1] 3 -1 2 5
```

Answer

$$S = \{(x_1 = 3, x_2 = -1, x_3 = 2, x_4 = 5)\}\$$

Solving in R using 'Row Reduction' (Gauss-Jordan Elimination)

For this, we need to use the package 'pracma'.

```
#install.packages("pracma")
library("pracma")
```

Setup into a single matrix, I will call it G.

```
G = matrix(data = c(-1, -2, -3, 7, 5, 5, -1, 6, 0, 5, 3, 5, 0, 2, 1, 1, -8, 9, 3, 30), nrow=4, ncol = 5)
```

Representation of matrix G.

```
##
        [,1] [,2] [,3] [,4] [,5]
## [1,]
          -1
                 5
                       0
## [2,]
           -2
                 5
                       5
                                 9
## [3,]
           -3
                -1
                       3
                            1
                                 3
           7
## [4,]
                                30
```

We can solve this equation by using the following command.

rref(G)

```
[,1] [,2] [,3] [,4] [,5]
##
## [1,]
           1
## [2,]
                           0
                               -1
           0
                 1
                      0
## [3,]
           0
                 0
                      1
                           0
                                 2
## [4,]
                      0
```

Answer

$$S = \{(x_1 = 3, x_2 = -1, x_3 = 2, x_4 = 5)\}\$$