

Matching & Regression: Accounting for Rival Explanations

Department of Government
London School of Economics and Political Science

- 1 Exam Preparation
- 2 Regression, Briefly
- 3 Matching and Conditioning
- 4 Multiple Regression

1 Exam Preparation

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**What do you think will be
on the exam?**

Sample Paper

`https://moodle.lse.ac.uk/mod/resource/view.php?id=534210`

- ST Exam is 50% of overall mark
 - 25%: 5 “shorter answer” questions (of 15); worth 5% of total mark each
 - 25%: 1 essay (of 4)
- Research Design Proposal is 50% of overall mark

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Uses of Regression

- 1 Description
- 2 Prediction
- 3 Causal Inference

Descriptive Inference

- 1 We want to understand a *population* of cases
- 2 We cannot observe them all, so:
 - 1 Draw a *representative* sample
 - 2 Perform mathematical procedures on sample data
 - 3 Use assumptions to make inferences about population
 - 4 Express uncertainty about those inferences based on assumptions

Parameter Estimation

- We want to observe population *parameter* β
- If we obtain a representative sample of population units:
 - Our sample statistic $\hat{\beta}$ is an unbiased estimate of β
 - Our sampling procedure dictates how uncertain we are about the value of β

Three Equations

1 Population:

$$Y = \beta_0 + \beta_1 X \ (+\epsilon)$$

2 Sample estimate:

$$\hat{y} = \hat{\beta}_0 + \hat{\beta}_1 x$$

3 Unit:

$$y_i = \hat{\beta}_0 + \hat{\beta}_1 x_i + e_i$$

$$y_i = \bar{y}_{0i} + (y_{1i} - y_{0i})x_i + (y_{0i} - \bar{y}_{0i})$$

Mathematically, regression. . .

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- . . . depending on sampling procedure, estimates those relationships in the population
- . . . depending on model fit, provides a way to predict outcome values for new cases
- . . . depending on model completeness, provides inferences about the effect of X on Y

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Causal inference is about comparing an observed outcome to a counterfactual, “potential outcome” for the same cases
Regression provides a “statistical solution” to the fundamental problem of causal inference (Holland)

An Example

- For example, if we think smoking might cause lung cancer, how would we know?
- How would we know if smoking caused lung cancer for an individual who smoked?
 - What's the relevant counterfactual?
- How would we know if smoking causes lung cancer on average across many individuals?
 - What's the relevant counterfactual?

Confounding

- A source of “endogeneity”
- Synonyms: selection bias, omitted variable bias
- In lay terms: the (non)correlation between X and Y does not reflect a causal relationship between X and Y are related for other reasons
 - Most commonly: Some Z causes both X and Y

Addressing Confounding

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- 1 Correlate a “putative” cause (X) and an outcome (Y)

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- 1 Correlate a “putative” cause (X) and an outcome (Y)
- 2 Identify all possible confounds (Z)
- 3 “Condition” on all confounds
 - Calculate correlation between X and Y at each combination of levels of Z

Mill's Method of Difference

If an instance in which the phenomenon under investigation occurs, and an instance in which it does not occur, have every circumstance save one in common, that one occurring only in the former; the circumstance in which alone the two instances differ, is the effect, or cause, or an necessary part of the cause, of the phenomenon.

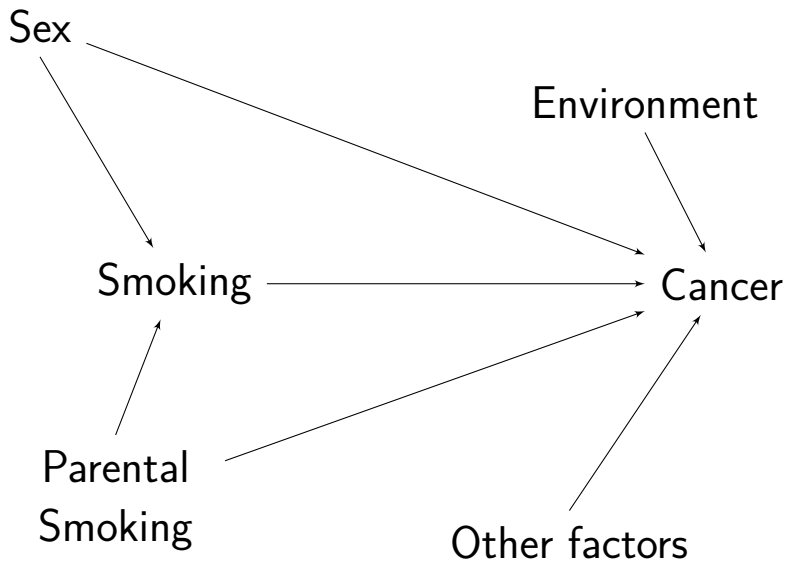
Smoking Example

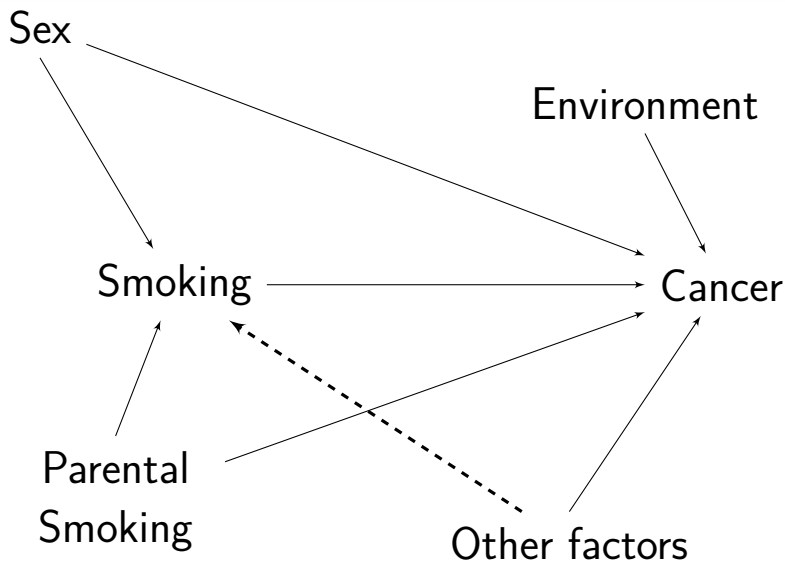
Smoking Example

- 1 Partition sample into “smokers” ($X = 1$) and “non-smokers” ($X = 0$)

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 - Sex
 - Parental smoking
 - etc.





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Smoking Example

- 1 Partition sample into “smokers” ($X = 1$) and “non-smokers” ($X = 0$)
- 2 Identify possible confounds
 - Sex
 - Parental smoking
 - etc.
- 3 Estimate difference in cancer rates between smokers and non-smokers within each group of *covariates*

Example I

| X | Y (Cancer) |
|-------------|-----------------------|
| Smokers | 0.15 |
| Non-smokers | 0.05 |

$$\begin{aligned}ATE &= \bar{Y}_{X=1} - \bar{Y}_{X=0} \\&= 0.15 - 0.05 \\&= 0.10\end{aligned}$$

Example II

| Z_1 (Sex) | X | Y (Cancer) |
|-------------|-------------|--------------|
| 0 | Smokers | ... |
| 0 | Non-smokers | ... |
| 1 | Smokers | ... |
| 1 | Non-smokers | ... |

$$ATE = p_{\text{Male}} * (\bar{Y}_{X=1, Z_1=1} - \bar{Y}_{X=0, Z_1=1}) + \\ p_{\text{Female}} * (\bar{Y}_{X=1, Z_1=0} - \bar{Y}_{X=0, Z_1=0})$$

Example III

| Z_2 (Parent) | Z_1 (Sex) | X | Y (Cancer) |
|----------------|-------------|-------------|--------------|
| 0 | 0 | Smokers | ... |
| 0 | 0 | Non-smokers | ... |
| 0 | 1 | Smokers | ... |
| 0 | 1 | Non-smokers | ... |
| 1 | 0 | Smokers | ... |
| 1 | 0 | Non-smokers | ... |
| 1 | 1 | Smokers | ... |
| 1 | 1 | Non-smokers | ... |

$$\begin{aligned}
 ATE = & p_{\text{Male, Parent non-smoker}} * (\bar{Y}_{X=1, Z_1=1, Z_2=0} - \bar{Y}_{X=0, Z_1=1, Z_2=0}) + \\
 & p_{\text{Female, Parent non-smoker}} * (\bar{Y}_{X=1, Z_1=0, Z_2=0} - \bar{Y}_{X=0, Z_1=0, Z_2=0}) + \\
 & p_{\text{Male, Parent smoker}} * (\bar{Y}_{X=1, Z_1=1, Z_2=1} - \bar{Y}_{X=0, Z_1=1, Z_2=1}) + \\
 & p_{\text{Female, Parent smoker}} * (\bar{Y}_{X=1, Z_1=0, Z_2=1} - \bar{Y}_{X=0, Z_1=0, Z_2=1}) +
 \end{aligned}$$

Exact Matching

- Repeat this partitioning of the space into “strata” (or “subclasses”)
- Requires at least one “treated” and one “untreated” case at every combination of every covariate
- More convenient notation:

$$\text{Naive Effect} = \bar{Y}_{X=1} - \bar{Y}_{X=0}$$

$$\text{ATE} = \bar{Y}_{X=1,\mathbf{z}} - \bar{Y}_{X=0,\mathbf{z}}$$

Note that matching is just a version of Mill's method of difference used for a large number of cases.

Omitted Variables

In the language of potential outcomes:

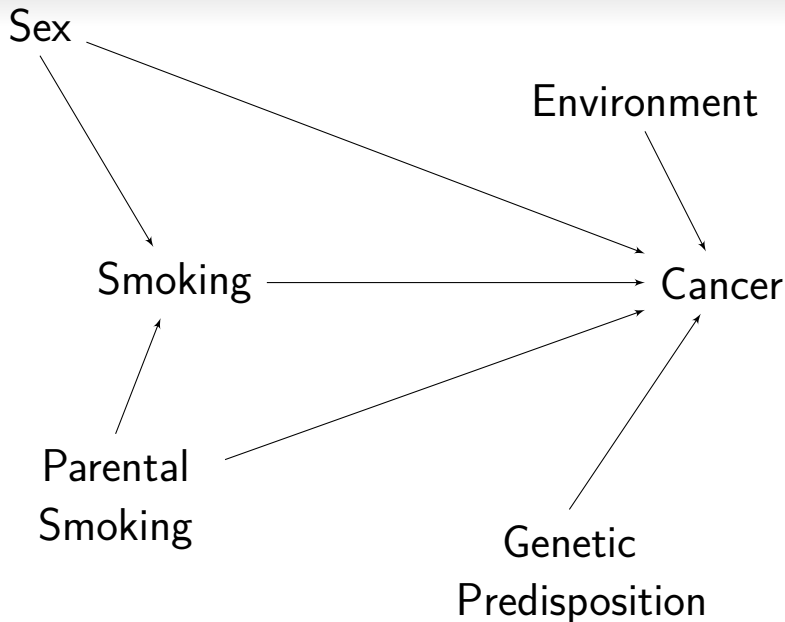
$$\underbrace{E[Y_i|X_i = 1] - E[Y_i|X_i = 0]}_{\text{Naive Effect}} =$$

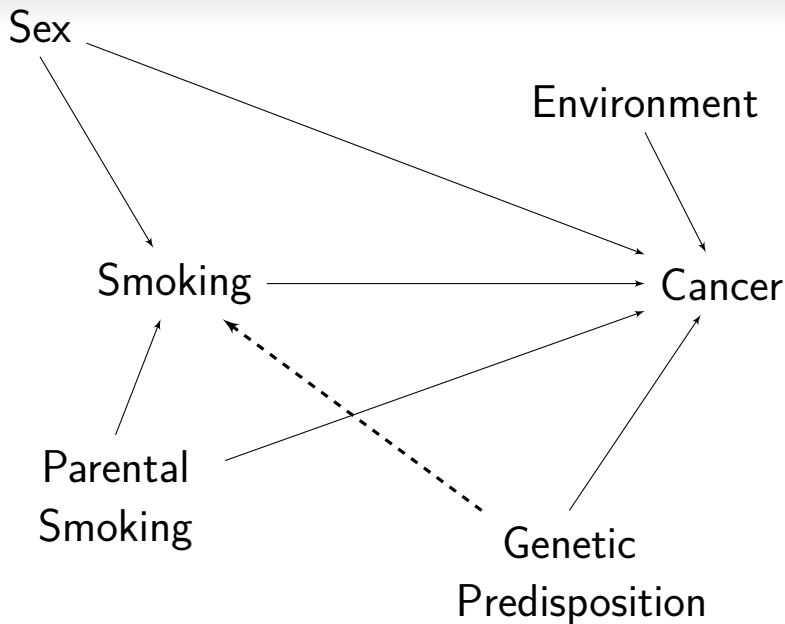
$$\underbrace{E[Y_{1i}|X_i = 1] - E[Y_{0i}|X_i = 1]}_{\text{Treatment Effect on Treated (ATT)}} + \underbrace{E[Y_{0i}|X_i = 1] - E[Y_{0i}|X_i = 0]}_{\text{Selection Bias}}$$

By conditioning, we assert that the potential (control) outcomes are equivalent between treated and non-treated cases, so the difference we observe between treatment and control outcomes is only the average causal effect of the “treatment”.

Caveat!

- We can only condition on *observed* confounding variables
- If we think other confounds might exist, but are unobservable, no form of conditioning can help us
 - Example: Tobacco companies argued that an unknown genetic factor was a common cause of both smoking addiction and lung cancer





Common Conditioning Strategies

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- 1 Condition on nothing (“naive effect”)

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Common Conditioning Strategies

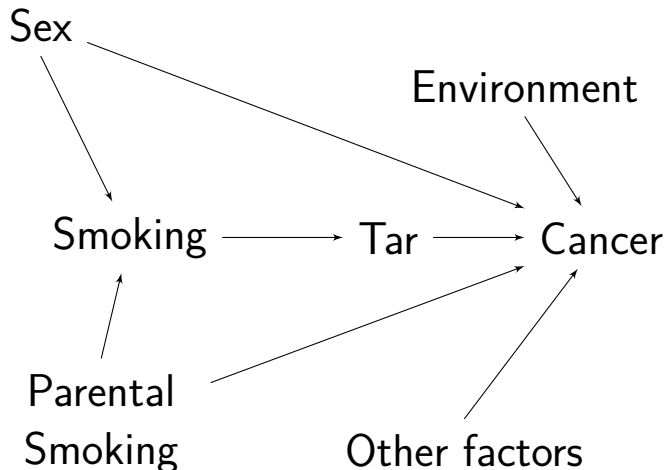
- 1 Condition on nothing (“naive effect”)
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- 3 Condition on all observables

Which of these are good strategies?

Post-treatment Bias

- We usually want to know the **total effect** of a cause
- If we include a mediator, D , of the $X \rightarrow Y$ relationship, the coefficient on X :
 - Only reflects the **direct** effect
 - Excludes the **indirect** effect of X through D
- So don't control for mediators!

Post-Treatment Bias



Post-Treatment Bias

| D (Tar) | X | Y (Cancer) |
|-----------|-------------|--------------|
| 0 | Smokers | ... |
| 0 | Non-smokers | ... |
| 1 | Smokers | ... |
| 1 | Non-smokers | ... |

Post-Treatment Bias

| D (Tar) | X | Y (Cancer) |
|-----------|-------------|--------------|
| 0 | Smokers | ... |
| 0 | Non-smokers | ... |
| 1 | Smokers | ... |
| 1 | Non-smokers | ... |

Imagine:

$$ATE_{\text{Tar}} = (\bar{D}_{X=1} - \bar{D}_{X=0}) = 1$$

$$ATE_{\text{Cancer of Tar}} = (\bar{Y}_{D=1} - \bar{Y}_{D=0}) = 1$$

Post-Treatment Bias

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Post-Treatment Bias

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Imagine:

$$ATE_{\text{Tar}} = (\bar{D}_{X=1} - \bar{D}_{X=0}) = 1$$

$$ATE_{\text{Cancer of Tar}} = (\bar{Y}_{D=1} - \bar{Y}_{D=0}) = 1$$

$$ATE_{\text{Cancer of Smoking}} = p_{D=1}(\bar{Y}_{X=1,D=1} - \bar{Y}_{X=0,D=1}) + \\ p_{D=0}(\bar{Y}_{X=1,D=0} - \bar{Y}_{X=0,D=0})$$

Exam

Regression

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Multiple Regression

Preview

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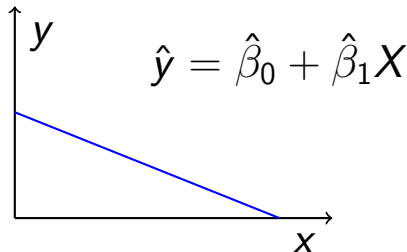
Multiple Regression

- Regression achieves the same objectives as matching
 - Estimate average causal of a variable conditional on other variables
- Requires a *linear* relationship between all RHS (X variables) and Y
 - Can be a set of binary indicator variables
- We interpret coefficient estimates as *marginal* average treatment effects

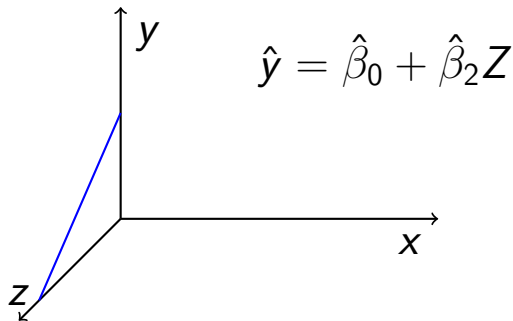
From Line to Surface I

- In simple regression, we estimate a **line**
- In multiple regression, we estimate a **surface**
- Each coefficient is the *marginal effect*, all else constant (at mean)
- This can be hard to picture in your mind

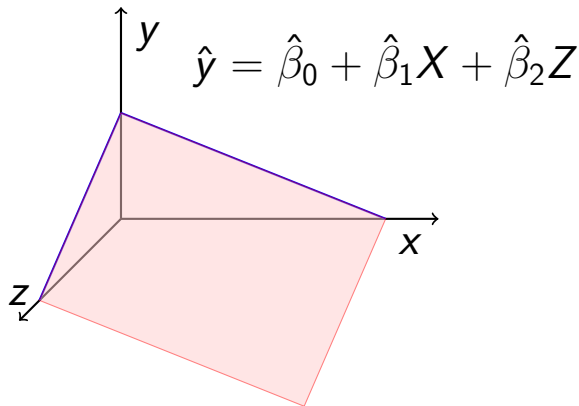
From Line to Surface II



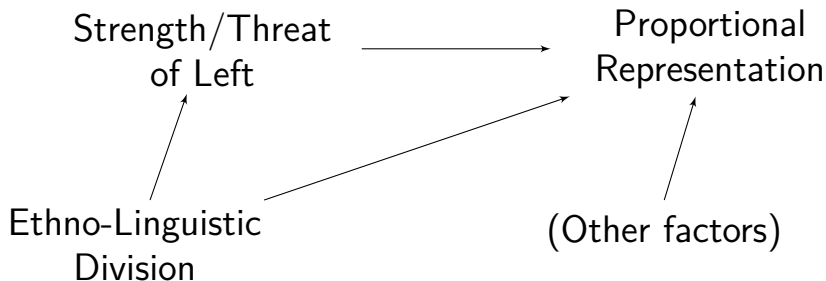
From Line to Surface II



From Line to Surface II



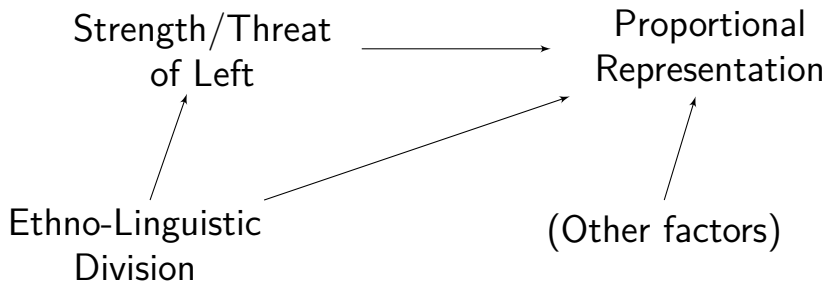
Cusack, Iversen, and Soskice



Testing Rival Hypotheses

- Rival hypotheses can be derived from two (or more) different theories
- We can conduct independent tests of each
 - Is there evidence consistent with Hyp 1?
 - Is there evidence consistent with Hyp 2?
- Regression allows us to test both simultaneously on the same data
 - Is the data more consistent with Hyp 1 or Hyp 2?
- Draw inference about causality and about validity of theories based on data

Cusack, Iversen, and Soskice



Cusack, Iversen, and Soskice

Business-Labour
Coordination

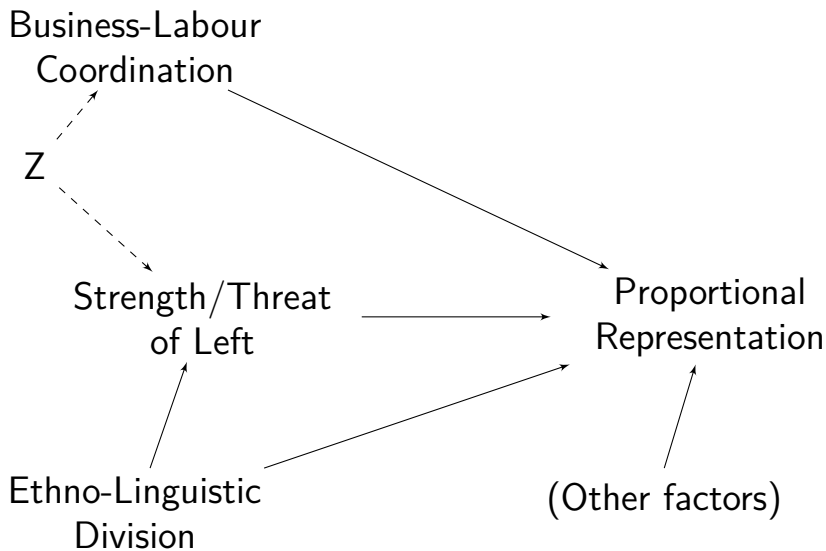
Ethno-Linguistic
Division

Proportional
Representation

(Other factors)

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graph LR; A[Business-Labour Coordination] --> C[Proportional Representation]; B[Ethno-Linguistic Division] --> C; D["(Other factors)"] --> C;
```

Cusack, Iversen, and Soskice



Rival Theories

- Rokkan–Boix:

$$PR = \beta_0 + \beta_1 \textit{Threat} + \epsilon \quad (1)$$

TABLE 3. Replication and Re-test of Boix's Model on the Choice of Electoral Rules in the Interwar Period

| Dependent Variable: Average Effective Threshold in 1919–1939 | (1) Replication Using Data Reported in Boix (1999) | (2) Replication as in (1) but with 19 Cases | (3) Replication Using our Timing and | (4) Replication as in (3) but with Dominance-based Threat Score |
|---|--|--|---|---|
| Constant | 31.30* (4.68) | 32.79* (4.93) | 29.64* (5.48) | 24.54* (5.82) |
| Threat | -.134* (.049) | -.143* (.052) | -.101 (.059) | -.029 (.062) |
| Ethnic–linguistic division X area dummy | -33.16* (14.75) | -35.28* (14.74) | -35.18* (16.48) | -33.92 (17.84) |
| Adj. R-squared | .33 | .37 | .22 | .09 |
| SEE | 10.57 | 10.50 | 11.71 | 12.67 |
| Number of Obs. | 22 | 19 | 19 | 19 |

* sig. at .05 level.

Note: Cols 2, 3, and 4 exclude Finland, Greece, and Luxembourg from the analysis.

Aside: Interpretation

- All our interpretation rules from earlier still apply in a multivariate regression
- Now we interpret a coefficient as an effect “all else constant”
- Generally, not good to give all coefficients a causal interpretation
 - Think “forward causal inference”
 - We're interested in the $X \rightarrow Y$ effect
 - All other coefficients are there as “controls”

Rival Theories

- Rokkan–Boix:

$$PR = \beta_0 + \beta_1 Threat + \epsilon \quad (1)$$

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- Cusack, Iversen, and Soskice:

$$PR = \beta_0 + \beta_2 \textit{Coordination} + \epsilon \quad (2)$$

TABLE 5. Preindustrial Coordination, Disproportionality of Representation, and Electoral System (Standard Errors in Parentheses)

| | Dependent Variable: Effective Threshold | | | | | |
|--|---|------------------|------------------|-------------------|-------------------|-----------------|
| | (1) | (2) | (3) | (4) | (5) | (6) |
| Constant | 26.35 (7.73) | 31.85* (3.36) | 31.99* (2.23) | 26.71* (6.97) | -1.90 (8.90) | 13.79 (8.74) |
| Threat (dominance-based measure) | -0.06 (0.10) | 0.02 (0.04) | — | -.22 (0.13) | -0.16 (0.09) | — |
| Coordination | — | -5.30* (0.66) | -5.46* (0.63) | — | — | — |
| Pre-1900 Disproportionality | — | — | — | — | 0.34* (0.09) | 0.37* (0.11) |
| Ethnic-linguistic division X area dummy | -36.90 (20.85) | -7.10 (9.63) | — | -32.29 (22.75) | -28.39 (14.65) | — |
| Adj. R-squared | 0.07 | 0.83 | 0.81 | 0.15 | 0.65 | 0.51 |
| SEE | 13.47 | 5.74 | 5.99 | 13.60 | 8.73 | 10.30 |
| No. of observations | 17 | 17 | 18 | 12 | 12 | 12 |

* Significant at .05 level.

Rival Theories

- Rokkan–Boix:

$$PR = \beta_0 + \beta_1 \textit{Threat} + \epsilon \quad (1)$$

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- Combined test:

$$PR = \beta_0 + \beta_1 \textit{Threat} + \beta_2 \textit{Coordination} + \epsilon \quad (3)$$

TABLE 5. Preindustrial Coordination, Disproportionality of Representation, and Electoral System (Standard Errors in Parentheses)

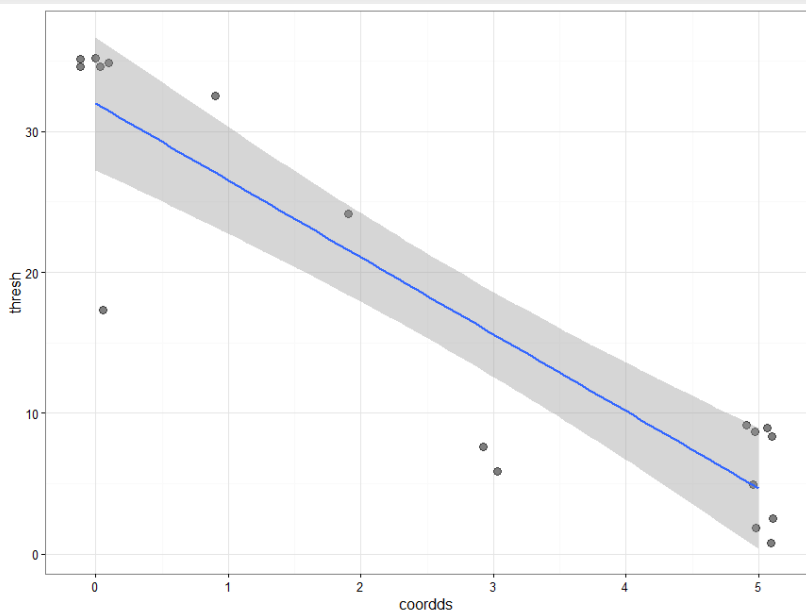
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* Significant at .05 level.

| | (1) | (2) |
|-------------------------|-----------------------|-----------------------|
| stthroct2 | 0.047 (0.035) | 0.008 (0.052) |
| coordds | -6.019*** (0.706) | -5.284*** (1.008) |
| dispro2 | 0.042 (0.052) | 0.083 (0.066) |
| fragdum | 3.624 (8.239) | 0.123 (8.911) |
| Constant | 28.239*** (5.866) | 25.211*** (6.565) |
| Observations | 13 | 12 |
| R ² | 0.947 | 0.948 |
| Adjusted R ² | 0.920 | 0.919 |
| Residual Std. Error | 4.217 (df = 8) | 4.207 (df = 7) |
| F Statistic | 35.673*** (df = 4; 8) | 32.084*** (df = 4; 7) |

Note:

* p<0.1; ** p<0.05; *** p<0.01



So the effect found by Rokkan and Boix was confounded by business–labour coordination. What was happening when they omitted the coordination variable?

Omitted Variable Bias

- We want to estimate:

$$Y = \beta_0 + \beta_1 X + \beta_2 Z + \epsilon$$

- We actually estimate:

$$\begin{aligned}\tilde{y} &= \tilde{\beta}_0 + \tilde{\beta}_1 x + \epsilon \\ &= \tilde{\beta}_0 + \tilde{\beta}_1 x + (0 * z) + \epsilon \\ &= \tilde{\beta}_0 + \tilde{\beta}_1 x + \nu\end{aligned}$$

- Bias: $\tilde{\beta}_1 = \hat{\beta}_1 + \hat{\beta}_2 \tilde{\delta}_1$, where $\tilde{z} = \tilde{\delta}_0 + \tilde{\delta}_1 x$

But have Cusack, Iversen, and Soskice considered all possible confounds?

TABLE 4. Indicators of Economic Structure and Organization ca. 1900

| | (1) Guild Tradition and Strong Local Economies | (2) Widespread Rural Cooperatives | (3) High Employer Coordination | (4) Industry/ Centralized vs. Craft/ Fragmented Unions | (5) Large Skill- Based Export Sector | (6) Coordination Index |
|----------------|---|--|--------------------------------------|--|---|------------------------------|
| Australia | No | No | No | No | No | 0 |
| Canada | No | No | No | No | No | 0 |
| Ireland | No | No | No | No | No | 0 |
| New Zealand | No | No | No | No | No | 0 |
| United Kingdom | No | No | No | No | No | 0 |
| United States | No | No | No | No | No | 0 |
| France | Yes | No | No | No | No | 1 |
| Japan | Yes | No | Yes | No | No | 2 |
| Italy | Yes | Yes | Yes | No | No | 3 |
| Finland | Yes | Yes | No | No | Yes | 3 |
| Austria | Yes | Yes | Yes | Yes | Yes | 5 |
| Belgium | Yes | Yes | Yes | Yes | Yes | 5 |
| Denmark | Yes | Yes | Yes | Yes | Yes | 5 |
| Germany | Yes | Yes | Yes | Yes | Yes | 5 |
| Netherlands | Yes | Yes | Yes | Yes | Yes | 5 |
| Switzerland | Yes | Yes | Yes | Yes | Yes | 5 |
| Norway | Yes | Yes | Yes | Yes | Yes | 5 |
| Sweden | Yes | Yes | Yes | Yes | Yes | 5 |

Sources: By column: (1) Crouch 1993; Herrigel (1996); Hechter and Brustein (1980) (2) Crouch 1993; Katzenstein 1985, ch. 4; Symes 1963; Marshall 1958; Leonardi 2006; Guinane 2001; Lewis 1978; (3)–(5) Crouch 1993; Thelen 2004; Swenson 2002; Mares 2003; Katzenstein 1985, ch. 4.

Note: Additive index in column (6) summarized across all indicators with 'Yes' = 1 and 'No' = 0.

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|----------------|---|--|--------------------------------------|--|---|------------------------------|
| Australia | No | No | No | No | No | 0 |
| Canada | No | No | No | No | No | 0 |
| Ireland | No | No | No | No | No | 0 |
| New Zealand | No | No | No | No | No | 0 |
| United Kingdom | No | No | No | No | No | 0 |
| United States | No | No | No | No | No | 0 |
| France | Yes | No | No | No | No | 1 |
| Japan | Yes | No | Yes | No | No | 2 |
| Italy | Yes | Yes | Yes | No | No | 3 |
| Finland | Yes | Yes | No | No | Yes | 3 |
| Austria | Yes | Yes | Yes | Yes | Yes | 5 |
| Belgium | Yes | Yes | Yes | Yes | Yes | 5 |
| Denmark | Yes | Yes | Yes | Yes | Yes | 5 |
| Germany | Yes | Yes | Yes | Yes | Yes | 5 |
| Netherlands | Yes | Yes | Yes | Yes | Yes | 5 |
| Switzerland | Yes | Yes | Yes | Yes | Yes | 5 |
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Note: Additive index in column (6) summarized across all indicators with 'Yes' = 1 and 'No' = 0.

| | (1) | (2) |
|-------------------------|-----------------------|-----------------------|
| stthroct2 | 0.058 (0.048) | 0.006 (0.043) |
| coordds | -5.556*** (1.578) | -0.398 (2.467) |
| dispro2 | 0.013 (0.102) | -0.049 (0.083) |
| fragdum | 4.983 (9.642) | 3.366 (7.465) |
| brit | 4.088 (12.258) | 30.412* (14.469) |
| Constant | 26.911*** (7.388) | 9.390 (9.253) |
| Observations | 13 | 12 |
| R ² | 0.948 | 0.970 |
| Adjusted R ² | 0.910 | 0.945 |
| Residual Std. Error | 4.472 (df = 7) | 3.449 (df = 6) |
| F Statistic | 25.390*** (df = 5; 7) | 39.083*** (df = 5; 6) |

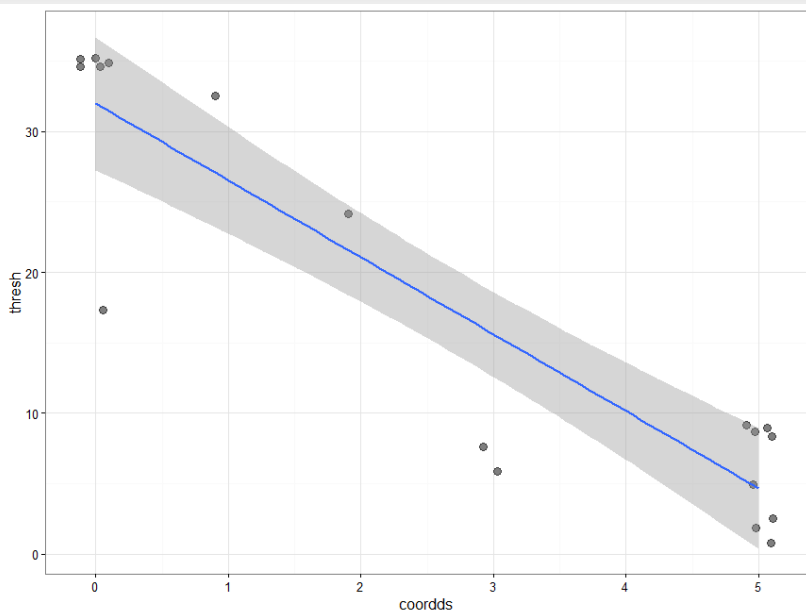
Note:

*p<0.1; **p<0.05; ***p<0.01

Aside: Interpolation/Extrapolation

In *prediction*, we may want to use our estimated coefficients to predict outcome values for new cases

- *Interpolation* is prediction within the interval covered by our observed data
- *Extrapolation* is prediction outside the interval covered by our observed data



Lingering Issues

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 - Inferences from data to population depend on generalizability

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- 3 Kellstedt and Whitten cover more in-depth mathematical requirements

Preview

- Next week: Experiments and Quasi-Experiments
- Following week: Research ethics
- Last week (Mar. 22):
 - Research Design Proposal Due!
 - Wrap-up course
- I am on leave for 2 weeks from April 21

