The Malthusian Hypothesis

Ömer Özak

Department of Economics Southern Methodist University

Economic Growth and Comparative Development

Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime
- The Modern Growth Regime

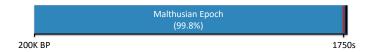
Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime
- The Modern Growth Regime

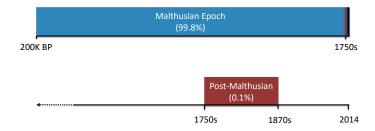
Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime
- The Modern Growth Regime

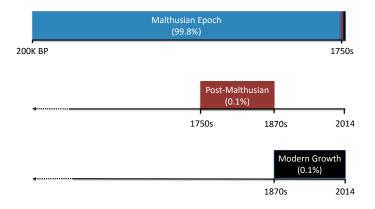
Phases of Development: Timeline of the Most Developed Economies



Phases of Development: Timeline of the Most Developed Economies



Phases of Development: Timeline of the Most Developed Economies



- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies
 - Higher population density
 - Similar levels of income per-capita in the long-rur

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- Characterized by Malthusian dynamics and the absence of economic growth
- Central characteristics of the period:
 - Positive effect of income on population growth
 - Diminishing returns to labor (reflecting the existence of fixed factor)
- Technological progress over this period
 - Increases income per capita in the short-run
 - Population adjust, as long as income remains above subsistence
 - Income per capita ultimately returns to its long-run level
- Technologically advanced & land-rich economies:
 - Higher population density
 - Similar levels of income per-capita in the long-run

- The dynamics of Irish economy (1650 1850)
 - Triggered by the cultivation of a new world crop potato
- The dynamics of the Chinese Economy (1500 1800)
 - Triggered by superior agricultural technology
- The dynamics of the English economy (1348 1700)
 - Triggered by the Black Death

- The dynamics of Irish economy (1650 1850)
 - Triggered by the cultivation of a new world crop potato
- The dynamics of the Chinese Economy (1500 1800)
 - Triggered by superior agricultural technology
- The dynamics of the English economy (1348 1700)
 - Triggered by the Black Death

- The dynamics of Irish economy (1650 1850)
 - Triggered by the cultivation of a new world crop potato
- The dynamics of the Chinese Economy (1500 1800)
 - Triggered by superior agricultural technology
- The dynamics of the English economy (1348 1700)
 - Triggered by the Black Death

- The dynamics of Irish economy (1650 1850)
 - Triggered by the cultivation of a new world crop potato
- The dynamics of the Chinese Economy (1500 1800)
 - Triggered by superior agricultural technology
- The dynamics of the English economy (1348 1700)
 - Triggered by the Black Death

- The dynamics of Irish economy (1650 1850)
 - Triggered by the cultivation of a new world crop potato
- The dynamics of the Chinese Economy (1500 1800)
 - Triggered by superior agricultural technology
- The dynamics of the English economy (1348 1700)
 - Triggered by the Black Death

- The dynamics of Irish economy (1650 1850)
 - Triggered by the cultivation of a new world crop potato
- The dynamics of the Chinese Economy (1500 1800)
 - Triggered by superior agricultural technology
- The dynamics of the English economy (1348 1700)
 - Triggered by the Black Death

- ullet The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly
 - 1845-1852 Potato blight destroys crops ⇒ Great Famine
 - Population decreases by about 2 million
 - (1M Famine death & 1M emigration to the New World)

- The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly

- ullet The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly
 - 1845-1852 Potato blight destroys crops \Longrightarrow Great Famine
 - Population decreases by about 2 million
 - (1M Famine death & 1M emigration to the New World)

- ullet The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly
 - 1845-1852 Potato blight destroys crops \Longrightarrow Great Famine
 - Population decreases by about 2 million
 - (1M Famine death & 1M emigration to the New World)

- ullet The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly
 - 1845-1852 Potato blight destroys crops ⇒ Great Famine
 - Population decreases by about 2 million
 - (1M Famine death & 1M emigration to the New World)

- ullet The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly
 - 1845-1852 Potato blight destroys crops ⇒ Great Famine
 - Population decreases by about 2 million
 - (1M Famine death & 1M emigration to the New World)

- ullet The Colombian Exchange \Longrightarrow massive cultivation of potato post-1650
 - 1650-1840s
 - Population increases from 2 to 6 million
 - Income per capita increases only very modestly
 - 1845-1852 Potato blight destroys crops ⇒ Great Famine
 - Population decreases by about 2 million
 - (1M Famine death & 1M emigration to the New World)

- Superior agricultural technology
 - 1500-1820
 - Population increases from 103 to 381 million
 - Share of China in world population increases from 23% to 37%
 - Income per capita was steady at \$600

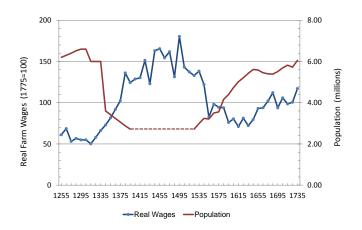
- Superior agricultural technology
 - 1500-1820
 - Population increases from 103 to 381 million
 - Share of China in world population increases from 23% to 37%
 - Income per capita was steady at \$600

- Superior agricultural technology
 - 1500-1820
 - Population increases from 103 to 381 million
 - Share of China in world population increases from 23% to 37%
 - Income per capita was steady at \$600

- Superior agricultural technology
 - 1500-1820
 - Population increases from 103 to 381 million
 - Share of China in world population increases from 23% to 37%
 - Income per capita was steady at \$600

- Superior agricultural technology
 - 1500-1820
 - Population increases from 103 to 381 million
 - Share of China in world population increases from 23% to 37%
 - Income per capita was steady at \$600

Malthusian Adjustments to the Black Death: England, 1348–1750



- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - \circ $I \uparrow \Longrightarrow AP_{i} \mid 1 \Longrightarrow v \mid$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Lanc
 - $0.1 \uparrow \Longrightarrow AB(1) \Longrightarrow v.1$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Lanc
 - $0.1 \uparrow \Longrightarrow AB(1) \Longrightarrow v.1$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - $a \land \uparrow \Rightarrow AP_{\ell} \land \Rightarrow v \land$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - $L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - $L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - $L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - $L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$

- Positive effect of income on population
 - $y \uparrow \Longrightarrow L \uparrow$
- Fixed factor of production Land
 - $L \uparrow \Longrightarrow AP_L \downarrow \Longrightarrow y \downarrow$

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
 - Labor
 - Land

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
 - Labor
 - Land

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
 - Labor
 - Land

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
 - Labor
 - Land

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
 - Labor
 - Land

- Overlapping-generations economy
- t = 0, 1, 2, 3...
- One homogeneous good
- 2 factors of production:
 - Labor
 - Land

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $_{o}$ X = land
- \bullet $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time :

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^c$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $_{o}$ X = land
- \bullet $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time :

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^c$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $\bullet X \equiv land$
- \bullet $A \equiv$ technological leve
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^c$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\circ}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\alpha}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\alpha}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\circ}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\alpha}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\alpha}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left[\frac{AX}{L_t}\right]^{\alpha}$$

$$Y_t = (AX)^{\alpha} L_t^{1-\alpha} \qquad 0 < \alpha < 1$$

- $L_t \equiv$ labor employed in period t
- $X \equiv land$
- $A \equiv$ technological level
- $AX \equiv$ effective resources
- Output per worker produced at time t

$$y_t = \frac{Y_t}{L_t} = \left\lceil \frac{AX}{L_t} \right\rceil^{\alpha}$$

- Land is fixed over time
 - Surface of planet earth
- Labor evolves endogenously
 - Determined by households' fertility rat

- Land is fixed over time
 - Surface of planet earth
- Labor evolves endogenously
 - Determined by households' fertility rate

- Land is fixed over time
 - Surface of planet earth
- Labor evolves endogenously
 - Determined by households' fertility rate

- Land is fixed over time
 - Surface of planet earth
- Labor evolves endogenously
 - Determined by households' fertility rate

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - · Work
 - Allocate income between consumption and children

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

Individuals

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

Individuals

- Live for 2 period
 - Childhood: (1st Period):
 - Passive economic agents
 - Consume fixed amount of their parental resources
 - Adulthood (2nd Period):
 - Work
 - Allocate income between consumption and children

Preferences of an adult at time t

$$\mathbf{u_t} = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual
- $c_t \equiv$ consumption of individual
- Budget constraint

$$\rho n_t + c_t \le y_t$$

ρ ≡ cost of raising a child

Preferences of an adult at time t

$$\mathbf{u_t} = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual
- $c_t \equiv$ consumption of individual
- Budget constraint

$$\rho n_t + c_t \le y_t$$

ρ ≡ cost of raising a child

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual
- ullet $c_t \equiv ext{ consumption of individual } :$
- Budget constraint

$$\rho n_t + c_t \leq y_t$$

ρ = cost of raising a child

Ömer Özak

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- $c_t \equiv$ consumption of individual t
- Budget constraint:

$$\rho n_t + c_t \leq y_t$$

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- $c_t \equiv$ consumption of individual t
- Budget constraint:



Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- $c_t \equiv$ consumption of individual t
- Budget constraint:

$$\rho n_t + c_t \le y_t$$

• $\rho \equiv \text{cost of raising a child}$

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- $c_t \equiv$ consumption of individual t
- Budget constraint:

$$\rho n_t + c_t \le y_t$$

• $\rho \equiv \text{cost of raising a child}$

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- $c_t \equiv$ consumption of individual t
- Budget constraint:

$$\rho n_t + c_t \leq y_t$$

• $\rho \equiv \text{cost of raising a child}$

Preferences of an adult at time t

$$u_t = (n_t)^{\gamma} (c_t)^{1-\gamma} \qquad \qquad 0 < \gamma < 1$$

- $n_t \equiv$ number of children of individual t
- $c_t \equiv$ consumption of individual t
- Budget constraint:

$$\rho n_t + c_t \leq y_t$$

• $\rho \equiv {\rm cost} \ {\rm of} \ {\rm raising} \ {\rm a} \ {\rm child}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]'$$

Since $v_t = (AX/L_t)^{c_t}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]'$$

Since $v_t = (AX/L_t)^{c_t}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]'$$

Since $y_t = (AX/L_t)^{\alpha}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]'$$

Since $y_t = (AX/L_t)^{\alpha}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]'$$

Since $v_t = (AX/L_t)^{\alpha}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\circ}$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\circ}$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$\mathbf{n_t} = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Since $y_t = (AX/L_t)^{\alpha}$

• Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Since $y_t = (AX/L_t)^{\alpha}$

Optimal expenditure on consumption and children

$$c_t = (1 - \gamma)y_t$$

$$\rho n_t = \gamma y_t$$

Optimal number of children

$$n_t = \frac{\gamma}{\rho} y_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

• Since $y_t = (AX/L_t)^{\alpha}$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)^{\alpha}$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

Population dynamics:

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• The evolution of the size of the working population

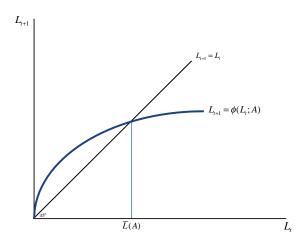
$$L_{t+1} = n_t L_t$$

where

$$n_t = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha}$$

Population dynamics:

$$L_{t+1} = \frac{\gamma}{\rho} \left[\frac{AX}{L_t} \right]^{\alpha} L_t = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$



The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha}(AX) \equiv \bar{L}(A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha}(AX) \equiv \bar{L}(A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha}(AX) \equiv \bar{L}(A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha}(AX) \equiv \bar{L}(A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$ar{L} = (rac{\gamma}{
ho})^{1/lpha}(AX) \equiv ar{L}(A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha}(AX) \equiv \bar{L}(A)$$

The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$\bar{L} = (\frac{\gamma}{\rho})^{1/\alpha}(AX) \equiv \bar{L}(A)$$

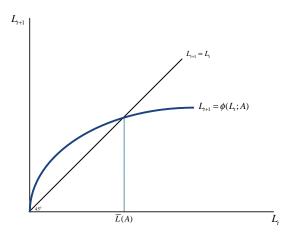
The evolution of the size of the working population

$$L_{t+1} = \frac{\gamma}{\rho} (AX)^{\alpha} L_t^{1-\alpha} \equiv \phi(L_t; A)$$

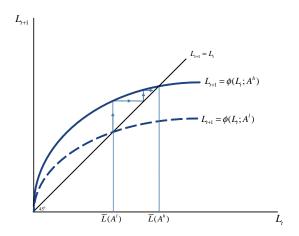
• Steady-State: $L_{t+1} = L_t = \bar{L}$

$$\bar{L} = \frac{\gamma}{\rho} (AX)^{\alpha} \bar{L}^{1-\alpha}$$

$$ar{L} = (rac{\gamma}{
ho})^{1/lpha}(AX) \equiv ar{L}(A)$$



Adjustment of Population to Advancements in Technology



• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{1}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{1}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{1}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{1}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{1}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{\rho^{\alpha}} = \frac{y_{t}}{\lceil \gamma \rceil^{\alpha}} q_{t}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$\mathbf{y_{t+1}} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

• The time path of income per worker

$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha} \equiv \psi(y_t)$$

The time path of income per worker

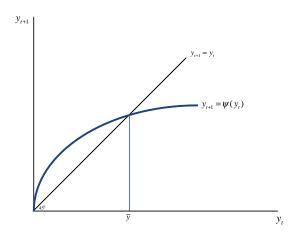
$$y_{t+1} = \left[\frac{AX}{L_{t+1}}\right]^{\alpha} = \left[\frac{AX}{n_t L_t}\right]^{\alpha} = \frac{y_t}{n_t^{\alpha}}$$

where

$$n_{t} = \frac{\gamma}{\rho} y_{t}$$

$$y_{t+1} = \frac{y_{t}}{n_{t}^{\alpha}} = \frac{y_{t}}{\left[\frac{\gamma}{\rho}\right]^{\alpha} y_{t}^{\alpha}}$$

$$y_{t+1} = \left[\frac{
ho}{\gamma}\right]^{lpha} y_t^{1-lpha} \equiv \psi(y_t)$$



The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{y}^{1-\alpha}$$

The steady-state level of income per worker

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]$$

The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

$$\bar{\mathbf{y}} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{\mathbf{y}}^{1-\alpha}$$

The steady-state level of income per worker

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]$$

The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{y}^{1-\alpha}$$

• The steady-state level of income per worker

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]$$

The time path of income per worker

$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

$$\bar{y} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{y}^{1-\alpha}$$

• The steady-state level of income per worker

$$m{ar{y}} = \left[rac{
ho}{\gamma}
ight]$$

The time path of income per worker

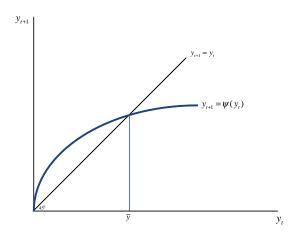
$$y_{t+1} = \left[\frac{\rho}{\gamma}\right]^{\alpha} y_t^{1-\alpha}$$

• Steady-State $y_{t+1} = y_t = \bar{y}$

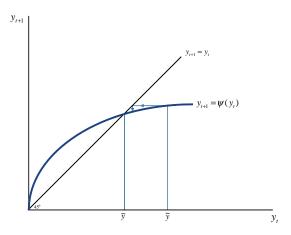
$$\bar{y} = \left[\frac{\rho}{\gamma}\right]^{\alpha} \bar{y}^{1-\alpha}$$

The steady-state level of income per worker

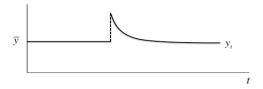
$$\bar{y} = \left[\frac{\rho}{\gamma}\right]$$



The Effect of Technological Advancement on income per Worker



The Effect of Technological Advancement on the Time Path of Population and Income per Worker





The Effect of Advancement in Technology or Land Productivity

 Increases the short-run and the steady-state level of the working population

$$\frac{\partial L_t}{\partial A} > 0$$
 and $\frac{\partial \bar{L}}{\partial A} > 0$

 Increases the level of income per capita in the short-run but does not affect the steady-state levels of income per worker

$$\frac{\partial y_t}{\partial A} > 0$$
 and $\frac{\partial \bar{y}}{\partial A} = 0$

- Variations in technology and land quality across countries will be reflected primarily in variation in population density:
 - Technological superiority will result primarily in higher population density without any sizable effect on income per-capita in the long-run
 - Superior land quality will result primarily in higher population density without any sizable effect on income per-capita in the long-run

- Variations in technology and land quality across countries will be reflected primarily in variation in population density:
 - Technological superiority will result primarily in higher population density without any sizable effect on income per-capita in the long-run
 - Superior land quality will result primarily in higher population density without any sizable effect on income per-capita in the long-run

- Variations in technology and land quality across countries will be reflected primarily in variation in population density:
 - Technological superiority will result primarily in higher population density without any sizable effect on income per-capita in the long-run
 - Superior land quality will result primarily in higher population density without any sizable effect on income per-capita in the long-run

- Variations in technology and land quality across countries will be reflected primarily in variation in population density:
 - Technological superiority will result primarily in higher population density without any sizable effect on income per-capita in the long-run
 - Superior land quality will result primarily in higher population density without any sizable effect on income per-capita in the long-run

Objective:

- Establish the causal effect of
 - Technology on Population in 1500

Hurdles

- Reverse Causality: Correlation between technology and population
- * Technology \$\infty\$ Technology (Scale effects in improvitions)
- · Omitted Variables Rias
- 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Omitted Variables Bias
 - 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Population → Technology (Scale effects in innovations)
 - 0.39.147.311.03
 - Omitted Variables Bias
 - a 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Technology

 Population (Malthusian forces)
 - Population

 Technology (Scale effects in innovations)
 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Technology ⇒ Population (Malthusian forces)
 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Technology ⇒ Population (Malthusian forces)
 - Population ⇒ Technology (Scale effects in innovations)
 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Technology ⇒ Population (Malthusian forces)
 - Population ⇒ Technology (Scale effects in innovations)
 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

- Objective:
 - Establish the causal effect of
 - Technology on Population in 1500
- Hurdles
 - Reverse Causality: Correlation between technology and population
 - Technology ⇒ Population (Malthusian forces)
 - Population ⇒ Technology (Scale effects in innovations)
 - Omitted Variables Bias:
 - 3rd factor (e.g., ability) affected Population & Technology

- Exploit exogenous sources of cross-country variation in technological level
 - Historical origins (thousands of years earlier):
 - unaffected by the population in 1500
 - Exogenous source of variations in these historical forces

- Exploit exogenous sources of cross-country variation in technological level
 - Historical origins (thousands of years earlier):
 - unaffected by the population in 1500
 - Exogenous source of variations in these historical forces

- Exploit exogenous sources of cross-country variation in technological level
 - Historical origins (thousands of years earlier):
 - unaffected by the population in 1500
 - Exogenous source of variations in these historical forces

- Exploit exogenous sources of cross-country variation in technological level
 - Historical origins (thousands of years earlier):
 - unaffected by the population in 1500
 - Exogenous source of variations in these historical forces

- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - Knowledge creation (science, technology & written languages
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - ullet \longrightarrow Origins of the observed patterns of comparative development

- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - ⇒ Knowledge creation (science, technology & written languages)
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - ullet \longrightarrow Origins of the observed patterns of comparative development

- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - ullet \Longrightarrow Knowledge creation (science, technology & written languages)
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - Origins of the observed patterns of comparative development

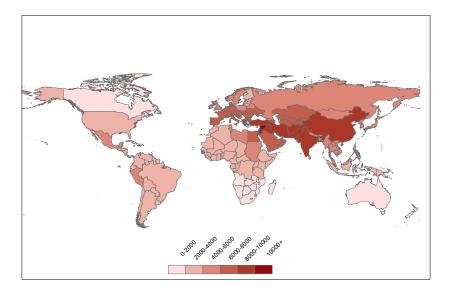
- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - Knowledge creation (science, technology & written languages)
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - ullet ullet Origins of the observed patterns of comparative development

- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - ullet \Longrightarrow Knowledge creation (science, technology & written languages)
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - ullet \Longrightarrow Origins of the observed patterns of comparative development

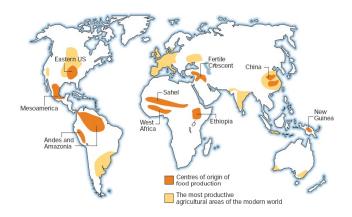
- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - Knowledge creation (science, technology & written languages)
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - Origins of the observed patterns of comparative development

- The transition from hunter-gatherer tribes to agricultural communities:
 - Emergence of non-food-producing class:
 - Knowledge creation (science, technology & written languages)
 - Technological head start and its persistent effect via:
 - Urbanization, nation states, colonization
- Variations in biogeographical characteristics conducive for the NR :
 - \Longrightarrow Origins of the observed patterns of comparative development

Variation in the Onset of the Neolithic Revolution



Independent Origins



Source: Diamond (Nature 2002)

- Geographical factors that maximized biodiversity (climate, latitude, landmass)
 - Availability of domesticable species of plants and animals
 - Onset of domestication
- Orientation of continents:
 - Diffusion of agricultural practices along similar latitudes

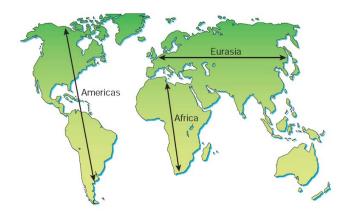
- Geographical factors that maximized biodiversity (climate, latitude, landmass)
 - Availability of domesticable species of plants and animals
 - Onset of domestication
- Orientation of continents:
 - Diffusion of agricultural practices along similar latitudes

- Geographical factors that maximized biodiversity (climate, latitude, landmass)
 - Availability of domesticable species of plants and animals
 - Sometimes of domestication
- Orientation of continents:
 - Diffusion of agricultural practices along similar latitudes

- Geographical factors that maximized biodiversity (climate, latitude, landmass)
 - Availability of domesticable species of plants and animals
 - Sometimes of domestication
- Orientation of continents:
 - Diffusion of agricultural practices along similar latitudes

- Geographical factors that maximized biodiversity (climate, latitude, landmass)
 - Availability of domesticable species of plants and animals
 - Onset of domestication
- Orientation of continents:
 - \Longrightarrow Diffusion of agricultural practices along similar latitudes

Orientation of Continents



Source: Diamond (Nature 2002)

The Diamond Hypothesis

- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution
 - Technological superiority

The Diamond Hypothesis

- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - ullet \longrightarrow Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution
 - Technological superiority

The Diamond Hypothesis

- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution:
 - Technological superiority

The Diamond Hypothesis

- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - ullet Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution:
 - Technological superiority

The Diamond Hypothesis

- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - ullet Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution:
 - Technological superiority

The Diamond Hypothesis

- The domination of Euro-Asia in the pre-colonial era reflects:
 - Larger number of domesticable species of plants and animals
 - East-West orientation
 - ullet Technological head start and its effect on development
- Earlier onset of the Neolithic Revolution:
 - Technological superiority

- Resolving: reverse causality
 - Variation in the onset of the Neolithic Revolution (NR) across the globe - a proxy for variation in the technological level
- Resolving: omitted variable bias (i.e., 3rd factor (e.g., ability)) affected population & NR
 - Variation in prehistoric domesticable species of plants and animals IV for the timing of the NR

- Resolving: reverse causality
 - Variation in the onset of the Neolithic Revolution (NR) across the globe - a proxy for variation in the technological level
- Resolving: omitted variable bias (i.e., 3rd factor (e.g., ability)) affected population & NR
 - Variation in prehistoric domesticable species of plants and animals IV for the timing of the NR

- Resolving: reverse causality
 - Variation in the onset of the Neolithic Revolution (NR) across the globe - a proxy for variation in the technological level
- Resolving: omitted variable bias (i.e., 3rd factor (e.g., ability)) affected population & NR
 - Variation in prehistoric domesticable species of plants and animals IV for the timing of the NR

- Resolving: reverse causality
 - Variation in the onset of the Neolithic Revolution (NR) across the globe - a proxy for variation in the technological level
- Resolving: omitted variable bias (i.e., 3rd factor (e.g., ability)) affected population & NR
 - Variation in prehistoric domesticable species of plants and animals IV for the timing of the NR

The Neolithic Revolution & Technological Level: 1000 BCE-1500 CE

	Technology Level 1000BCE-1500CE						
	1000	1000BCE		1CE		500CE	
	(1)	(2)	(3)	(4)	(5)	(6)	
Years Since Neolithic Revolution	0.72*** (0.06)	0.47*** (0.12)	0.56*** (0.06)	0.28** (0.12)	•	0.34*** (0.10)	
Continental FE	No	Yes	No	Yes	No	Yes	
Additional Geographical Controls	No	Yes	No	Yes	No	Yes	
Adjusted- R^2	0.51	0.60	0.31	0.63	0.55	0.82	
Observations	112	111	134	133	113	112	

Notes: Standardized coefficients from an Ordinary Least Squares (OLS) regression. Heteroskedasticity robust standard error estimates are reported in parentheses; *** denotes statistical significance at the 1% level, ** at the 5% level, and * at the 10% level, all for two-sided hypothesis tests.

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- ullet $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv \text{vector of geographical controls for country } i$
- $D_i \equiv$ vector of continental fixed effect in country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

$$\ln P_{i,t} = \alpha_{0,t} + \alpha_{1,t} \ln T_{i,t} + \alpha_{2,t} \ln X_i + \alpha'_{3,t} \Gamma_i + \alpha'_{4,t} D_i + \delta_{i,t}$$

$$\ln y_{i,t} = \beta_{0,t} + \beta_{1,t} \ln T_{i,t} + \beta_{2,t} \ln X_i + \beta'_{3,t} \Gamma_i + \beta'_{4,t} D_i + \varepsilon_{i,t}$$

- $P_{i,t} \equiv$ population density of country i in year t
- $y_{i,t} \equiv$ income per capita of country i in year t
- $T_i \equiv$ years elapsed since the onset of agriculture in country i
- $X_i \equiv$ measure of land productivity for country i
- $\Gamma_i \equiv$ vector of geographical controls for country i
- $D_i \equiv$ vector of continental fixed effect in country i

Determinants of Population Density in 1500 CE

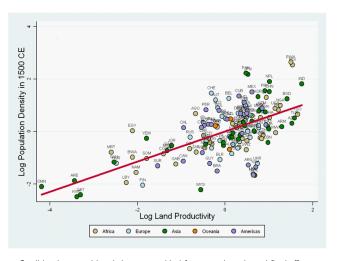
OLS OLS Dependent V 33*** 298) 0.587*** (0.071) -0.425***	OLS ariable: Log p 1.025)*** (0.223 0.641*** (0.059) -0.353***	OLS opulation dens 1.087*** (0.184) 0.576*** (0.052)	1.389*** (0.224) 0.573*** (0.095)	2.077*** (0.391) 0.571*** (0.082)
0.587*** (0.071) 0.425***	1.025)*** (0.223 0.641*** (0.059)	1.087*** (0.184) 0.576*** (0.052)	1.389*** (0.224) 0.573*** (0.095)	2.077*** (0.391) 0.571***
0.587*** (0.071) -0.425***	(0.223 0.641*** (0.059)	(0.184) 0.576*** (0.052)	(0.224) 0.573*** (0.095)	(0.391) 0.571***
(0.071) -0.425***	(0.059)	(0.052)	(0.095)	
	-0.353***			
(0.124)	(0.104)	-0.314*** (0.103)	-0.278** (0.131)	-0.248** (0.117)
		-0.392*** (0.142)	0.220 (0.346)	0.250 (0.333)
		0.899*** (0.282)	1.185*** (0.377)	1.350*** (0.380)
Yes Yes .47 147	Yes 147	Yes 147	Yes 96	Yes 96
.40 0.60	0.66	0.73	0.73	0.70
				14.65
				0.44
	.47 147 .40 0.60	47 147 147 .40 0.60 0.66	(0.142) 0.899*** (0.282) 7es Yes Yes Yes 47 147 147 147 .40 0.60 0.66 0.73	(0.142) (0.346) 0.899*** 1.185*** (0.282) (0.377) Ves Yes Yes Yes Yes 47 147 147 147 96

Effects on Income per Capita versus Population Density

	OLS (1)	OLS (2)	OLS (3)	OLS (4)	OLS (5)	OLS (6)
	Log Income Per Capita in			Log Population Density in		
-	1500 CE	1000 CE	1 CE	1500 CE	1000 CE	1 CE
Log years since Neolithic	0.159 (0.136)	0.073 (0.045)	0.109 (0.072)	1.337** (0.594)	0.832** (0.363)	1.006** (0.483)
Log land productivity	0.041 (0.025)	- 0.021 (0.025)	- 0.001 (0.027)	0.584*** (0.159)	0.364*** (0.110)	0.681** (0.255)
Log absolute latitude	-0.041 (0.073)	0.060 (0.147)	-0.175 (0.175)	0.050 (0.463)	-2.140 ** (0.801)	-2.163** (0.979)
Distance to nearest coast or river	0.215 (0.198)	-0.111 (0.138)	0.043 (0.159)	-0.429 (1.237)	-0.237 (0.751)	0.118 (0.883)
% land within 100 km of coast or river	0.124 (0.145)	-0.150 (0.121)	0.042 (0.127)	1.855** (0.820)	1.326** (0.615)	0.228 (0.919)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	31	26	29	31	26	29
\mathbb{R}^2	0.66	0.68	0.33	0.88	0.95	0.89

Ömer Özak

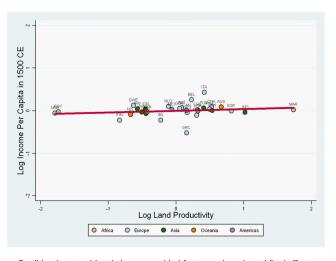
Land Productivity and Population Density in 1500



Conditional on transition timing, geographical factors, and continental fixed effects.

Source: Ashraf-Galor (AER 2011)

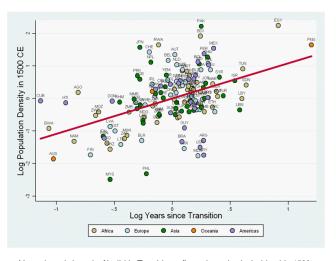
Land Productivity and Income per Capita in 1500



Conditional on transition timing, geographical factors, and continental fixed effects.

Source: Ashraf-Galor (AER 2011)

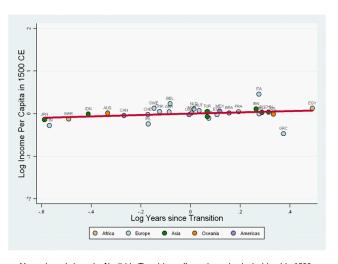
Technology and Population Density in 1500



Years elapsed since the Neolithic Transition reflects the technological level in 1500.

Conditional on land productivity, geographical factors, and continental fixed effects.

Technology and Income per Capita in 1500



Years elapsed since the Neolithic Transition reflects the technological level in 1500.

Conditional on land productivity, geographical factors, and continental fixed effects.

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

- Robustness to the inclusion of direct measures of technology
 - Exploit variation in a direct measure of the technology level
 - Variation in prehistoric biogeographic endowments IV for this direct measure of technology
- Robustness to the distance from the technological frontier
- Robustness to the exclusion of unobserved time-invariant country fixed effects
 - First-difference estimation strategy (with a lagged explanatory variable)
 - The effect of changes in the level of technology in 1000 BCE-1 CE on population density and income per capita in 1-1000CE

Robustness to Direct Measures of Technological Level

	OLS	OLS	OLS	OLS	OLS	OLS		
	(1)	(2)	(3)	(4)	(5)	(6)		
			Dependent					
	Log Po	pulation	Log Income Per		Log Po _l	oulation		
		Density in:		Capita in:		ty in:		
	1000 CE	1 CE	1000 CE	1 CE	1000 CE	1 CE		
Log Technology Index in Relevant Period	4.315*** (0.850)	4.216*** (0.745)	0.064 (0.230)	0.678 (0.432)	12.762*** (0.918)	7.461** (3.181)		
Log land productivity	0.449*** (0.056)	0.379*** (0.082)	-0.016 (0.030)	0.004 (0.033)	0.429** (0.182)	0.725** (0.303)		
Log absolute latitude	-0.283** (0.120)	-0.051 (0.127)	0.036 (0.161)	-0.198 (0.176)	-1.919*** (0.576)	-2.350*** (0.784)		
Distance to nearest coast or river	-0.638*** (0.188)	-0.782*** (0.198)	-0.092 (0.144)	0.114 (0.164)	0.609 (0.469)	0.886 (0.904)		
% land within 100 km of coast or river	0.385 (0.313)	0.237 (0.329)	-0.156 (0.139)	0.092 (0.136)	1.265** (0.555)	0.788 (0.934)		
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes		
Observations	140	129	26	29	26	29		
R^2	0.61	0.62	0.64	0.30	0.97	0.88		
Notes: Robus	Notes: Robust standard errors in parentheses; *** $p<0.01$, ** $p<0.05$, * $p<0.1$							

The Causal Effect of Technological Level on Population Density

	OLS	OLS	IV	OLS	OLS	IV
	(1)	(2)	(3)	(4)	(5)	(6)
		Depend	lent Variable:	Population De		
		1000CE			1CE	
Log Technology Index in Relevant Period	4.315*** (0.850)	4.198*** (1.164)	14.530*** (4.437)	4.216*** (0.745)	3.947*** (0.983)	10.798** (2.857)
Log land productivity	0.449*** (0.056)	0.498*** (0.139)	0.572*** (0.148)	0.379*** (0.082)	0.350** (0.172)	0.464** (0.182)
Log absolute latitude	-0.283** (0.120)	-0.185 (0.151)	-0.209 (0.209)	-0.051 (0.127)	0.083 (0.170)	-0.052 (0.214)
Distance to nearest coast or river	-0.638*** (0.188)	-0.363 (0.426)	-1.155* (0.640)	-0.782*** (0.198)	-0.625 (0.434)	-0.616 (0.834)
% land within 100 km of coast or river	0.385 (0.313)	0.442 (0.422)	0.153 (0.606)	0.237 (0.329)	0.146 (0.424)	-0.172 (0.642)
Continental dummies Observations	Yes	Yes 92	Yes 92	Yes 129	Yes 83	Yes
R ²	140 0.61	0.55	0.13	0.62	0.58	83 0.32
First-stage F-statistic Overid. p-value			12.52 0.941			12.00 0.160

Ömer Özak

Robustness to Technology Diffusion and other Geographic Characteristics

	(1)	(2)	(3)	(4)	(5)	(6)
	Log Population		Log Income Per		Log Population	
	Density	in 1500	Capita in 1500		Density in 1500	
Log Technology Index in Relevant Period	0.828*** (0.208)	0.877*** (0.214)	0.117 (0.221)	0.103 (0.214)	1.498** (0.546)	1.478** (0.556)
Log land productivity	0.559*** (0.048)	0.545*** (0.063)	0.036 (0.032)	0.047 (0.037)	0.596*** (0.123)	0.691*** (0.122)
Log Distance to Frontier	-0.186*** (0.035)	-0.191*** (0.036)	-0.005 (0.011)	-0.001 (0.013)	-0.130* (0.066)	-0.108* (0.055)
Small Island Dummy	0.067 (0.582)	0.086 (0.626)	-0.118 (0.216)	-0.046 (0.198)	1.962** (0.709)	2.720*** (0.699)
Landlocked Dummy	0.131 (0.209)	0.119 (0.203)	0.056 (0.084)	0.024 (0.101)	1.490*** (0.293)	1.269*** (0.282)
% Land in Temperate Climate Zones		-0.196 (0.513)		-0.192 (0.180)		-1.624* (0.917)
Continental dummies	Yes	Yes	Yes	Yes	Yes	Yes
Observations	147	147	31	31	31	31
R ²	0.76	0.76	0.67	0.67	0.94	0.96

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children

- Population levels positively associated with
 - Technology
 - Land Productivity
- Income per capita levels
 - Independent of both
 - Determined by preferences for children