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Economic Growth and Comparative Development

# Phases of Development: Standard of Living

- The Malthusian Epoch
- The Post-Malthusian Regime
- The Modern Growth Regime

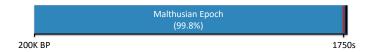
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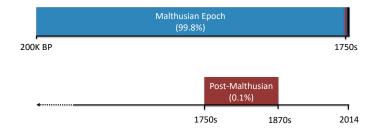
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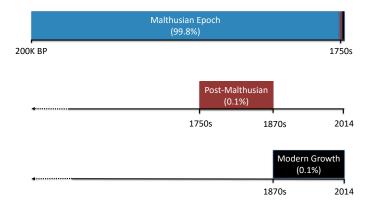
# Phases of Development: Timeline of the Most Developed Economies



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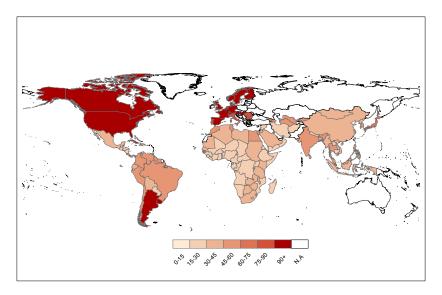
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- Fertility, mortality and population growth decline very rapidly
- The impact of technological progress on output per capita are no longer counterbalanced by population growth
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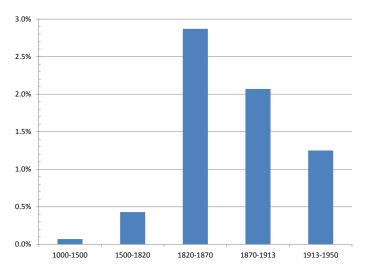
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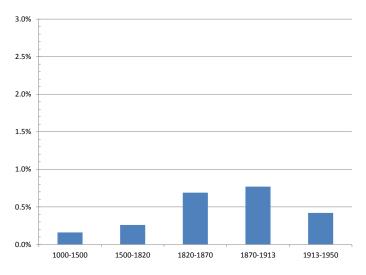
# Variation in years elapsed since the Onset of the Fertility Decline



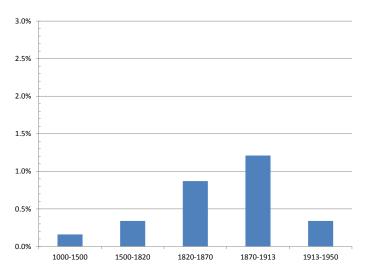
# Early Fertility Decline - Western Offshoots



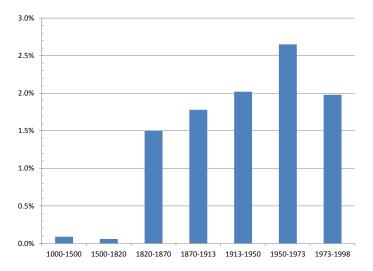
# Early Fertility Decline - Western Europe



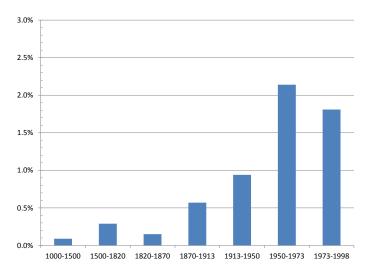
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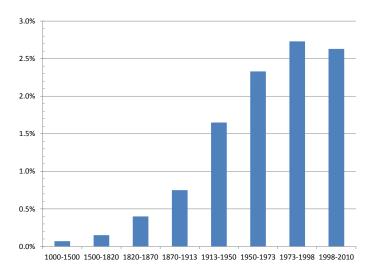
# Late Fertility Decline - Latin America



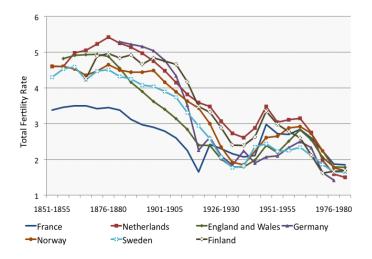
## Late Fertility Decline - Asia



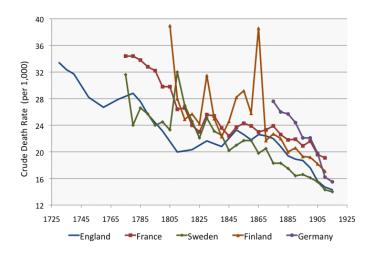
# Late Fertility Decline - Africa



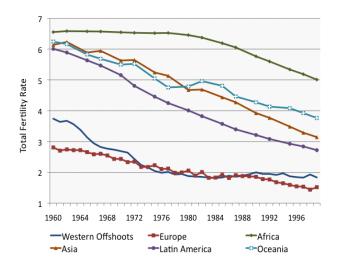
# The Demographic Transition in Western Europe: Total Fertility Rates



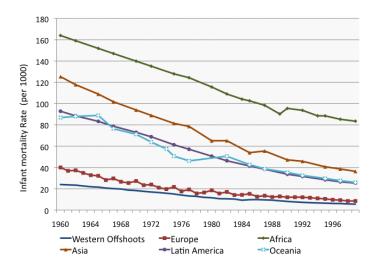
# Mortality Decline Western Europe: 1730-1920



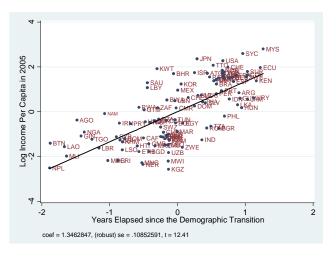
#### The Evolution of Total Fertility Rate across Regions, 1960-1999



#### Decline in infant mortality rates across regions, 1960-1999



# Timing of the Demographic Transition and Current Income per Capita



Conditional on absolute latitude.

- The Rise in Income (Becker, 1960)
  - The cost of raising children is primarily parental time
    - The rise in income increased the opportunity cost of raising
  - The income elasticity of child quality is larger than that of quantity
    - The rise in income  $\Rightarrow$  substitution of child quality for quantity
- The Decline in Child Mortality
  - Decline in child mortality enabled families to attain their desirable
    - The mortality decline  $\Rightarrow$  reduction in fertility

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- The Old-Age Security Hypothesis (Caldwell, 1976)
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# Child rearing is time-intensive

Household's Budget constraint

$$y \tau n + c \leq y$$

- $y \equiv$  household's income
- $c \equiv$  household's consumption
- $n \equiv$  household's children
- $\tau \equiv$  time cost per child
- $y\tau \equiv$  opportunity cost of raising a child
- Equivalently

$$c \leq y(1-\tau n)$$

- 1 = household's time endowment
- $(1 \tau n) \equiv$  labor force participation
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# • The rise in income generates two conflicting effects:

• An income effect:

$$y \tau n + c \leq [y] \uparrow$$

- More income can be devoted to raising children
- operates towards  $n \uparrow$
- A substitution effect:

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#### The Rise in Income - Theoretical Evaluation

# • Preference-based theory (unattractive)

- Innate bias against child quantity beyond a certain level of income non-refutable
- Non-robust (e.g., the class of homothetic preferences will not trigger a fertility decline)

#### The Rise in Income - Theoretical Evaluation

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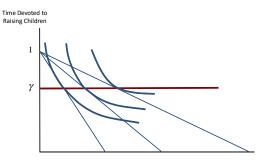
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### The Rise in Income: Testable predictions

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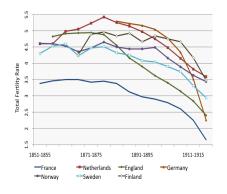
### The Rise in Income: Refuting Cross Country Evidence

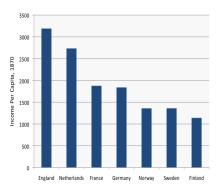
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# Simultaneous DT across European Countries that Differ in Income per Capita





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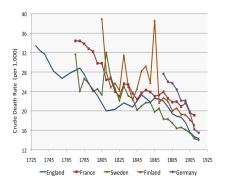
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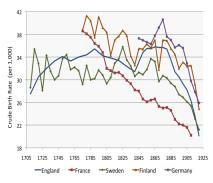
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- England: The decline in mortality started in England in the 1730s (140 years before the fertility decline) and was accompanied by a steady increase in fertility rates until 1800

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- Institutions supporting individuals in their old age were formed well before the demographic transition
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- Prior to the demographic transition, richer individuals who presumably had better access to financial markets, had larger number of surviving children

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  - Women have physiological comparative advantage in mental (rather than physical) tasks
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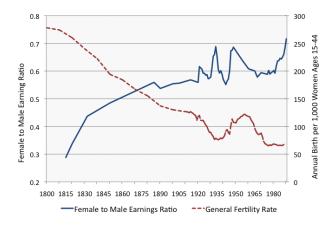
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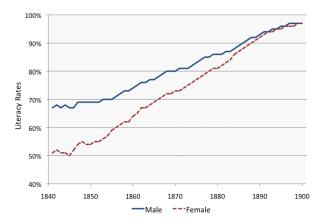
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#### Evolution of the Gender Earninig Ratio - US



# Evolution of the Gender Literacy Gap - England



- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

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- $\tau \equiv$  time cost per child
- $w^F \tau \equiv$  opportunity cost of raising a child

- Child rearing is time-intensive
- Women are the prime care-takers engaged in child rearing
- Budget constraint (if only women raise children)

$$w^F \tau n + c \le w^M + w^F$$

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  - An income effect:

$$w^F \tau n + c \le w^M + [w^F] \uparrow$$

- More income for raising children  $\implies$  operates towards  $n \uparrow$
- A substitution effect:

$$\uparrow [w^F \tau] n + c \le w^M + w^F$$

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• If women work and raise children, an increase in  $w^F$  increases the opportunity cost of raising children more than family income, i.e.,

$$w^F ~\uparrow ~\Longrightarrow ~|{\sf Income~effect}| < |{\sf Substitution~effect}|$$
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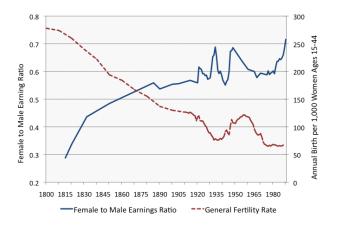
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## Women's Relative Wages and Fertility - US



#### Women's Relative Wages and Fertility - Evidence

- US (1970s):  $w^F \uparrow \implies n \Downarrow \& w^M \uparrow \implies n \uparrow$  (Heckman and Walker ECT 79)
- Sweden's demographic transition:  $(w^F/w^M) \uparrow \implies n \Downarrow$  (Schultz 1985)
- France (1876–1896): reduction in the gender literacy gap had an adverse effect on fertility, accounting for income per capita, educational attainment, and mortality rates (Murphy 2015)

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$$u = (1 - \gamma) \ln c + \gamma [\ln n + \beta \ln h]$$

- $c \equiv consumption$
- $n \equiv \text{(surviving) children}$
- $h \equiv$  quality (human capital) of each child
- $\bullet$   $\beta \equiv$  degree of preference for child quality;  $\beta < 1$

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$$yn(\tau^q + \tau^e e) + c \le y$$

- $y \equiv$  household potential income
- $au^q \equiv$  fraction of the household's unit-time endowment required to raise a child, regardless of quality
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$$h=h(e,g)$$

- $h_e(e,g) > 0 \& h_{ee}(e,g) < 0$ 
  - HC is increasing (at decreasing rates) in the parental time investment in the education of the child
- $h_g(e,g) < 0 \& h_{gg}(e,g) > 0$ 
  - HC is decreasing in the rate of technological progress (obsolescence of HC in a changing technological environment)
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$$\{n, e, c\} = \arg\max \gamma [\ln n + \beta \ln h(e, g)] + (1 - \gamma) \ln c$$
 
$$s.t. \quad yn(\tau^q + \tau^e e) + c \le y$$

since 
$$c = y[1 - n(\tau^q + \tau^e e)] \iff$$

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with respect to n:

$$\frac{\gamma}{n} = \frac{(1-\gamma)y(\tau^q + \tau^e e)}{y[1-n(\tau^q + \tau^e e)]}$$

$$\gamma[1 - n(\tau^q + \tau^e e)] = (1 - \gamma)(\tau^q + \tau^e e)n$$

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$$\gamma[1 - n(\tau^q + \tau^e e)] = (1 - \gamma)(\tau^q + \tau^e e)n$$

$$n(\tau^q + \tau^e e) = \gamma$$

$$\{\textit{n},\textit{e}\} = \arg\max\gamma[\ln\textit{n} + \beta\ln\textit{h}(\textit{e},\textit{g})] + (1-\gamma)\ln\textit{y}[1-\textit{n}(\tau^\textit{q} + \tau^\textit{e}\textit{e})]$$

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$$\frac{\gamma\beta h_e(e,g)}{h(e,g)} = \frac{(1-\gamma)yn\tau^e}{y[1-n(\tau^q+\tau^e e)]}$$

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$$rac{\gamma \beta h_{\mathrm{e}}(\mathrm{e},\mathrm{g})}{h(\mathrm{e},\mathrm{g})} = n au^{\mathrm{e}} \quad \Longrightarrow \quad rac{\beta h_{\mathrm{e}}(\mathrm{e},\mathrm{g})}{h(\mathrm{e},\mathrm{g})} = rac{ au^{\mathrm{e}}}{( au^{\mathrm{q}} + au^{\mathrm{e}}\mathrm{e})}$$

$$\beta h_e(e,g)(\tau^q + \tau^e e) = \tau^e h(e,g)$$

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$$n = \gamma/(\tau^q + \tau^e e)$$
 $\tau^e h(e,g) = \beta h_e(e,g)(\tau^q + \tau^e e)$ 

$$e = e(g, \beta, \tau^e, \tau^q),$$
  

$$n = \gamma/[\tau^q + \tau^e e(g, \beta, \tau^e, \tau^q)]$$

$$\begin{split} n &= \gamma/(\tau^q + \tau^e e) \\ \tau^e h(e,g) &= \beta h_e(e,g)(\tau^q + \tau^e e) \\ e &= e(g,\beta,\tau^e,\tau^q), \\ n &= \gamma/[\tau^q + \tau^e e(g,\beta,\tau^e,\tau^q)] \end{split}$$



# The optimal level of investment in child quality increases if:

• The technological environment changes more rapidly

$$\partial e(g, \beta, \tau^e, \tau^q)/\partial g > 0$$

Preferences for child quality are highe

$$\partial e(g, \beta, \tau^e, \tau^q)/\partial \beta > 0$$

• The cost of raising a child (regardless of quality) increases

$$\partial e(g, \beta, \tau^e, \tau^q)/\partial \tau^q > 0$$

The cost of educating a child decreases

$$\partial e(g, \beta, \tau^e, \tau^q)/\partial \tau^e < 0$$

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# The optimal number of children decreases if:

• The technological environment changes more rapidly

$$\partial n/\partial g < 0$$

• Preferences for child quality are higher

$$\partial n/\partial \beta < 0$$

• The cost of raising a child (regardless of quality) increases

$$\partial n/\partial \tau^q < 0$$

$$\partial n/\partial au^e < 0$$
 if  $[\partial e/\partial au^e][ au^e/e] > -1$ 

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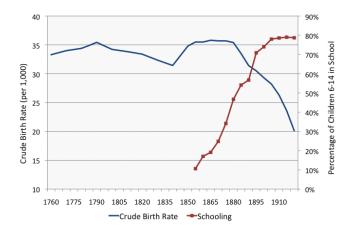
$$\partial n/\partial \beta < 0$$

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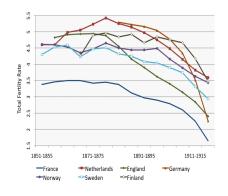
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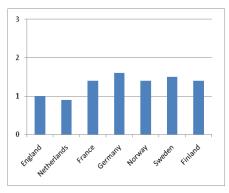
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# Human Capital Formation and the DT - England



#### Growth Rates 1870-1913 and DT





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- US (1910s): Eradication of hookworm a positive shock to the return to child quality - had an adverse effect on fertility (Bleakley-Lange-2009)
- Prussia (19th century): the rise in human capital formation has had an adverse effect on fertility (IV: Land concentration & Distance from the birthplace of Protestantism - Wittenberg) (Becker-Cinnirella-Woessmann 2010)
- France (1876–96): the level of education attainment had an adverse effect on fertility rates during France's demographic transition, accounting for income per capita, the gender literacy gap, and mortality rates. (Murphy 2015)
- England (1580-1871) Adverse effect of family size on children's literacy.

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