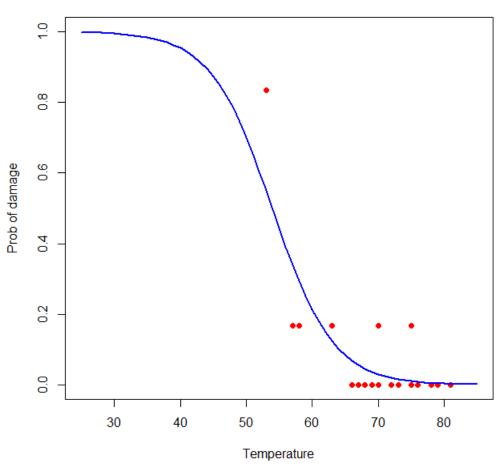
Generalized linear modeling with

Challenger disaster



Source: Faraway (2006).





- 0/1 data (activity, infection, presence, sex)
- proportional data (0 100 %)
- number of successes vs. number of failures
- count data (species richness)



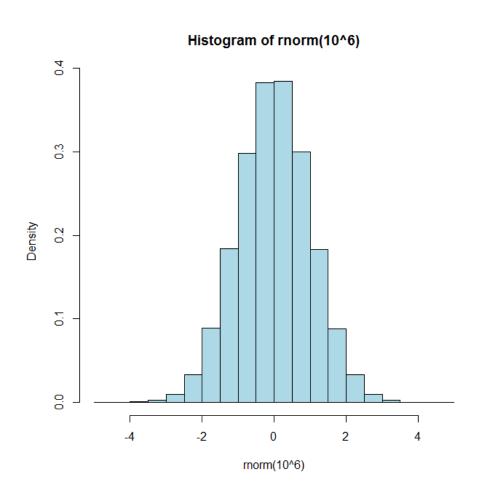


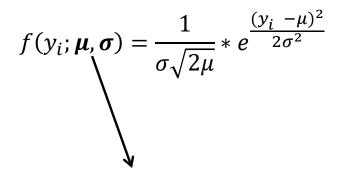
- 1. distribution of the response
- systematic part (covariates)
- 3. link-function between expected value of the response and the systematic part

Normal distribution



seit 1558



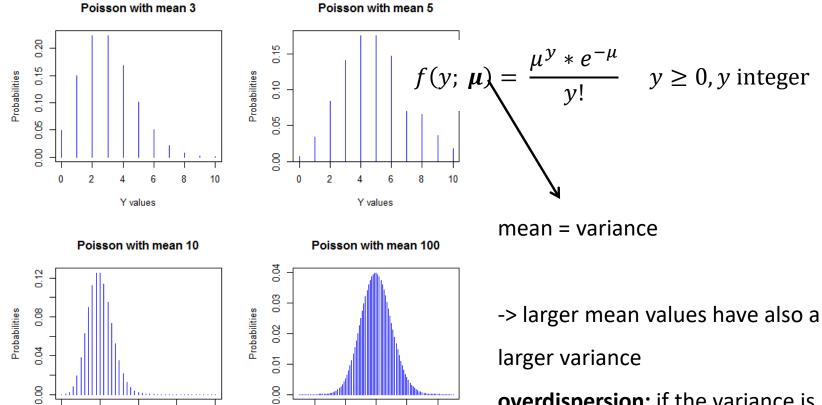


defined by mean and standard deviation

Poisson distribution







60

80

100

Y values

120

Modified after: Zuur et al. (2009).

30

20

Y values

10

overdispersion: if the variance is larger than the mean

Further common distributions



- 1. Bernoulli/binomial distribution -> presence/absence data
- 2. Negative binomial distribution -> one possible that way might account for overdispersion
- **3. Gamma distribution** -> can be used for a continous response variable that has positive values (> 0)

Predictor function



$$g(x_i) = \alpha + \beta_1 X_{1i} + \dots + \beta_n X_{ni}$$





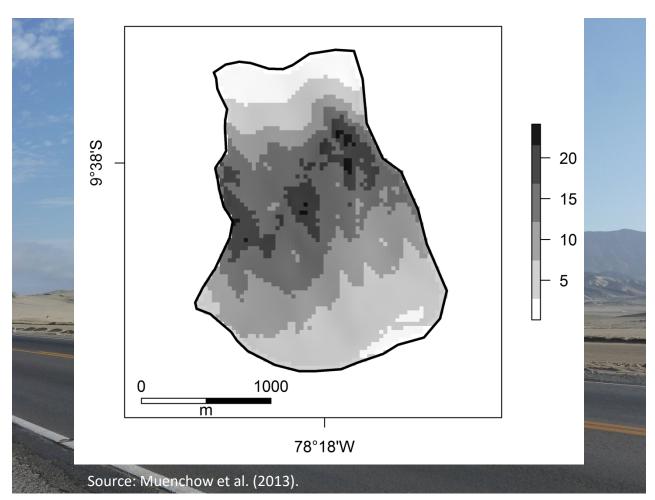
- distribution -> increase in spread
- 2. Poisson distribution avoid negative realizations
- 3. exponential link -> no negative fitted values
- 4. Maximum likelihood algorithm (see Zuur 2009: 213)

$$Y_i \sim P(\mu_i)$$
 and $E[Y_i] = \mu_i = e^{\alpha + \beta_i X_{1i} + \dots + \beta_n X_{ni}}$
$$\log(E[Y_i]) = \alpha + \beta_i X_{1i} + \dots + \beta_n X_{ni}$$

$$\log_{-\text{link}}$$







Binomial GLM

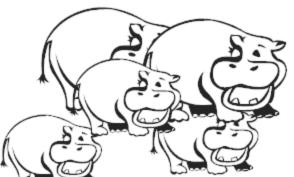


Absence (= 0)

- 1. Express 0 and 1 as probability P
- 2. Apply a series of transformationson P
- 3. back-transform to 0-1 intervall



I am not here, because the habitat is not good!



Here we are!

Presence (= 1)

modified after Zuur et al. (2009).

Concept of Odds



$$O_i = \frac{\pi_i}{1 - \pi_i}$$

with O_i = Odds for the *i*th observation

 π_i = Probability of the *i*th observation

-> Value not any longer restricted to 0 and 1!!!

Concept of Odds



$$O_i = \frac{0.9}{(1 - 0.9)} = 9$$

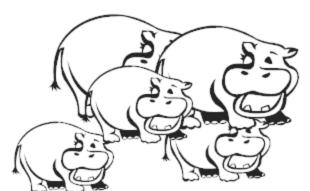
Odds of 9 -> it is **9 times** more likely to record a hippo than not to record one.

Or: In **9 from 10** plots you will find a hippo.

Absence (= 0)



I am not here, because the habitat is not good!



Here we are!

Presence (= 1)

modified after Zuur et al. (2009).





$$\log - \lim \left(\frac{\pi_i}{1 - \pi_i} \right) = \eta$$

with η = predictor function

-> Negative values are possible





$$\pi_i = \frac{e^{\eta}}{1 + e^{\eta}}$$

-> term lies always between 0 and 1 (back-transformation)!!!





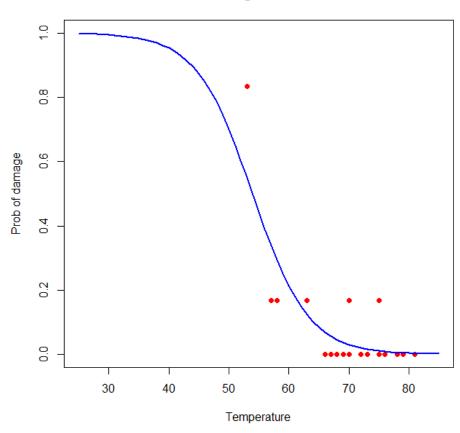
$$Y_i \sim B(1; P_i) \text{ and } E[Y_i] = P_i = \pi_i = \frac{e^{\alpha + \beta_i X_{1i} + \dots + \beta_n X_{ni}}}{1 + e^{\alpha + \beta_i X_{1i} + \dots + \beta_n X_{ni}}}$$

- appropriate distribution (Bernoulli)
- Maximum likelihood algorithm (see Zuur et al., 2007: 93)





Challenger disaster



Source: Faraway (2006).







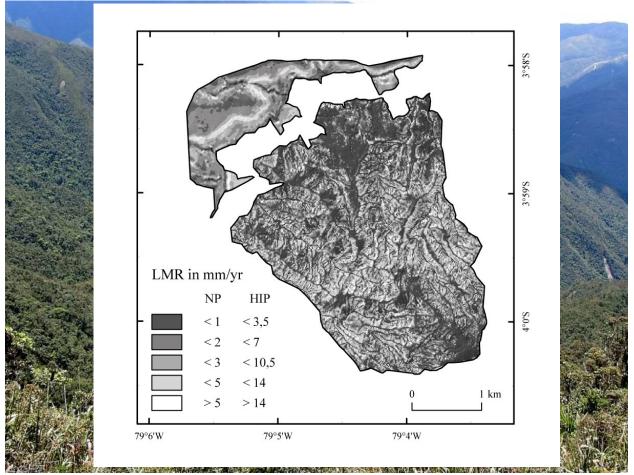


Foto: Michael Richter.

Source: Muenchow et al. (2011).

Literature



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